

Concepts of Object-Oriented Programming

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Chair of Programming Methodology

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Meeting the Requirements

Cooperating Program Parts with Well-Defined Interfaces

- Objects (data + code)
- Interfaces
- Encapsulation

Classification and Specialization

- Classification, subtyping
- Polymorphism
- Substitution principle

Highly Dynamic Execution Model

- Active objects
- Message passing

Correctness

- Interfaces
- Encapsulation
- Simple, powerful concepts

Topics in this Section

- Cooperating program parts ...
 - How do we define components?

- ... with well-defined interfaces
 - What is the interface of a component?
 - How do we describe the interface of a component?
 - How do we make sure clients use a component correctly?

Topics in this Section

- Cooperating program parts ...
 - How do we define components?

- ... with well-defined interfaces
 - What is the interface of a component?
 - How do we describe the interface of a component?
 - How do we make sure clients use a component correctly?



Types
and
contracts

4. Types

4.1 Bytecode Verification

4.2 Parametric Polymorphism

Mobile Code: Motivation

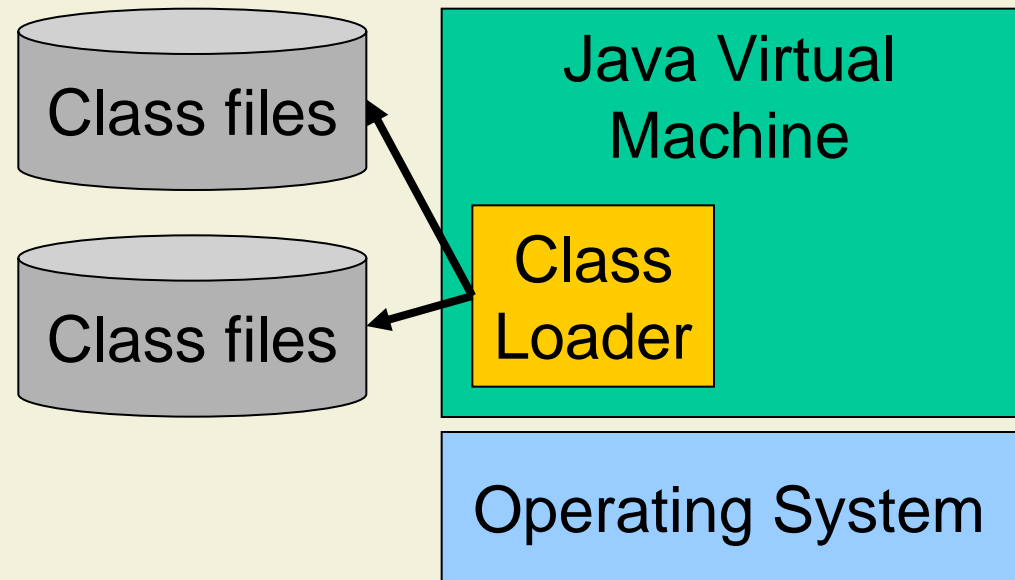
- Download and execution of code, e.g., Java applets
 - Web pages
 - Mobile devices

- Upload of code
 - Customizing servers

- Automatic distribution of code and patches in distributed systems

Class Loaders

- Programs are compiled to bytecode
 - Platform-independent format
 - Organized into class files
- Bytecode is interpreted on a virtual machine
- Class loader gets code for classes and interfaces on demand
- Programs can contain their own class loaders



Example: Specialized Class Loader

Error
handling
partly
omitted

```
public class MyLoader extends ClassLoader {  
    byte[ ] getClassData( String name ) { ... }  
  
    public synchronized Class loadClass( String name )  
        throws ClassNotFoundException {  
  
        Class c = findLoadedClass( name );  
        if ( c != null ) return c;  
  
        try { c = findSystemClass( name ); return c; }  
        catch ( ClassNotFoundException e ) { }  
  
        byte[ ] data = getClassData( name );  
        return defineClass( name, data, 0, data.length ); }  
}
```

Java

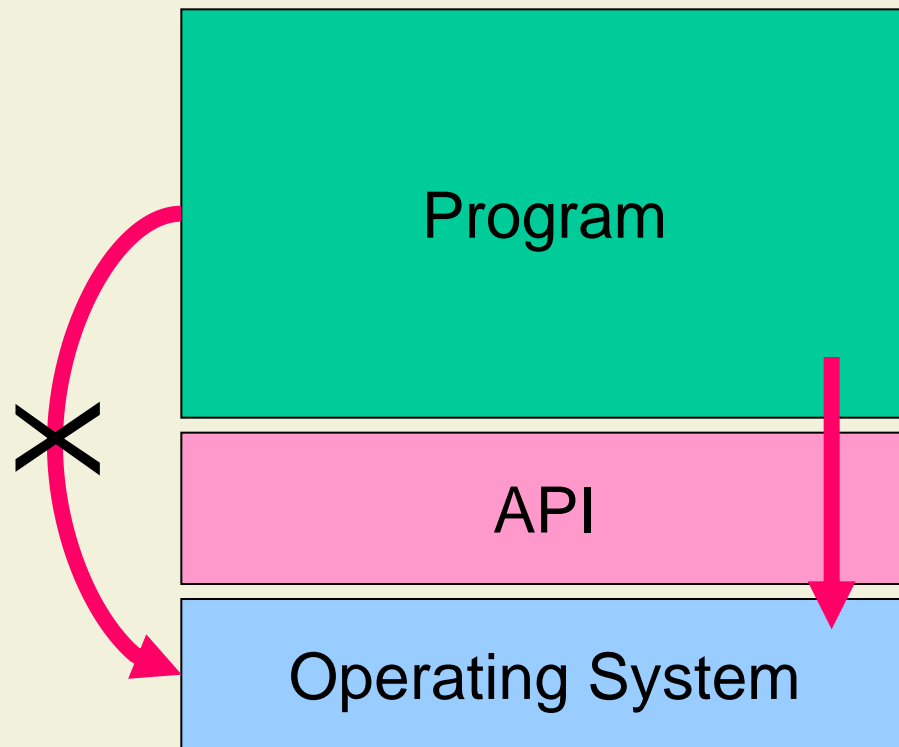
Security for Java Programs

■ Sandbox

- Applets get access to system resources only through an API
- Access control can be implemented

■ Security relies on

- Type safety
- Code does not by-pass sandbox



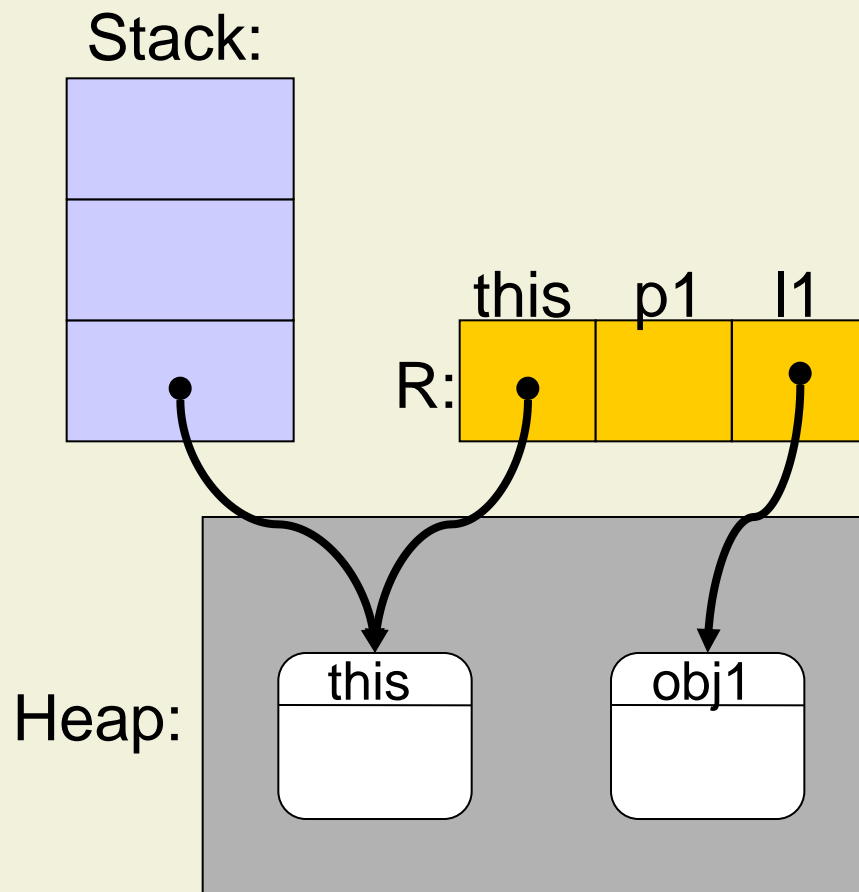
Security in Mobile Environments

- Mobile code cannot be trusted
 - Code may not be type safe
 - Code may destroy or modify data
 - Code may expose personal information
 - Code may crash the underlying VM
 - Code may purposefully degrade performance (denial of service)

- How to guarantee a minimum level of security?
 - Untrusted code producer
 - Untrusted compiler

Java Virtual Machine

- JVM is stack-based
- Most operations pop operands from a stack and push a result
- Registers store method parameters and local variables
- Stack and registers are part of the method activation record

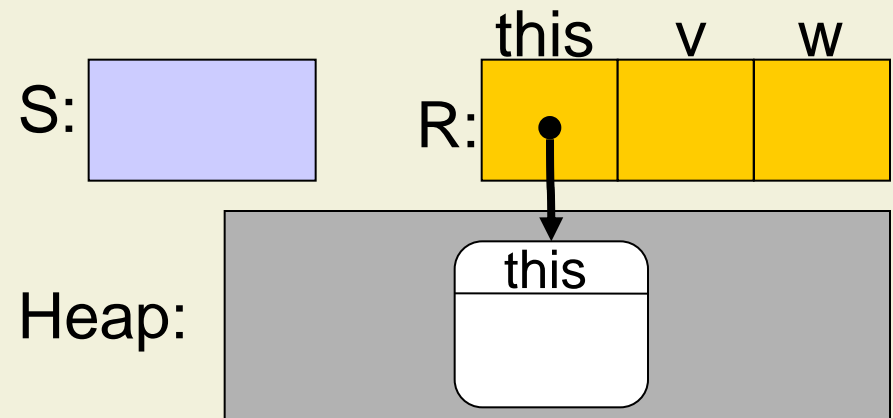


Java Bytecode

- Instructions are typed
- Load and store instructions access registers
- Control is handled by intra-method branches (goto, conditional branches)

```
class C {  
  void m( ) {  
    int v;  
    Object w;  
    v = 5;  
    w = this;  
  }  
}
```

```
iconst 5  
istore 1  
aload 0  
astore 2  
return
```

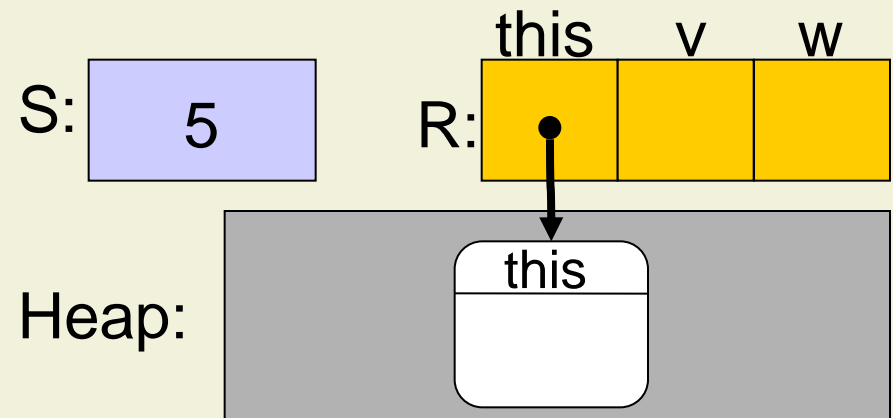


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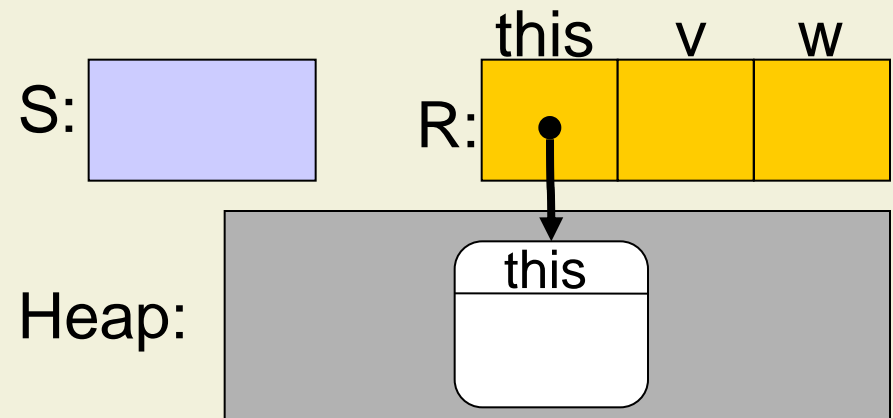


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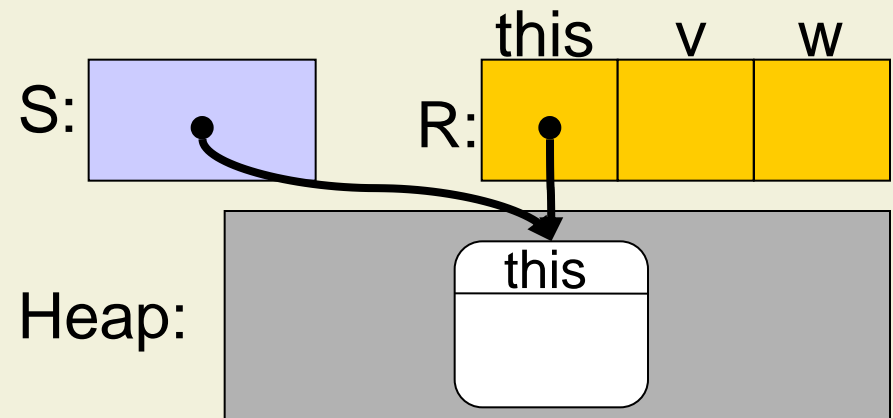


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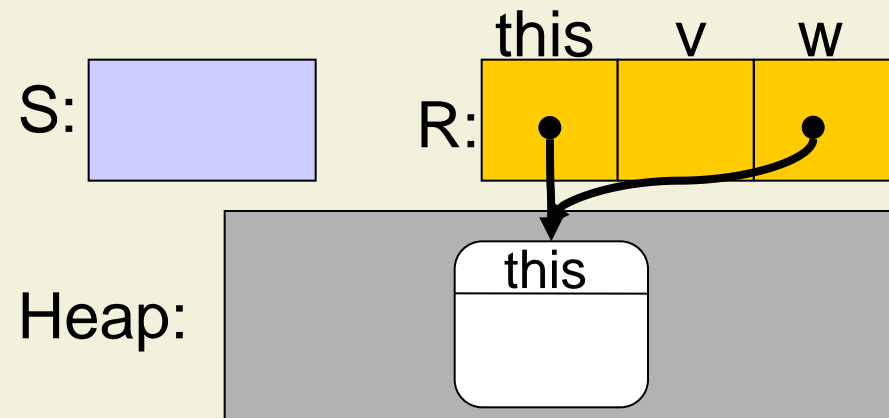


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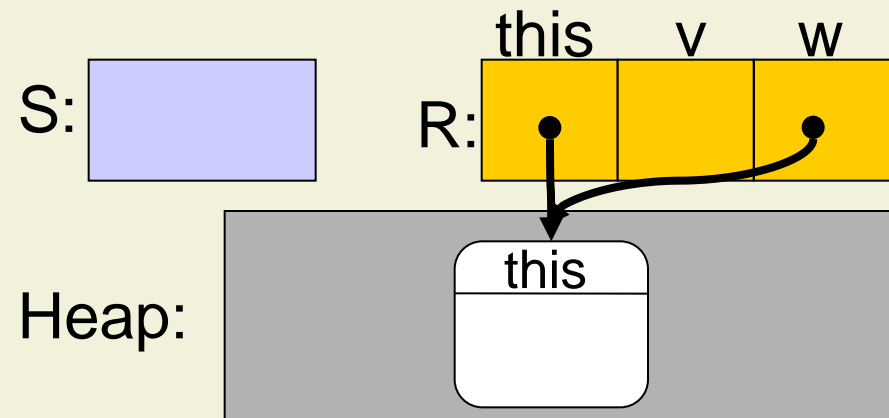


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```



Bytecode Verification

- Proper execution requires that
 - Each instruction is type correct
 - Only initialized variables are read
 - No stack over- or underflow occurs
 - Etc.

