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Alternative Approach for the Determination of Mean Free Paths of Electron Scattering in Liquid Water Based on Experimental Data

Axel Schild,* Michael Peper, Conaill Perry, Dominik Rattenbacher, and Hans Jakob Wörner

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ABSTRACT: Mean free paths of low-energy electrons in liquid water are of importance for modeling many physicochemical processes, but neither theoretical predictions nor experimental results have converged for these parameters. We therefore introduce an approach to determine elastic and inelastic mean free paths (EMFP, IMFP) based on experimental data. We show that ab initio calculations of electron scattering with water clusters converge with cluster size, thus providing access to condensed-phase scattering. The results are used in Monte Carlo simulations to extract EMFP and IMFP from recent liquid-microjet experiments that determined the effective attenuation length (EAL) and the photoelectron angular distribution (PAD) following oxygen 1s-ionization of liquid water. For electron kinetic energies from 10 to 300 eV, we find that the IMFP is noticeably larger than the EAL. The EMFP is longer than that of gas-phase water and the IMFP is longer compared to latest theoretical estimations, but both EMFP and IMFP are much shorter than suggested by experimental measurements of integral cross sections for amorphous ice.



K nowledge of the scattering properties of electrons in liquid water is vital for understanding and for modeling many physicochemical processes, for example, the effect of radiation damage in living tissue.¹⁻³ To accurately model the interaction of electrons with water molecules, e.g., with Monte Carlo simulations,^{4,5} the differential scattering cross sections (DCS) as well as the total cross sections for many possible types of interactions are needed. Those quantities are experimentally accessible for gas-phase water,⁶⁻⁹ but for water in the liquid phase they are difficult to obtain.

Instead of the cross sections, the elastic mean free path (EMFP) and the inelastic mean free path (IMFP) for a given electron kinetic energy (eKE) can be used as a measure for the probability to scatter. The IMFP is a particularly relevant parameter because it represents the effective path length that an electron can travel in liquid water before it scatters inelastically, thereby losing some of its energy and thus changing the probability of damaging solvated molecules. Hence, there has been much interest in determining the IMFP theoretically as well as experimentally: On the one hand, there have been a number of theoretical estimations of the IMFP.¹⁰⁻²² Especially for eKE below 100 eV, the often utilized models, which are based on the dielectric function, have limitations that need to be overcome. These include, e.g., the neglect of electron-exchange effects and an overestimation of the needed energy-loss function in the presence of an energy gap in the excitation spectrum (see Emfietzoglou et al.¹⁸ and Nguyen-Truong²² for details). On the other hand, the mean free path is a quantity that eludes direct measurements. What has been measured directly, however, are the effective attenuation lengths (EAL) of electrons in liquid water²³⁻²⁵ and the photoelectron angular distributions (PAD) of electrons generated through core-level ionization inside liquid water.²⁶ While the EAL provides a lower bound for the IMFP, the measured PAD of liquid water was used to estimate the IMFP directly with a simplified model. It was found that for an eKE below ≈ 100 eV, the IMFP appears to be considerably shorter and flatter than previously assumed.²⁶ A recent improvement of the theoretical algorithms used to determine the IMFP within the dielectric formalism yielded results that qualitatively agree with the experimental observations.²²

There have also been attempts to determine scattering cross sections from photoelectron imaging of water droplets²⁷ with the surprising finding that the IMFP and scattering cross sections²⁸ were identical to those measured for amorphous ice.²⁹ In a subsequent work,³⁰ attempts were made to explain angle-resolved photoelectron-imaging results for water clusters with the cross sections from ref 28, but they had to be rescaled to qualitatively reproduce the experimental results. Discussions of these previous results in the literature^{19,31} show that it is thus appropriate to conclude that there is no consensus regarding the EMFP and IMFP values for electron scattering in liquid water, neither from theoretical nor from experimental approaches. This situation motivates the present work.

In the following, we present an alternative approach to determine the EMFP and IMFP of electron scattering in liquid

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water based on experimental data. Our approach relies on extensive *ab initio* quantum-scattering calculations of electrons with water clusters of variable size to achieve a first-principles description of electron scattering in liquid water. The approach includes, at a quantum-mechanical level, the key characteristics that distinguish electron scattering in the gas and condensed phases. These differences originate from (i) multiple-scattering and interference effects originating from scattering at neighboring molecules in the condensed phase and (ii) the modification of the electronic structure of the water molecules through condensation. Verifying the convergence of our scattering calculations with respect to cluster size ensures that the relevant effects have been taken into account.

