# Automated projection spectroscopy (APSY) 

## Supplementary Material

Sebastian Hiller, Francesco Fiorito, Kurt Wüthrich and Gerhard Wider

Institut für Molekularbiologie und Biophysik
Eidgenössische Technische Hochschule Zürich (ETH)
CH-8093 Zürich, Switzerland

## Experimental schemes for APSY NMR

The pulse sequence for the 4D APSY-HNCOCA experiment (Fig. 6) was derived from the pulse sequence for $3 \mathrm{D} \mathrm{HN}(\mathrm{CO}) \mathrm{CA}$ (1) by adding an evolution period for ${ }^{13} \mathrm{C}$, similar to 4 D TROSY-HNCOCA (2). At a ${ }^{1} \mathrm{H}$ frequency of 750 MHz , the three indirect dimensions $\omega_{1}\left({ }^{15} \mathrm{~N}\right)$, $\omega_{2}\left({ }^{13} \mathrm{C}^{\prime}\right)$ and $\omega_{3}\left({ }^{13} \mathrm{C}^{\alpha}\right)$ were recorded with spectral widths of $1600 \mathrm{~Hz}, 1900 \mathrm{~Hz}$ and 5700 Hz , respectively, and projected onto one indirect dimension using two projection angles $\alpha$ and $\beta$ (Table 1). The interscan delay was 1 s , and 8 transients were accumulated per data point in the indirect dimension. 1024 complex points were recorded in the direct dimension, with a sweep width of 11.0 ppm . Prior to Fourier transformation, the FID was multiplied with a $75^{\circ}$-shifted sine bell (3) and zero-filled to 2048 complex points. In the indirect dimension, the data was multiplied with a $75^{\circ}$-shifted sine bell and zero-filled to the nearest-next power of 2 complex points before Fourier transformation (4). The spectra were phased automatically using PROSA (5). The baseline was corrected using the IFLAT method (6) in the direct dimension and polynomials in the indirect dimension. $j=27$ projections were recorded with the following projection angles $\alpha$ and $\beta$, and numbers of complex points in the indirect dimension, $n:(\alpha, \beta, n)=\left(0^{\circ}, 0^{\circ}, 48\right),\left(0^{\circ}, 90^{\circ}, 42\right),\left(90^{\circ}, 0^{\circ}, 16\right),\left( \pm 30^{\circ}, 0^{\circ}, 54\right),\left( \pm 60^{\circ}, 0^{\circ}, 44\right)$, $\left(0^{\circ}, \pm 30^{\circ}, 48\right),\left(0^{\circ}, \pm 60^{\circ}, 64\right),\left(90^{\circ}, \pm 30^{\circ}, 24\right),\left(90^{\circ}, \pm 60^{\circ}, 40\right),\left( \pm 30^{\circ}, \pm 30^{\circ}, 56\right),\left( \pm 60^{\circ}, \pm 30^{\circ}\right.$, $56),\left( \pm 45^{\circ}, \pm 60^{\circ}, 64\right)$.

In the 5D APSY-HACACONH experiment, the pulse sequence of Kim and Szyperski (7) was modified to suppress magnetization pathways starting on glycine $\mathrm{H}^{\alpha}$ (8) (Fig. 7). (Magnetization transfers starting at glycines produce pairs of peaks for which 4 of the 5 chemical shifts are identical, differing only in the $\mathrm{H}^{\alpha}$-shift. Such pairs of peaks are close in the multidimensional space. In principle, APSY could cope with this situation.) At a ${ }^{1} \mathrm{H}$ frequency of 500 MHz , the four indirect dimensions $\omega_{1}\left({ }^{1} \mathrm{H}^{\alpha}\right), \omega_{2}\left({ }^{13} \mathrm{C}^{\alpha}\right), \omega_{3}\left({ }^{13} \mathrm{C}^{\prime}\right)$, and $\omega_{4}\left({ }^{15} \mathrm{~N}\right)$ were measured with spectral widths of $2000 \mathrm{~Hz}, 3600 \mathrm{~Hz}, 1600 \mathrm{~Hz}$ and 1550 Hz , respectively, and projected onto one indirect dimension using three projection angles $\alpha, \beta$ and $\gamma$ (Table 1). In total, 28 projections were recorded with 128 complex points in the indirect dimension, using the parameters given in Table 2. The 28 projection spectra are shown in Fig. 9. The interscan delay was 1 s , and 4 transients were accumulated per data point in the indirect dimension. 1024 complex points were recorded in the direct dimension with a spectral width of 12.0 ppm . The projection spectra were processed in the same way as described above for the 4D APSYHNCOCA experiment.

