

Feedback Control for Manipulation

Russ Tedrake
Sept 11, 2018



**Massachusetts
Institute of
Technology**



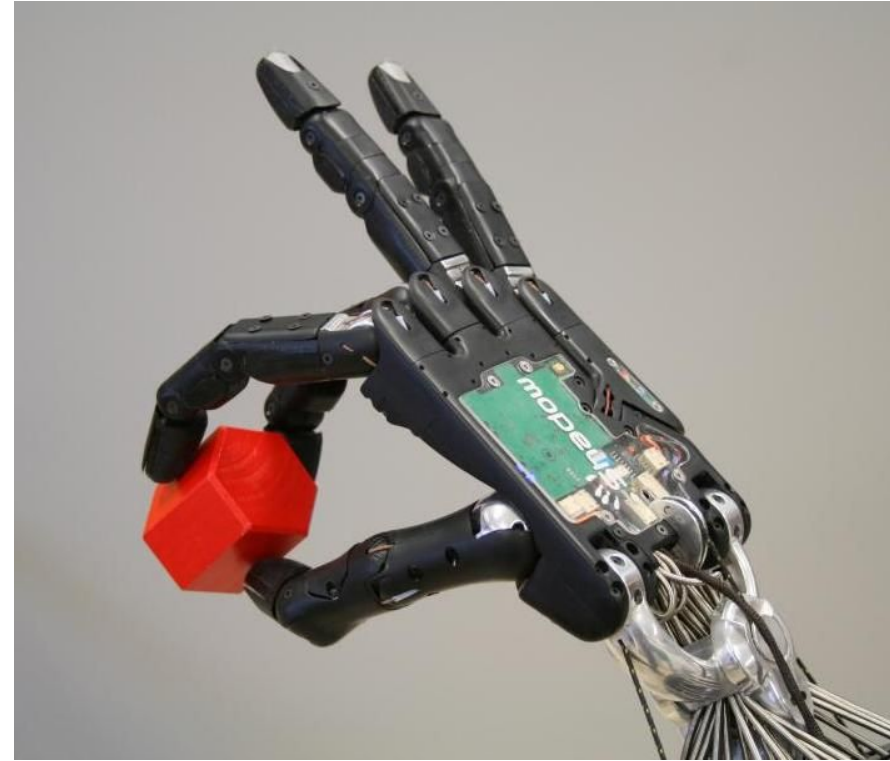
TOYOTA
RESEARCH INSTITUTE



Aaron showed success stories.