- Java Virtual Machine guarantees these properties
 - By **bytecode verification** when a class is loaded
 - By **dynamic checks at run time**

Bytecode Verification via Type Inference

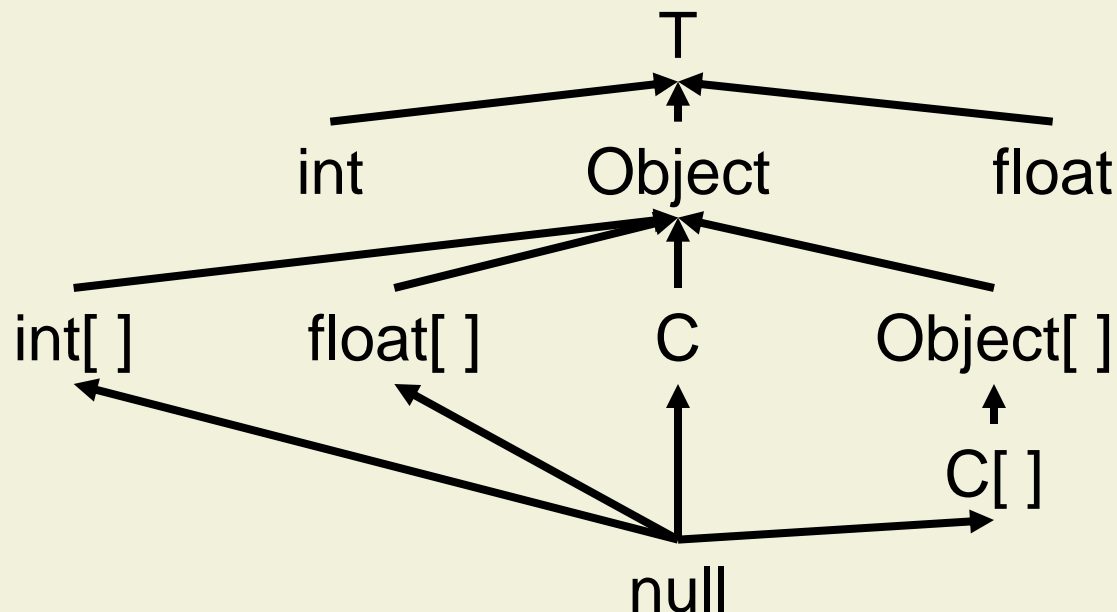
- The Bytecode verifier **simulates** the execution of the program
- Operations are performed on **types instead of values**
- For each instruction, a rule describes how the **operand stack and local variables** are modified

$$\begin{aligned} i: (S, R) &\rightarrow (S', R') \\ \text{iadd}: (\text{int.int.S}, R) &\rightarrow (\text{int.S}, R) \end{aligned}$$

- Errors are denoted by the **absence of a transition**
 - Type mismatch
 - Stack over- or underflow

Types of the Inference Engine

- Primitive types
- Object and array reference types
- null type for the null reference
- T for uninitialized registers



Selected Rules

- Maximum stack size (MS) and maximum number of parameters and local variables (MR) are stored in the classfile
- Rule for method invocation uses method signature (no jump)

iconst n:

$(S, R) \rightarrow (\text{int}.S, R)$, if $|S| < MS$

iload n:

$(S, R) \rightarrow (\text{int}.S, R)$,
if $0 \leq n < MR \wedge R(n) = \text{int} \wedge |S| < MS$

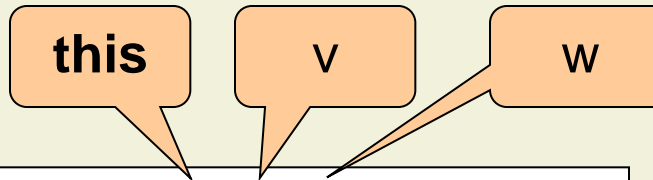
astore n:

$(t.S, R) \rightarrow (S, R\{n \leftarrow t\})$,
if $0 \leq n < MR \wedge t <: \text{Object}$

invokevirtual C.m. σ :

$(t'_n \dots t'_1.t'.S, R) \rightarrow (r.S, R)$, if
 $\sigma = r(t_1, \dots, t_n) \wedge t' <: C \wedge t'_i <: t_i$

Example



```
int v;
Object w;
v = 5;
w = this;
```

```
iconst 5
istore 1
aload 0
astore 2
return
```

```
( [ ] , [ C,T,T ] ) →
( int , [ C,T,T ] ) →
( [ ] , [ C,int,T ] ) →
( C , [ C,int,T ] ) →
( [ ] , [ C,int,C ] )
```

```
int v;
Object w;
v = 5;
w = v;
```

```
iconst 5
istore 1
iload 1
astore 2
return
```

```
( [ ] , [ C,T,T ] ) →
( int , [ C,T,T ] ) →
( [ ] , [ C,int,T ] ) →
( int , [ C,int,T ] )
stuck
```

astore
expects an
object type
on top of
the stack!

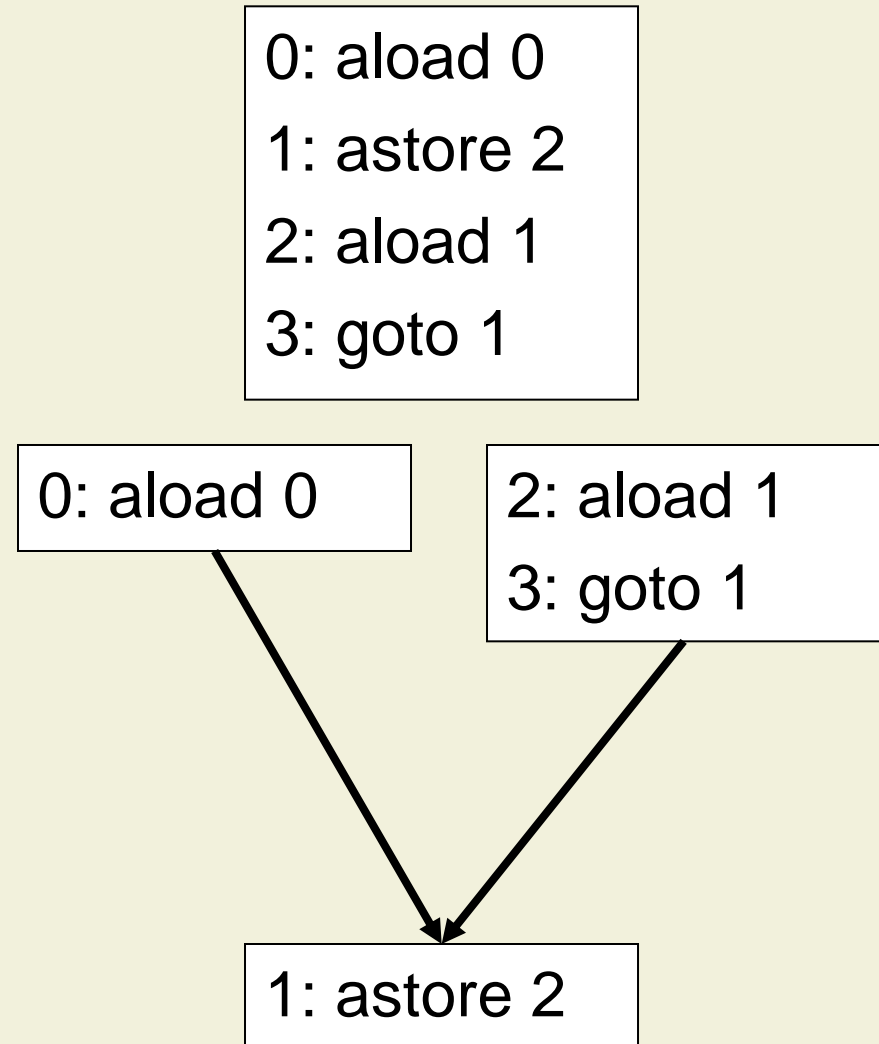
Smallest Common Supertype

- Branches lead to **joins**
in control flow

```
0: aload 0  
1: astore 2  
2: aload 1  
3: goto 1
```

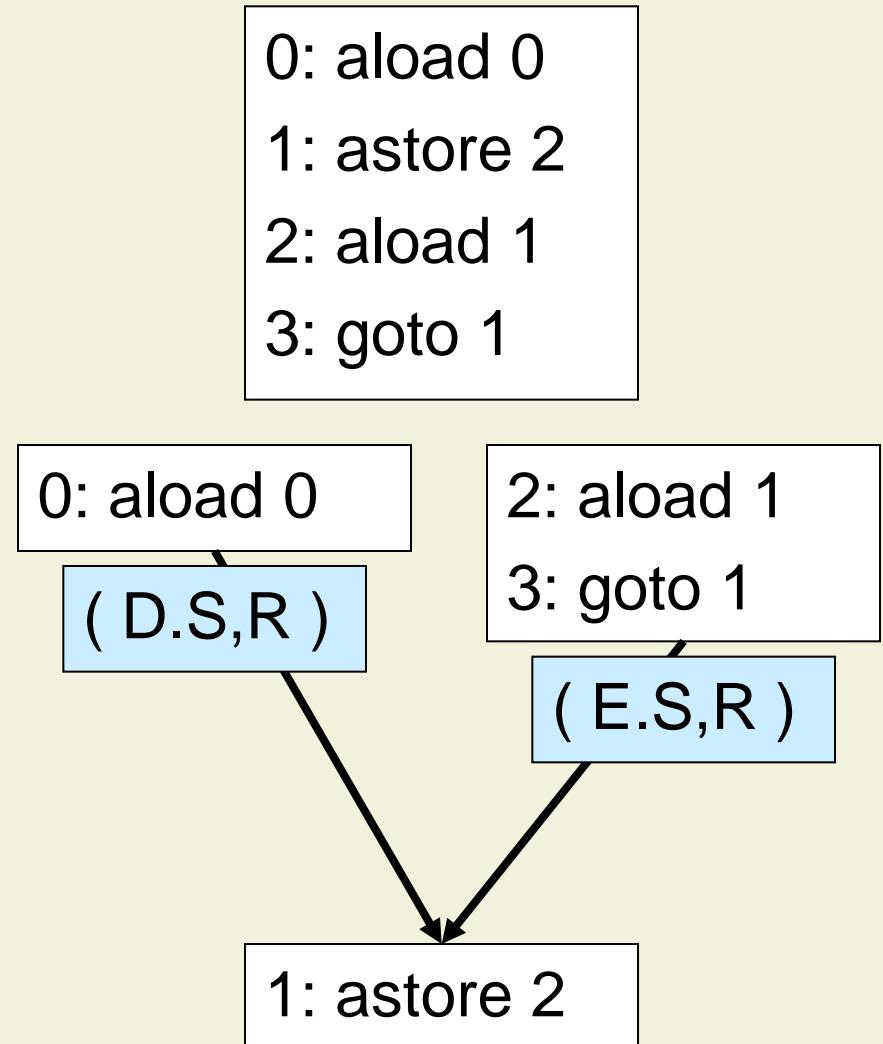
Smallest Common Supertype

- Branches lead to **joins** in control flow
- Instructions can have **several predecessors**



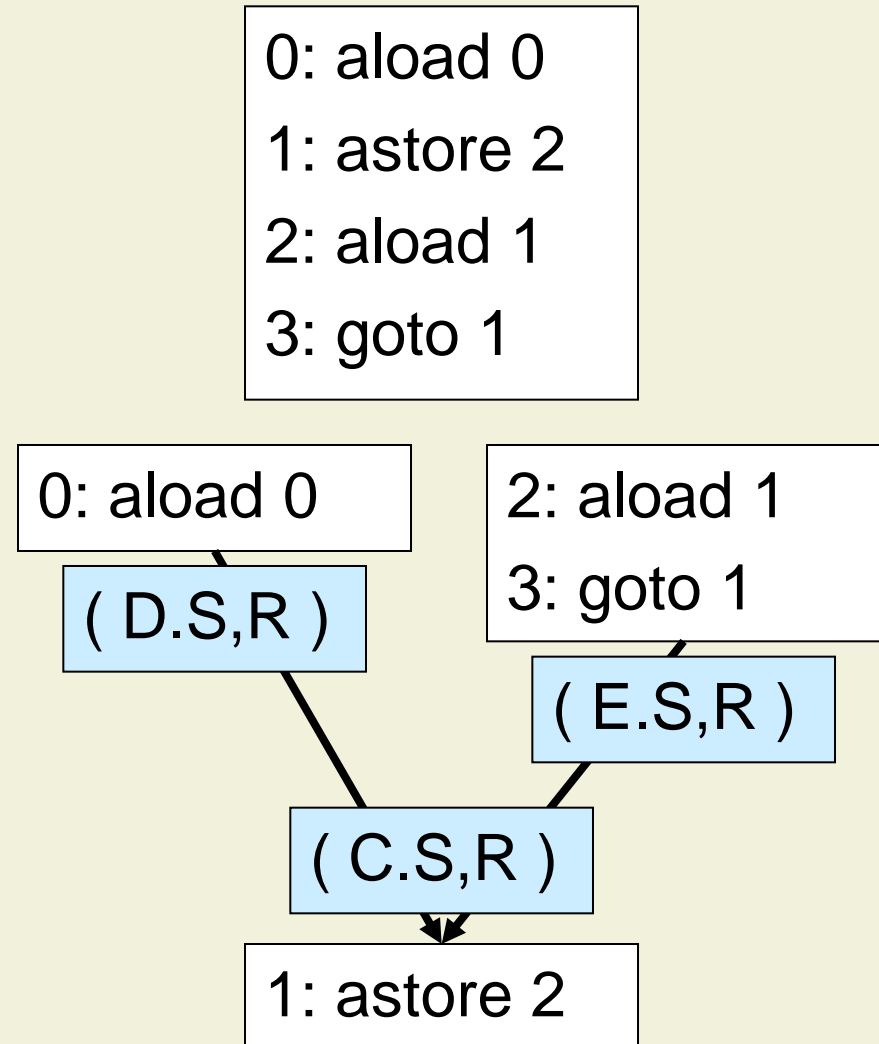
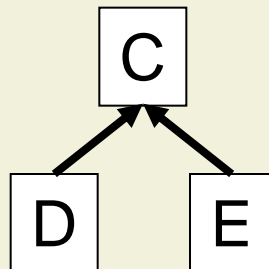
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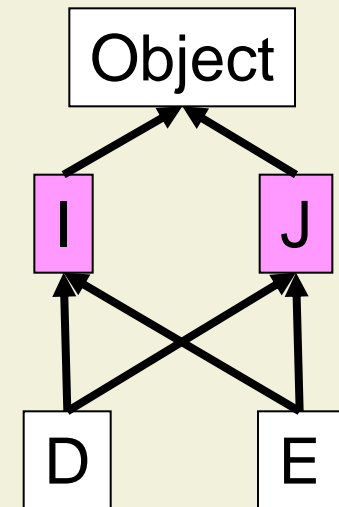
Smallest Common Supertype

- Branches lead to **joins** in control flow
- Instructions can have **several predecessors**
- Smallest common supertype** is selected (T if no other common supertype exists)



