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**Title:** *Circular law for sparse random regular digraphs.*

**Abstract:** Fix a constant  $C \geq 1$  and let  $d = d(n)$  satisfy  $d \leq \ln^C n$  for every large integer  $n$ . Denote by  $M_n$  the adjacency matrix of a uniform random directed  $d$ -regular graph on  $n$  vertices. We show that, as long as  $d \rightarrow \infty$  with  $n$ , the empirical spectral distribution of the appropriately rescaled matrix  $M_n$  converges weakly in probability to the circular law. This result, together with an earlier work of Cook, settles the problem of weak convergence of the empirical distribution in directed  $d$ -regular setting with the degree tending to infinity. As a crucial element of our proof, we develop a technique of bounding intermediate singular values of  $A_n$ , based on studying random normals to the rowspaces. This is a joint work with A. Lytova, K. Tikhomirov, N. Tomczak-Jaegermann, and P. Youssef.