# Physisorption and pore size analysis

#### Gerhard Pirngruber Direction Catalyse et Séparation gerhard.pirngruber@ifpen.fr



## **CV Gerhard Pirngruber**

- 1995 1999 PhD in heterogeneous catalysis
  - Universiteit Twente (NL)
- **2000 2005 Oberassistent** 
  - ETH Zurich, Inst of Chemical and Bioengineering
  - Research activity
    - zeolites
    - mesoporous silica
- 2005 now R&D Scientist, project leader
  - IFP Energies nouvelles, Catalysis and Separation Division
  - Research activity
    - 2005 2012 : CO2 capture, separation of hydrocarbons
    - 2012 now: hydrotreating and hydrocracking catalysts



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#### Porous solids in catalysis

#### Supported catalysts

- e.g. noble metals, transition metal sulfides
- Porous support
  - provides surface for dispersing the catalyst
  - provides mechanical stability
  - has an influence on diffusion of reactants and products
  - has an influence on adsorption of reactants and products
  - determines reactor volume

#### Porous catalysts

- Zeolites
- Oxydes

Optimising porosity is often the key to improving catalytic performance.



## Types of porosity

- Porous cristalline structures
  - Zeolites,
  - Metal Organic Frameworks



- Ordered or disordered stacking of small particles generates an interparticles porosity
  - oxides (silica, alumina, etc.)
  - activated carbon



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## Characterisation of porosity

#### Physisorption (N<sub>2</sub>, Ar, Kr)

- surface area
- pore volume
- pore size distribution

#### Hg intrusion

- pore volume
- pore size distribution
- surface area
- Imaging methods
  - Transmission Electron Microscopy
  - Secondary Electron Microscopy



## Terminology

- Adsorption is a surface phenomenon.
- Adsorbent = solid that provides a surface for adsorption.
- Adsorbate = molecule adsorbed on the surface.
- Adsorptive = molecule susceptible of being adsorbed.
- Physisorption: no formation of chemical bonds, no transfer of electron density
- Chemisorption: formation of a chemical bond (exchange of electrons)



## Terminology

#### IUPAC distinguishes 3 catagories of pore sizes

- Micropores < 2 nm</p>
- Mesopores 2 50 nm
- Macropores > 50 nm



## Forces involved in physisorption

- van der Waals forces
  - amplified by multiple interactions with atoms or pore wall (i)



maximal when size of adsobate (j) close to pore size



## Forces involved in physisorption

#### Electrostatic forces

- Any non-symmetric charge distribution in the adsorbent generates an electric field
- adsorbates with an electric moment (dipole, quadrupole) interact with the electric field
- undesirable in analysis of porosity/pores size because surface chemistry/chemical composition enter into the game
- N<sub>2</sub> has a small quadrupole moment → use of Ar, Kr is preferable for precise micropore size analysis



## Adsorption in micropores

#### Gradual filling of pore volume starting from surfcae Saturation zone

Transition zone additional adsorbateadsorbate interactions

Initial slope depends on adsorbentadsorbate interactions

#### Pressure

Adsorbed amount









#### Adsorption in macropores



- Opposite pore wall is too far away to influence adsorption and provoke capillary condensation
- First monolayer, then multilayer adsorption



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#### How to measure an adsorption isotherm?

#### Volumetric method





#### Material balance

Reservoir : 1 Sample cell : 2

 without adsorption (He), sample cell initially under vacuum

 $- n_{tot} = \frac{pV_1}{RT_1} + \frac{pV_2}{RT_2} + n_{ads}$ 

with adsorption (N<sub>2</sub>)

determined with He

quantity initially present in the reservoir



## **Experimental difficulties**

#### Precise measurment of pressure required

- difficult at low pressure
- b difficult to measure a micropore distribution

#### Isotherme !!

- T<sub>2</sub> in principle 77 K (temperature of liquid N<sub>2</sub>)
  - part of the cell is not plunged into liquid N2, but is at ambient temperature
  - temperature gradient must be the same as during the initial calibration of the volume with He
- pay attention to the level of liquid N<sub>2</sub>



#### Example zeolite NaX



Micropores are entirely filled at very low pressure.