Handling Multiple Subtyping

- With multiple subtyping, **several smallest common supertypes** may exist
- JVM solution
 - Ignore interfaces
 - Treat all interface types as Object
 - Works because of single inheritance of classes
- Problem
 - **invokeinterface** I.m cannot check whether target object implements I
 - Run-time check is necessary



Inference Algorithm

- Inference is a fixpoint iteration

```
in( 0 ) := ( [ ] , [ P0, ..., Pn, T, ..., T ] )  
worklist := { i | instri is an instruction of the method }  
while worklist ≠ ∅ do  
  i := min( worklist )  
  remove i from worklist  
  out( i ) := apply_rule( instri, in( i ) )  
  foreach q in successors( i ) do  
    in( q ) := pointwise_scs( in( q ), out( i ) )  
    if in( q ) has changed then worklist := worklist ∪ { q }  
  end  
end
```

Pointwise SCS

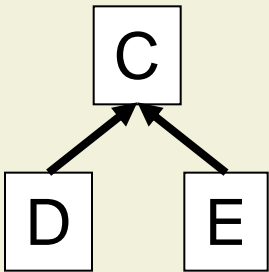
- $\text{scs}(s, t)$ is the smallest common supertype of s and t

$$\begin{aligned} \text{pointwise_scs} \big(& ([s_1, \dots, s_k], [t_0, \dots, t_n]), \\ & ([s'_1, \dots, s'_k], [t'_0, \dots, t'_n]) \big) = \\ & ([\text{scs}(s_1, s'_1), \dots, \text{scs}(s_k, s'_k)], [\text{scs}(t_0, t'_0), \dots, \text{scs}(t_n, t'_n)]) \end{aligned}$$

- pointwise_scs is undefined for stacks of different heights
 - Bytecode verification results in an error

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



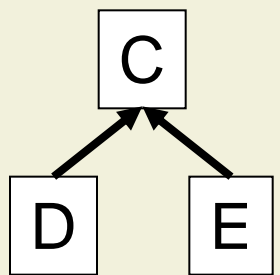
worklist

- 0 1 2 3

	in	out
0:	([], [D,E,T])	
1:		
2:		
3:		

Inference Example

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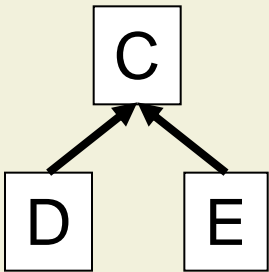
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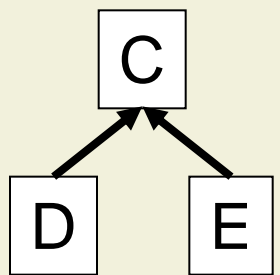
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- 1 2 3

	in	out
0:	$([], [D, E, T])$	$([D], [D, E, T])$
1:		
2:		
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Inference Example

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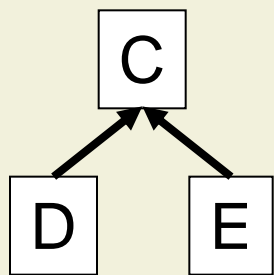
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	in	out
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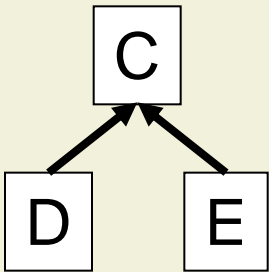
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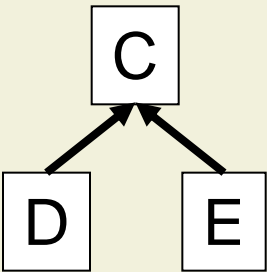
worklist

2 3

	in	out
0:	$([], [D, E, T])$	$([D], [D, E, T])$
1:	$([D], [D, E, T])$	$([], [D, E, D])$
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3:		

Inference Example

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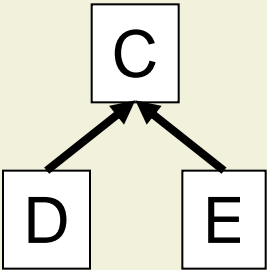
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0:	$([], [D, E, T])$	$([D], [D, E, T])$
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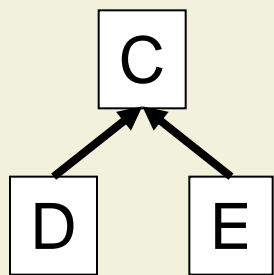
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3

	in	out
0:	$([], [D, E, T])$	$([D], [D, E, T])$
1:	$([D], [D, E, T])$	$([], [D, E, D])$
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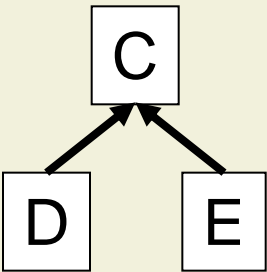
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3

	in	out
0:	$([], [D, E, T])$	$([D], [D, E, T])$
1:	$([D], [D, E, T])$	$([], [D, E, D])$
2:	$([], [D, E, D])$	$([E], [D, E, D])$
3:		

Inference Example

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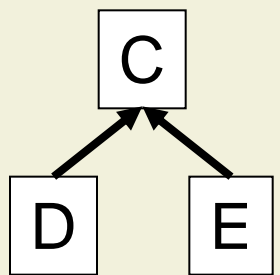
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3

	in	out
0:	$([], [D, E, T])$	$([D], [D, E, T])$
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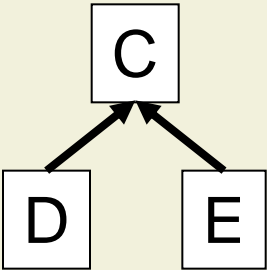
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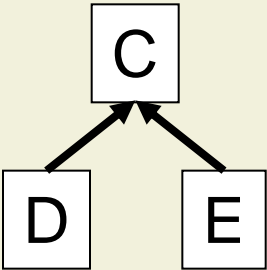
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2:	$([], [D, E, D])$	$([E], [D, E, D])$
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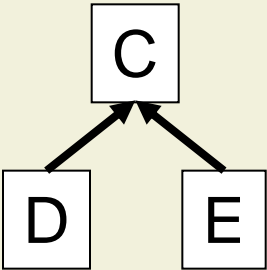
worklist



	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D])
2:	([], [D,E,D])	([E], [D,E,D])
3:	([E], [D,E,D])	([E], [D,E,D])

Inference Example

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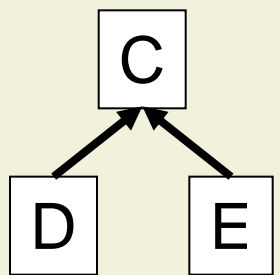
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1

	in	out
0:	$([], [D, E, T])$	$([D], [D, E, T])$
1:	$([D], [D, E, T])$ $([C], [D, E, T])$	$([], [D, E, D])$
2:	$([], [D, E, D])$	$([E], [D, E, D])$
3:	$([E], [D, E, D])$	$([E], [D, E, D])$

Inference Example

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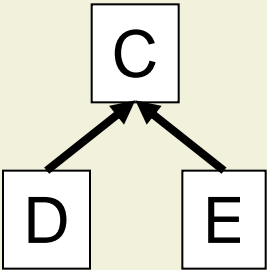
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	in	out
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2:	([], [D,E,D])	([E], [D,E,D])
3:	([E], [D,E,D])	([E], [D,E,D])

Inference Example

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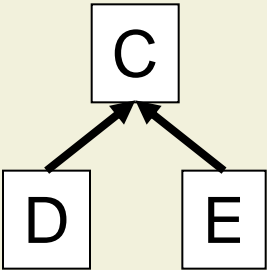
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	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D])	([E], [D,E,D])
3:	([E], [D,E,D])	([E], [D,E,D])

Inference Example

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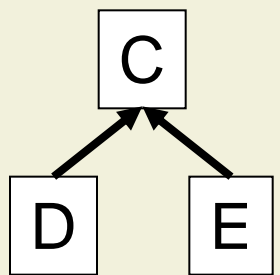
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	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D]) ([], [D,E,C])	([E], [D,E,D])
3:	([E], [D,E,D])	([E], [D,E,D])

Inference Example

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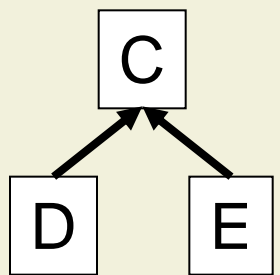
worklist

2

	in	out
0:	([] , [D,E,T])	([D] , [D,E,T])
1:	([D] , [D,E,T]) ([C] , [D,E,T])	([] , [D,E,D]) ([] , [D,E,C])
2:	([] , [D,E,D]) ([] , [D,E,C])	([E] , [D,E,D])
3:	([E] , [D,E,D])	([E] , [D,E,D])

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



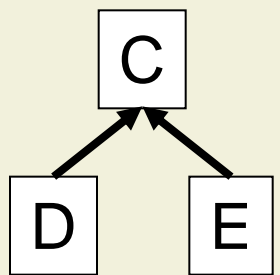
worklist



	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D]) ([], [D,E,C])	([E], [D,E,D])
3:	([E], [D,E,D])	([E], [D,E,D])

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



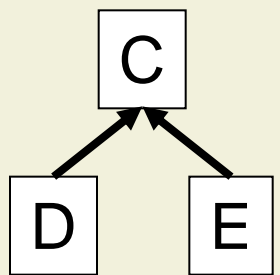
worklist



	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D]) ([], [D,E,C])	([E], [D,E,D]) ([E], [D,E,C])
3:	([E], [D,E,D])	([E], [D,E,D])

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



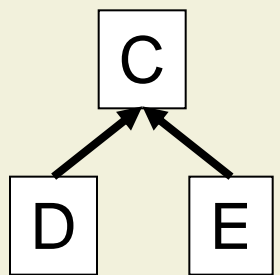
worklist



	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D]) ([], [D,E,C])	([E], [D,E,D]) ([E], [D,E,C])
3:	([E], [D,E,D]) ([E], [D,E,C])	([E], [D,E,D])

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



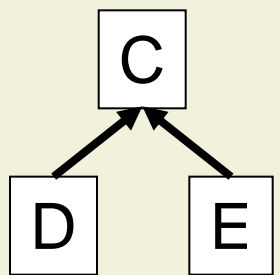
worklist

3

	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D]) ([], [D,E,C])	([E], [D,E,D]) ([E], [D,E,C])
3:	([E], [D,E,D]) ([E], [D,E,C])	([E], [D,E,D])

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



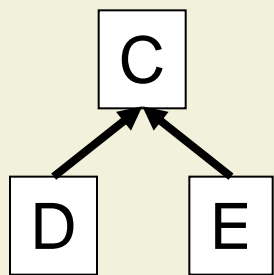
worklist



	in	out
0:	([] , [D,E,T])	([D] , [D,E,T])
1:	([D] , [D,E,T]) ([C] , [D,E,T])	([] , [D,E,D]) ([] , [D,E,C])
2:	([] , [D,E,D]) ([] , [D,E,C])	([E] , [D,E,D]) ([E] , [D,E,C])
3:	([E] , [D,E,D]) ([E] , [D,E,C])	([E] , [D,E,D])

Inference Example

0: aload 0
1: astore 2
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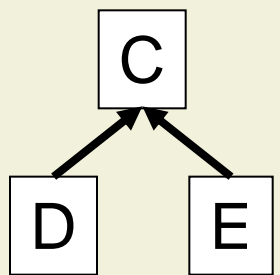
worklist



	in	out
0:	([] , [D,E,T])	([D] , [D,E,T])
1:	([D] , [D,E,T]) ([C] , [D,E,T])	([] , [D,E,D]) ([] , [D,E,C])
2:	([] , [D,E,D]) ([] , [D,E,C])	([E] , [D,E,D]) ([E] , [D,E,C])
3:	([E] , [D,E,D]) ([E] , [D,E,C])	([E] , [D,E,D]) ([E] , [D,E,C])

Inference Example

0: aload 0
1: astore 2
2: aload 1
3: goto 1



worklist



	in	out
0:	([], [D,E,T])	([D], [D,E,T])
1:	([D], [D,E,T]) ([C], [D,E,T])	([], [D,E,D]) ([], [D,E,C])
2:	([], [D,E,D]) ([], [D,E,C])	([E], [D,E,D]) ([E], [D,E,C])
3:	([E], [D,E,D]) ([E], [D,E,C])	([E], [D,E,D]) ([E], [D,E,C])

Type Inference: Discussion

■ Advantages

- Determines the **most general solution** that satisfies the typing rules
- Might be more general than what is permitted by compiler
- Very little type information required in class file

■ Disadvantages

- Fixpoint computations may be slow
- Solution for interfaces is **imprecise** and **requires run-time checks**

■ Alternative: type checking (since Java 6)

Bytecode Verification via Type Checking

- Extend class file to store type information

([int] , [C,int,T])

- Type information can be declared for each bytecode instruction
- Type information **required** at the beginning of all **basic blocks**:
 - At jump target
 - At entry point of exception handler

} Includes all join points
- Computation of SCS no longer necessary
 - Avoid fixpoint computation and interface problem

Type Checking Algorithm

- Use and check declared types wherever available
- Infer types otherwise

```
foreach basic block of a method body do  
  in := types( start )  
  foreach { i | instri is an instruction of basic block } do  
    in := apply_rule( instri, in )  
    foreach q in successors( i ) do  
      if types( q ) is declared then  
        check that in is assignable to types( q )  
        in := types( q )  
      end  
    end  
  end  
end
```

Type Checking Algorithm

- Use and check declared types wherever available
- Infer types otherwise

foreach basic block of a method body **do**

in := types(start)

foreach { i | instr_i is an instruction of basic block } **do**

in := apply_rule(instr_i, in)

foreach q in successors(i) **do**

if types(q) is declared **then**

check that in is assignable to types(q)

in := types(q)

end

end

end

Required
types

Type Checking Algorithm

- Use and check declared types wherever available
- Infer types otherwise

foreach basic block of a method body **do**

in := types(start)

Required
types

foreach { i | instr_i is an instruction of basic block } **do**

in := apply_rule(instr_i, in)

Check conditions and infer
next configuration

foreach q in successors(i) **do**

if types(q) is declared **then**

check that in is assignable to types(q)

in := types(q)

end

end

end

Type Checking Algorithm

- Use and check declared types wherever available
- Infer types otherwise

foreach basic block of a method body **do**

in := types(start)

foreach { i | instr_i is an instruction of basic block } **do**

in := apply_rule(instr_i, in)

foreach q in successors(i) **do**

if types(q) is declared **then**

check that in is assignable to types(q)

in := types(q)

end

end

end

Required
types

Check conditions and infer
next configuration

Check
declared types

Type Checking Algorithm

- Use and check declared types wherever available
- Infer types otherwise

foreach basic block of a method body **do**

in := types(start)

Required
types

foreach { i | instr_i is an instruction of basic block } **do**

in := apply_rule(instr_i, in)

Check conditions and infer
next configuration

foreach q in successors(i) **do**

if types(q) is declared **then**

check that in is assignable to types(q)

in := types(q)