We then use Monte Carlo electron-trajectory calculations to connect these ab initio results with experimental observables. To uniquely determine EMFP and IMFP values that are consistent with experimental observations, we need two independent measurements. For this purpose, we chose the measurements of the EAL by Suzuki et al.²⁵ and of the PAD by Thürmer et al.,²⁶ both realized by ionizing the oxygen 1s orbital of liquid water in microjets. We use classical-trajectory Monte Carlo simulations to describe the electron transport. Such calculations are expected to be valid for kinetic energies above ca. 10 eV, where quantum-interference effects have been shown to become negligible.³² In our approach, the only free parameters are the EMFP and the IMFP, while all other input parameters are determined from *ab initio* calculations or from the measurements. The assumptions made in the Monte Carlo simulations are described in the Supporting Information.

The EMFP and IMFP are defined by assuming that for both elastic and inelastic scattering, the probability of not having scattered until a distance r is

$$P(r) = \frac{1}{r_{\rm MFP}} e^{-r/r_{\rm MFP}}$$
(1)

Then, $\int_0^\infty r P(r) dr = r_{\text{MFP}}$ is the corresponding mean free path.

The EAL is a distance parameter that describes the exponential decay of the number of electrons S(z) detected outside the liquid,

$$S(z) \propto \exp(-z/r_{\rm EAL})$$
 (2)

as a function of the distance z from their point of creation to the surface. It is measured for an eKE corresponding to the kinetic energy after ionization. Since the depth of the conduction band (the electron affinity) of liquid water is well below 1 eV,³³⁻³⁵ we neglect it due to the comparably high eKE \geq 10 eV that we consider. The EAL is related to the IMFP, because inelastic scattering is responsible for the loss of signal S(z) with starting depth z of the electron, and the EAL is a lower bound for the IMFP.

For an isotropic sample ionized with linearly polarized light, the PAD relative to the direction of polarization is given by³⁶

$$PAD(\theta) \propto 1 + \beta P_2(\cos \theta)$$
 (3)

where θ is the polar angle, P_2 is the Legendre polynomial of second order, and β is the asymmetry parameter. The PAD of photoemission from a dense medium is closely related to the mean number of elastic collisions before inelastic scattering occurs,

$$\langle N_{\rm ela} \rangle = \frac{r_{\rm IMFP}}{r_{\rm EMFP}}$$
(4)

because each elastic collision changes the angular distribution of the electrons at the observed eKE.

The DCS for electronically, vibrationally, and rotationally elastic $(J = 0 \rightarrow J' = 0)$ scattering are computed with the program ePolyScat^{37,38} for water clusters of different sizes and shapes with nuclear configurations taken from Temelso et al.,³⁹ and also for some structures based on the modeling of experimental data for the first solvation shell of liquid water.⁴⁰ ePolyScat solves the variational Schwinger equation using single-center expansions, and we use molecular-orbital data from Hartree–Fock calculations with a cc-pVTZ basis set obtained with the program Gaussian⁴¹ as input.

The most important result from these calculations is that the DCS rapidly converge with the number of water molecules in the cluster (see Figure S1 of the Supporting Information). With increasing kinetic energy, the DCS are found to converge more rapidly as a function of cluster size. These observations can be intuitively explained by relating the de-Broglie wavelength λ_{dB} of the scattering particle to the extension of the target. Whereas the molecular-level description of a 10 eV electron ($\lambda_{dB} \approx 3.9$ Å) collision requires a cluster of 6–7 water molecules to reach convergence, a 50 eV electron ($\lambda_{\rm dB} \approx$ 1.7 Å) collision is well described by a much smaller cluster. The observed rapid convergence of the DCS suggests that such cluster calculations can be a good approximation for the DCS of bulk liquids.⁴² In the present work, we used the DCS of the largest considered cluster, $(H_2O)_7$, to describe the DCS of bulk water.

The Monte Carlo trajectory calculations were realized with the Python module CLstunfti, which is available at https:// gitlab.com/axelschild/CLstunfti. Here, we only give a brief overview of the computational model: Electrons at a given eKE are represented by classical trajectories, and an EMFP and IMFP are chosen for the simulation. To simulate ionization, an ionization depth z is selected and initial directions for the trajectories are sampled from the experimental gas-phase PAD. To account for inelastic scattering, each trajectory is given a random maximum path length to travel according to the distribution (1) and using $r_{\rm MFP} = r_{\rm IMFP}$. It is assumed that inelastic scattering happens at this distance and that if this happens, the electron is no longer detected within the relevant eKE range. This separation of scattering into elastic and inelastic events is based on the experimental observation of well separated groups of primary and secondary electrons. Only the primary electrons, which form a well-defined Gaussian distribution of ~1.5 eV width are detected in the simulated photoelectron experiments. The secondary electrons, which have experienced one or more electronically inelastic scattering events corresponding to an energy loss of 7 eV or more, are not considered. To propagate the trajectories after the ionization event, a travel distance is selected randomly for each trajectory according to the distribution (1) with $r_{\rm MFP} = r_{\rm EMFP}$. If the trajectory ends outside the liquid (the liquid surface is located at z = 0, i.e., it is flat) or if its path is longer than the maximum path length for the trajectory (i.e., when inelastic scattering would happen), it is counted to the measured signal or it is discarded, respectively. If this is not the case, elastic scattering happens, the position of the trajectory is updated and a new direction is chosen according to the DCS. This last step is repeated until all trajectories have either