Figures Supplementary Material


Figure 6. Pulse sequence used for 4D APSY-HNCOCA. Radio-frequency pulses were applied at 118.0 ppm for ${ }^{15} \mathrm{~N}$, at 174.0 ppm for ${ }^{13} \mathrm{C}^{\prime}$, at 56.0 ppm for ${ }^{13} \mathrm{C}^{\alpha}$, and at 4.7 ppm for ${ }^{1} \mathrm{H}$. The carrier frequency on the carbon channel was switched between the ${ }^{13} \mathrm{C}$, and ${ }^{13} \mathrm{C}^{\alpha}$ carrier positions where indicated by the two vertical arrows. Narrow and wide bars represent $90^{\circ}$ and $180^{\circ}$ pulses, respectively. Pulses marked with an upper case letter were applied as shaped pulses; A: Gaussian shape, duration $100 \mu \mathrm{~s}$; B: Gaussian shape, $120 \mu \mathrm{~s}$; C: I-burp (9), $200 \mu \mathrm{~s} ; \mathrm{D}:$ Gaussian shape, $80 \mu \mathrm{~s}$; E: RE-burp (9), $350 \mu \mathrm{~s}$ (durations depend on the spectrometer frequency, here 750 MHz ). All other pulses were rectangular pulses applied with high power. The last six ${ }^{1} \mathrm{H}$ pulses represent a 3-9-19 WATERGATE element (10). Grey ${ }^{13} \mathrm{C}^{\alpha}$-pulses were applied to compensate for off-resonance effects of selective pulses (11). Decoupling using DIPSI-2 (12) on ${ }^{1} \mathrm{H}$ and WALTZ-16 (13) on ${ }^{15} \mathrm{~N}$ is indicated by rectangles. $t_{4}$ is the acquisition period. On the line marked PFG, curved shapes indicate sine bell-shaped pulsed magnetic field gradients applied along the z -axis, with the following durations and strengths: $\mathrm{G}_{1}, 700 \mu \mathrm{~s}, 13 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{2}, 1000 \mu \mathrm{~s}, 35 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{3}, 1000 \mu \mathrm{~s}, 35 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{4}, 800 \mu \mathrm{~s}, 16$ $\mathrm{G} / \mathrm{cm} ; \mathrm{G}_{5}, 800 \mu \mathrm{~s}, 13 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{6}, 800 \mu \mathrm{~s}, 18 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{7}, 1000 \mu \mathrm{~s}, 28 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{8}, 1000 \mu \mathrm{~s}, 28$ G/cm. Phase cycling: $\phi_{1}=\{y,-y\} \phi_{2}=\{x, x,-x,-x\}, \phi_{3}=\{4 x, 4-x\}, \phi_{4}=\{x,-x,-x, x,-x$, $\mathrm{x}, \mathrm{x},-\mathrm{x}\}$, all other pulses $=\mathrm{x}$. The following delays were used: $\tau=2.7 \mathrm{~ms}, \delta=13.75 \mathrm{~ms}, \eta=$ $4.5 \mathrm{~ms}, \lambda=200 \mu \mathrm{~s}$. The indirect evolution times $t_{1}-t_{3}$ were incremented according to the projections angles $\alpha$ and $\beta$ (see text and Table 1). Quadrature detection for the indirect dimensions was achieved using the hypercomplex Fourier transformation method for projections (14), with the phases $\psi_{1}-\psi_{3}$.


