

# Formal Methods and Functional Programming

## Solutions of Exercise Sheet 14: Modelling and LTL

Sample Promela files that solve Assignments 1, 2, 3, and 5 are posted online.

### Assignment 4

*First part:*

- $T \not\models \varphi_1, \gamma = s_1 s_4 s_5 s_4 s_5 s_4 \dots$

- $T \models \varphi_2$

There does not exist a loop in which  $r$  does not hold at some point.

- $T \models \varphi_3$

$\neg r$  holds in  $s_1$  and  $s_4$ , but  $s_1$  cannot be a next state, hence only  $s_4$  is of interest. In all states reachable in a single transition from  $s_4$   $r$  holds, hence the formula holds.

- $T \not\models \varphi_4, \gamma = s_1 s_4 s_5 s_5 s_5 \dots$

- $T \models \varphi_5$

$p$  holds in  $s_1$  and in all states after  $s_1$   $q$  or  $r$  hold.

- $T \not\models \varphi_6, \gamma = s_1 s_4 s_2 s_4 s_2 s_4 s_2 \dots$

- $T \not\models \varphi_7, \gamma = s_1 s_4 s_2 s_4 s_2 s_4 s_2 \dots$

- $T \models \varphi_8$

The only way to satisfy the antecedent is to go into a loop  $s_5 s_5 s_5 \dots$ , and in this loop the consequent is also satisfied, hence the formula holds. In all traces that do not have an infinite suffix of  $s_5$ 's, the antecedent is false, and the formula holds trivially. Therefore, the formula holds for all traces.

*Second part:*

- $\Diamond \Box \neg(p \wedge \neg q \wedge \neg r)$

- $\Box(r \rightarrow \bigcirc q)$
- $\bigcirc \Box(p \rightarrow r)$
- $\Box((p \wedge q \wedge r) \rightarrow ((p \wedge q \wedge r) \vee \neg r))$
- $\Diamond(q \wedge \bigcirc \Diamond q)$
- $\Box \Diamond q$
- $(p \wedge \bigcirc \Box \neg p) \rightarrow (\Box \Diamond \neg r)$
- $\Box(\neg p \wedge q \wedge \neg r \rightarrow \bigcirc \neg(\neg p \wedge q \wedge \neg r))$