Check
declared types

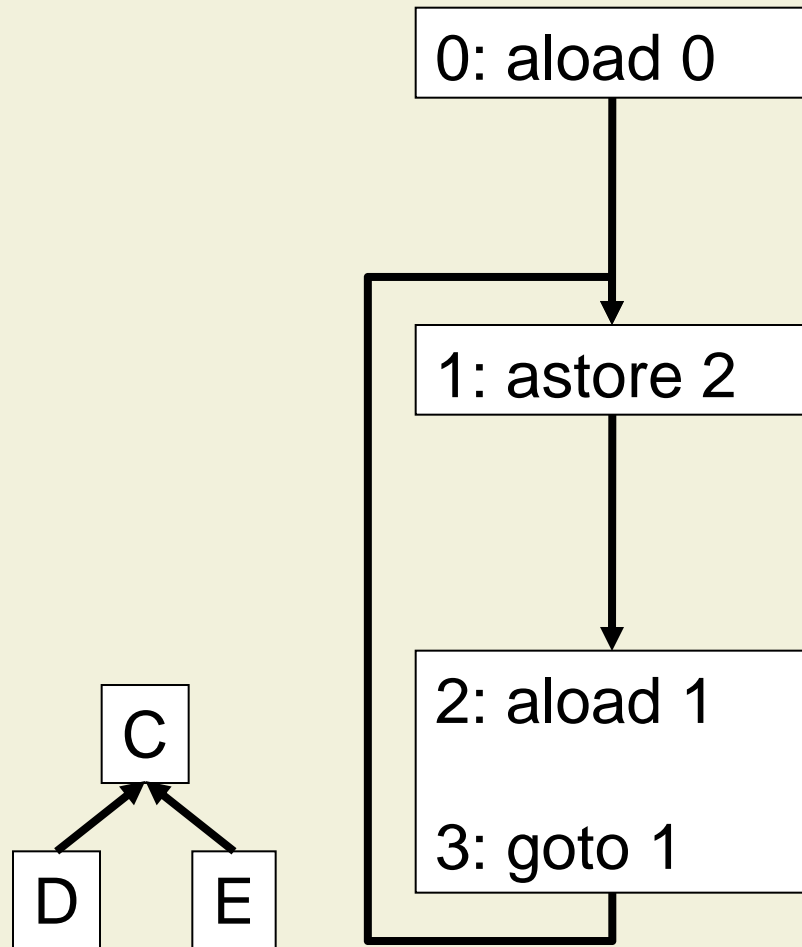
Use declared
types if instr_i is
not a jump