I want to discuss where control theory has ~~fallen short.~~ **Vistas.**

Nobody uses feedback control in state-of-the-art manipulation

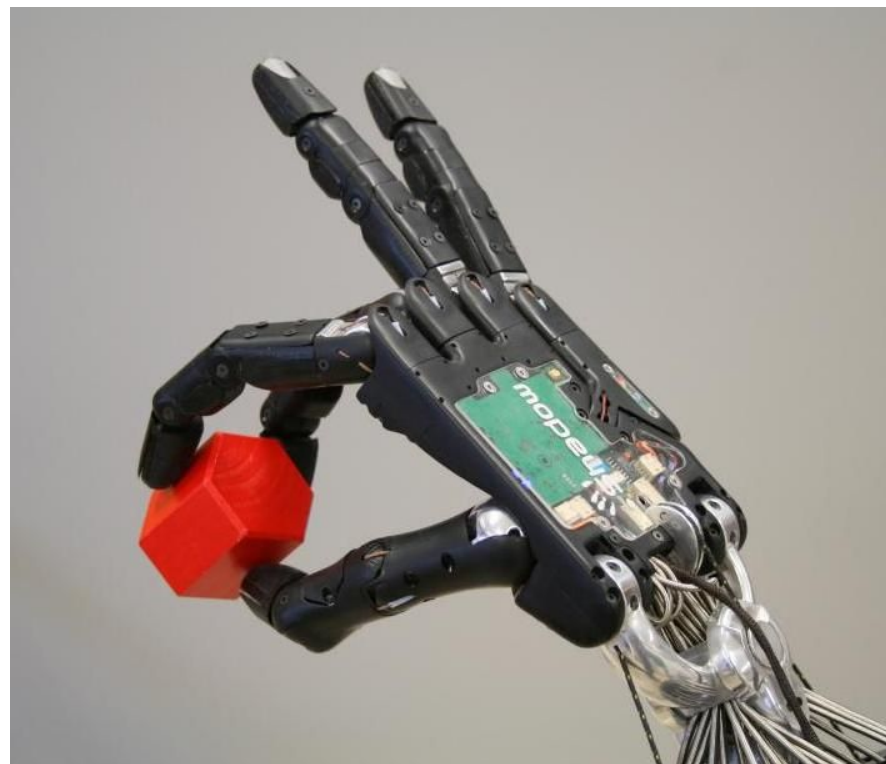


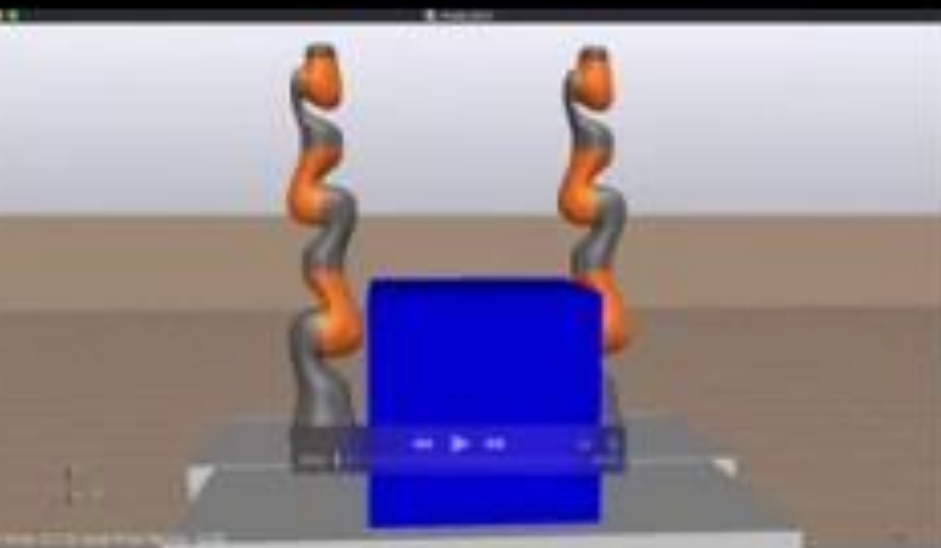
...despite common agreement
that robustness is a bottleneck.

*“Most robots fail to pick up most
objects most of the time”*

-- Stefanie Tellex, 2016.

Let me be a bit more precise...





principled

Nobody uses feedback control in manipulation



Why no feedback?

- Don't need it?
 - Underactuated hands and enveloping grasps work well





Why no feedback?

- Don't need it?
 - Underactuated hands and enveloping grasps work well
 - ... but there is much more to manipulation than enveloping grasps!
- Don't have the right sensors?
 - But we do have contact sensors (albeit expensive and not super robust)
 - and depth cameras are amazing
- Inaccurate models? Uncertainty?
 - But good control should accommodate these
 - ... for most tasks we have sufficient control authority

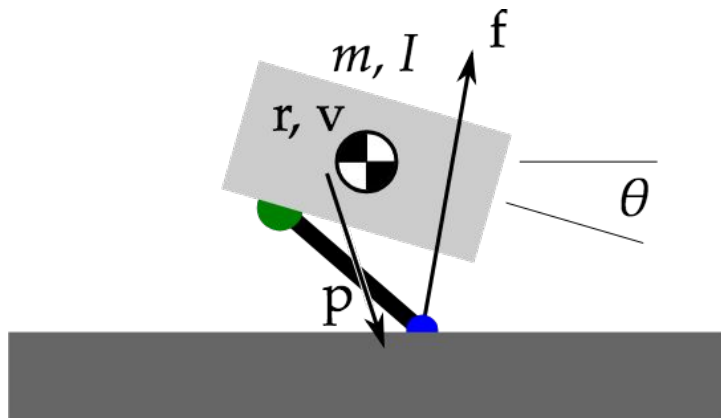
- I think it's a failing of our algorithms

Three core challenges / vistas

1. Combinatorics (of non-smooth mechanics in *contact-rich* interactions)
2. Severe partial observability + uncertainty
 - Full-state feedback often not viable/practical.
 - Central role of **Perception**.
 - Solution? Principled approaches to **Output Feedback**?
3. Wrong specification language
 - Mismatch between the way modern systems are being specified and the requirements we (typically) consume in control.

Combinatorics of Contact

Non-smooth mechanics of contact

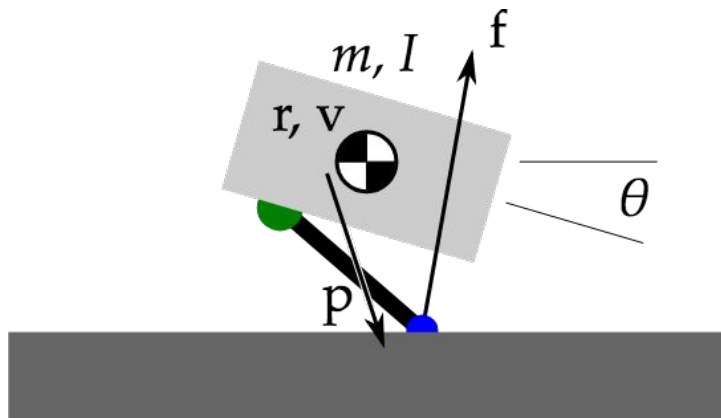


- Second-order differential equations ($F=ma$)
- but contact forces are
 - discontinuous (or stiff) in state -- no force unless we have contact.
 - set-valued (e.g. Coulomb friction)

⇒ (measure) differential inclusions /
time-stepping linear complementarity problems

What does this imply for MPC?

MPC for contact mechanics



Linearization cannot capture even the local dynamics.