Figure 7. Pulse sequence used for the 5D APSY-HACACONH experiment. Radio-frequency pulses were applied at 4.7 ppm for ${ }^{1} \mathrm{H}$, at 118.0 ppm for ${ }^{15} \mathrm{~N}$, at 173.0 ppm for ${ }^{13} \mathrm{C}^{\prime}$ and at 54 ppm for ${ }^{13} \mathrm{C}^{\alpha}$. Narrow and wide bars represent $90^{\circ}$ and $180^{\circ}$ pulses, respectively. Pulses marked "A" were applied as Gaussian shapes, with $120 \mu$ s duration at a ${ }^{1} \mathrm{H}$ frequency of 500 MHz. All other pulses on ${ }^{13} \mathrm{C}^{\alpha}$ and ${ }^{13} \mathrm{C}^{\prime}$ had rectangular shape, with a duration of $\sqrt{3} /\left(\Delta \omega\left(\mathrm{C}^{\alpha}, \mathrm{C}^{\prime}\right) \cdot 2\right)$ and $\sqrt{15} /\left(\Delta \omega\left(\mathrm{C}^{\alpha}, \mathrm{C}^{\prime}\right) \cdot 4\right)$ for $90^{\circ}$ and $180^{\circ}$ pulses, respectively. Pulses on ${ }^{1} \mathrm{H}$ and ${ }^{15} \mathrm{~N}$ were applied with rectangular shape and high power. The last six ${ }^{1} \mathrm{H}$ pulses represent a 3-9-19 WATERGATE element (10). Grey pulses on ${ }^{13} \mathrm{C}^{\prime}$ and ${ }^{13} \mathrm{C}^{\alpha}$ were applied to compensate for off-resonance effects of selective pulses (11). Decoupling using DIPSI-2 (12) on ${ }^{1} \mathrm{H}$ and WALTZ-16 (13) on ${ }^{15} \mathrm{~N}$ is indicated by rectangles. $t_{5}$ represents the acquisition period. On the line marked PFG, curved shapes indicate sine bell-shaped pulsed magnetic field gradients applied along the $z$-axis with the following durations and strengths: $\mathrm{G}_{1}, 800 \mu \mathrm{~s}$, $18 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{2}, 800 \mu \mathrm{~s}, 26 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{3}, 800 \mu \mathrm{~s}, 13 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{4}, 800 \mu \mathrm{~s}, 23 \mathrm{G} / \mathrm{cm} ; \mathrm{G}_{5}, 800 \mu \mathrm{~s}, 26$ $\mathrm{G} / \mathrm{cm} ; \mathrm{G}_{6}, 800 \mu \mathrm{~s}, 23 \mathrm{G} / \mathrm{cm}$. Phase cycling: $\phi_{1}=\{\mathrm{x}, \mathrm{x},-\mathrm{x},-\mathrm{x}\} \phi_{2}=\{\mathrm{x},-\mathrm{x}\}, \phi_{3}=\{\mathrm{x},-\mathrm{x},-\mathrm{x}$, $\mathrm{x}\}, \psi_{1}=\mathrm{y}$, all other pulses $=\mathrm{x}$. The following initial delays were used: $t_{1}^{\mathrm{a}}=t_{1}^{\mathrm{c}}=1.9 \mathrm{~ms}$, $t_{1}^{\mathrm{b}}=0 \mathrm{~ms}, \quad t_{2}^{\mathrm{a}}=4.7 \mathrm{~ms}, \quad t_{2}^{\mathrm{b}}=8.8 \mathrm{~ms}, \quad t_{2}^{\mathrm{c}}=13.5 \mathrm{~ms}, \quad t_{3}^{\mathrm{a}}=t_{3}^{\mathrm{c}}=11.0 \mathrm{~ms}, \quad t_{3}^{\mathrm{b}}=0 \mathrm{~ms}$, $t_{4}^{\mathrm{a}}=t_{4}^{\mathrm{c}}=11.0 \mathrm{~ms}, t_{4}^{\mathrm{b}}=0 \mathrm{~ms}$. The delays $\tau=2.7 \mathrm{~ms}$ and $\eta=3.6 \mathrm{~ms}$ were fixed, and the delays $\delta$ and $\varepsilon$ were adjusted to $\delta=\left(t_{4}^{\mathrm{a}}+t_{4}^{\mathrm{b}}-t_{4}^{\mathrm{c}}\right) / 2$ and $\varepsilon=4.7 m s+\left(t_{3}^{\mathrm{a}}+t_{3}^{\mathrm{b}}-t_{3}^{\mathrm{c}}\right) / 2$ during the experiment. In the indirect four dimensions, constant-time or semi-constant time evolution
periods were applied, depending on the increment for the dimension resulting from the chosen projection angles $\alpha, \beta$ and $\gamma$ (Table 2). Quadrature detection for the indirect dimensions was achieved using the hypercomplex Fourier transformation method for projections (14) with the phases $\psi_{1}, \psi_{2}, \psi_{3}$ and $\psi_{4}\left(\psi_{1}, \psi_{2}\right.$ and $\psi_{3}$ were incremented and $\psi_{4}$ was decremented in $90^{\circ}$ steps).