end

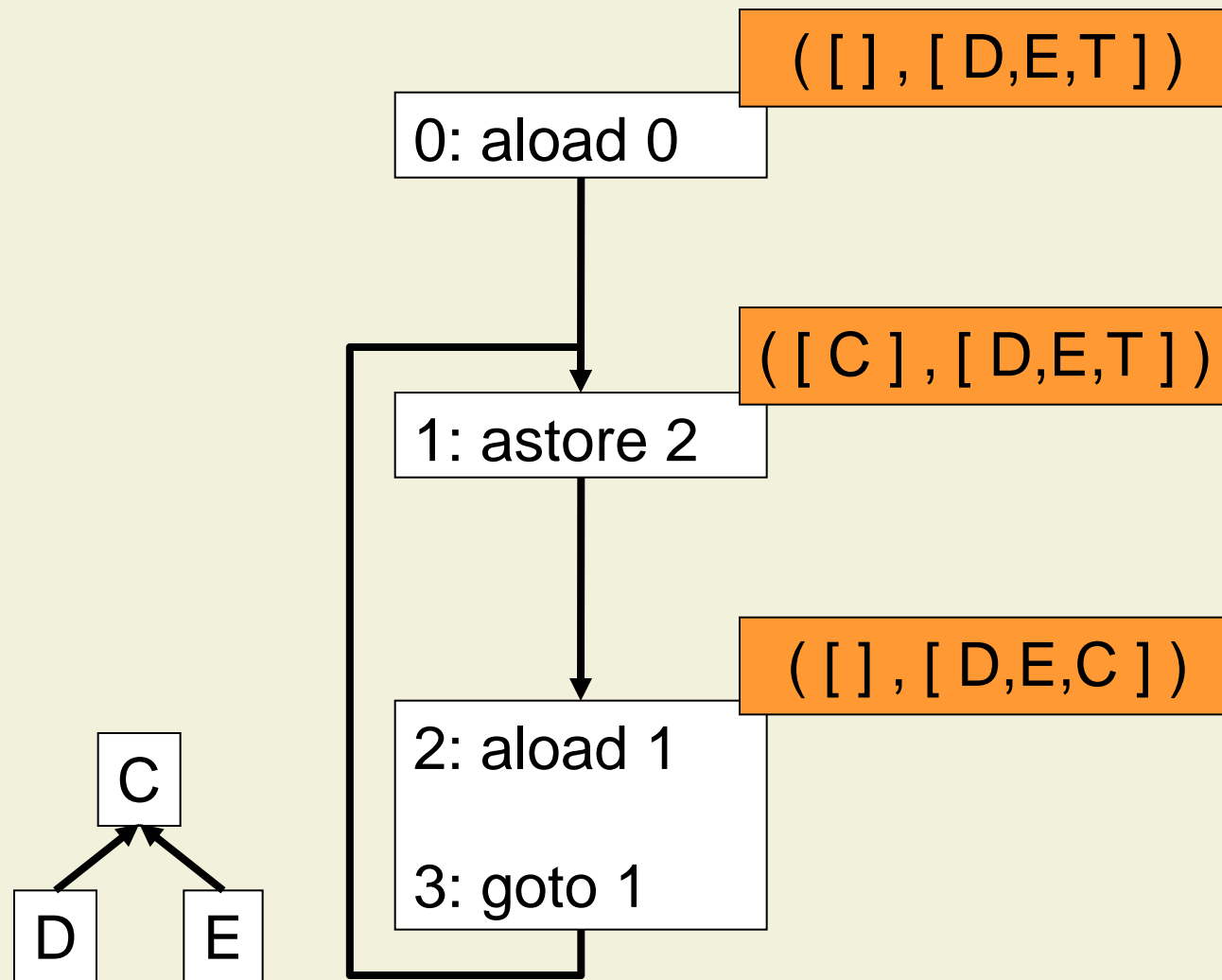
end

end

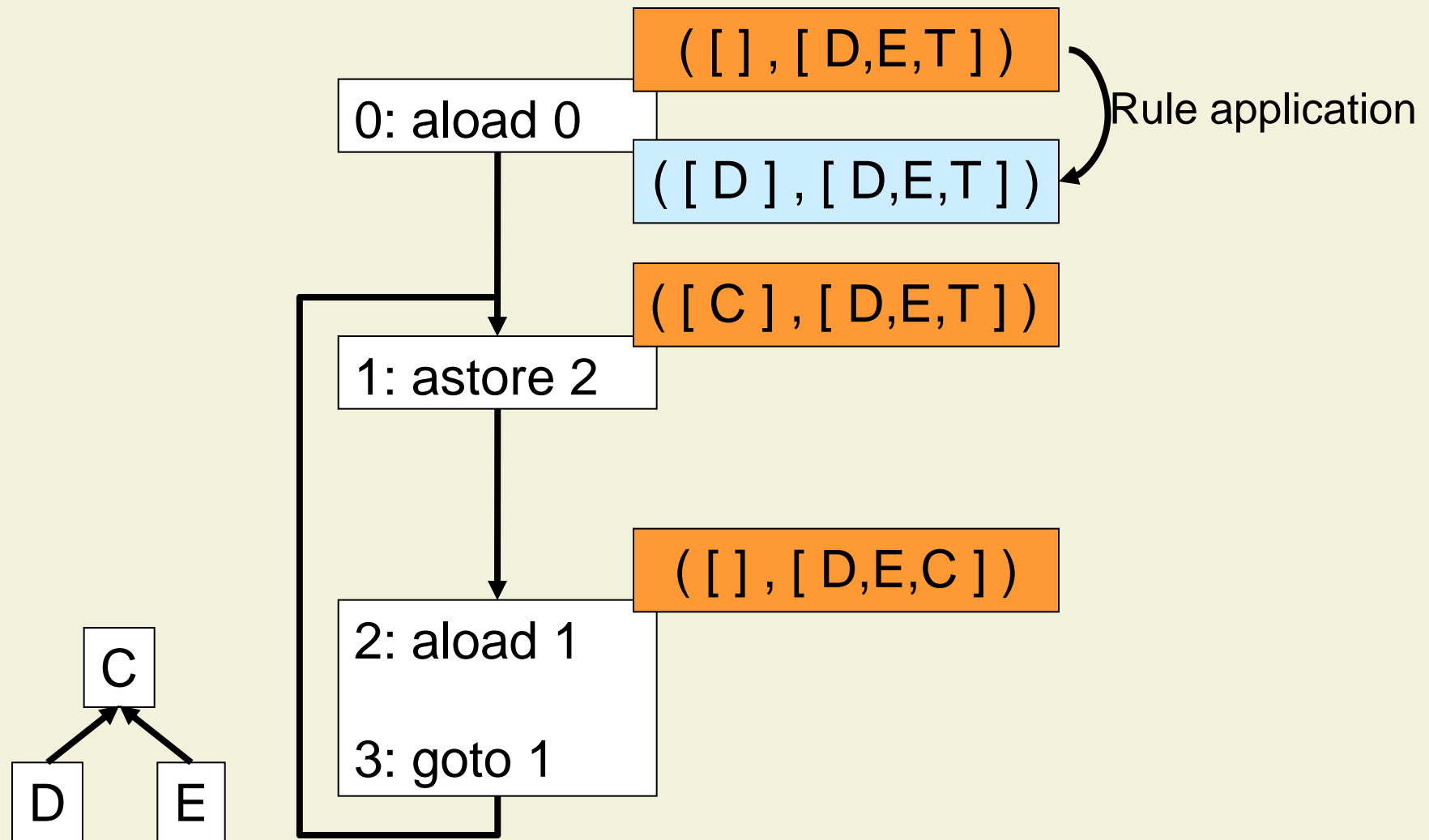
Type Checking Example



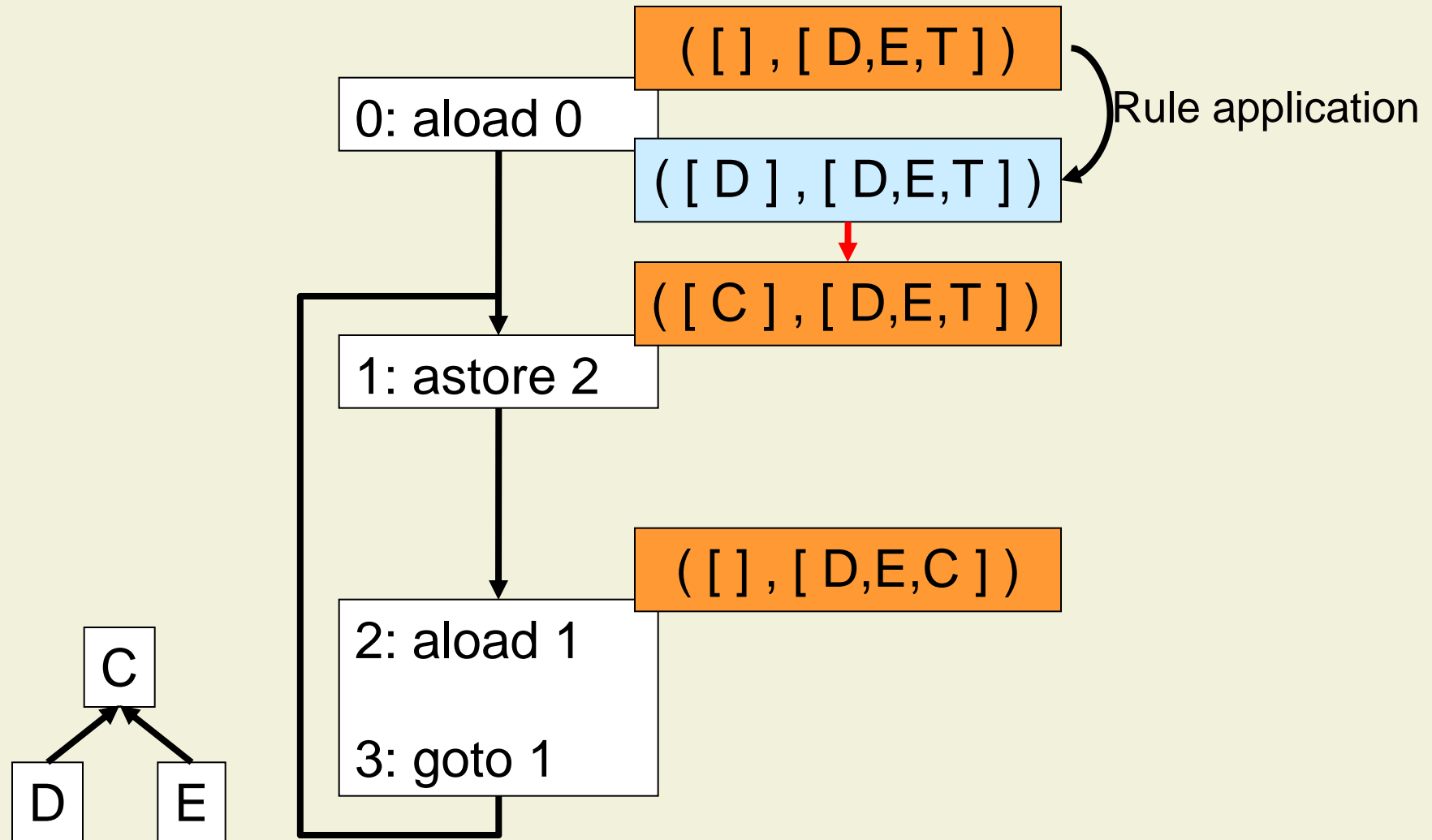
Type Checking Example



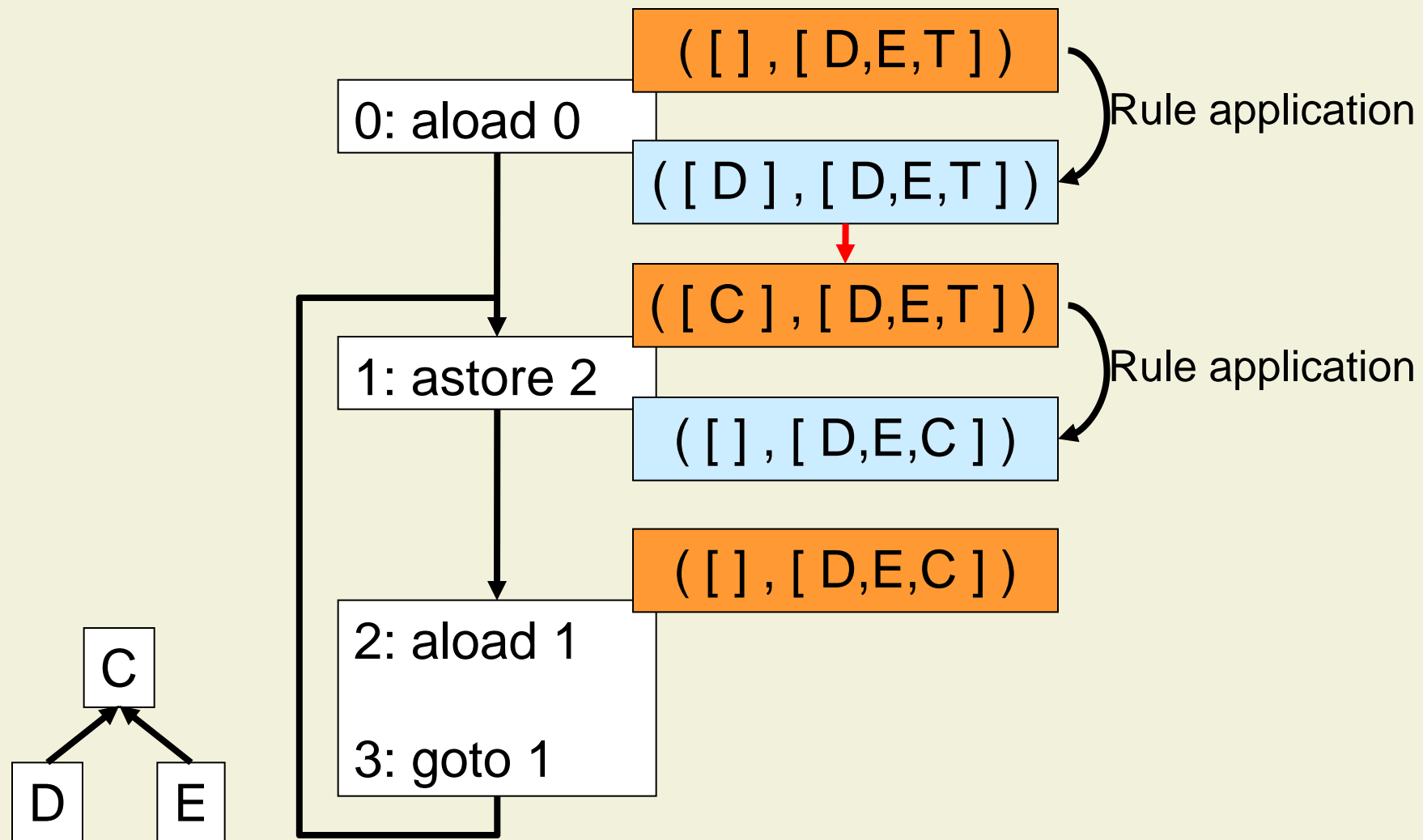
Type Checking Example



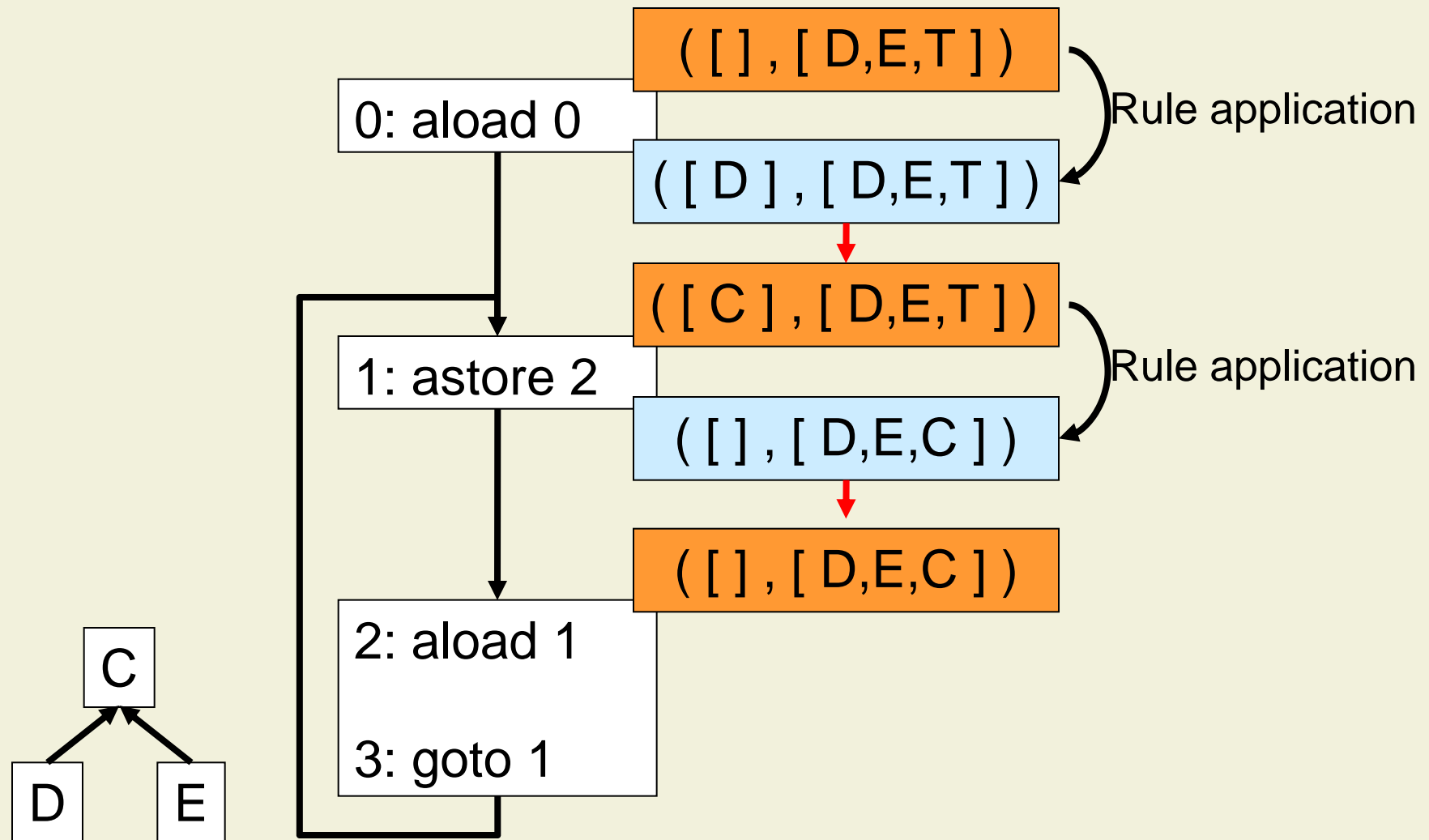
Type Checking Example



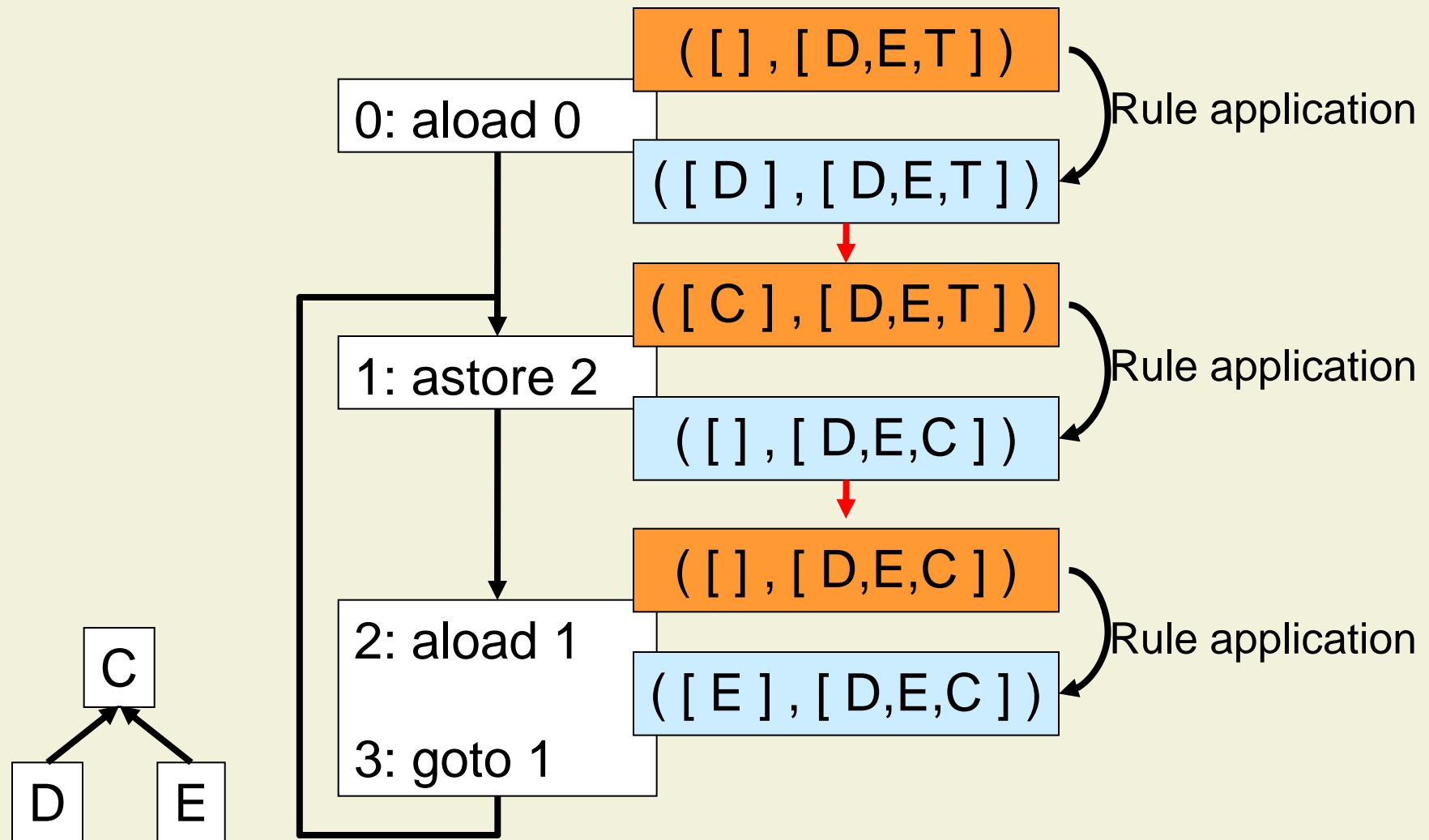
Type Checking Example



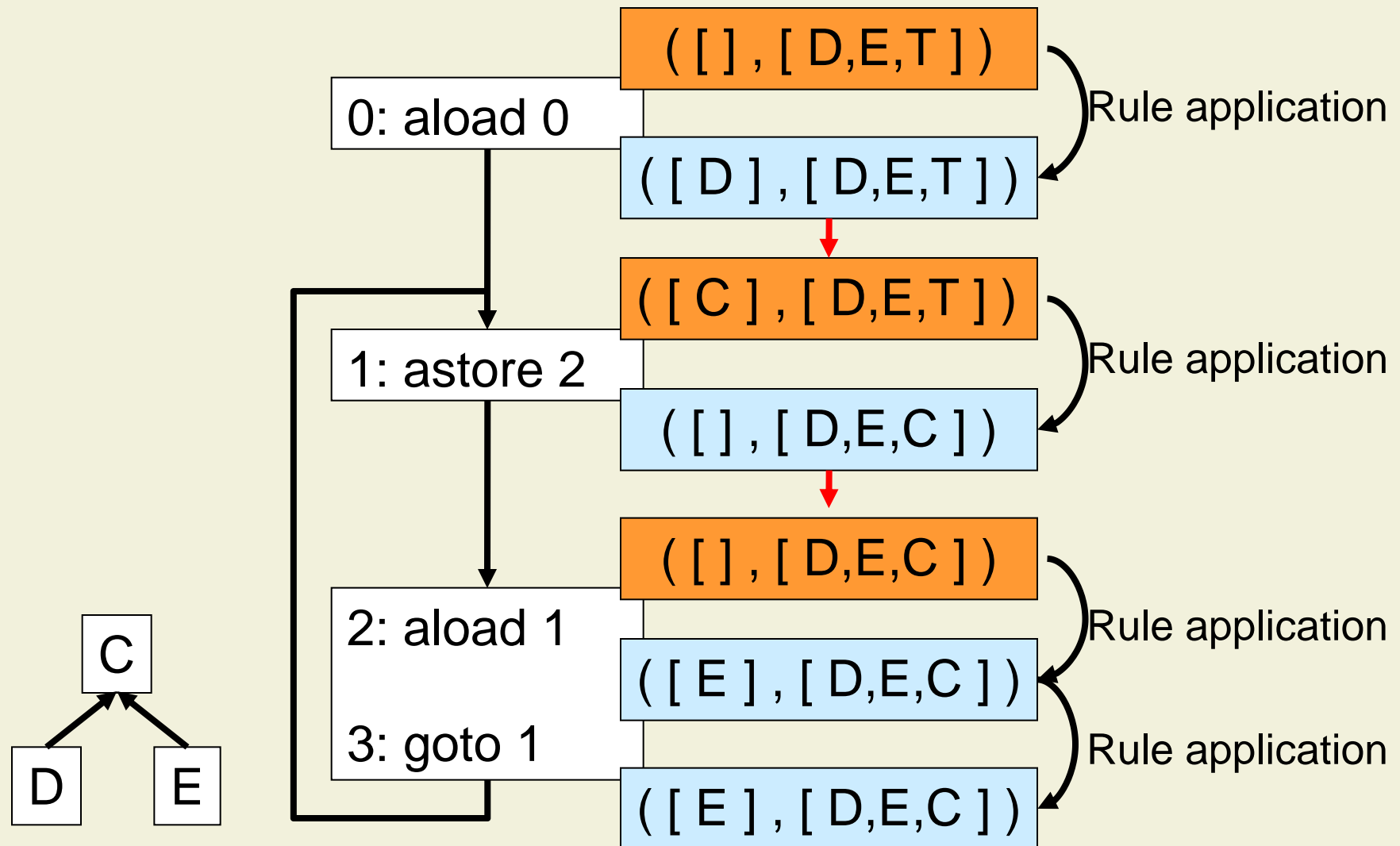
Type Checking Example



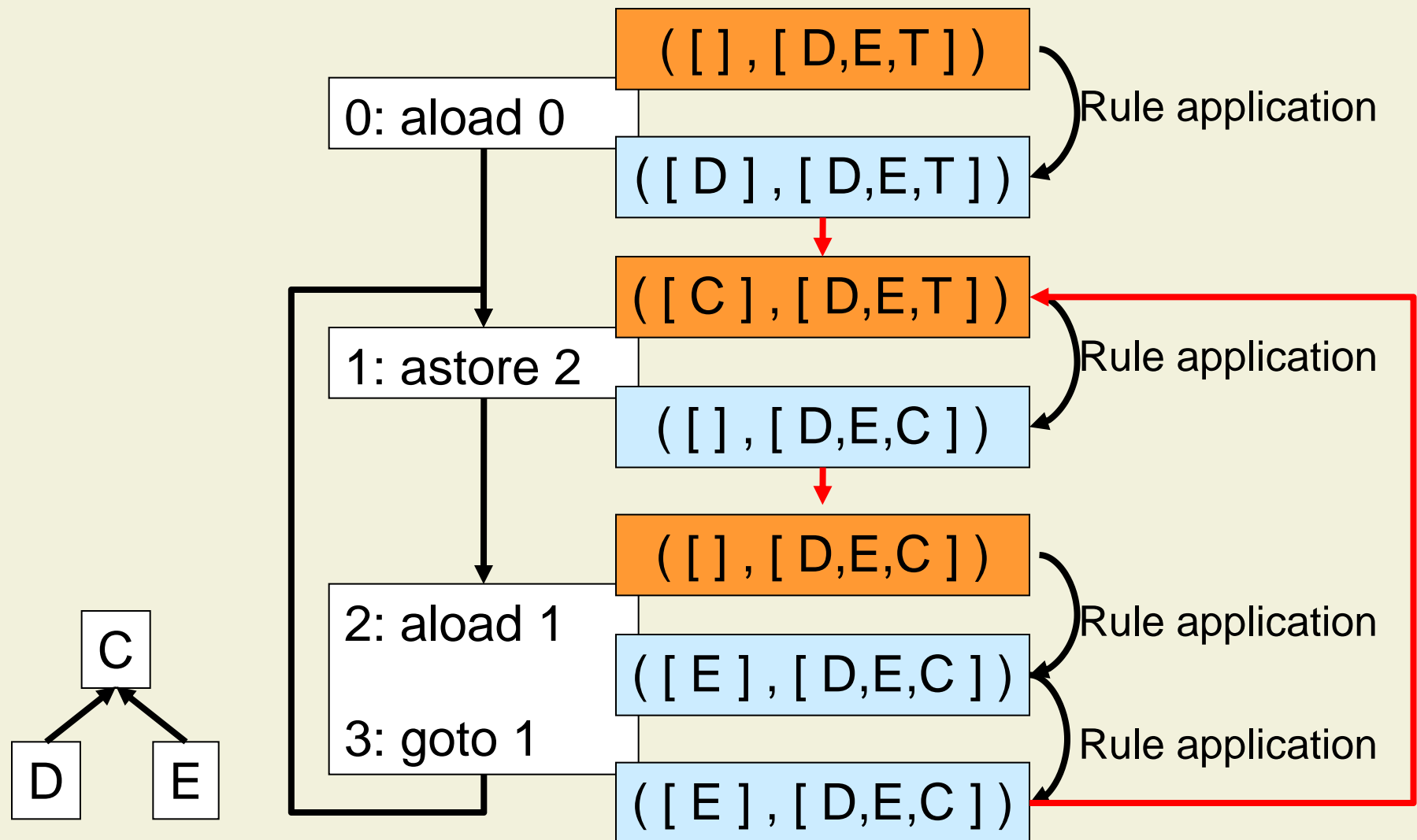
Type Checking Example



Type Checking Example



Type Checking Example



Bytecode Verification: Summary

- Bytecode verification enables secure mobile code
 - For programs written in typed bytecode
- Bytecode verification can be done via **type inference** or **type checking**
- Some run-time type checks are still necessary
 - For instance, casts and co-variant arrays

