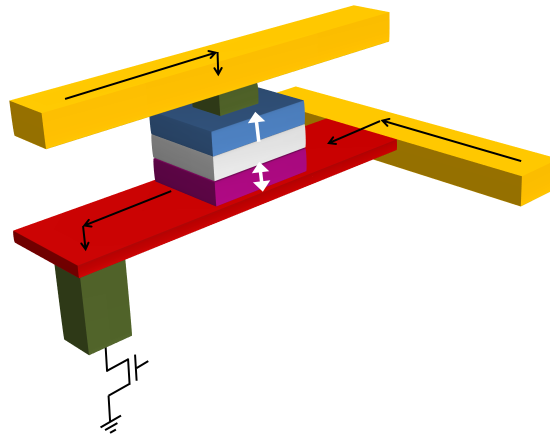
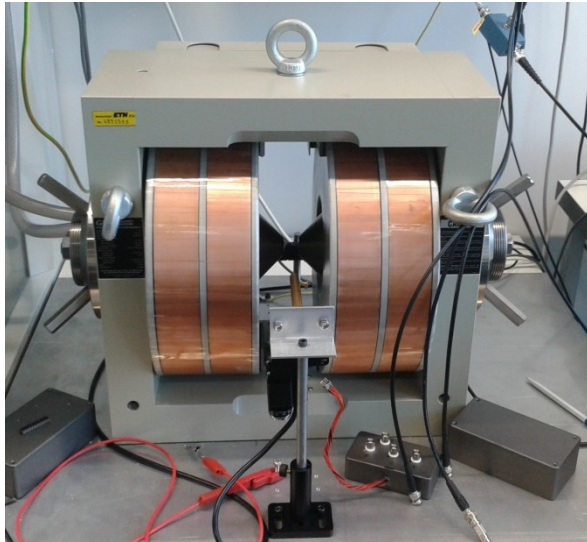