Locally valid approximation looks like a piecewise-affine system (PWA):

$$\mathcal{D}^i := \{(x, u) \mid F^i x + G^i u \leq h^i\}$$

$$x^+ = A^i x + B^i u + c^i,$$

$$i \in \mathcal{I} \mid (x, u) \in \mathcal{D}^i,$$

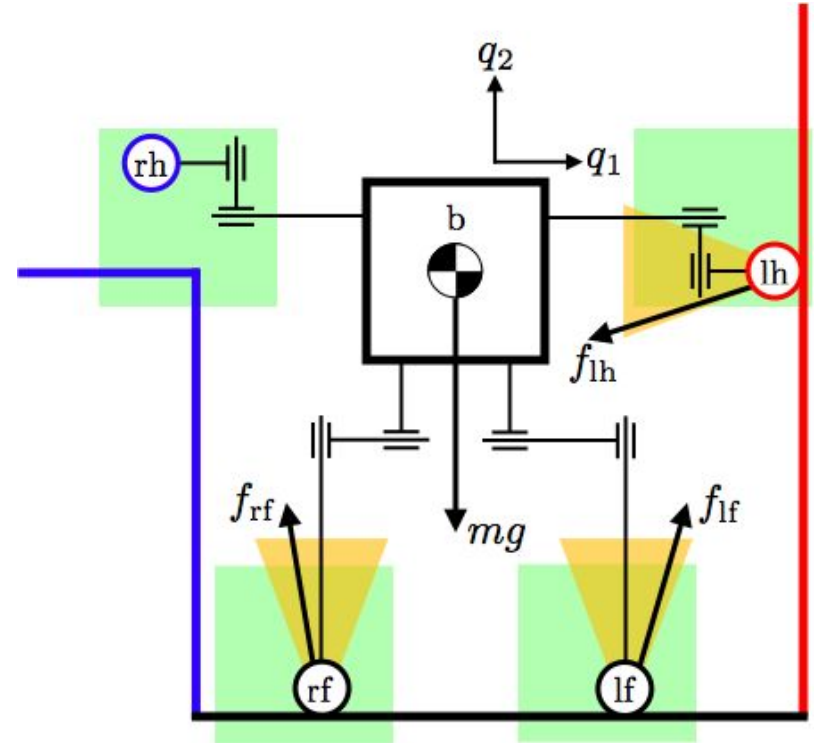
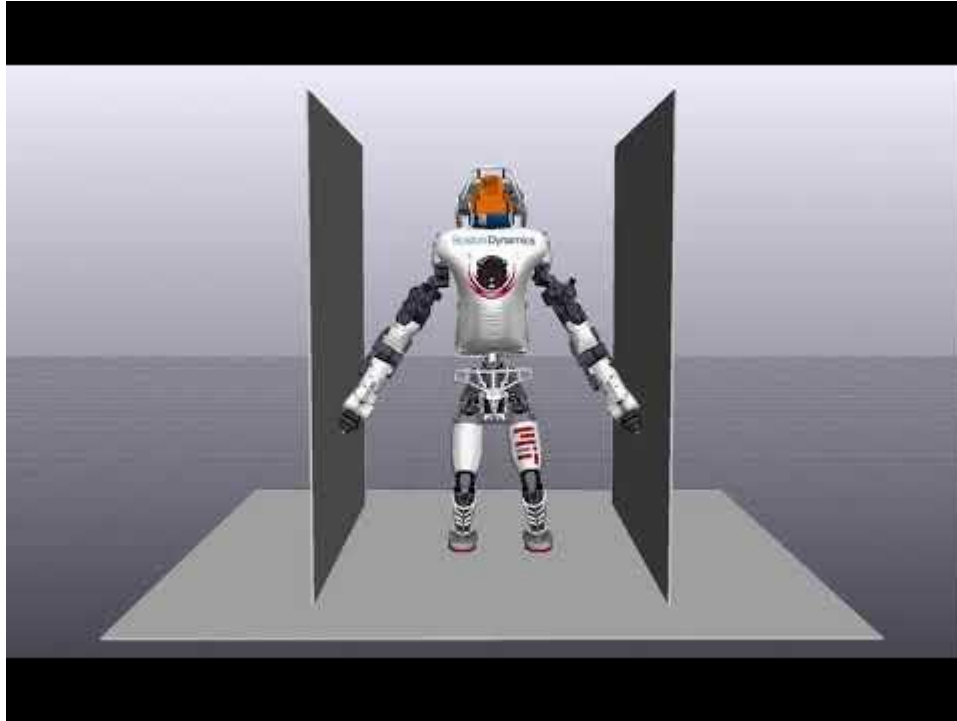
MPC for contact mechanics

(Local) “contact MPC” problem naturally formulated as a ***mixed-integer convex optimization***.

$$\begin{aligned} \min_{u(t), x(t)} \quad & \|x(N)\|_P^2 + \sum_{t=0}^{N-1} \|x(t)\|_Q^2 + \|u(t)\|_R^2 \\ \text{s.t.} \quad & x(t+1) = A_i x(t) + B_i u(t) + c_i \quad \text{if } (x(t), u(t)) \in \mathcal{D}_i \\ & x(0) = x_0 \\ & x(N) \in \mathcal{X}_N \end{aligned}$$

An important lesson from walking robots

Linearize in the “right” coordinates -- (here, centroidal dynamics)



A computational bottleneck

Mixed-integer problem has, at least,

$2 \times (\text{number of potential contact } \mathbf{pairs}) \times (\text{number of timesteps})$

binary variables. [Some of this is real, some is a limitation of our transcription]

We are not yet close to solving this at real-time rates. Currently exploring:

- Tighter formulations (from disjunctive programming)
- Approximate explicit MPC
- Lyapunov-based (LMI/sums-of-squares) synthesis
- ...