Type Inference for Source Programs

- Type inference can also be done on source code
 - For example, C# 3.0 and Scala **infer types of local variables**
 - **Reduce annotation overhead**, especially with generics

```
def sum( a: Array[ Int ] ): Int = {  
  val it = a.elements  
  var s = 0;  
  while( it.hasNext ) { s = s + it.next }  
  s  
}
```

Scala

Type Inference for Source Programs

- Type inference can also be done on source code
 - For example, C# 3.0 and Scala **infer types of local variables**
 - **Reduce annotation overhead**, especially with generics

```
def sum( a: Array[ Int ] ): Int = {  
  val it = a.elements  
  var s = 0;  
  while( it.hasNext ) { s = s + it.next }  
  s  
}
```

Scala

```
def client = {  
  var a = 1  
  a = "Hello"  
}
```

Scala

Type Inference for Source Programs

- Type inference can also be done on source code
 - For example, C# 3.0 and Scala **infer types of local variables**
 - **Reduce annotation overhead**, especially with generics
- Type annotations can still be used to support inference

```
def sum( a: Array[ Int ] ): Int = {  
  val it = a.elements  
  var s = 0;  
  while( it.hasNext ) { s = s + it.next }  
  s  
}
```

Scala

```
def client = {  
  var a = 1  
  a = "Hello"  
}
```

Scala

```
def client = {  
  var a: Any = 1  
  a = "Hello"  
}
```

Scala

Inference of Method and Field Types

- Inference of method signatures generally requires knowledge of all implementations
- Inference of field types generally requires knowledge of all assignments to the field
- Inference of these types is non-modular
 - Or based on speculation

```
class A {  
  var f = 5;  
  def foo( p: Int ) = {  
    p  
  }  
}
```

Scala

Inference of Method and Field Types

- Inference of method signatures generally requires knowledge of all implementations
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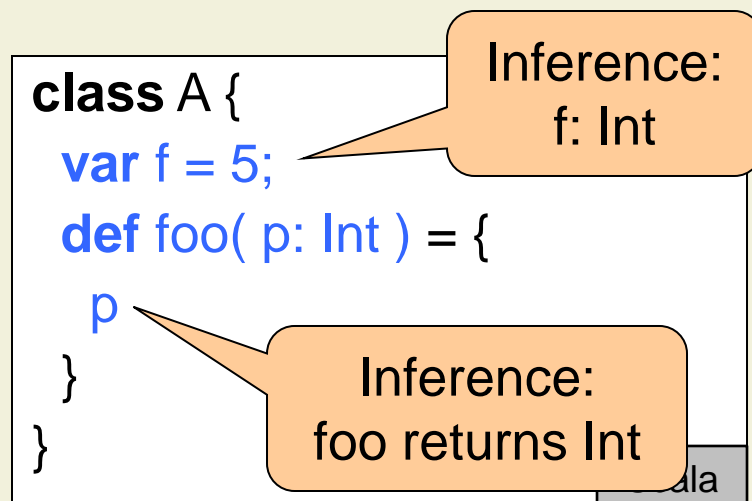
```
class A {  
  var f = 5;  
  def foo( p: Int ) = {  
    p  
  }  
}
```

Inference:
f: Int

Scala

Inference of Method and Field Types

- Inference of method signatures generally requires knowledge of all implementations
- Inference of field types generally requires knowledge of all assignments to the field
- Inference of these types is non-modular
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Inference of Method and Field Types

- Inference of method signatures generally requires knowledge of all implementations
- Inference of field types generally requires knowledge of all assignments to the field
- Inference of these types is non-modular
 - Or based on speculation

```
class A {  
  var f = 5;  
  def foo( p: Int ) = {  
    p  
  }  
}
```

Inference: f: Int

Inference: foo returns Int

Scala

```
class B extends A {  
  f = "Hello";  
  override def foo( p: Int ) = {  
    "Hello"  
  }  
}
```

Scala

4. Types

4.1 Bytecode Verification

4.2 Parametric Polymorphism

Polymorphism Revisited

- Not all polymorphic code is best expressed using subtype polymorphism
- Recovering precise type information requires **downcasts**

```
class Queue {  
    Object elem;  
    Queue next;  
    void enqueue( Object e ) { ... }  
    Object dequeue( ) { ... }  
}
```

Java

```
Queue q = new Queue( );  
String s = "Hello";  
q.enqueue( s );  
String t = ( String ) q.dequeue( );
```

Java

Polymorphism Revisited

- Not all polymorphic code is best expressed using subtype polymorphism
- Recovering precise type information requires **downcasts**
- Subtype relations are sometimes **not desirable**
 - E.g., covariant arrays

```
class Queue {  
    Object elem;  
    Queue next;  
    void enqueue( Object e ) { ... }  
    Object dequeue( ) { ... }  
}
```

Java

```
Queue q = new Queue( );  
String s = "Hello";  
q.enqueue( s );  
String t = ( String ) q.dequeue( );
```

Java

```
static void fill( Object[ ] a, Object val )  
{ ... }
```

Java

Parametric Polymorphism

- Classes and methods can be **parameterized with types**
- Clients provide instantiations for type parameters
- **Modularity**: generic code is type checked once and for all (without knowing the instantiations)

```
class Queue<T> {  
    T elem;  
    Queue<T> next;  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

Java

```
Queue<String> q;  
q = new Queue<String>( );  
String s = "Hello";  
q.enqueue( s );  
String t = q.dequeue( );
```

Java

```
static <T> void fill( T[ ] a, T val )  
{ ... }
```

Java

Type Checking Generic Code

- Type checking a generic class often **requires information about its type arguments**
 - Availability of methods
- Constraints can be expressed by specifying **upper bounds** on type parameters

```
class Queue<T> {  
    T elem;  
    Queue<T> next;  
  
    void enqueue( T e ) {  
        if( next == null ) { ... }  
        else {  
            if( e.compareTo( elem ) <= 0 ) {  
                next.enqueue( elem );  
                elem = e;  
            } else next.enqueue( e );  
        }  
    }  
    ...  
}
```

Java

Upper Bounds: Example

```
interface Comparable<T> {  
    int compareTo( T o );  
}
```

Java

```
class Queue<T extends Comparable<T>> {  
    T elem;  
    Queue<T> next;  
  
    void enqueue( T e ) {  
        if( next == null ) { ... }  
        else {  
            if( e.compareTo( elem ) <= 0 ) {  
                next.enqueue( elem );  
                elem = e;  
            } else next.enqueue( e );  
        }  
    }  
    ...  
}
```

Java

Upper Bounds: Example

```
interface Comparable<T> {  
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```
class Queue<T extends Comparable<T>> {  
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        if( next == null ) { ...  
        else {  
            if( e.compareTo( elem ) <= 0 ) {  
                next.enqueue( elem );  
                elem = e;  
            } else next.enqueue( e );  
        }  
    }  
    ...  
}
```

Typecheck under the
assumption
 $T \leq \text{Comparable}\langle T \rangle$

Java

Upper Bounds: Example

```
interface Comparable<T> {  
    int compareTo( T o );  
}
```

Java

```
Queue<String> q;  
// String implements  
    Comparable<String>
```

Java

```
class Queue<T extends Comparable<T>> {  
    T elem;  
    Queue<T> next;  
  
    void enqueue( T e ) {  
        if( next == null ) { ...  
        else {  
            if( e.compareTo( elem ) <= 0 ) {  
                next.enqueue( elem );  
                elem = e;  
            } else next.enqueue( e );  
        }  
    }  
    ...  
}
```

Typecheck under the
assumption
 $T \leq \text{Comparable} \langle T \rangle$

Java

Upper Bounds: Example

```
interface Comparable<T> {
    int compareTo( T o );
}
```

Java

```
Queue<String> q;
// String implements
    Comparable<String>
```

Java

```
Queue<Person> q;
// Person does not
    implement
    Comparable<Person>
```

Java

```
class Queue<T extends Comparable<T>> {
    T elem;
    Queue<T> next;

    void enqueue( T e ) {
        if( next == null ) { ...
        else {
            if( e.compareTo( elem ) <= 0 ) {
                next.enqueue( elem );
                elem = e;
            } else next.enqueue( e );
        }
    }
    ...
}
```

Typecheck under the
assumption
 $T \leq \text{Comparable}\langle T \rangle$

Java

Subtyping and Generics

```
class Queue<T extends Comparable<T>> { ... }
```


Subtyping and Generics

```
class Queue<T extends Comparable<T>> { ... }
```

- Generic types are subtypes of their declared supertypes

```
Object o = new Queue<String>( );
```

Subtyping and Generics

```
class Queue<T extends Comparable<T>> { ... }
```

- Generic types are subtypes of their declared supertypes
- Type variables are subtypes of their upper bounds

```
Object o = new Queue<String>( );
```

```
void foo( T p ) {  
    Comparable<T> v = p;  
}
```

Subtyping and Generics

```
class Queue<T extends Comparable<T>> { ... }
```

- Generic types are subtypes of their declared supertypes
- Type variables are subtypes of their upper bounds
- How about different instantiations of the same generic class?

```
Object o = new Queue<String>( );
```

```
void foo( T p ) {  
    Comparable<T> v = p;  
}
```

```
List<Person> o;  
o = new List<Student>( );  
o = new List<Object>( );
```

Covariant Type Arguments

- Covariance:
If $S <: T$ then
 $C<S> <: C<T>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

Covariant Type Arguments

- Covariance:
If $S <: T$ then
 $C<S> <: C<T>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<Object> q ) {  
    q.enqueue( "Hello" );  
}
```

Covariant Type Arguments

- Covariance:
If $S <: T$ then
 $C<S> <: C<T>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<Object> q ) {  
    q.enqueue( "Hello" );  
}
```

Not type safe if q had
type Queue<Integer>

Covariant Type Arguments

- Covariance:
If $S \leq T$ then
 $C \langle S \rangle \leq C \langle T \rangle$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<Object> q ) {  
    q.enqueue( "Hello" );  
}
```

Not type safe if q had
type Queue<Integer>

```
Object get( Queue<Object> q ) {  
    return q.dequeue( );  
}
```

Covariant Type Arguments

- Covariance:
If $S <: T$ then
 $C<S> <: C<T>$
- Covariance is unsafe
when a generic type
argument is used for
variables that are
written by clients
 - Mutable fields
 - Method arguments

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<Object> q ) {  
    q.enqueue( "Hello" );  
}
```

Not type safe if q had
type Queue<Integer>

```
Object get( Queue<Object> q ) {  
    return q.dequeue( );  
}
```


Contravariant Type Arguments

- Contravariance:
If $S <: T$ then
 $C<T> <: C<S>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

Contravariant Type Arguments

- Contravariance:
If $S <: T$ then
 $C<T> <: C<S>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<String> q ) {  
    q.enqueue( "Hello" );  
}
```

Contravariant Type Arguments

- Contravariance:
If $S <: T$ then
 $C<T> <: C<S>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<String> q ) {  
    q.enqueue( "Hello" );  
}
```

```
String get( Queue<String> q ) {  
    return q.dequeue( );  
}
```

Contravariant Type Arguments

- Contravariance:
If $S <: T$ then
 $C<T> <: C<S>$

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<String> q ) {  
    q.enqueue( "Hello" );  
}
```

```
String get( Queue<String> q ) {  
    return q.dequeue( );  
}
```

Not type safe if q had
type Queue<Object>

Contravariant Type Arguments

- Contravariance:
If $S <: T$ then
 $C<T> <: C<S>$
- Contravariance is unsafe when a generic type argument is used for variables that are read by clients
 - Fields
 - Method results

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

```
void put( Queue<String> q ) {  
    q.enqueue( "Hello" );  
}
```

```
String get( Queue<String> q ) {  
    return q.dequeue( );  
}
```

Not type safe if q had
type Queue<Object>

Java/C# Solution: Non-Variance

- Generic types in Java/C# are **non-variant** (neither co- nor contravariant)
- Non-variance is **statically type safe**
 - No run-time checks needed

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

Java

```
Queue<Object> o;  
o = new Queue<String>( );
```

Java

```
Queue<String> o;  
o = new Queue<Object>( );
```

Java

Java/C# Solution: Non-Variance

- Generic types in Java/C# are **non-variant** (neither co- nor contravariant)
- Non-variance is **statically type safe**
 - No run-time checks needed
- Non-variance is sometimes overly restrictive

```
class Queue<T> {  
    void enqueue( T e ) { ... }  
    T dequeue( ) { ... }  
}
```

Java

```
Queue<Object> o;  
o = new Queue<String>( );
```

Java

```
Queue<String> o;  
o = new Queue<Object>( );
```

Java

```
class Random<T> {  
    T next( ) { ... }  
}
```

Java/C#: Generics vs. Arrays

- Recall: Java/C# arrays are covariant
- But an array `T[]` is not much different from a class `Array<T>`

```
Object[ ] o;  
o = new String[ 5 ];
```

Java

```
Queue<Object> o;  
o = new Queue<String>( );
```

Java

Java/C#: Generics vs. Arrays

- Recall: Java/C# arrays are covariant
- But an array `T[]` is not much different from a class `Array<T>`
- Run-time checks
 - Covariant arrays require run-time checks for each update
 - Covariant generics would need checks for field updates and argument passing
- Covariant generics would require more run-time checks in more bytecode instructions

```
Object[ ] o;  
o = new String[ 5 ];
```

Java

```
Queue<Object> o;  
o = new Queue<String>( );
```

Java

Eiffel Solution: Covariance

- Generic types in Eiffel are **covariant**
- Design is consistent with covariance for method arguments and fields
 - But **not statically type safe**

```
class Queue[ T ] ... end
```

Eiffel

```
o: Queue[ ANY ]  
s: Queue[ STRING ]  
create s.make  
o := s
```

Eiffel

```
o: Queue[ ANY ]  
s: Queue[ STRING ]  
create o.make  
s := o
```

Eiffel

Scala Solution: Variance Annotations

- By default, generic types in Scala are **non-variant**

```
class Queue[T] {  
  def enqueue( e: T ) = { ... }  
  def dequeue: T = { ... }  
}
```

Scala

```
Queue[ AnyRef ] o;  
o = new Queue[ String ]( );
```

Scala

```
Queue[ String ] o;  
o = new Queue[ AnyRef ]( );
```

Scala

Scala Solution: Variance Annotations

- By default, generic types in Scala are **non-variant**
- Programmers can supply **variance annotations** to allow **co-** and **contravariance**

```
class Queue[T] {  
  def enqueue( e: T ) = { ... }  
  def dequeue: T = { ... }  
}
```

Scala

```
Queue[ AnyRef ] o;  
o = new Queue[ String ]( );
```

Scala

```
Queue[ String ] o;  
o = new Queue[ AnyRef ]( );
```

Scala

Scala Solution: Variance Annotations

- By default, generic types in Scala are **non-variant**
- Programmers can supply **variance annotations** to allow **co- and contravariance**
- Type checker imposes **restrictions** on use of variance annotations

```
class Queue[T] {  
  def enqueue( e: T ) = { ... }  
  def dequeue: T = { ... }  
}
```

Scala

```
Queue[ AnyRef ] o;  
o = new Queue[ String ]( );
```

Scala

```
Queue[ String ] o;  
o = new Queue[ AnyRef ]( );
```

Scala

Covariance Annotations

- A covariance annotation (+) is useful when type variable occurs **only in positive positions**
 - Result type
 - Types of immutable fields

```
class Random[ +T ] {  
  def next: T = { ... }  
}
```

Scala

```
val r: Random[ AnyRef ] =  
    new Random[ String ]( )  
val a = r.next
```

Scala

Covariance Annotations

- A covariance annotation (+) is useful when type variable occurs **only in positive positions**

- Result type
- Types of immutable fields

- Type checker prevents other occurrences

```
class Random[ +T ] {  
  def next: T = { ... }  
}
```

Scala

```
val r: Random[ AnyRef ] =  
    new Random[ String ]()  
val a = r.next
```

Scala

```
class Random[ +T ] {  
  def next: T = { ... }  
  def initialize( i: T ) = { ... }  
}
```

Scala

Contravariance Annotations

- A contravariance annotation (-) is useful when type variable occurs **only in negative positions**
 - Parameter type

```
class OutputChannel[ -T ] {  
  def write( x: T ) = { ... }  
}
```

Scala

```
val o: OutputChannel[ String ] =  
  new OutputChannel[ AnyRef ]( )  
o.write( "Hello" )
```

Scala

Contravariance Annotations

- A contravariance annotation (-) is useful when type variable occurs **only in negative positions**
 - Parameter type
- Type checker prevents other occurrences

```
class OutputChannel[ -T ] {  
  def write( x: T ) = { ... }  
}
```

Scala

```
val o: OutputChannel[ String ] =  
  new OutputChannel[ AnyRef ]( )  
o.write( "Hello" )
```

Scala

```
class OutputChannel[ -T ] {  
  def write( x: T ) = { ... }  
  def lastWritten: T = { ... }  
}
```

Scala

Working with Non-Variant Generics

- How can we write code that works with many different instantiations of a generic class?