Isotherm is totally flat once micropores are filled.



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#### Examples - ZnO



#### no micropores

#### mesopores generated by stacking of inidividual particles



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#### Comparison of two ZnO samples



Surface : 65811 > 70299
 Pore size : 70299 > 65811



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## Example – $AI_2O_3$



#### no micropores

high surface area, broad pore size distribution



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## Comparison Al<sub>2</sub>O<sub>3</sub>



Surface : 79999 > 61399 > 47148
Pore size : 47148 > 61399 > 79999



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## Quantitative treatment of N<sub>2</sub> isotherms

#### Pore volume: V<sub>micro</sub>, V<sub>meso</sub>, V<sub>total</sub>

- t-plot
- Dubinin-Radushkevitch
- Surface area
  - BET (Brunauer-Emerett-Teller)
  - Langmuir
- Pore size distribution
  - Micropores
    - Horwath-Kawazoe, Saito-Foley
  - Mesopores

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- BJH (Brunauer-Joyner-Halenda)
- DFT (Density Functional Theory)



#### Determination of the surface area

#### BET (Brunauer Emmet Teller): multilayer adsorption

- first layer: adsorption on the surface
- all the other layers are considered like a condensed liquid



 $n_m$  = number of surface adsorption sites (monolayer)  $n_{ads}$  = total number of adsorbed molecules



## **BET** equation



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#### Exemple ZnO

#### **Isothermes**



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	S <sub>BET</sub> (m²/g)	C <sub>BET</sub>
65811	74	136
70299	36	237

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## Example NaX

- The multilayer adsorption model does not apply well to microporous solids when the pores are filled.
- Choose a lower pressure range for microporous solids.
  - **p**/ $p_0 = 0.05 0.10$
- C constant may be negative.
   Does not make physical sense
  - lower the pressure range further



$$S_{BET} = \frac{4.355}{0.0064 - 0.00003} = 685m^2 / g$$



#### Langmuir Surface Area

#### Langmuir theory

- is a model of monolayer adsorption
- this hypothesis is never fulfilled
- Do not use Langmuir surface areas !!
- S<sub>Langmuir</sub> is always > S<sub>BET</sub> because multilayer adsorption is treated like monolayer adsorption.



#### Determination of the pore volume



In some cases possible without using any model.



#### Conversion gas volume – pore volume

- Volume of adsorbed gas correponds to a certain number of moles
  - STP = Standard Temperature Pressure

T = 273 K, p = 1 bar = 100 kPa

$$n_{ads} = \frac{V_{ads}p}{RT}$$

- The adsorbed phase is considered like a liquid phase
  - Density of liquid N<sub>2</sub> at 77 K : 0.807 g/ml

$$V_p = \frac{m_{N2}}{\rho_{N2,liq}} = \frac{n_{ads} \cdot M_{N2}}{\rho_{N2,liq}}$$

$$V_p(ml/g) = 1.5468 \cdot 10^{-3} \cdot V_{ads}(cm^3 STP/g)$$



## t-plot

- Transform adsorbed amount in an average thickness
   (t) of the adsorbed layer
- For multilayer adsorption on a flat surface





 $\frac{ads}{S}$ 

## Universal curve t vs. $p/p_0$

- The isotherms  $(V_{ads}/S_{BET})$  of many low surface area oxides  $(SiO_2, Al_2O_3, ZrO_2, TiO_2, MgO)$ form a universal curve  $t = f(p/p_0).$
- Numerical description of that curve
  - valid for t = 3.5 10 Å
  - and  $p/p_0 = 0.1 0.8$

Harkins Jura

Halsey





Fig. 12.3. The adsorption of nitrogen on nonporous samples of silica and alumina, the surface areas ranging from 2.6–11.5 m<sup>2</sup> g<sup>-1</sup> for silica and from 58–153 m<sup>2</sup> g<sup>-1</sup> for alumina.  $n/n_{\rm m}$  is plotted against  $p/p^\circ$ . *n* is the number of moles adsorbed per gram of adsorbent and  $n_m$  is the monolayer capacity, expressed in the same units. Line A:  $\bullet =$  silica; + = alumina. Line B: the BET isotherm (Eqn. 12.19) with c values of 100-200.



