

(Danckwerts)





















$$\frac{1}{Pe} \frac{u_{i+1} - 2u_i + u_{i-1}}{\Delta z^2} - \frac{u_i - u_{i-1}}{\Delta z} - Da \cdot u_i^n = 0$$
$$u_0 - \frac{1}{Pe} \frac{u_1 - u_0}{\Delta z} = 1 \longrightarrow u_0 = \frac{1}{1 + \frac{1}{Pe\Delta z}} \left(\frac{1}{Pe\Delta z}u_1 + 1\right)$$
$$\frac{u_{N+1} - u_N}{\Delta z} = 0 \longrightarrow u_{N+1} = u_N$$

i = 1, 2, ..., N

System of nonlinear equations!!!

Numerical Methods for Chemical Engineers

Assignment 1

- Solve the steady state tubular reactor for 20 different Peclet numbers (between 0.01 and 100) and for a first (n=1) and a second (n=2) order reaction. Use a Damköhler number of unity. Complete the template rhs.m by implementing the non-linear equations to solve
- 2. Plot the conversion at the end of the reactor $1 \frac{c_{\text{out}}}{c_{\text{in}}}$ vs. the Peclet number for both reaction orders Also plot the ratio between the conversions of the first order and second order reaction
 - •What is better for these reactions, a lot of back-mixing (Pe small, CSTR) or ideal plug flow (Pe large, PFR)?
 - •What influence does the reaction order have overall and at low or high Peclet numbers?

Complete the template TubReact_steady_state.m





Dynamic tubular reactor

Boundary conditions:

$$u(0) - \frac{1}{Pe} \frac{\partial u}{\partial z}(0) = 1$$
 $\frac{\partial u}{\partial z}(1) = 0$











i = 1, 2, ..., N

System of nonlinear ODEs!!! Stiff...

Assignment 2

- 1.Solve the dynamic tubular reactor from initial 0 to final time of 5 with MATLAB's ode23s Use the rhs.m from assignment 1 and the template TubReact_dynamic.m Consider only a first order reaction with Pe=100 and Da=1
- 2.Plot the dimensionless concentration at the end of the reactor vs. dimensionless time
- 3.At what time does the solution reach a steady state, i.e. how many reactor volumes of solvent will you need?