Figure 1. Top: contour plots of the effective attenuation length EAL (left) and the β -parameter describing the photoelectron angular distribution of the liquid (right) depending on the value of the elastic mean free path (EMFP) and the average number of elastic collisions $\langle N_{ela} \rangle$. Bottom: line plots of the EAL depending on $\sqrt{\langle N_{ela} \rangle}$ for fixed EMFP (left) and depending on the EMFP for fixed $\langle N_{ela} \rangle$ (right). Small vertical lines indicate the standard deviation of the fit to (2). The plots show results for an electron kinetic energy of 20 eV and the differential scattering cross sections obtained with ePolyScat for (H₂O)₇ clusters.

reached the surface (contributing to the measured signal) or have been discarded due to their path being longer than the preselected maximum path.

To simulate the EAL measurement, the ionizing beam is assumed to have a polarization vector that is perpendicular to the water surface and the number of escaped electrons is counted depending on the chosen starting depth z of the trajectories. For the simulation of the PAD of the liquid phase, random starting depths are chosen. As done in the experiment, the direction of the polarization vector of the ionizing beam is varied. In both experiments, the escaped electrons are counted if they exit with a small polar angle. Ideally, the detection angle should be very small. In the simulations we chose it to be 1°, but the results discussed in the following are not very sensitive to this angle as long as it is chosen to be small enough. Test calculations with collection angles of 15° (which are approximately the experimental collection angles) yield similar numerical results compared to the ones presented below. We also use importance sampling with an exponential distribution for the initial starting depths of the trajectories to make the simulation more efficient, as trajectories starting deep inside the liquid have a low probability of reaching the surface due to inelastic scattering.

We start the discussion of the results with those observations that we expect to have a general character and could thus be useful in interpreting other experimental results. To the best of our knowledge, these dependencies have not been reported before. Figure 1 illustrates the dependence of the experimental observables EAL and β on the EMFP and the average number of elastic collisions $\langle N_{\rm ela} \rangle$ for an eKE of 20 eV. We recall that $\langle N_{\rm ela} \rangle$ encodes the dependence on the IMFP via (4). We find that (i) for fixed EMFP the EAL is increasing as $\sqrt{\langle N_{ela} \rangle}$, (ii) for fixed EMFP the parameter β is decreasing as $1/\langle N_{ela} \rangle$ within the investigated range (top and bottom-left panels of Figure 1), (iii) for fixed $\langle N_{ela} \rangle$ the EAL is proportional to the EMFP, and (iv) for fixed $\langle N_{ela} \rangle$ the parameter β is independent of the EMFP (top and bottom-right panels of Figure 1). The reasons for these dependencies are the following: The (in)dependencies (iii) and (iv) on the EMFP can be explained by a scaling argument: For fixed $\langle N_{ela} \rangle$, it follows from (4) that trajectories from a simulation with $r_{\text{EMFP}} = r_2$ are equivalent to those for $r_{\text{EMFP}} = r_1$ if scaled by the factor r_2/r_1 . The scaling leaves the final PAD invariant and changes the depth distribution from which the measured trajectories originate linearly with the EMFP. The linear dependence (i) of the EAL on $\sqrt{\langle N_{\rm ela} \rangle}$ is due to scattering of trajectories into other

directions than the forward direction—the EAL is for the trajectories like the root-mean-square translation distance of a random walk, which also scales like \sqrt{n} where *n* is the number of steps.⁴³ All dependencies are monotonic; hence, a set of values for the EAL and β corresponds to a unique set of values for the EMFP and IMFP. These dependencies also illustrate a general protocol for analyzing the experimental results. The measurement of β uniquely defines $\langle N_{\rm ela} \rangle$, i.e., the ratio of IMFP to EMFP, when the elastic DCS is known. Knowing $\langle N_{\rm ela} \rangle$, the measurement of the EAL uniquely defines the EMFP, which in turn defines the IMFP. As a consequence, an overestimation of the EAL would result in EMFP and IMFP values that are both too long by the same factor. Errors in the measurement of β would affect the ratio of IMFP to EMFP.