Tight formulations for PWA MPC

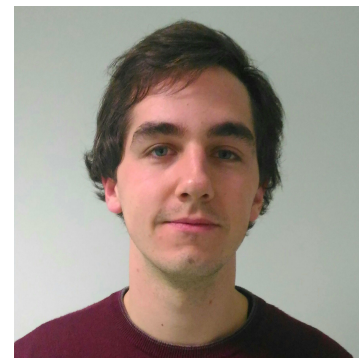
Obviously rich background in Hybrid MPC. (*Bemporad, Morari,*)

Performance of mixed-integer solvers depends on

- number of decision variables
- tightness of the convex relaxations during branch and bound
- complex (secret) heuristics in commercial solvers

Leverage (well-known) results from **disjunctive programming** to discuss the “strength” of our MI formulations.

Tight formulations for PWA MPC



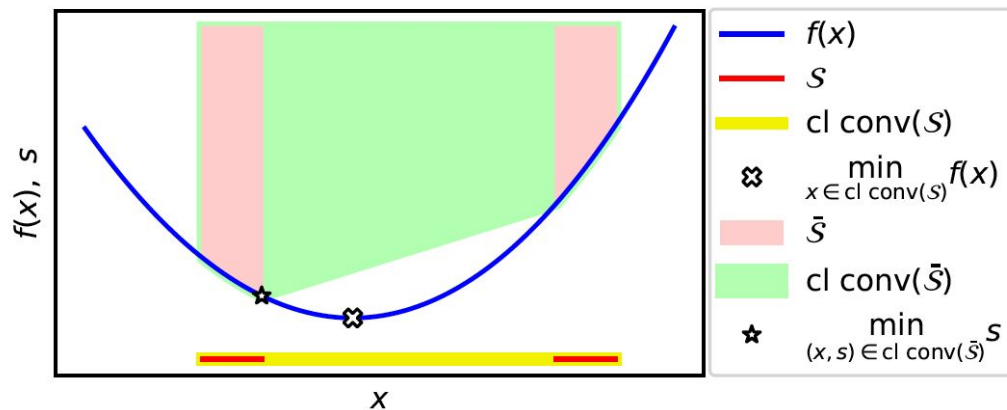
Key ideas:

- Convex hull formulation for subgroups of decision variables
 - balance tightness of relaxation with number of binary variables.
- Use the objective in the convex hull

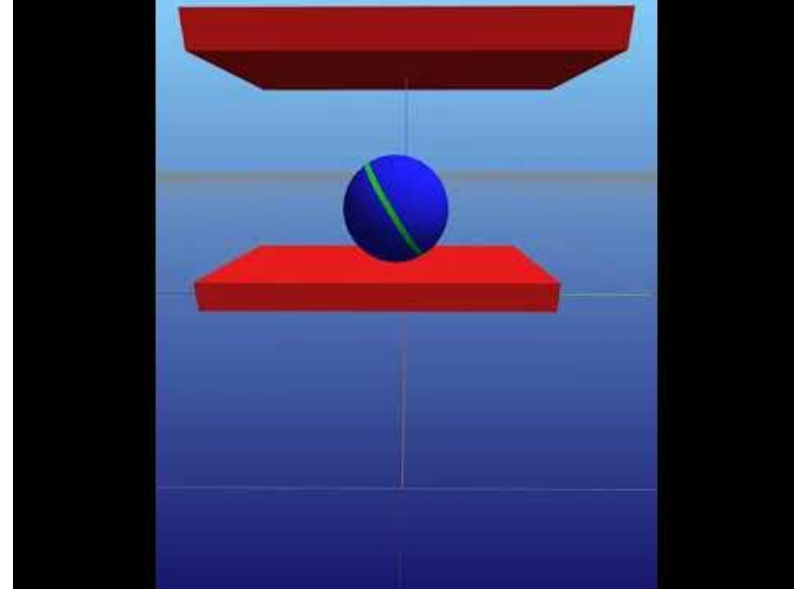
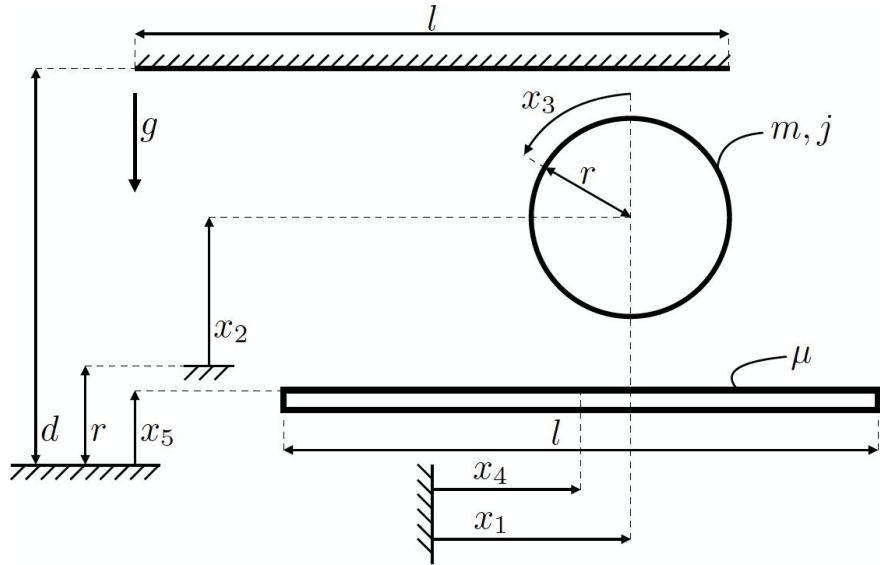
Mixed-Integer Formulations for Optimal Control of Piecewise-Affine Systems