Isotherm expressed as  $V_{ads} = f(t)$ 



## **Interpretation of t-plots**

#### Adsorption on a non-porous solid





#### Adsorption on a microporous solid

- micropores rapidly filled
- then adsorption on external surface





#### Example zeolite NaX



V<sub>micro</sub> = 175 cm<sup>3</sup> STP/g = 0.271 ml/g



#### Surface BET vs. Surface t-plot



	S <sub>BET</sub> (m²/g)	S <sub>t-plot</sub>
65811	74	70
70299	36	34

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#### Micro- and mesoporous solids





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## t-plot may be ambiguous

#### Zeolite beta with supermicropores

- no clear linear region in the t-plot
- micropore volume depends on the interval chosen for extrapolation



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#### Méthode de Dubinin-Radushkevitch

#### Théorie de remplissage de micropores

$$\frac{V_{ads}}{V_{micro}} = \exp\left[-\left(A/E\right)^2\right] \qquad A = -RT \ln \frac{p}{p_{vap,sat}}$$

- A = potentiel d'adsorption
- E = energie caracteristique de l'adsorbant
- p<sub>vap,sat</sub> = pression vapeur saturante
  - $p_{vap,sat} = p_0 (1 \text{ atm}) \text{ pour } N_2 \text{ à } 77 \text{K}$
- Equation linéarisée

$$\log V_{ads} = \log V_{micro} - D \log \left(\frac{p}{p_0}\right)^2$$



#### Example NaX







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## Average pore size

#### From geometrical rules

• Cylindrical Pore:

• V = pore volume 
$$\begin{cases} V = \pi r^2 h \\ S = surface \end{cases} \quad \begin{cases} V = \pi r^2 h \\ S = 2\pi r h \end{cases} \quad \begin{cases} \frac{S}{V} = \frac{2}{r} \\ \frac{S}{V} = \frac{2}{r} \end{cases} \quad d = \frac{4V}{S} \end{cases}$$

Spherical pore :

$$\begin{cases} V = \frac{4}{3}\pi r^{3} \\ S = 4\pi r^{2} \end{cases}$$

• Slit pore :

$$\begin{cases} V = lhr \\ S = lh \end{cases}$$

 $\frac{S}{V} = \frac{3}{r} \quad d = \frac{6V}{S}$ 

 $\frac{S}{V} = \frac{1}{r} \qquad d = \frac{2V}{S}$ 



#### Mesopore size distribution

#### via the theory of capillary condensation



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V<sub>ads</sub>

## Kelvin equation

## Capillary forces in the pore lower the vapor pressure of the condensed liquid

 $\mu_{cap} = RT ln \frac{p_{cap}}{m}$  $\mu_{vap} = RTln \frac{p_{vap}}{r}$  $p_0$  $p_0$ ΔΙ unconfined liquid capillary

Evaporate n moles from capillary and condense on a flat surface. You have to overcome the capillary forces, i.e. the surface tension γ.

 $W = \Delta A \gamma cos \theta = 2\pi r \Delta l \gamma cos \theta$ 

The work done to overcome the surface tension is equal to change in chemical potential.

$$W = n ln \frac{p_{vap}}{p_{cap}}$$

Explains why vapor pressure of the unconfined liquid is higher than in the capillary.

## **Generalized Kelvin equation**

 $\frac{dV}{dA} = \frac{V_m \gamma cos\theta}{RT ln \frac{p_{cap}}{p_{vap}}}$ 

dV/dA = change in volume per change in interface area Vm = molar volume

#### dV/dA depends on the pore geometry

- Sphere: dV/dA = r/2
- Cylinder dV/dA = r
- Slit dV/dA = d distance between slits

Relation to curvature of the pore

$$\frac{dV}{dA} = \frac{r_m}{2} \qquad \qquad ln\frac{p_{cap}}{p_{vap}} = \frac{2}{r_m}RT\gamma cos\theta$$



#### **Capillary condensation**



- Multilayer adsorption on the surface: layer thickness t 1
  - At a certain effective pore radius r<sub>p</sub>-t, capillary condensation occurs
- Pore is filled. There is a step in the adsorption isotherm.