We now turn to the discussion of the mean free paths obtained from the analysis of the experimental results. The top panel of Figure 2 shows the dependencies of the retrieved EMFP and IMFP (blue and orange triangles, respectively) on the eKE. For comparison, the experimentally determined EAL used in the simulations is shown (stars), as well as literature values for the EMFP corresponding to the total elastic scattering cross section for gas-phase water,^{11,44} and the most recent theoretical estimation of the IMFP for liquid water (lines).²² Figure 2 also contains the mean free paths for purely elastic, quasi-elastic (i.e., including all inelastic processes with energy losses of up to 1 eV) and electronically inelastic scattering determined by Michaud et al.²⁹ from experiments on amorphous ice. We note that all cross sections reported by Luckhaus et al. 28 are identical to those of Michaud et al. 29 for all energies (from 1.7 eV upward) reported in the latter. A comparison to the many other estimations of the IMFP can, e.g., be found in Nguyen-Truong.²²

The EMFP determined in our work (orange triangles) is larger by a factor of 2–3 compared to previous estimates based on gas-phase data (orange line). It is smaller by a factor of 2–4 than the quasi-elastic mean free paths of Michaud et al.²⁹ (orange tripods). We note that the purely elastic EMFP of Michaud et al.²⁹ (brown tripods) is more than one order of magnitude longer than our EMFP and up to two orders of magnitude longer than the previous estimates.

The IMFP determined in our work (blue triangles) is found to be longer than the latest theoretical estimate²² (blue line) by a nearly constant factor of ~2. Our IMFP is smaller than the electronic IMFP determined by Michaud et al.²⁹ (blue tripods) by up to one order of magnitude at 10 eV but seems to merge with the latter around 80 eV. Our IMFP is longer than the experimental EAL by a factor of ~3 for an eKE of 10 eV, getting closer to the EAL for higher eKE, but always remaining longer than the EAL, as required. In our simulations, we find that the EAL becomes equal to the IMFP only if we set the EMFP to be very long such that no elastic scattering happens at all.

For eKE \geq 60 eV, both the IMFP and EMFP are larger than the EAL and comparable in magnitude. The EMFP eventually becomes somewhat larger than the IMFP for eKE \geq 100 eV, which is lower than the crossing point of the previous estimates around 200 eV. This does not mean, however, that elastic scattering becomes unimportant in the photoelectron experiments. A significant influence of elastic scattering at these high eKE can indeed be deduced from the experimental data because the PAD for the liquid phase remains different from that of the gas phase up to an eKE of 300 eV.²⁶ We will return to this point below.



Figure 2. Top: elastic (EMFP) and inelastic (IMFP) mean free paths from our simulation. For comparison, the measured elastic mean free paths (EAL, extracted from Suzuki et al.²⁵) as well as the EMFP from Tomita et al.¹¹ (corresponding to the integrated scattering cross sections for gas-phase water from Märk et al.⁴⁴), the IMFP from Nguyen-Truong,²² and mean free paths obtained from Michaud et al.²⁹ for amorphous ice are shown. The elastic (λ_{ela}), quasi-elastic (λ_{qela}), and inelastic (λ_{inel}) mean free paths for Michaud et al.²⁹ are obtained from the (integral) cross sections of the first column of Table 2, the sum of the cross sections for all columns of Table 2 and of all but "Others" in Table 3, and the cross sections "Others" in Table 3 of that reference, respectively. Bottom: average number of elastic collisions (N_{ela}). The values from Thürmer et al.²⁶ are shown for comparison.

It is also interesting to note that our EMFP and IMFP values display an energy dependence very similar to the literature values but are consistently longer by a factor of $\sim 2-3$. This means that both sets of data, although completely independent, agree on the ratio of IMFP to EMFP, hence on $\langle N_{ela} \rangle$. Assuming that this ratio is correct, the vertical offset of our values of EMFP and IMFP can be traced back to the experimental EAL since, as we showed above, both the EMFP and the IMFP scale linearly with the input EAL for a fixed $\langle N_{ela} \rangle$. A reduction of the EAL by a factor of ~3 would bring our EMFP and IMFP values into agreement with the previous estimates. What speaks in favor of such a correction are the expectations that (i) the dielectric formalism used to determine the IMFP from the measured energy-loss function of liquid water should be accurate above 100 eV^{22} and (ii) the EMFP of liquid water might be expected to converge to that of isolated molecules for sufficiently high kinetic energies of a few

hundred electronvolts, where the electron scattering is dominated by core-shell electrons that are not affected by solvation and multiple scattering is negligible. What speaks against such a correction are the experimental results of Michaud et al.²⁹ on amorphous ice, which would then lie even much further away from those for liquid water.