Tobia Marcucci and Russ Tedrake

Computer Science and Artificial Intelligence Laboratory
Massachusetts Institute of Technology
{tobiam,russt}@mit.edu



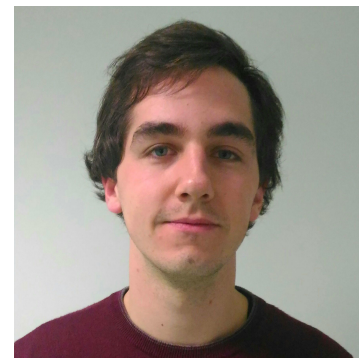
Example: 2D (frictional) ball reorientation



Traditional formulation does not find a feasible solution in 1 hour

Tight formulations solve to **global** optimality in ~ 320 seconds

Approximate Explicit MPC



Still cannot achieve real-time rates (but still trying!)

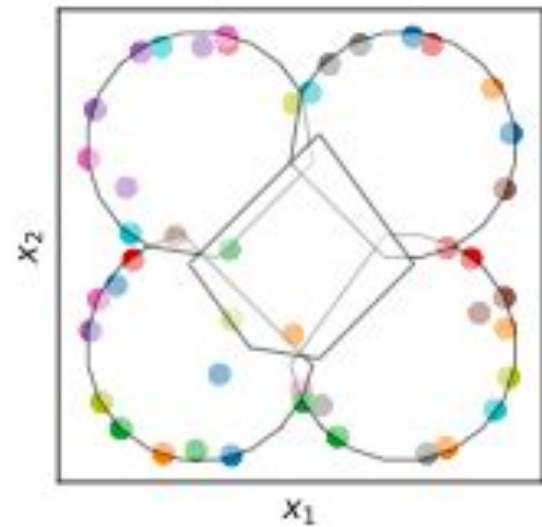
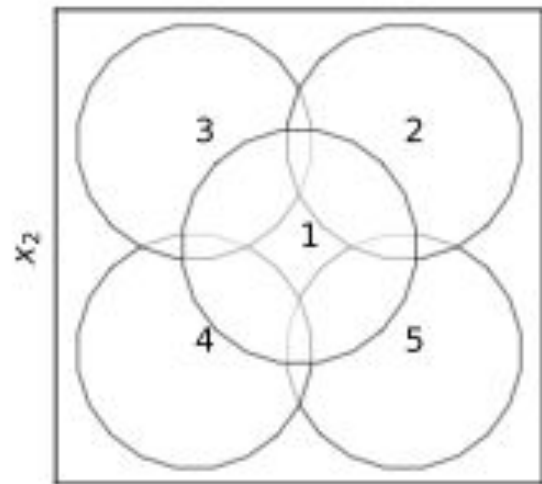
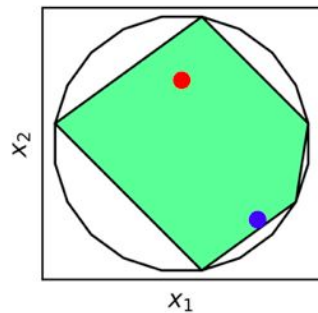
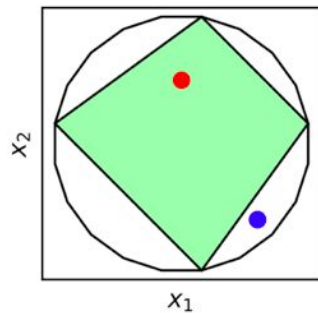
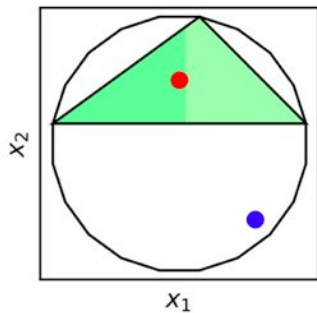
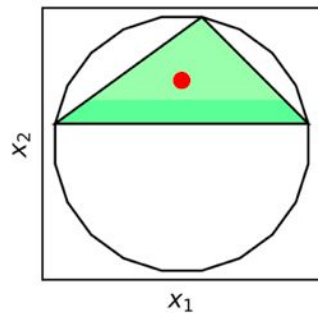
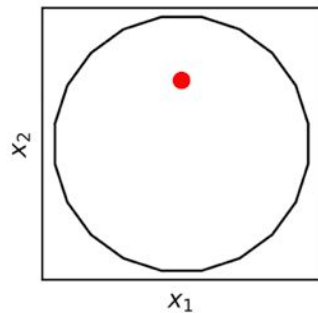
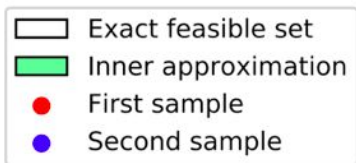
What about Explicit MPC?

