

# Gradient Based Optimization of **MATSim Using Iterative** Backpropagation

A.U.Z Patwary<sup>1</sup>, Francesco Ciari<sup>1</sup>, Enoch Lee<sup>2</sup> and Hong K. Lo<sup>2</sup>

<sup>1</sup> Department of Civil, Geological and Mining Engineering, Polytechnique Montreal, Canada

<sup>2</sup> Department of Civil and Environmental Engineering, HKUST, China



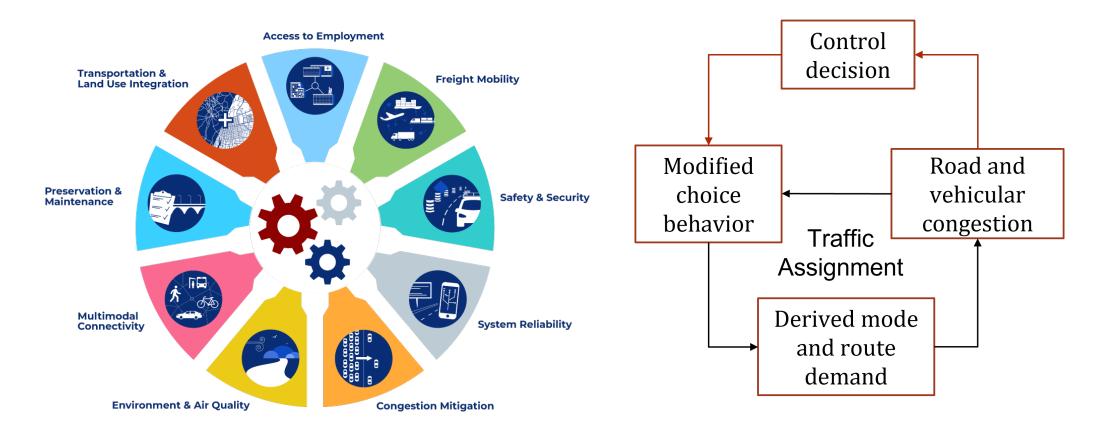








#### Introduction



# Challenges

- Mathematical Complexity
  - No closed-form formulation
  - No analytical gradient

#### Computation Time

- 25 days for 100% HK scenario
- 2 days for 10% Montreal scenario
- Tight simulation budget (maximum 20)
- High dimension problems
  - OD estimation (49,000 variables for HK network)
  - Pricing optimization
  - Toll Optimization etc.

## Solution Algorithms

- Heuristics:
  - **Genetic Algorithm** (Amirjamshidi and Roorda,2019; Chiappone et al., 2016; Spiliopoulou et al., 2015; Yu and Fan, 2017)
  - Monte Carlo Sampling (de Oliveira and Cunha, 2019;Henclewood et al., 2017)
  - Artificial Bee Colony (D. Huang et al., 2016b; Szeto and Jiang, 2012)
  - SPSA (Lee and Ozbay, 2009; Ma et al., 2007; Lu et al.,
  - 2015 and Oh et al.,2019)

#### • Response surface:

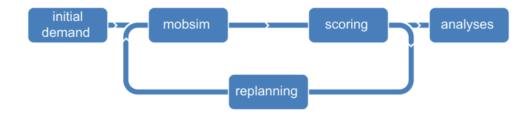
- **Generic** (Polynomial, interpolation, etc.)
- Hybrid (Generic + Traffic Model) (Osorio and Chong 2015, Zhang 2016, Osori 2019, Patwary et al. 2021)

#### Gradient Based TA Optimization

Beneficial for **high dimensional** optimization. **Moving towards negative gradient** direction is **sufficient for minimization**.

Numerical (finite difference) gradient is too costly to evaluate. (2d+1) function evaluation.

Cyclic dependencies (iterative loop) prevents closed form gradient formulation.