The bottom panel of Figure 2 shows the average number of elastic collisions $\langle N_{\rm ela} \rangle$ obtained from the present results (triangles) in comparison to a previous analysis of the measured β -parameters for the gas-phase and for liquid water by Thürmer et al.²⁶ Also in this case, the $\langle N_{ela} \rangle$ agree reasonably well. This is, however, a coincidence. In the analysis of the experimental results by Thürmer et al.²⁶ $\langle N_{ela} \rangle$ was estimated by successive convolution of the PAD of the gas phase with a DCS originating from an educated guess until the measured PAD of the liquid was obtained. This analysis has two potential deficiencies: A minor problem is that a convolution with the DCS to account for multiple collisions is incorrect for the three-dimensional problem. Instead, for a DCS $D_{\rm S}(\theta)$ with polar angle θ , the angular distribution in the bulk $D^{(n+1)}(\theta)$ after n + 1 collisions is obtained from that after n collisions as

$$D^{(n+1)}(\theta) = \int_{0}^{\pi} \int_{0}^{2\pi} D^{(n)}(\vartheta) D_{S}(\vartheta') \sin(\vartheta) \, d\vartheta \, d\varphi$$
(5)

with

$$\cos \vartheta' = \cos(\vartheta) \cos(\theta) + \cos(\varphi) \sin(\vartheta) \sin(\theta) \tag{6}$$

The difference to a convolution is small but noticeable, as shown in the Supporting Information.

More important is the neglect of surface effects in the analysis of Thürmer et al.,²⁶ as (5) is only valid in the bulk. Due to the relatively short EAL, in the experiment the contribution from water molecules ionized close to the surface is important. If initially emitted in the direction of the detector, the corresponding electrons cannot scatter as often as those ionized deeper inside the bulk. Hence, to generate the same final angular distribution, electrons ionized deeper in the liquid have to contribute, which requires more elastic collisions and, consequently, a larger IMFP.

The influence of the surface is illustrated in Figure 3, where the PAD is shown after n collisions as determined inside the liquid and outside the liquid, for an eKE of 20 eV and for an EMFP of 0.2 nm. For the latter case, an average over the distance of the ionization site from the surface was performed. While in the bulk about four collisions are needed to obtain the measured distribution of the liquid, more than 10 collisions are needed if the surface effect is taken into account. The inclusion of the surface in the simulation is thus crucial for the analysis of the measurement. Nevertheless, the difference of the $\langle N_{\rm ela} \rangle$ shown in Figure 2 is small, because we find larger EMFP values compared to the values used by Thürmer et al.²⁶ Before concluding, we note that the EMFP and IMFP values determined in our work are related to physical ab initio DCS used in our simulations. This must be kept in mind, both when comparing our results with other sources, some of which assume isotropic scattering and the associated transport cross sections,45 and when using our results in simulations. In Table 1 of the Supporting Information, a numerical factor is provided that can be used to convert our mean-free paths to those corresponding to the transport cross section.



Figure 3. Photoelectron angular distribution (PAD, scaled such that the maximum is 1) for oxygen-1s ionization of liquid water after scattering in the bulk only (left) and determined outside the liquid (right). The kinetic energy of the scattered electron is 20 eV and the elastic mean free path is set to 0.2 nm. Starting from the initial PAD (dotted line) each line above corresponds to one additional collision. The dotted and dash-dotted line correspond to measured PADs of the gas-phase and the liquid-phase oxygen 1s electrons from Thürmer et al.²⁶

In conclusion, we have introduced a novel, straightforward, and general method to obtain the EMFP and IMFP of electrons scattering in liquids that is based on the simulation of two types of experiments. Our approach is possible due to the discovery of a rapid convergence of the DCS of water clusters with cluster size, which provides the first ab initio molecularlevel description of electron scattering in liquid water. It is found that to be consistent with the measured EAL and PAD of soft-X-ray photoelectron experiments, the liquid-phase IMFP must be longer than the latest estimate from the dielectric formalism²² and the liquid-phase EMFP must be longer than that obtained from scattering data of gas-phase water,¹¹ respectively. We also find that on average only few elastic collisions are possible before inelastic scattering occurs even for relatively low eKE, but that elastic scattering remains important for eKE values up to 300 eV. In the studied photoelectron experiments, the importance of elastic scattering is accentuated by the surface sensitivity resulting from the EAL.