- Note that the hybrid case loses some of the nice properties (policy is still locally affine, but critical regions are no longer simple polytopes)
- Exact explicit MPC still intractable
- *Can we approximate this function (ideally guaranteeing strict feasibility) with simpler functions?*

One Approach:

- Sample in the state space, solve the MIQP.
- Approximate the feasible set of the QP with the integer solution fixed.
- Find new sample that is outside existing feasible sets (via rejection sampling)
- Repeat

Approximating QP feasible sets



System has 8 states, 8 inputs
593 selected mode sequences
(out of $5^{10} \approx 10^7$)
QPs are solved in ~ 25 ms

Still ***guarantee closed-loop stability.***
(but sacrificed global optimality)

Still working hard on it...

Limitations:

- Requires expensive precomputation phase. (maybe ok?)
- Depends heavily on state estimation.

Also exploring SDP relaxations, etc.

I believe good policies exist that take a much simpler form. They may also be more robust.

- Formal design of (simple) reactive controllers. Aka “output feedback”.

Output Feedback

What is the state space of this system?

Does (full) state estimation / feedback even make sense?

With my controls hat on:

- Model-order reduction + (reduced) state estimation + control?
 - Note: relevant subspace depends on the objective
 - “Subspace” identification may be more like “representation learning”
- ...



It was very interesting to hear stories last night about the birth of state-space methods / modern control.

But I feel that we are now reaching its limits.

Output Feedback

Simplest(?) case to describe:

$$\begin{aligned}x^+ &= Ax + Bu \\ y &= Cx + Du\end{aligned}$$

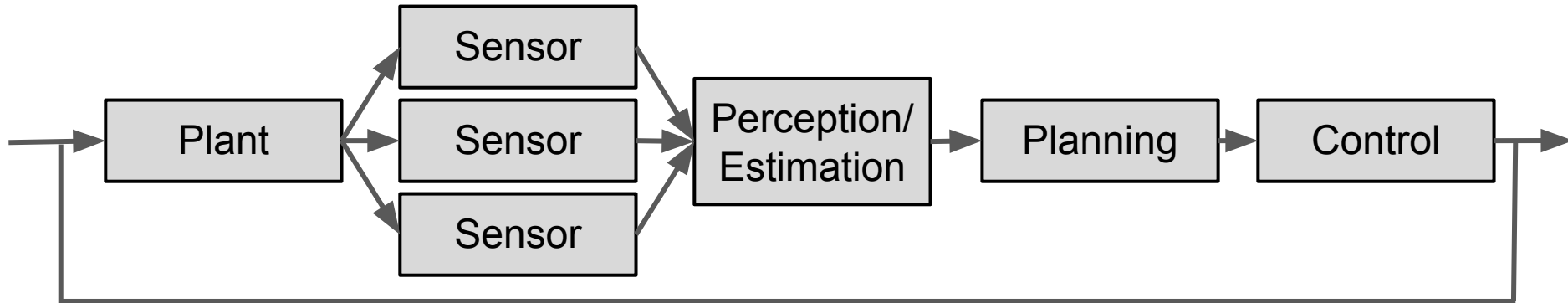
Want to find feedback gains K such that $u = -Ky$ stabilizes the system.

This “static” output feedback known to be NP hard [Blondel, ‘97]

Dynamic output feedback when the controller has internal state.

LQG is the special case we can solve.

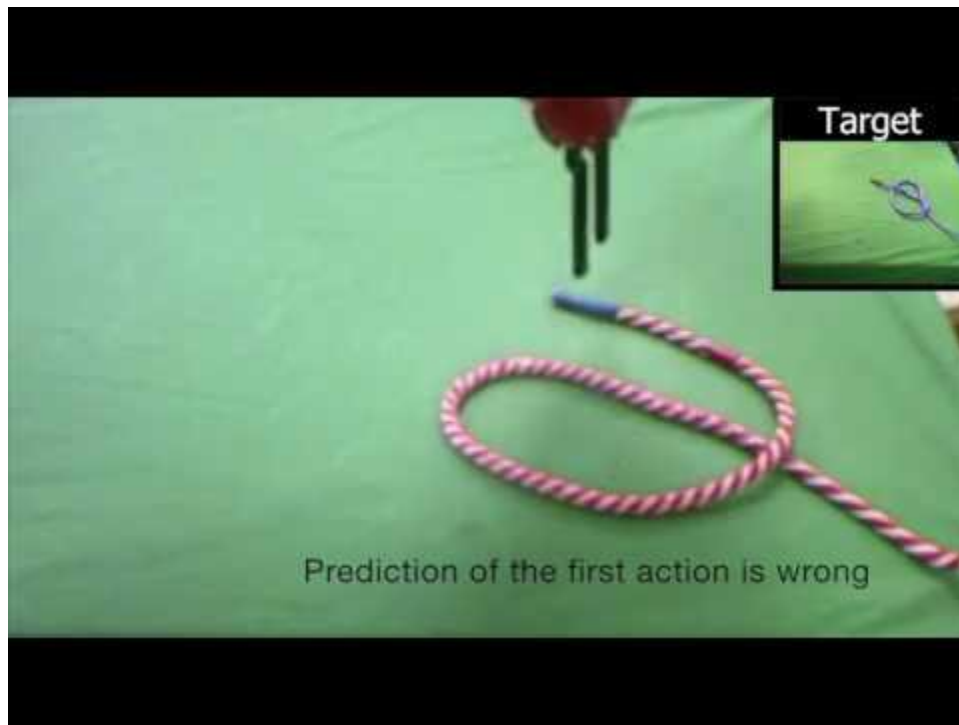
But the complexity of perception breaks our existing tools...