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#### Example isotherm with hysteresis





## Application of the Kelvin equation



## Origin of the hysteresis

Adsorption: cylindrical meniscus  $r_m = 2r_{eff}$  Desorption: hemisperical meniscus  $r_m = r_{eff}$ 

- The lower r<sub>m</sub>, the lower is the pressure of capillary condensation/evaporation
- $r_{m,ads} = 2 r_{m,des}$
- Capillary evaporation at a lower pressure than capillary condensation
- $\rightarrow$  Hysteresis loop in isotherm



## Origin of the hysteresis

- Truth seems to be complicated than in Cohan's theory.
- Cohan's theory, based on the shape of mensiscus, theory suggests that different vapor liquid equilibria exist in a spherical or cylindrical meniscus, which leads to hysteresis => is an equilibrium picture.
- Molecular simulations (DFT) suggest that adsorption branch is not in thermodynamic equilibrium, but is a metastable state.



## Hysteresis and metastability



- Adsorption branch comprises metastable states.
  - grand free energy of filled pore is lower than that of the empty pore in the hysteresis

- Desorption branch is in thermodynamic equilibrium.
- Reason for metastability in adsorption branch
  - barrier of nucleation by formation of a liquid bridge across the pore
  - condensation occurs when limit of metastability is reached



#### Pore size distribution – BJH model



#### Mathematic description - BJH



- In each desorption step  $p_{n-1} \rightarrow p_n$ , capillary evaporation occurs from a pore of size  $r_{pn}$
- The volume desorbed in that step (∆V<sub>n</sub>) can be related to the pore volume by the geometrical relation given above.
- Complication: Reduction in layer thickness in the pores, which were already emptied, also contribute the pores, which were already emptied, also contribute the provision of porous solids Surface Science and Catalysis Course G Pirngruber 28 october 2014

#### **The BJH-equation**

E.P. Barret, L.G. Joyner, P.P. Halenda, JACS 73 (1951) 373.



capillary evaporation

correction term

For each desorption step the average diameter of the pore, which undergoes capillary evaporation is calculated from the Kelvin equation and the t-plot equation: r<sub>p</sub> = r<sub>k</sub> + t

$$\log \frac{p}{p_0} = 0.034 - \frac{13.99}{t^2}$$
$$\log \frac{p}{p_0} = \frac{-4.14}{r_k}$$

- At is the change in layer thickness in each desorption step
- $\Delta V_n$  is the volume desorbed in each step
- $\rightarrow\,$  A plot of pore volume vs. pore radius is obtained.



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## Limits of the BJH-model

- BJH underestimates the pore size below 7.5 nm WHY?
  - Model separates the adsorbed film and the capillary condensate – not a realistic picture
  - Fluid-wall interactions are neglected
  - Kelvin equation may not be valid in very narrow pores
    - Surface tension might increase with curvature
- One should speak about a BJH-value rather than pore diameter.



## Adsorption vs. desorption isotherm

- Adsorption isotherm Pros and cons
  - Condensation can be delayed not in thermodynamic equilibrium
  - Cylindrical meniscus not stable not advisable to use adsorption branch for cylindrical pores
- Desorption branch Pros and cons
  - Evaporation not delayed, in thermodynamic equilibrium generally preferred
  - Ink-bottle type pores: smallest openening determines the desorption
  - In a network of interconnected pores: percolation (transport) effects determine the desorption
  - Conclusion: look at both and compare them



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#### Ink-bottle pores



- In desorption smallest pore openening is determining.
- When pressure of capillary evaporation is reached for the smallest pore opening, whole pore is suddenly emptied.
  - Sudden drop in the desorption isotherm type H2



## Pore network effects



N<sub>2</sub> can only desorb from pore A and C if pore B has already been emptied.

Seaton, CES, 1991.

 Desorption branch of isotherm not in thermodynamic equilibrium any more, due to pore blocking.