Working with Non-Variant Generics

- How can we write code that works with many different instantiations of a generic class?
- Solution 1: Method type arguments

```
static <T> void printAll( Collection<T> c ) {  
    for ( T e : c ) { System.out.println( e ); }  
}
```

Java

Working with Non-Variant Generics

- How can we write code that works with many different instantiations of a generic class?
- Solution 1: Method type arguments

```
static <T> void printAll( Collection<T> c ) {  
    for ( T e : c ) { System.out.println( e ); }  
}
```

Java

- Solution 2: Wildcards

```
static void printAll( Collection<?> c ) {  
    for ( Object e : c ) { System.out.println( e ); }  
}
```

Java

Wildcards and Existential Types

- A wildcard represents an **unknown type**

```
static void printAll( Collection<?> c ) {  
    for ( Object e : c ) { System.out.println( e ); }  
}
```

Java

- Interpretation as **existential type**
 - “There exists a type argument T such that c has type Collection<T>”
 - Existential quantifier is instantiated automatically by the type system

```
Collection<String> c = new ArrayList<String>( );  
...  
printAll( c );
```

Java

Wildcards and Existential Types

- A wildcard represents an **unknown type**

```
static void printAll( Collection<?> c ) {  
    for ( Object e : c ) { System.out.println( e ); }  
}
```

Java

- Interpretation as **existential type**
 - “There exists a type argument T such that c has type Collection<T>”
 - Existential quantifier is instantiated automatically by the type system

```
Collection<String> c = new ArrayList<String>( );  
...  
printAll( c );
```

Wildcard instantiated
with String

Java

Wildcard Examples

```
static Collection<?> id( Collection<?> c ) {  
    return c;  
}
```

Wildcard Examples

```
static Collection<?> id( Collection<?> c ) {  
    return c;  
}
```

Two existential
types

Wildcard Examples

Correct: type checker
instantiates type argument
with c's type argument

```
static Collection<?> id( Collection<?> c ) {  
    return c;  
}
```

Two existential
types

Wildcard Examples

Correct: type checker
instantiates type argument
with c's type argument

```
static Collection<?> id( Collection<?> c ) {  
    return c;  
}
```

Two existential
types

```
Collection<String> c = new ArrayList<String>( );  
Collection<String> d = id( c );
```

Wildcard Examples

Correct: type checker
instantiates type argument
with c's type argument

```
static Collection<?> id( Collection<?> c ) {  
    return c;  
}
```

Two existential
types

```
Collection<String> c = new ArrayList<String>( );  
Collection<String> d = id( c );
```

Type error: existential
types might have
different instantiations
(modular type checking)

Wildcard Examples (cont'd)

```
static void merge( Collection<?> c, Collection<?> d ) {  
    for( Object e : c ) { d.add( e ); }  
}
```

Wildcard Examples (cont'd)

```
static void merge( Collection<?> c, Collection<?> d ) {  
    for( Object e : c ) { d.add( e ); }  
}
```

Two existential
types

Wildcard Examples (cont'd)

```
static void merge( Collection<?> c, Collection<?> d ) {  
    for( Object e : c ) { d.add( e ); }  
}
```

Two existential
types

Type error: d might
expect elements of
different type

Wildcard Examples (cont'd)

```
class Spooler {  
    Collection<?> task;  
  
    void setTask( Collection<?> c ) {  
        task = c;  
    }  
    void print( ) {  
        for ( Object e : task ) { System.out.println( e ); }  
    }  
}
```

Wildcard Examples (cont'd)

```
class Spooler {  
    Collection<?> task;  
  
    void setTask( Collection<?> c ) {  
        task = c;  
    }  
  
    void print( ) {  
        for ( Object e : task ) { System.out.println( e ); }  
    }  
}
```

Correct: type checker
instantiates task's type
argument with c's

Wildcard Examples (cont'd)

```
class Spooler {  
    Collection<?> task;  
  
    void setTask( Collection<?> c ) {  
        task = c;  
    }  
  
    void print( ) {  
        for ( Object e : task ) { System.out.println( e ); }  
    }  
}
```

Cannot be simulated
with method type
parameters

Correct: type checker
instantiates task's type
argument with c's

Wildcard Examples (cont'd)

```
class Spooler {  
    Collection<?> task;  
  
    void setTask( Collection<?> c ) {  
        task = c;  
    }  
  
    void print( ) {  
        for ( Object e : task ) { System.out.println( e ); }  
    }  
}
```

Cannot be simulated
with method type
parameters

Correct: type checker
instantiates task's type
argument with c's

Works because
every Java object
has toString method

Constrained Wildcards

```
static void printFormatted( Collection<?> c ) {  
    for ( Object e : c ) {  
        String s = e.format( 80 );  
        System.out.println( s );  
    }  
}
```

Constrained Wildcards

```
static void printFormatted( Collection<?> c ) {  
    for ( Object e : c ) {  
        String s = e.format( 80 );  
        System.out.println( s );  
    }  
}
```

Type error: elements
might not support
method format

Constrained Wildcards: Upper Bounds

```
interface Format {  
    String format( int width );  
}
```

```
static void printFormatted( Collection<? extends Format> c ) {  
    for ( Format e : c ) {  
        String s = e.format( 80 );  
        System.out.println( s );  
    }  
}
```

Constrained Wildcards: Upper Bounds

```
interface Format {  
    String format( int width );  
}
```

```
static void printFormatted( Collection<? extends Format> c ) {  
    for ( Format e : c ) {  
        String s = e.format( 80 );  
        System.out.println( s );  
    }  
}
```

Typecheck under the
assumption
? <: Format

Constrained Wildcards: Upper Bounds

```
interface Format {  
    String format( int width );  
}
```

```
static void printFormatted( Collection<? extends Format> c ) {  
    for ( Format e : c ) {  
        String s = e.format( 80 );  
        System.out.println( s );  
    }  
}
```

Typecheck under the
assumption
? <: Format

```
Collection<Object> c = new ArrayList<Object>( );  
printFormatted( c );
```

Constrained Wildcards: Upper Bounds

```
interface Format {  
    String format( int width );  
}
```

```
static void printFormatted( Collection<? extends Format> c ) {  
    for ( Format e : c ) {  
        String s = e.format( 80 );  
        System.out.println( s );  
    }  
}
```

Typecheck under the
assumption
? <: Format

```
Collection<Object> c = new ArrayList<Object>( );  
printFormatted( c );
```

Compile-time error:
Object is not a subtype of
the upper bound Format

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
}
```

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
}
```

Overly
restrictive

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<?> other ) {  
        value = other.value;  
    }  
  
}
```

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<?> other ) {  
        value = other.value;  
    }  
}
```

Not type
correct

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<? extends T> other ) {  
        value = other.value;  
    }  
  
}
```

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<? extends T> other ) {  
        value = other.value;  
    }  
}
```

Typecheck under
the assumption

? <: T

More Bounded Wildcards

Typecheck under
the assumption

$? \leq T$

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<? extends T> other ) {  
        value = other.value;  
    }  
  
    void copyTo( Cell<?> other ) {  
        other.value = value;  
    }  
}
```

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<? extends T> other ) {  
        value = other.value;  
    }  
  
    void copyTo( Cell<?> other ) {  
        other.value = value;  
    }  
}
```

Typecheck under
the assumption

$? <: T$

Not type
correct

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<? extends T> other ) {  
        value = other.value;  
    }  
  
    void copyTo( Cell<? super T> other ) {  
        other.value = value;  
    }  
}
```

Typecheck under
the assumption

? <: T

Wildcard can
also have
lower bounds

More Bounded Wildcards

```
class Cell<T> {  
    T value;  
  
    void copyFromT( Cell<T> other ) {  
        value = other.value;  
    }  
  
    void copyFrom( Cell<? extends T> other ) {  
        value = other.value;  
    }  
  
    void copyTo( Cell<? super T> other ) {  
        other.value = value;  
    }  
}
```

Typecheck under
the assumption

$? \leq T$

Typecheck under
the assumption

$T \leq ?$

Wildcard can
also have
lower bounds

Wildcards vs. Additional Type Parameters

- Often wildcards can be replaced by additional class or method type arguments
 - C# does not have wildcards

```
static <T> void printAll( Collection<T> c ) {  
    for ( T e : c ) { System.out.println( e ); }  
}
```

Java

```
static void printAll( Collection<?> c ) {  
    for ( Object e : c ) { System.out.println( e ); }  
}
```

Java

Wildcards vs. Method Type Parameters

```
void copyFrom( Cell<? extends T> other ) {  
    value = other.value;  
}
```

```
<S extends T> void copyFrom( Cell<S> other ) {  
    value = other.value;  
}
```

Wildcards vs. Method Type Parameters

```
void copyFrom( Cell<? extends T> other ) {  
    value = other.value;  
}
```

```
<S extends T> void copyFrom( Cell<S> other ) {  
    value = other.value;  
}
```

```
Cell<String> s;  
Cell<Object> o;  
s = new Cell<String>();  
o = new Cell<Object>();  
o.copyFrom( s );
```

Wildcards vs. Method Type Parameters

```
void copyFrom( Cell<? extends T> other ) {  
    value = other.value;  
}
```

```
<S extends T> void copyFrom( Cell<S> other ) {  
    value = other.value;  
}
```

```
Cell<String> s;  
Cell<Object> o;  
s = new Cell<String>();  
o = new Cell<Object>();  
o.copyFrom( s );
```

Identical client code:
instantiations of
wildcard and method
type argument are
inferred

Wildcards vs. Method Type Parameters

```
void copyFrom( Cell<? extends T> other ) {  
    value = other.value;  
}
```

```
<S extends T> void copyFrom( Cell<S> other ) {  
    value = other.value;  
}
```

```
void copyTo( Cell<? super T> other ) {  
    other.value = value;  
}
```

```
<S super T> void copyTo( Cell<S> other ) {  
    other.value = value;  
}
```

```
Cell<String> s;  
Cell<Object> o;  
s = new Cell<String>();  
o = new Cell<Object>();  
o.copyFrom( s );
```

Identical client code:
instantiations of
wildcard and method
type argument are
inferred

Wildcards vs. Method Type Parameters

```
void copyFrom( Cell<? extends T> other ) {  
    value = other.value;  
}
```

```
<S extends T> void copyFrom( Cell<S> other ) {  
    value = other.value;  
}
```

```
void copyTo( Cell<? super T> other ) {  
    other.value = value;  
}
```

```
<S super T> void copyTo( Cell<S> other ) {  
    other.value = value;  
}
```

```
Cell<String> s;  
Cell<Object> o;  
s = new Cell<String>();  
o = new Cell<Object>();  
o.copyFrom( s );
```

Identical client code:
instantiations of
wildcard and method
type argument are
inferred

Java does not support
lower bounds for type
parameters

Wildcards vs. Class Type Parameters

```
class Wrapper {  
    Cell<?> data;  
}
```

```
class Wrapper<T> {  
    Cell<T> data;  
}
```

Wildcards vs. Class Type Parameters

```
class Wrapper {  
    Cell<?> data;  
}
```

```
Wrapper w = new Wrapper( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

```
class Wrapper<T> {  
    Cell<T> data;  
}
```

Wildcards vs. Class Type Parameters

```
class Wrapper {  
    Cell<?> data;  
}
```

```
Wrapper w = new Wrapper( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

```
class Wrapper<T> {  
    Cell<T> data;  
}
```

```
Wrapper w = new Wrapper<Object>( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

Wildcards vs. Class Type Parameters

```
class Wrapper {  
  Cell<?> data;  
}
```

Instantiation can
change over time

```
Wrapper w = new Wrapper( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

```
class Wrapper<T> {  
  Cell<T> data;  
}
```

```
Wrapper w = new Wrapper<Object>( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

Wildcards vs. Class Type Parameters

```
class Wrapper {  
  Cell<?> data;  
}
```

Instantiation can
change over time

```
Wrapper w = new Wrapper( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

```
class Wrapper<T> {  
  Cell<T> data;  
}
```

```
Wrapper w = new Wrapper<Object>( );  
w.data = new Cell<String>( );  
w.data = new Cell<Object>( );
```

With type argument,
instantiation is fixed
when object is created

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

TreeSet needs to
compare set elements

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

TreeSet needs to
compare set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```


Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

TreeSet needs to
compare set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```

Universal comparator
for all persons

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

TreeSet needs to
compare set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```

Universal comparator
for all persons

```
TreeSet<Student> s = new TreeSet<Student>( new PersonComp() );
```

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

TreeSet needs to
compare set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```

Universal comparator
for all persons

```
TreeSet<Student> s = new TreeSet<Student>( new PersonComp() );
```

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<E> c ) { ... }  
    ... }
```

TreeSet needs to
compare set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```

Universal comparator
for all persons

```
TreeSet<Student> s = new TreeSet<Student>( new PersonComp() );
```

Compile-time error: PersonComp is not
a subtype of Comparator<Student>

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<? super E> c ) { ... }  
    ... }
```

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```

Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
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class TreeSet<E> {  
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```

TreeSet needs to compare
at least set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
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Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
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at least set elements

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class Person { ... }
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class Student extends Person { ... }
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class PersonComp implements Comparator<Person> {  
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TreeSet<Student> s = new TreeSet<Student>( new PersonComp() );
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Wildcards vs. Type Parameters (cont'd)

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interface Comparator<T> {  
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class TreeSet<E> {  
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```

TreeSet needs to compare
at least set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
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```
TreeSet<Student> s = new TreeSet<Student>( new PersonComp() );
```


Wildcards vs. Type Parameters (cont'd)

```
interface Comparator<T> {  
    int compare( T fst, T snd );  
}
```

```
class TreeSet<E> {  
    TreeSet( Comparator<? super E> c ) { ... }  
    ... }
```

TreeSet needs to compare
at least set elements

```
class Person { ... }
```

```
class Student extends Person { ... }
```

```
class PersonComp implements Comparator<Person> {  
    int compare( Person fst, Person snd ) { ... }  
}
```

```
TreeSet<Student> s = new TreeSet<Student>( new PersonComp() );
```

Wildcard instantiated with Person,
which is a supertype of Student

Subtyping and Generics: Wildcards

- The bounds for a wildcard determine the set of possible instantiations

```
Cell<? extends Person> c;  
Cell<? super PhDStudent> d;
```

- S is a subtype of T if for each type argument, the set of possible instantiations for S is a subset of the set of possible instantiations for T

Subtyping and Generics: Wildcards

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Cell<? extends Person> c;  
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- S is a subtype of T if for each type argument, the set of possible instantiations for S is a subset of the set of possible instantiations for T

```
c = new Cell<Student>( );
```