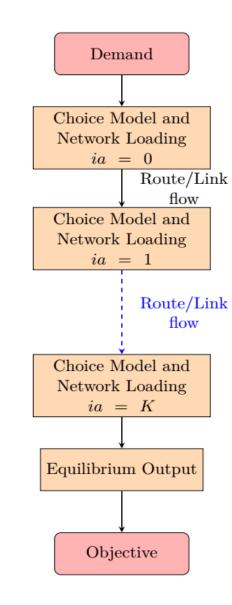


## **IB** Gradient Estimation

TA solution procedures operates in two steps:

Auxiliary Flow Computation: Calculates the choice model (scoring and choice strategy) and network loading model (Mobsim), generating subsequent flow as a function of the flow and cost of previous iteration.

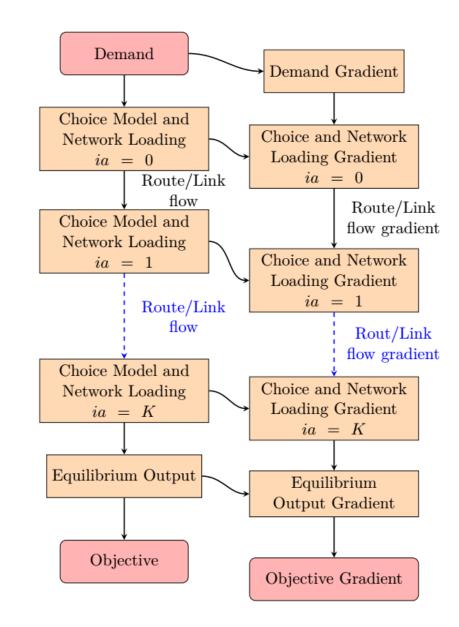
**Flow Update:** Updates the flow by merging previous iteration's flow and newly calculated flow with a decaying merge rule. **(MSA in MATSim)** 



### **IB** Gradient Estimation

IB introduces a **'gradient backpropagation**' step along with the network loading step.

Gradient Backpropagation: It uses information from the network loading step to calculate the flow gradient of the current iteration as a function of the flow gradient of the previous iteration.



## Pros and Cons of IB

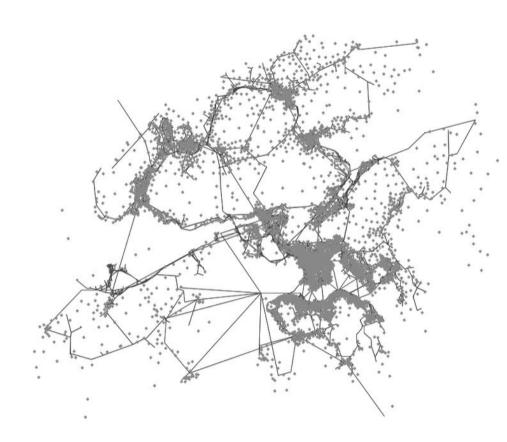
#### Pros:

- Requires one function evaluation to obtain high-dimensional, accurate analytical gradient.
- Efficient in computation, can run parallelly on GPU.
- Works well with large-scale, multi-modal network.

#### Cons:

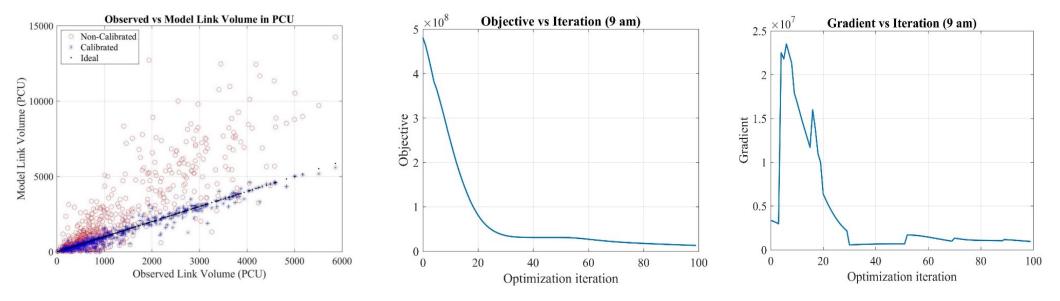
- Requires formulation through the choice and network loading model.
- Only **implemented in static setting** for now.