- Sensors include cameras \Rightarrow sensor model is a photo-realistic rendering engine
- Perception components (especially) include deep neural networks.
- Plant model has to capture distributions over natural scenes (lighting conditions)

Deep Learning for Control

Deep learning has another name for it: End-to-end learning. (aka “Pixels to torques”)



Pulkit Agrawal et al
2017

Deep Learning for Control

Many approaches:

- Reinforcement Learning
- Imitation Learning
- “Self-supervised” learning

Static Output Feedback w/ Convolutional Networks

Dynamic Output Feedback w/ Recurrent Networks

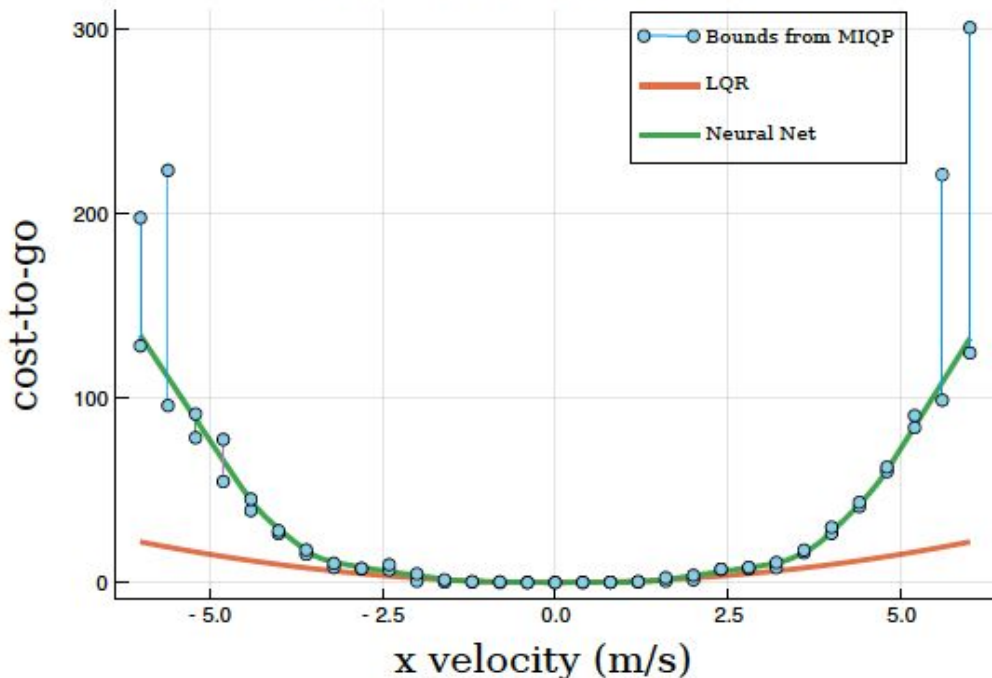
Most applications to date use only stochastic gradient descent

Learned Value Interval Supervision

Can we use samples from MIQP to train a neural network controller?

- Structurally reasonable match to explicit MPC solutions.
- Expensive to solve MIQP to optimality
- Early termination of solver (or non-uniqueness of optimal soln) complicate policy learning
- But early termination of solver still gives bounds on cost-to-go.

Learned Cost-To-Go



Systems theory applied to Deep Nets

Q: Can we derive meaningful input/output bounds on a deep neural network?

Evaluating Robustness of Neural Networks with Mixed Integer Programming

Vincent Tjeng Kai Xiao Russ Tedrake
Massachusetts Institute of Technology
Cambridge, MA 02139
{vtjeng, kaix, russt}@mit.edu

- For ReLU networks (with max-pooling, etc):
 - Can produce weak bounds on very large networks (using the LP relaxation)¹
 - Branch-and-bound gives progressively tighter bounds; optimal bounds on modest architectures (MNIST)
- New work w/ Sasha Megretski on L2 gains for recurrent nets using IQC

Output Feedback for Manipulation (summary)

**Simple, robust, output feedback
controllers exist... and I don't know how
to find them (reliably)**

Authoring Requirements

(perhaps my version of the “data-driven control” theme)

Machine learning is challenging the way that we perform systems engineering:

Rules of Machine Learning:



Best Practices for ML Engineering

Martin Zinkevich

This document is intended to help those with a basic knowledge of machine learning get the benefit of Google's best practices in machine learning. It presents a style for machine learning, similar to the Google C++ Style Guide and other popular guides to practical programming. If you have taken a class in machine learning, or built or worked on a machine-learned model, then you have the necessary background to read this document.

27 Feb 2018 | 16:48 GMT

Creating Driving Tests for Self-Driving Cars

Volvo-backed Zenuity wants to prove that autonomous vehicles can drive more safely than humans

By Erik Coelingh and Jonas Nilsson



Still a disconnect between **requirements** used in industry and problem formulations for robust control

Author distributions over environments/scenarios is hard; “corner cases” from large scale testing remain central

L2-gain-style computations are not enough¹

Scenario-based verification and synthesis

Standard robust control formulation:

Find a controller $u = K(y)$ that minimizes some objective over many realizations of the plant (worst case, in expectation, etc).