Subtyping and Generics: Wildcards

- The bounds for a wildcard determine the set of possible instantiations

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Cell<? super PhDStudent> d;
```

- S is a subtype of T if for each type argument, the set of possible instantiations for S is a subset of the set of possible instantiations for T

```
c = new Cell<Student>( );
```

Instantiation is fixed
(singleton set)

Subtyping and Generics: Wildcards

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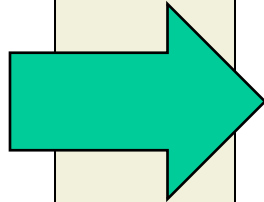
```
Cell<? extends Student> e = ...;  
c = e;
```

Type Erasure

- Java introduced generics in version 1.4
- For **backwards compatibility**, Sun did not want to change the virtual machine
- **Generic type information is erased** by compiler
 - $C<T>$ is translated to C
 - T is translated to its upper bound
 - Casts are added where necessary
- Only one classfile and only one class object to represent all instantiations of a generic class

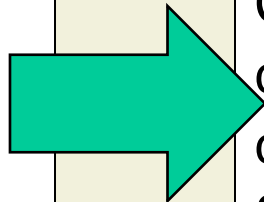
Type Erasure: Example

```
class Cell<T extends Object> {  
    T value;  
  
    void set( T v ) {  
        value = v;  
    }  
  
    T get( ) {  
        return value;  
    }  
}
```



```
class Cell {  
    Object value;  
  
    void set( Object v ) {  
        value = v;  
    }  
  
    Object get( ) {  
        return value;  
    }  
}
```

```
Cell<String> c;  
c = new Cell<String>( );  
c.set( "Hello" );  
String s = c.get( );
```



```
Cell c;  
c = new Cell( );  
c.set( "Hello" );  
String s = ( String ) c.get( );
```

Erasure: Missing Run-Time Information

```
void foo( Cell<?> c ) {  
    if( c instanceof Cell<String> )  
        ...  
}
```

Java

Erasure: Missing Run-Time Information

```
void foo( Cell<?> c ) {  
    if( c instanceof Cell<String> )  
        ...  
}
```

Java

Compile-time error:
generic types not
allowed with **instanceof**

Erasure: Missing Run-Time Information

```
void foo( Cell<?> c ) {  
    if( c instanceof Cell<String> )  
        ...  
}
```

Java

Compile-time error:
generic types not
allowed with **instanceof**

```
Class c = Cell<String>.class;
```

Java

Erasure: Missing Run-Time Information

```
void foo( Cell<?> c ) {  
    if( c instanceof Cell<String> )  
        ...  
}
```

Java

Compile-time error:
generic types not
allowed with **instanceof**

```
Class c = Cell<String>.class;
```

Java

Compile-time error:
class object of generic
types not available

Erasure: Missing Run-Time Information

```
void foo( Cell<?> c ) {  
    if( c instanceof Cell<String> )  
        ...  
}
```

Java

Compile-time error:
generic types not
allowed with **instanceof**

```
Class c = Cell<String>.class;
```

Java

Compile-time error:
class object of generic
types not available

```
Cell<String>[ ] a;  
a = new Cell<String>[10];
```

Java

Erasure: Missing Run-Time Information

```
void foo( Cell<?> c ) {  
    if( c instanceof Cell<String> )  
        ...  
}
```

Java

Compile-time error:
generic types not
allowed with **instanceof**

```
Class c = Cell<String>.class;
```

Java

Compile-time error:
class object of generic
types not available

```
Cell<String>[ ] a;  
a = new Cell<String>[10];
```

Java

Compile-time error:
arrays of generic types
not allowed

Run-Time Information for Generics in C#

```
void Foo( object c ) {  
    if( c is Cell<string> )  
        ...  
}
```

C#

Run-Time Information for Generics in C#

```
void Foo( object c ) {  
    if( c is Cell<string> )  
        ...  
}
```

C# does not
have wildcards

C#

Run-Time Information for Generics in C#

```
void Foo( object c ) {  
    if( c is Cell<string> )  
        ...  
}
```

C# does not
have wildcards

C# can perform
dynamic type test

C#

Run-Time Information for Generics in C#

```
void Foo( object c ) {  
    if( c is Cell<string> )  
        ...  
}
```

C# does not
have wildcards

C# can perform
dynamic type test

C#

```
System.Type type = typeof( Cell<string> );
```

C#

Run-Time Information for Generics in C#

```
void Foo( object c ) {  
    if( c is Cell<string> )  
        ...  
}
```

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C#

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System.Type type = typeof( Cell<string> );
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C# has run-time
representation

Run-Time Information for Generics in C#

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    if( c is Cell<string> )  
        ...  
}
```

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```
System.Type type = typeof( Cell<string> );
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representation

```
Cell<String>[ ] a;  
a = new Cell<string>[10];
```

C#

Run-Time Information for Generics in C#

```
void Foo( object c ) {  
    if( c is Cell<string> )  
        ...  
}
```

C# does not
have wildcards

C# can perform
dynamic type test

C#

```
System.Type type = typeof( Cell<string> );
```

C# has run-time
representation

```
Cell<String>[ ] a;  
a = new Cell<string>[10];
```

C# can perform run-time
check for array update

Erasure: Missing Run-Time Checks

```
String demo( Cell<?> c ) {  
    Cell<String> cs = ( Cell<String> ) c;  
    ...  
    return cs.val;  
}
```

Java

Erasure: Missing Run-Time Checks

```
String demo( Cell<?> c ) {  
    Cell<String> cs = ( Cell<String> ) c;  
    ...  
    return cs.val;  
}
```

Java

```
void main( ) {  
    Cell<Object> co = new Cell<Object>( );  
    co.val = new Integer( 5 );  
    demo( co );  
}
```

Java

Erasure: Missing Run-Time Checks

```
String demo( Cell<?> c ) {  
    Cell<String> cs = ( Cell<String> ) c;  
    ...  
    return cs.val;  
}
```

No run-time
check for this
cast!

Java

```
void main( ) {  
    Cell<Object> co = new Cell<Object>( );  
    co.val = new Integer( 5 );  
    demo( co );  
}
```

Java

Erasure: Missing Run-Time Checks

```
String demo( Cell<?> c ) {  
    Cell<String> cs = ( Cell<String> ) c;  
    ...  
    return cs.val;  
}
```

No run-time
check for this
cast!

Type invariant broken:
object in cs is not of
type Cell<String>!

```
void main( ) {  
    Cell<Object> co = new Cell<Object>( );  
    co.val = new Integer( 5 );  
    demo( co );  
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```

Java

Erasure: Missing Run-Time Checks

```
String demo( Cell<?> c ) {  
    Cell<String> cs = ( Cell<String> ) c;  
    ...  
    return cs.val;  
}
```

No run-time
check for this
cast!

Run-time error:
cs.val is not a
string

Type invariant broken:
object in cs is not of
type Cell<String>!

```
void main( ) {  
    Cell<Object> co = new Cell<Object>( );  
    co.val = new Integer( 5 );  
    demo( co );  
}
```

Java

Other Consequences of Erasure

- Static fields are shared by all instantiations of a generic class

```
class Count<T> {  
    static int c = 0;  
}
```

Other Consequences of Erasure

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class Count<T> {  
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```
Count<string>.c = 1;  
Count<object>.c = 2;
```

C#

Other Consequences of Erasure

- Static fields are shared by all instantiations of a generic class

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class Count<T> {  
    static int c = 0;  
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Count<string>.c = 1;  
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C#

```
Count.c = 1;  
Count.c = 2;
```

Java

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- Static fields are shared by all instantiations of a generic class

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class Count<T> {  
    static int c = 0;  
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Count<string>.c = 1;  
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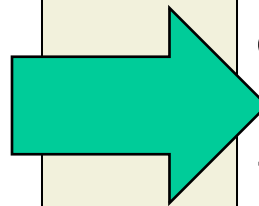
C#

```
Count.c = 1;  
Count.c = 2;
```

Java

- Lower bounds for type parameters

```
class Cell<T super L> {  
    T value;  
}
```



```
class Cell {  
    Object value;  
}
```

Other Consequences of Erasure

- Static fields are shared by all instantiations of a generic class

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class Count<T> {  
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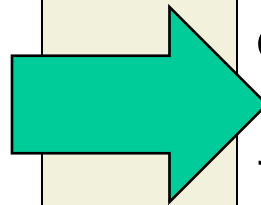
C#

```
Count.c = 1;  
Count.c = 2;
```

Java

- Lower bounds for type parameters

```
class Cell<T super L> {  
    T value;  
}
```



```
class Cell {  
    Object value;  
}
```

- Enforcing lower bound would require many run-time checks (e.g., for each field update)

C++ Templates

- Templates allow classes and methods to be **parameterized**
- Clients provide instantiations for template parameters

```
template<class T> class Queue {  
    T elem;  
    Queue<T>* next;  
public:  
    void enqueue( T e ) { ... };  
    T dequeue( void ) { ... };  
};
```

C++

```
Queue<int> *q;  
q = new Queue<int>( );  
int s = 5;  
q->enqueue( s );  
int t = q->dequeue( );
```

C++

```
template<class T> void fill( T a[ ], T v )  
{ ... };
```

C++

Template Instantiation

```
template<class T> class Queue {  
    T elem;  
    Queue<T>* next;  
    ...  
};
```

```
Queue<int> *q;  
...
```

Template Instantiation

```
class Queueint {  
    int elem;  
    Queueint* next;  
    ...  
};
```

```
Queueint *q;  
...
```


Template Instantiation

```
template<class T> class Queue {  
    T elem;  
    Queue<T>* next;  
    ...  
};
```

Compiler generates
class for given
template instantiation

```
class Queueint {  
    int elem;  
    Queueint* next;  
    ...  
};
```

```
Queue<int> *q;  
...
```

Template Instantiation

```
Queueint *q;  
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Template Instantiation

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template<class T> class Queue {  
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Queue<int> *q;  
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Template Instantiation

```
Queueint *q;  
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Client code uses
generated class

Template Instantiation

```
template<class T> class Queue {  
    T elem;  
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};
```

Compiler generates
class for given
template instantiation

```
class Queueint {  
    int elem;  
    Queueint* next;  
    ...  
};
```

Type checking is
done for generated
class, not for template

```
Queue<int> *q;  
...
```

Template Instantiation

```
Queueint *q;  
...
```

Client code uses
generated class

Templates and Type Checking

```
template<class T> class Queue {  
    T elem; Queue<T>* next;  
public:  
    void enqueue( T e ) {  
        if( next == NULL ) {  
            elem = e; next = new Queue<T>( );  
        } else {  
            if( e.compareTo( elem ) <= 0 )  
                next->enqueue( elem ); elem = e;  
            else next->enqueue( e );  
        }  
    };  
    T dequeue( void ) { return "Hello"; };  
};
```

Templates and Type Checking

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template<class T> class Queue {  
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            else next->enqueue( e );  
        }  
    };  
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};
```

Compiler does not type
check template code

Templates and Type Checking

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            elem = e; next = new Queue<T>( );  
        } else {  
            if( e.compareTo( elem ) <= 0 )  
            { next->enqueue( elem ); elem = e; }  
            else next->enqueue( e );  
        }  
    };  
    T dequeue( void ) { return "Hello"; };  
};
```

Compiler does not
check availability
of methods

Compiler does not type
check template code

Templates and Type Checking

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template<class T> class Queue {  
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```
Queue<int> *q;  
q = new Queue<int>( );
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Templates and Type Checking

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            { next->enqueue( elem ); elem = e; }  
            else next->enqueue( e );  
        }  
    };  
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Queue<int> *q;  
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Templates and Type Checking

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            elem = e; next = new Queue<T>( );  
        } else {  
            if( e.compareTo( elem ) <= 0 )  
            { next->enqueue( elem ); elem = e; }  
            else next->enqueue( e );  
        }  
    };  
    T dequeue( void ) { return "Hello"; };  
};
```

Compiler does not
check availability
of methods

```
Queue<int> *q;  
q = new Queue<int>( );
```

Compiles even
though template
is instantiated

Compiler does not type
check template code

Templates and Type Checking

```
template<class T> class Queue {  
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        }  
    };  
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};
```

Compiler does not
check availability
of methods

```
Queue<int> *q;  
q = new Queue<int>( );
```

Compiles even
though template
is instantiated

```
Queue<int> *q;  
q = new Queue<int>( );  
int s = 5;  
q->enqueue( s );  
int t = q->dequeue( );
```

Compiler does not type
check template code

Templates and Type Checking

```
template<class T> class Queue {  
    T elem; Queue<T>* next;  
public:  
    void enqueue( T e ) {  
        if( next == NULL ) {  
            elem = e; next = new Queue<T>( );  
        } else {  
            if( e.compareTo( elem ) <= 0 )  
            { next->enqueue( elem ); elem = e; }  
            else next->enqueue( e );  
        }  
    };  
    T dequeue( void ) { return "Hello"; };  
};
```

Compiler does not
check availability
of methods

Compiler does not type
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```
Queue<int> *q;  
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Compiles even
though template
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Queue<int> *q;  
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```

Templates and Type Checking

```

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    T elem; Queue<T>* next;
public:
    void enqueue( T e ) {
        if( next == NULL ) {
            elem = e; next = new Queue<T>( );
        } else {
            if( e.compareTo( elem ) <= 0 )
            { next->enqueue( elem ); elem = e; }
            else next->enqueue( e );
        }
    };
    T dequeue( void ) { return "Hello"; };
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```

Compiler does not
check availability
of methods

```

Queue<int> *q;
q = new Queue<int>( );

```

Compiles even
though template
is instantiated

Compile-time errors:
template methods
not type correct

```

Queue<int> *q;
q = new Queue<int>( );
int s = 5;
q->enqueue( s );
int t = q->dequeue( );

```

Compiler does not type
check template code

Templates and Type Checking (cont'd)

- Template code is not type checked
 - Type errors are not detected before instantiation
- No need for upper bounds on type parameters
 - Availability of methods is not checked anyway
 - Template has to document (informally) what it expects from its type arguments
- Different instantiations of templates are unrelated
 - Use template methods to write polymorphic methods
- Templates do not require run-time support
 - Run-time types correspond to generated classes

Template Meta-Programming

```
template <int n> class Fact {  
public:  
    static const int val = Fact<n-1>::val * n;  
};
```

Template Meta-Programming

```
template <int n> class Fact {  
public:  
    static const int val = Fact<n-1>::val * n;  
};
```

Template parameters
need not be types

Template Meta-Programming

```
template <int n> class Fact {  
public:  
    static const int val = Fact<n-1>::val * n;  
};
```

Template parameters
need not be types

```
class Fact<0> {  
public:  
    static const int val = 1;  
};
```

Template Meta-Programming

```
template <int n> class Fact {  
public:  
    static const int val = Fact<n-1>::val * n;  
};
```

Template parameters
need not be types

```
class Fact<0> {  
public:  
    static const int val = 1;  
};
```

Templates can
be specialized

Template Meta-Programming

```
template <int n> class Fact {  
public:  
    static const int val = Fact<n-1>::val * n;  
};
```

Template parameters
need not be types

```
class Fact<0> {  
public:  
    static const int val = 1;  
};
```

Templates can
be specialized

```
int main( ) {  
    printf( "fact 3 = %d\n", Fact<3>::val );  
    printf( "fact 4 = %d\n", Fact<4>::val );  
    printf( "fact 5 = %d\n", Fact<5>::val );  
    return 0;  
}
```

Template Meta-Programming

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Templates can
be specialized

Compiler generates
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Through constant
propagation, values
are **computed by
compiler**

```
int main( ) {  
    printf( "fact 3 = %d\n", Fact<3>::val );  
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Generic Types vs. Templates: Summary

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Templates

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- Modular type checking of generic class
 - Overhead (e.g., upper bounds)

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- Type checking per instantiation
 - Flexibility like with structural typing

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Templates

- Type checking per instantiation
 - Flexibility like with structural typing
- No need for run-time support
- Meta-programming is Turing-complete