The reliability of the mean free paths obtained in our work depends on the accuracy of the experimental input as well as on the accuracy of the DCS used for bulk liquid water. The sensitivity of the retrieved mean free paths on the input parameters is illustrated in Figure S3 of the Supporting Information. Hence, further experimental studies would be highly desirable and we hope that our analysis will stimulate additional measurements, also on other liquids. The program code used for this work is available as Python module at https://gitlab.com/axelschild/CLstunfti and can be used to obtain improved values for the EMFP and IMFP when additional experimental or theoretical data becomes available. We expect that our method to determine the mean free paths will become a powerful tool for understanding electron scattering in liquid media, when combined with accurate experimental and theoretical input data. This opens the door

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for gaining better knowledge of the properties of liquid water, for the exploration of the scattering properties of other liquids, and for the interpretation of attosecond time-resolved measurements in the liquid phase.^{46,47}

ASSOCIATED CONTENT

1 Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpclett.9b02910.

Information about the calculated DCS, the model for the Monte Carlo simulations, test calculations of the meanfree paths, and estimation of the number of elastic collisions if the presence of the surface is ignored (PDF)

AUTHOR INFORMATION

Corresponding Author

Axel Schild – ETH Zürich, Laboratorium für Physikalische Chemie, 8093 Zürich, Switzerland; orcid.org/0000-0002-0852-0938; Email: axel.schild@phys.chem.ethz.ch

Authors

Michael Peper – ETH Zürich, Laboratorium für Physikalische Chemie, 8093 Zürich, Switzerland

- **Conaill Perry** ETH Zürich, Laboratorium für Physikalische Chemie, 8093 Zürich, Switzerland
- **Dominik Rattenbacher** ETH Zürich, Laboratorium für Physikalische Chemie, 8093 Zürich, Switzerland; Max Planck Institute for the Science of Light, 91058 Erlangen, Germany

Hans Jakob Wörner – ETH Zürich, Laboratorium für Physikalische Chemie, 8093 Zürich, Switzerland; Octid.org/ 0000-0002-8877-0872

Complete contact information is available at: https://pubs.acs.org/10.1021/acs.jpclett.9b02910

Notes

The authors declare no competing financial interest.

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REFERENCES

(1) Wang, C.-R.; Nguyen, J.; Lu, Q.-B. Bond Breaks of Nucleotides by Dissociative Electron Transfer of Nonequilibrium Prehydrated Electrons: A New Molecular Mechanism for Reductive DNA Damage. *J. Am. Chem. Soc.* **2009**, *131*, 11320–11322.

(2) Kumar, A.; Sevilla, M. D. Proton-Coupled Electron Transfer in DNA on Formation of Radiation-Produced Ion Radicals. *Chem. Rev.* **2010**, *110*, 7002–7023.

(3) Nikjoo, H.; Emfietzoglou, D.; Liamsuwan, T.; Taleei, R.; Liljequist, D.; Uehara, S. Radiation track, DNA damage and response – a review. *Rep. Prog. Phys.* **2016**, *79*, 116601.

(4) Champion, C. Theoretical cross sections for electron collisions in water: structure of electron tracks. *Phys. Med. Biol.* **2003**, *48*, 2147–2168.

(5) Shin, W.-G.; Bordage, M.-C.; Emfietzoglou, D.; Kyriakou, I.; Sakata, D.; Min, C. H.; Lee, S. B.; Guatelli, S.; Incerti, S. Development of a new Geant4-DNA electron elastic scattering model for liquidphase water using the ELSEPA code. *J. Appl. Phys.* **2018**, *124*, 224901. (6) Katase, A.; Ishibashi, K.; Matsumoto, Y.; Sakae, T.; Maezono, S.; Murakami, E.; Watanabe, K.; Maki, H. Elastic scattering of electrons by water molecules over the range 100–1000 eV. *J. Phys. B: At. Mol. Phys.* **1986**, *19*, 2715–2734.

(7) Cho, H.; Park, Y. S.; Tanaka, H.; Buckman, S. J. Measurements of elastic electron scattering by water vapour extended to backward angles. *J. Phys. B: At., Mol. Opt. Phys.* **2004**, *37*, 625–634.

(8) Khakoo, M. A.; Silva, H.; Muse, J.; Lopes, M. C. A.; Winstead, C.; McKoy, V. Electron scattering from H₂O: Elastic scattering. *Phys. Rev. A: At., Mol., Opt. Phys.* **2008**, 78, 052710.

(9) Khakoo, M. A.; Silva, H.; Muse, J.; Lopes, M. C. A.; Winstead, C.; McKoy, V. Erratum: Electron scattering from H₂O: Elastic scattering [Phys. Rev. A 78, 052710 (2008)]. *Phys. Rev. A: At., Mol., Opt. Phys.* **2013**, 87, 049902.