But the realizations are drawn from distributions over tasks / environments

- which are very hard to author,
- typically sample-based,
- typically incredibly sparse (and expensive to obtain)

Need principled approaches to optimal experiment design, system ID, and “distributional robustness” that scale to this complexity.

- Mixing statistical methods and systems theory to address the complexity of distributional robustness

Scalable End-to-End Autonomous Vehicle Testing via Rare-event Simulation

NIPS 2018

Search Algorithm	$\gamma = 0.14$	$\gamma = 0.16$	$\gamma = 0.18$	$\gamma = 0.40$	$\gamma = 0.42$
Naive	$(2.0 \pm 2.0)e-5$	$(22.0 \pm 6.6)e-5$	$(82.0 \pm 12.8)e-5$	$(334.4 \pm 8.0)e-4$	$(389.7 \pm 8.6)e-4$
Cross-entropy	$(3.2 \pm 2.6)e-6$	$(25.8 \pm 4.5)e-5$	$(84.6 \pm 9.3)e-5$	$(334.5 \pm 8.0)e-4$	$(386.4 \pm 8.6)e-4$

Table 1: Estimate of rare-event probability p_γ (non-vision ego policy), with standard deviations

Search Algorithm	$\gamma = 0.26$	$\gamma = 0.28$	$\gamma = 0.30$	$\gamma = 0.50$	$\gamma = 0.52$
Naive	$(8.0 \pm 4.0)e-3$	$(8.0 \pm 4.0)e-3$	$(12.0 \pm 4.9)e-3$	$(13.8 \pm 1.5)e-2$	$(15.6 \pm 1.6)e-2$
Cross-entropy	$(2.7 \pm 2.1)e-3$	$(5.4 \pm 2.7)e-3$	$(6.4 \pm 2.7)e-3$	$(7.6 \pm 1.0)e-2$	$(8.1 \pm 1.0)e-2$

Table 2: Estimate of rare-event probability p_γ (vision-based ego policy), with standard deviations

My path forward

Scaling optimization-based synthesis to manipulation

I believe (to my core) in structured optimization and machine learning.

In ML: “whomever has the most data will win”.

For me: I covet parametric models (of mechanics, sensors, controllers, ...).

Models should enable optimization-based design/analysis:

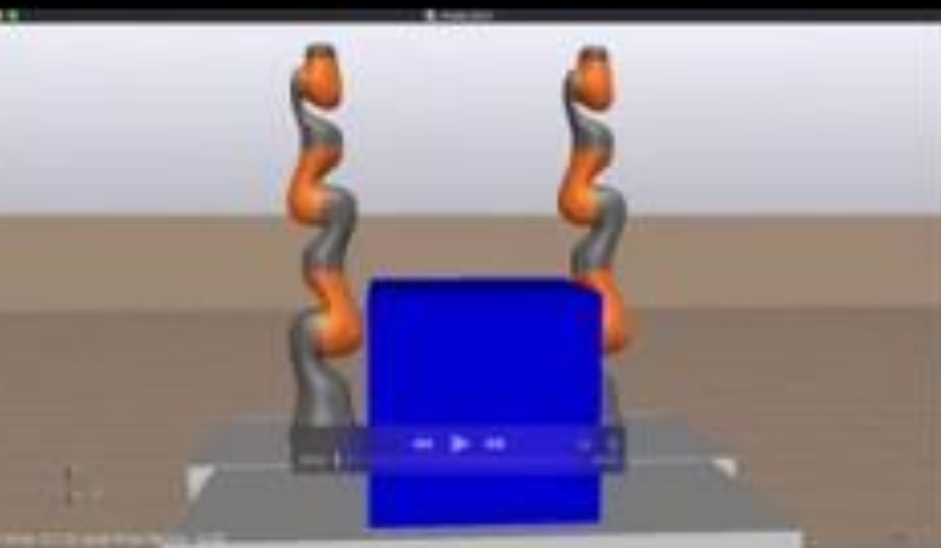
- Gradients (via autodiff)
- Introspection of sparsity, convexity
- Facilitate varying levels of fidelity

<http://drake.mit.edu> (on github)

- A [modeling framework](#)
 - Rigorous about declaring state, parameters uncertainty, etc.
 - Physics engine, Rendering engine, Sensor models, ...
 - Gradients, Sparsity, Convexity, ...
- An [optimization library](#)
- Optimization algorithms for dynamical systems (planning, feedback design, perception/estimation, system identification...)

DRAKE
A PLANNING, CONTROL,
AND ANALYSIS TOOLBOX FOR
NONLINEAR DYNAMICAL SYSTEMS





Summary: Three core challenges / vistas

Nobody uses (principled) feedback control in manipulation.

1. Combinatorics (of non-smooth mechanics in *contact-rich* interactions)
2. Severe partial observability + uncertainty
 - Are we reaching the limits of state space methods?
 - Simple, robust, output feedback controllers exist and I don't know how to find them reliably
3. Control should align w/ best practices for Machine Learning Engineering