- Desorption is controlled by a percolation process.
  - probability that the pore is connected to the outer surface.







- If pore size distribution is calculated from desorption branch, an artificially narrow pore size distribution is obtained
- The adsorption branch has to be used to calculate the pore size distribution.



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#### Ink-bottle type hysteresis loop



 Narrow peak in the pore size distribution of the adsorption branch is an artefact caused by the forced closure of the isotherm at p/p<sub>0</sub> = 0.43

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#### Isotherm without hysteresis loop





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## Closure point of the isotherm

- Critical temperature inside a pore lower than in bulk: T<sub>c,pore</sub> < T<sub>c, bulk</sub>
- T<sub>c,pore</sub> decreases with decreasing pore diameter<sup>1</sup>
- Above T<sub>c</sub> no condensate-vapour meniscus
- For narrow pores T<sub>c</sub> < 77 K</p>
- No hysteresis for filling and emptying of these pores
- $T_{c,pore} < 77$  K for pores, which show capillary condensation at  $p/p_0 = 0.4 \rightarrow closure point of isotherm$
- $T_c(Ar) > T_c(N_2) \rightarrow Ar$  isotherms show hysteresis when  $N_2$  isotherms don't<sup>2</sup>

[1] R. Evans, J. Phys. Condensed Matter 2 (1990) 8989.[2] M. Thommes, R. Köhn, M. Fröba, J.Phys.Chem. B 104.

## Summary – Pore size analysis

- BJH relies on Kelvin equation and the universal tcurve for determining pore size distribution
  - both concepts have weaknesses
- Alternative methods exist
  - Density Functional Theory
  - Broekhoff de Boer improvement of BJH
  - Derjaguin concept of disjoining pressure
    - surface tension concept that takes interaction with solid into account
- Every model assumes a certain pore geometry (cylindrical, spherical, slit-shaped) – influences the results!!
- The adsorption and the desorption branch contain Chara different information deat look at both 28 october 2014



#### Literature

#### Textbooks on adsorption

- D.A. Ruthven, Principles of Adsorption and Adsorption Processes, Wiley
- D.D. Do, Adsorption Analysis: Equilibria and Kinetics, Imperial College Press
- Review articles discussing a more moderne view of hysteresis effects and pore size analysis
  - P.A. Monson, Understanding adsorption/desorption hysteresis for fluids in mesoporous materials using simple molecular models and classical density functional theory, Microporous Mesoporous Materials 160 (2012) 47.
  - B. Coasne et al., Adsorption, intrusion and freezing in porous silica: the view from the nanoscale, Chem. Soc. Rev. 42 (2013) 4141.

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# Alternative explanation of the Kelvin equation

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## Physical principles of capillary condensation

#### Vapour pressure of a liquid under external pressure

External pressure



 $p_g =$  new vapour pressure of  $H_2O$   $p_{g0} =$  original vapour pressure of  $H_2O$   $\Delta p_1 =$  external pressure on liquid ( $H_2O$ ), which induces the change in vapour pressure

$$v_1$$
 = molar volume of liquid (H<sub>2</sub>O)

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- Equibrium gas-liquid μ<sub>g</sub> = μ<sub>l</sub> vapour pressure p<sub>g,0</sub>
- Equilibrium disturbed by external pressure

$$\begin{array}{l} d\mu_g = d\mu_l \ \rightarrow \ v_l \ dp_l = v_g \ dp_g \\ v_l \ dp_l = RT/p_g \ ^* \ dp_g \\ v_l \Delta p_l = RT \ ln \ (p_g/p_{g0}) \end{array}$$

 $p_g = p_{g,0} \cdot \exp(\frac{v_l}{RT} \Delta p_l)$ 



Vapour pressure of a drop of liquid

$$p_{in} - p_{out} = \frac{2\gamma}{r}$$

 $\gamma$  = surface tension r = radius of curvature

$$p_l - p_{out} = \frac{2\gamma}{r}$$





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Vapour pressure of a liquid void



$$p_g = p_{g,0} \cdot \exp(-\frac{2v_l \gamma}{RT \cdot r})$$

Kelvin equation: vapour pressure inside a void is lowered

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