(10) Ashley, J. Interaction of low-energy electrons with condensed matter: stopping powers and inelastic mean free paths from optical data. J. Electron Spectrosc. Relat. Phenom. **1988**, 46, 199–214.

(11) Tomita, H.; Kai, M.; Kusama, T.; Ito, A. Monte Carlo simulation of physicochemical processes of liquid water radiolysis. *Radiat. Environ. Biophys.* **1997**, *36*, 105–116.

(12) Dingfelder, M.; Hantke, D.; Inokuti, M.; Paretzke, H. G. Electron inelastic-scattering cross sections in liquid water. *Radiat. Phys. Chem.* **1998**, *53*, 1–18.

(13) Akkerman, A.; Akkerman, E. Characteristics of electron inelastic interactions in organic compounds and water over the energy range 20 – 10000 eV. J. Appl. Phys. **1999**, 86, 5809–5816.

(14) Pimblott, S. M.; Siebbeles, L. D. Energy loss by non-relativistic electrons and positrons in liquid water. *Nucl. Instrum. Methods Phys. Res., Sect. B* **2002**, *194*, 237–250.

(15) Emfietzoglou, D.; Nikjoo, H. The Effect of Model Approximations on Single-Collision Distributions of Low-Energy Electrons in Liquid Water. *Radiat. Res.* **2005**, *163*, 98.

(16) Emfietzoglou, D.; Nikjoo, H. Accurate Electron Inelastic Cross Sections and Stopping Powers for Liquid Water over the 0.1–10 keV Range Based on an Improved Dielectric Description of the Bethe Surface. *Radiat. Res.* **2007**, *167*, 110.

(17) Emfietzoglou, D.; Kyriakou, I.; Abril, I.; Garcia-Molina, R.; Nikjoo, H. Inelastic scattering of low-energy electrons in liquid water computed from optical-data models of the Bethe surface. *Int. J. Radiat. Biol.* **2012**, *88*, 22–28.

(18) Emfietzoglou, D.; Kyriakou, I.; Garcia-Molina, R.; Abril, I. Inelastic mean free path of low-energy electrons in condensed media: beyond the standard models. *Surf. Interface Anal.* **2017**, *49*, 4–10.

(19) Shinotsuka, H.; Da, B.; Tanuma, S.; Yoshikawa, H.; Powell, C. J.; Penn, D. R. Calculations of electron inelastic mean free paths. XI. Data for liquid water for energies from 50eV to 30 keV. *Surf. Interface Anal.* **2017**, *49*, 238–252.

(20) Garcia-Molina, R.; Abril, I.; Kyriakou, I.; Emfietzoglou, D. Inelastic scattering and energy loss of swift electron beams in biologically relevant materials. *Surf. Interface Anal.* **2017**, *49*, 11–17.

(21) Emfietzoglou, D.; Papamichael, G.; Nikjoo, H. Monte Carlo Electron Track Structure Calculations in Liquid Water Using a New Model Dielectric Response Function. *Radiat. Res.* **2017**, *188*, 355.

(22) Nguyen-Truong, H. T. Low-energy electron inelastic mean free paths for liquid water. J. Phys.: Condens. Matter 2018, 30, 155101.

(23) Ottosson, N.; Faubel, M.; Bradforth, S. E.; Jungwirth, P.; Winter, B. Photoelectron spectroscopy of liquid water and aqueous solution: Electron effective attenuation lengths and emission-angle anisotropy. *J. Electron Spectrosc. Relat. Phenom.* **2010**, *177*, 60–70 Special issue "Water and Hydrogen Bonds".

(24) Buchner, F.; Schultz, T.; Lübcke, A. Solvated electrons at the water-air interface: surface versus bulk signal in low kinetic energy photoelectron spectroscopy. *Phys. Chem. Chem. Phys.* **2012**, *14*, 5837–5842.

(25) Suzuki, Y.-I.; Nishizawa, K.; Kurahashi, N.; Suzuki, T. Effective attenuation length of an electron in liquid water between 10 and 600 eV. *Phys. Rev. E* 2014, *90*, 010302.

(26) Thürmer, S.; Seidel, R.; Faubel, M.; Eberhardt, W.; Hemminger, J. C.; Bradforth, S. E.; Winter, B. Photoelectron Angular

Distributions from Liquid Water: Effects of Electron Scattering. *Phys. Rev. Lett.* **2013**, *111*, 173005.

(27) Signorell, R.; Goldmann, M.; Yoder, B. L.; Bodi, A.; Chasovskikh, E.; Lang, L.; Luckhaus, D. Nanofocusing, shadowing, and electron mean free path in the photoemission from aerosol droplets. *Chem. Phys. Lett.* **2016**, 658, 1–6.