Figure 8. Region of a 4D APSY-HNCOCA spectrum of 434-repressor(1-63) measured with the experimental scheme shown in Fig. 6. The projection was recorded with the angles $\alpha=0^{\circ}$ and $\beta=90^{\circ}$, which corresponds to a $\left(\mathrm{H}^{\mathrm{N}(i)}, \mathrm{C}^{\alpha(i-1)}\right)$ correlation spectrum. The spectral region shown contains 24 resonances that were all correctly identified by APSY in the associated 4D space. The black dots indicate the peak coordinates from the final 4D APSY peak list. The assignment of the resonances is given using the one-letter amino acid code and the sequence number of the amide proton.


Figure 9. 28 2D projections al to a28 of the 5D-APSY-HACACONH experiment measured using the scheme of Fig. 7 with the protein TM1290 on a 500 MHz spectrometer equipped with a z-gradient triple resonance cryogenic probehead. The dimension $\omega_{1-4}$ is the projection of the four indirect dimensions $\omega_{1}\left({ }^{1} \mathrm{H}^{\alpha}\right), \omega_{2}\left({ }^{13} \mathrm{C}^{\alpha}\right), \omega_{3}\left({ }^{13} \mathrm{C}^{\prime}\right)$, and $\omega_{4}\left({ }^{15} \mathrm{~N}\right)$ obtained with the projection angles $\alpha, \beta$ and $\gamma$ (Tables 1 and 2). The scales are centered on the carrier frequencies of 118.0 ppm for ${ }^{15} \mathrm{~N}, 173.0 \mathrm{ppm}$ for ${ }^{13} \mathrm{C}^{\prime}, 54.0 \mathrm{ppm}$ for ${ }^{13} \mathrm{C}^{\alpha}$, and 4.7 ppm for ${ }^{1} \mathrm{H}$. The projection angles and the spectral widths in the projected indirect dimension are given in Table 2. All projections are plotted with identical contour parameters.

## Tables Supplementary Material

Table 2. Projection angles and spectral widths $(S W)^{a}$ in the dimension $\omega_{1-4}^{b}$ used for recording the 28 2D projection spectra a1-a 28 shown in Figure 9.

|  | $\alpha$ | $\beta$ | $\gamma$ | $S W[\mathrm{~Hz}]$ |
| :---: | :---: | :---: | :---: | :---: |
| a1 | $0^{\circ}$ | $0^{\circ}$ | $0^{\circ}$ | 1550 |
| a2 | $90^{\circ}$ | $0^{\circ}$ | $0^{\circ}$ | 1600 |
| a3 | $0^{\circ}$ | $90^{\circ}$ | $0^{\circ}$ | 3600 |
| a4 | $0^{\circ}$ | $0^{\circ}$ | $90^{\circ}$ | 2000 |
| a5 | $30^{\circ}$ | $0^{\circ}$ | $0^{\circ}$ | 2142 |
| a6 | $-30^{\circ}$ | $0^{\circ}$ | $0^{\circ}$ | 2142 |
| a7 | $60^{\circ}$ | $0^{\circ}$ | $0^{\circ}$ | 2161 |
| a8 | $-60^{\circ}$ | $0^{\circ}$ | $0^{\circ}$ | 2161 |
| a9 | $0^{\circ}$ | $30^{\circ}$ | $0^{\circ}$ | 3142 |
| a10 | $0^{\circ}$ | $-30^{\circ}$ | $0^{\circ}$ | 3142 |
| a11 | $0^{\circ}$ | $60^{\circ}$ | $0^{\circ}$ | 3893 |
| a12 | $0^{\circ}$ | $-60^{\circ}$ | $0^{\circ}$ | 3893 |
| a13 | $0^{\circ}$ | $0^{\circ}$ | $30^{\circ}$ | 2342 |
| a14 | $0^{\circ}$ | $0^{\circ}$ | $-30^{\circ}$ | 2342 |
| a15 | $0^{\circ}$ | $0^{\circ}$ | $60^{\circ}$ | 2507 |
| a16 | $0^{\circ}$ | $0^{\circ}$ | $-60^{\circ}$ | 2507 |
| a17 | $90^{\circ}$ | $30^{\circ}$ | $0^{\circ}$ | 3186 |
| a18 | $90^{\circ}$ | $-30^{\circ}$ | $0^{\circ}$ | 3186 |
| a19 | $90^{\circ}$ | $60^{\circ}$ | $0^{\circ}$ | 3918 |
| a20 | $90^{\circ}$ | $-60^{\circ}$ | $0^{\circ}$ | 3918 |
| a21 | $90^{\circ}$ | $0^{\circ}$ | $30^{\circ}$ | 2386 |
| a22 | $90^{\circ}$ | $0^{\circ}$ | $-30^{\circ}$ | 2386 |
| a23 | $90^{\circ}$ | $0^{\circ}$ | $60^{\circ}$ | 2532 |
| a24 | $90^{\circ}$ | $0^{\circ}$ | $-60^{\circ}$ | 2532 |
| a25 | $0^{\circ}$ | $90^{\circ}$ | $30^{\circ}$ | 4118 |
| a26 | $0^{\circ}$ | $90^{\circ}$ | $-30^{\circ}$ | 4118 |
| a27 | $0^{\circ}$ | $90^{\circ}$ | $60^{\circ}$ | 3532 |
| a28 | $0^{\circ}$ | $90^{\circ}$ | $-60^{\circ}$ | 3532 |

