Statistical and Numerical Methods Exercise 12, HS24

17/12/2024

1 Surface Response Method (core)

The fictional catalyst $In_{2(x)}Al_{2(1-x)}O_3$ doped with Pt is used to hydrogenate CO_2 to dimethyl ether (DME). The postdoc, who is too busy with other projects, asks you to find the optimum Indium fraction x in percent (%) with the optimal platinum doping concentration in parts per million (ppm) for the maximum rate of DME generation [g_{DME} h^{-1} kg_{cat}^{-1}] in your reactor.

- 1. Find the template Template_SurfaceResponse.m online.
- 2. Make a pseudo code with the while/for loops and logic statements needed. Write down the broad calculation required for the surface response method and place them in the pseudo code.
- 3. Implement the **first**-order response surface and confidence interval calculation in your code. In which direction is the steepest gradient? Is there curvature found for the starting point?

 Tip: Use fit([X , Y], Z , 'poly11'); for a first order fit.
- 4. Implement the search in the steepest ascent direction and stop when a maxima is found.
- 5. Implement the **second**-order response surface calculation into your code and find the optimum. Tip: Use fit([X , Y], Z , 'poly22'); for a second order fit.
- 6. Plot the optimum you found with scatter3(X_{optimum}, Y_{optimum}, Z_{optimum}, PointSize, "filled"). Is it close to the global optimum in the plot? What is needed to get closer to the global optimum?
- 7. Optional: Explore changing the starting position, λ , increment values and error amplitude eps in the function experiment (x1, x2). Do you get the same result?

2 Principal Component Analysis

One of the first multivariate data sets was introduced by Sir Ronal Fisher in 1936. This data quantifies the morphologic variation of Iris flowers of three related species.

- 1. Read in the dataset Fisher Iris.xlsx.
- 2. Standardize the four numerical X variables using the function zscore.
- 3. Perform a Principal Component Analysis using the function pca on the standardized data.
- 4. Plot the specific and cumulative variance explained by the principal components normalizing it by the maximal variance explained such that $R_{\text{max}}^2 = 1$.
 - What can you interpret regarding the general correlation structure of the variables?
 - How many 'main effects' seem to be present in the data?
- 5. Plot the loadings and scores of the first two principal components using the function biplot.
 - Can you observe different groups? Distinguish those groups by showing the different flower species
 in different colors and labeling them with their species name using text and an additional scatter
 plot.
 - What can you conclude regarding the correlation of the variables and the 'main effects' in the data?
- 6. Investigate the correlation matrix (using the function corrcoef) to support your first conclusion.

- 7. Which species features most of the abnormal observations?
 - Use the Hotelling's T2 distance in the plane of the first two PCs (t₁ and t₂) for each observation *i* comparing it to a critical value of 6.3 (corresponds to 95 % level)
 - Using the variances of t_1 and t_2 , s_1^2 and s_2^2 , it can be defined as

$$T_i^2 = \frac{t_{i1}^2}{s_1^2} + \frac{t_{i2}^2}{s_2^2}$$

- 8. Which species can be worst explained by the model with two PCs? How could you improve this deviation from the model plane?
 - Calculate the SPE value for each observation comparing it to critical level of 0.6 (corresponds to 95 % level).
 - You can access the residuals using the function pcares.
- 9. What would happen without the initial standardization step?