VORONOÏ PERCOLATION IN THE HYPERBOLIC PLANE

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ABSTRACT. We consider site percolation on Voronoï cells generated by a Poisson point process on the hyperbolic plane \mathbb{H}^2 . Each cell is coloured black independently with probability p, otherwise the cell is coloured white. Benjamini and Schramm proved the existence of three phases: For $p \in [0, p_c]$ all black clusters are bounded and there is a unique infinite white cluster. For $p \in (p_c, p_u)$, there are infinitely many unbounded black and white clusters. For $p \in [p_u, 1]$ there is a unique infinite black cluster and all white clusters are bounded. The critical values p_c and p_u depend on the intensity of the Poisson point process. We prove that both p_c and p_u tend to 1/2 as the intensity tends to infinity. This confirms a conjecture of Benjamini and Schramm.

(Based on joint work with Tobias Müller)