${ }^{\text {a }}$ The spectral width $S W$ in the projected indirect dimensions is calculated from $S W=\sum_{z=1}^{4} \mathrm{p}_{1}^{z} \cdot S W_{z}$, where the $\mathrm{p}_{1}^{z} \mathrm{~s}$ are the coordinates of the unit vector $\overrightarrow{\mathrm{p}}_{1}$ (Eq. (1)) and the $S W_{z}$ are the spectral widths of the individual four indirect dimensions.
${ }^{\mathrm{b}}$ The dimension $\omega_{1-4}$ is the projection of the four indirect dimensions $\omega_{1}\left({ }^{1} \mathrm{H}^{\alpha}\right), \omega_{2}\left({ }^{13} \mathrm{C}^{\alpha}\right)$, $\omega_{3}\left({ }^{13} \mathrm{C}^{\prime}\right)$ and $\omega_{4}\left({ }^{15} \mathrm{~N}\right)$ with the projection angles $\alpha, \beta$ and $\gamma$ (Tables 1 and 2 ).

Table 3. Data base of proteins used to generate the Figure 5. In addition to these 53 proteins, the chemical shifts of 434-repressor(1-63) (BMRB data 2539 and unpublished data) were used.

| BMRB <br> number | number of residues |
| :---: | :---: |
| 4070 | 205 |
| 4093 | 138 |
| 4188 | 138 |
| 4193 | 214 |
| 4198 | 161 |
| 4215 | 136 |
| 4288 | 105 |
| 4384 | 262 |
| 4572 | 75 |
| 4575 | 211 |
| 4599 | 161 |
| 4671 | 159 |
| 4679 | 165 |
| 4881 | 179 |
| 4913 | 115 |
| 4938 | 132 |
| 4959 | 148 |
| 5013 | 120 |
| 5177 | 166 |
| 5308 | 107 |
| 547 | 148 |
| 5540 | 148 |
| 5557 | 170 |
| 5598 | 102 |
| 5629 | 111 |
| 5761 | 119 |
| 5884 | 138 |


| 5928 | 140 |
| :--- | ---: |
| 5976 | 103 |
| 6125 | 228 |
| 6133 | 116 |
| 6236 | 117 |
| 6295 | 251 |
| 5560 | 116 |
| 4101 | 214 |
| 4267 | 179 |
| 4282 | 183 |
| 4321 | 166 |
| 4376 | 185 |
| 4848 | 240 |
| 4854 | 165 |
| 5054 | 199 |
| 5232 | 288 |
| 5316 | 187 |
| 5398 | 187 |
| 5483 | 282 |
| 5627 | 187 |
| 5668 | 184 |
| 5756 | 242 |
| 5823 | 215 |
| 6202 | 182 |
| 6241 |  |
|  |  |

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