(28) Luckhaus, D.; Yamamoto, Y.; Suzuki, T.; Signorell, R. Genuine binding energy of the hydrated electron. *Science Advances* **2017**, *3*, e1603224.

(29) Michaud, M.; Wen, A.; Sanche, L. Cross Sections for Low-Energy (1-100 eV) Electron Elastic and Inelastic Scattering in Amorphous Ice. *Radiat. Res.* **2003**, *159*, 3–22.

(30) Gartmann, T. E.; Hartweg, S.; Ban, L.; Chasovskikh, E.; Yoder, B. L.; Signorell, R. Electron scattering in large water clusters from photoelectron imaging with high harmonic radiation. *Phys. Chem. Chem. Phys.* **2018**, *20*, 16364–16371.

(31) Bartels, D. M. Is the Hydrated Electron Vertical Detachment Genuinely Bimodal? J. Phys. Chem. Lett. 2019, 10, 4910-4913.

(32) Liljequist, D. A study of errors in trajectory simulation with relevance for 0.2–50eV electrons in liquid water. *Radiat. Phys. Chem.* **2008**, 77, 835–853.

(33) Coe, J. V.; Earhart, A. D.; Cohen, M. H.; Hoffman, G. J.; Sarkas, H. W.; Bowen, K. H. Using cluster studies to approach the electronic structure of bulk water: Reassessing the vacuum level, conduction band edge, and band gap of water. *J. Chem. Phys.* **1997**, *107*, 6023–6031.

(34) Chen, W.; Ambrosio, F.; Miceli, G.; Pasquarello, A. Ab initio Electronic Structure of Liquid Water. *Phys. Rev. Lett.* **2016**, *117*, 186401.

(35) Gaiduk, A. P.; Pham, T. A.; Govoni, M.; Paesani, F.; Galli, G. Electron affinity of liquid water. *Nat. Commun.* **2018**, *9*, 247.

(36) Reid, K. L. Photoelectron Angular Distributions. Annu. Rev. Phys. Chem. 2003, 54, 397.

(37) Gianturco, F. A.; Lucchese, R. R.; Sanna, N. Calculation of low energy elastic cross sections for electron- CF_4 scattering. *J. Chem. Phys.* **1994**, *100*, 6464–6471.

(38) Natalense, A. P. P.; Lucchese, R. R. Cross section and asymmetry parameter calculation for sulfur 1s photoionization of SF_6 . *J. Chem. Phys.* **1999**, *111*, 5344–5348.

(39) Temelso, B.; Archer, K. A.; Shields, G. C. Benchmark Structures and Binding Energies of Small Water Clusters with Anharmonicity Corrections. *J. Phys. Chem. A* **2011**, *115*, 12034– 12046.

(40) Wernet, P.; Nordlund, D.; Bergmann, U.; Cavalleri, M.; Odelius, M.; Ogasawara, H.; Näslund, L. Å.; Hirsch, T. K.; Ojamäe, L.; Glatzel, P.; et al. The Structure of the First Coordination Shell in Liquid Water. *Science* **2004**, *304*, 995–999.

(41) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Scalmani, G.; Barone, V.; Mennucci, B.; Petersson, G. A.; et al. *Gaussian 09*, Revision D.01; Gaussian Inc.: Wallingford, CT, 2013.

(42) Blanco, F.; Muñoz, A.; Almeida, D.; da Silva, F. F.; Limão-Vieira, P.; García, G. Clustering and condensation effects in the electron scattering cross sections from water molecules. *Int. J. Mass Spectrom.* **2014**, 365–366, 287–294.

(43) Sethna, J. P. Statistical Mechanics: Entropy, Order Parameters, and Complexity; Oxford University Press: Oxford, Great Britain, 2006. (44) Märk, T. D.; Hatano, Y.; Linder, F. Atomic and molecular data

for radiotherapy and radiation research; IAEA: Vienna, 1995.

(45) Jablonski, A.; Powell, C. Relationships between electron inelastic mean free paths, effective attenuation lengths, and mean escape depths. *J. Electron Spectrosc. Relat. Phenom.* **1999**, *100*, 137–160.

(46) Jordan, I.; Huppert, M.; Brown, M. A.; van Bokhoven, J. A.; Wörner, H. J. Photoelectron spectrometer for attosecond spectroscopy of liquids and gases. *Rev. Sci. Instrum.* **2015**, *86*, 123905.

(47) Jordan, I.; Jain, A.; Gaumnitz, T.; Ma, J.; Wörner, H. J. Photoelectron spectrometer for liquid and gas-phase attosecond spectroscopy with field-free and magnetic bottle operation modes. *Rev. Sci. Instrum.* **2018**, *89*, 053103.