

Exercise 3

Subtyping and Behavioral Subtyping

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Task 1

In this question, we are in a nominal subtyping setting. Some languages have a special type `MyType` that represents the *dynamic type* of `this` object.

- (a) Consider the following code:

```
class Point
{
    int x,y;
    boolean equals(MyType other)
    { return x == other.x && y == other.y; }
}

class ColorPoint extends Point
{
    int color;
    override boolean equals(MyType other)
    { return super.equals(other) && color == other.color; }
}
```

This definition requires that the dynamic type of the parameter of `equals` is a subtype of the dynamic type of `this`.

Consider the following definitions that give static types to some variables:

```
Point p;
ColorPoint cp1, cp2;
```

and the following calls:

```
p.equals(cp1)    // A
p.equals(cp2)    // B
cp1.equals(p)    // C
cp2.equals(cp1)  // D
cp1.equals(cp2)  // E
```

Assume a sound, statically-checked type system. Which of the calls above must be forbidden and which may be allowed? Why?

- (b) Answer the same question, assuming that `ColorPoint` is *final*, i.e., we may not declare new classes as its subtypes.
- (c) Assume now that the language includes the feature of *exact types*. An exact type is written `@C` where `C` is a normal type. When we declare that an object `o` is of type `@C`, then `o` is of type `C`, but does not belong to any of the other subtypes of `C`. Assume that the definitions of our variables are changed as follows:

```
@Point p;
@ColorPoint cp1;
ColorPoint cp2;
```

and do not assume that `ColorPoint` is `final`. Which calls should be forbidden now? Why?

Hint. The classes shown here may be subclassed in code that is not available. The type-checker *cannot* make the assumption that there are no other class definitions elsewhere.

Task 2

Let `SortedArray` be a Java class, which has a private field `A`. The field `A` must be a sorted (in increasing order) array of integers with no duplicates. The following method inserts a value into the array:

```
void insert (int x)
{
    int[] B = new int[A.length + 1];
    int i = 0;
    while (i < A.length && A[i] < x)
    {
        B[i] = A[i];
        i++;
    }
    B[i] = x;
    while (i < A.length)
    {
        B[i+1] = A[i];
        i++;
    }
    A = B;
}
```

Give an appropriate invariant for the class, as well as a precondition and a postcondition for the method `insert`. You may use quantifiers (\forall, \exists) in your annotations. Note that the invariant is automatically checked at the end of the method body and you do not need to explicitly include it in the postcondition.

Hint: Consider what happens when the item to be inserted into the array already exists. Do *not* change the implementation to avoid this situation.

Task 3

Alice and Bob are two software developers. Alice is writing a small class `Cell` that stores an integer. The class supports methods for setting/getting/increasing the integer. Bob is going to write code that uses the class `Cell`.

Here are the contracts of the methods (the bodies are omitted):

```
class Cell {

    public int n;
    // this field is public for simplicity
    // generally this is not a recommended practice

    /// requires true
    /// ensures n == p
    public void set(int p) { ... }
```

```

    /// requires true
    /// ensures result == n
    public int get() { ... }

    /// requires true
    /// ensures n > old(n)
    public void inc() { ... }
}

```

In this exercise we will experiment with modifying the specifications. In particular, if we modify a specification, this might become:

- *more restrictive* for a party. For example, a specification that is more restrictive for Alice might not allow some implementations that were OK with the old specification. A specification that is more restrictive for Bob might mean that a piece of code that Bob wrote cannot guarantee something that it had guaranteed before.
- *more flexible* for a party. If a specification S is more flexible than a specification S' for a party P , then S' is more restrictive than S for P .
- it might be the case that the new specification is neither more restrictive nor more flexible for a party. For example, the new specification makes some previously correct code illegal, while it also makes some previously illegal code correct.

For example, if we modify the postcondition of `get` such that:

```
result == n || result == -n
```

the specification becomes more flexible for Alice, because she is allowed the, previously illegal, implementation of `get`:

```
return n > 5 ? n : -n;
```

while, at the same time, it becomes more restrictive for Bob, because the following code

```
c.set(3); x = c.get();
```

does not guarantee the postcondition `x == 3` anymore.

For each of the following specification changes (subtasks a-d), do the following:

- Write formally the new pre/postconditions (not invariants). Only write the pre/postconditions that change.
- Compare the flexibility of the new specifications to the old ones, from the point of view of both Alice and Bob.
- Justify your answers for both parties by *providing code*.

Note that a postcondition should be satisfiable for any valid pre-state. You can assume that the implementation of the methods do not call each other.

- It is only allowed to set `n` to a strictly positive value.
- `inc` should increase `n` by exactly one.
- `inc` should increase `n` by any amount, but it should guarantee that the final value of `n` is strictly positive.
- `inc` should increase `n` by exactly one *and* should guarantee that the final value of `n` is strictly positive. If necessary, add preconditions to ensure that it is possible for Alice to achieve this goal.

Task 4

(from a previous exam)

Assume we add an `otherwise` clause to method contracts in Java, which gives a condition on the state after the method throws an exception. The implementation of the method has to guarantee that the condition in the `otherwise` clause is true whenever the method returns exceptionally (that is, via throwing an exception).

Consider a class with an integer field `f` and the following Java method and its precondition and an `otherwise`-clause (reminder: `final` parameters cannot be assigned to):

```
/// requires   n > 0
/// otherwise  f < 0
void foo(final int n) throws IOException
```

Assume method `foo` is overridden in a subclass and that we do not use specification inheritance. Which of the following functions ...

1. ... override `foo` correctly based on the variance rules of Java *and*
2. ... have preconditions and `otherwise`-clauses that would be allowed if the subclass should be a behavioral subtype?

For this, decide what kind of relationship between `otherwise`-clauses of behavioral subtypes should exist, basing your decision on the substitution principle.

For this exercise, assume `FileNotFoundException <: IOException <: Exception` and that there is no integer overflow.

- (a) **requires** `n == 0`
 otherwise `f == -1`
 void foo(**final int** n) **throws** `FileNotFoundException`
- (b) **requires** `n > 0`
 otherwise `f * f > 0`
 void foo(**final int** n) **throws** `IOException`
- (c) **requires** `n >= 0`
 otherwise `f < -n`
 void foo(**final int** n) **throws** `Exception`
- (d) **requires** `n != 0`
 otherwise `f == -n`
 void foo(**final int** n) **throws** `IOException`
- (e) None of the above would be allowed

Would your answer be the same if `n` were not `final` ?

Task 5

Assume a language with structural subtyping, contravariant arguments, and covariant return types. Is it possible to create the classes A, B, and C that meet all of the following requirements?

1. B is a structural subtype of A, and C is a structural subtype of B.
2. B is not a behavioral subtype of A.
3. C is a behavioral subtype of both A and B.

4. The signatures of any two methods of A, B, or C should be different. For this exercise the signature is the combination of return type, method name, and argument order and types. Note that different signatures do not preclude structural subtyping.
5. The classes do not have any fields.

If it is possible to meet all the above requirements, write the classes A, B, and C.

If it is not possible to meet all the requirements, explain why not. Then pick a requirement and remove it. Write down the classes A, B, and C that meet the remaining four requirements.

In both cases specify the behavior of the classes using contracts. You do not need to provide method bodies. You may use existing Java classes in your solution, if you want to.