#### Application of IB in static HK Network

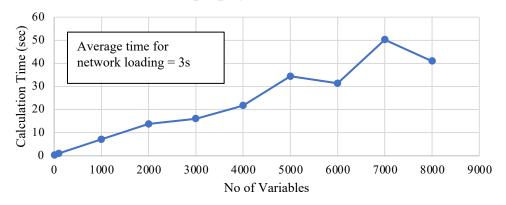


- The network contains **8,797 nodes**, **18,207 physical links**, **1,446 transit lines**, and **2,684 transit routes** with **9,222 stops** or stations.
- The number of time-specific **transit** direct and transfer **links is 433,812.**
- Transit hyper path is extracted from MATSim. The total number of transit hyper paths are 603,628 and auto routes are 56,676.
- **591 peak hour** measurements from ATC 2016 are used for calibration.
- The total number of **origin-destination pairs** in the model is **165,509.**
- The model is static, and the calibration is performed per time step for origin and destination multiplier, i.e., θ ∈ {θ<sub>0,t</sub>, θ<sub>D,t</sub>} to save memory.
- Variable size is 8,301. Max memory consumption is 130 GB.

#### **HK OD Multiplier Calibration Result**



Gradient Backpropagation Calculation Time

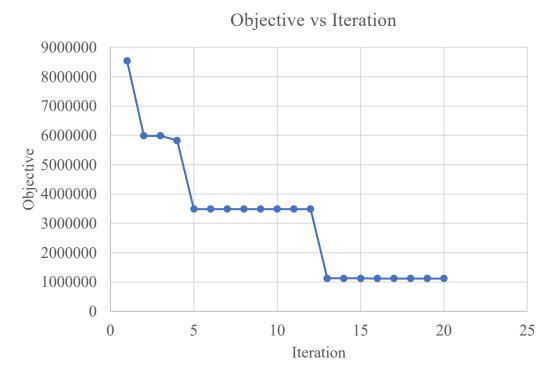


- Objective Reduction: 98.27%
- Initial vs Final MAPE: 95.29 vs 21.23%
- Initial vs Calibrated Mean GEH: 24.18 vs 6.09
- We have used ADAM (King Ma and Ba 2015) as gradient based optimizer.

#### Using static IB for MATSim optimization

If max sim iteration reached, Stop. New Generate New Parameter Variable Perform ADAM optimization Start with The **polynomial/generic** using combined IB and Simulation Run new polynomial gradient model gradient works as Variables a gradient corrector. For Demands Generate polynomial Simulation and routes gradient observation a "close enough" model we can drop this New analytical Fit metamodel bridging layer. model

## Results from a Toy Network (MATSim)



# $O_1$ $O_2$ D Train = Bus

No Polynomial Function Used Variables: origin destination demand multipliers (O1,O2,D) OD: O1-D, O2-D Known: Link Counts, Train and bus passenger counts.

#### Insight:

Gradient of the fitted underdetermined polynomial worsen the convergence. Alternative metamodel should be used. (Suggestions?)

## Dynamic Extension of IB

Key insight:

The **travel time gradient** of a route in dynamic setting **is inverse to the route output flow rate**.

Can be calculated in two ways:

- **1. Finite difference** on a **fixed time step DNL model**.
- 2. Flow the gradients through the network.

We have picked Link transmission model (LTM) for its simple link and node model formulation. The insight from LTM will help push the algorithm towards event-based algorithms, i.e., Mobsim in MATSim.

#### Conclusion

- A metamodel corrected gradient based optimization of MATSim is explored.
- As future work, **IB** is extended for Link Transmission Model (LTM) and preferably to MATSim directly.

# Thanks for your attention.

## Questions?

ashraf-uz-zaman.patwary@polymtl.ca