Introduction to spin torques and spin-orbit torques in metal layers

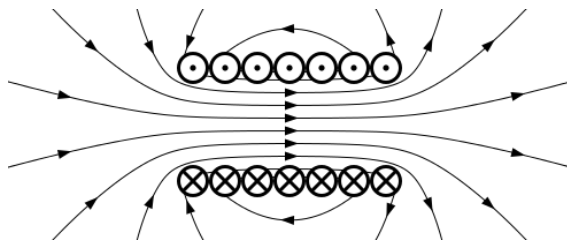
Pietro Gambardella

Department of Materials, ETH Zurich, Switzerland

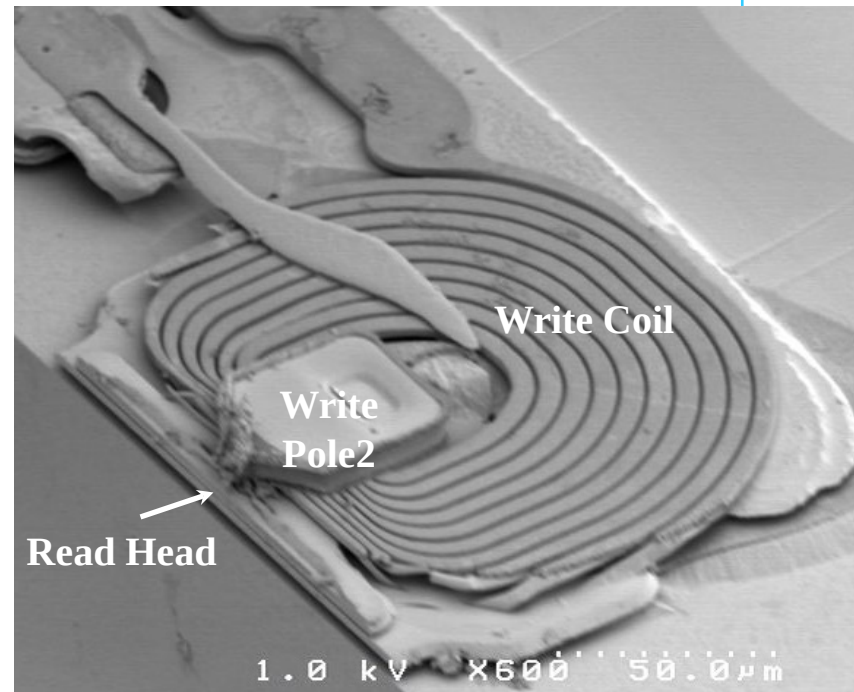
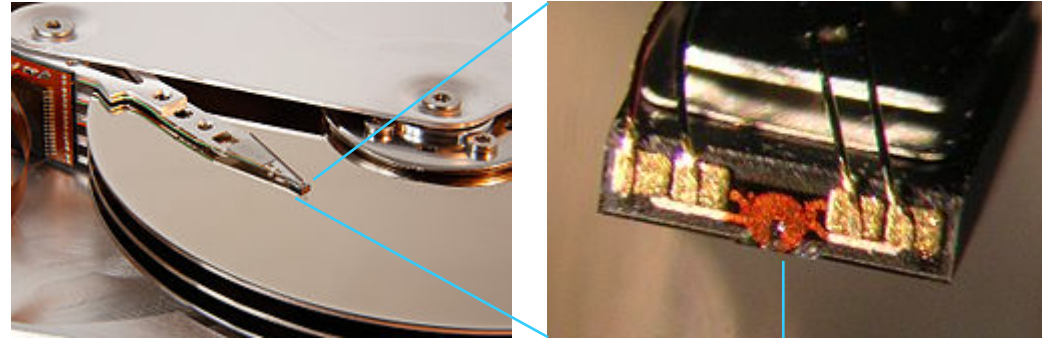




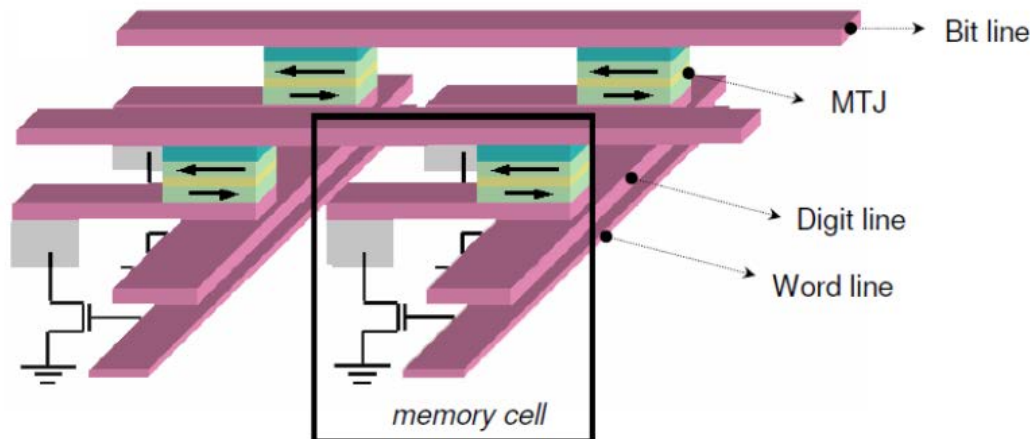
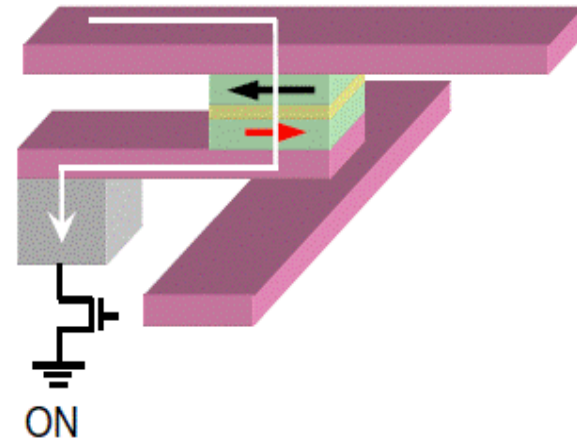
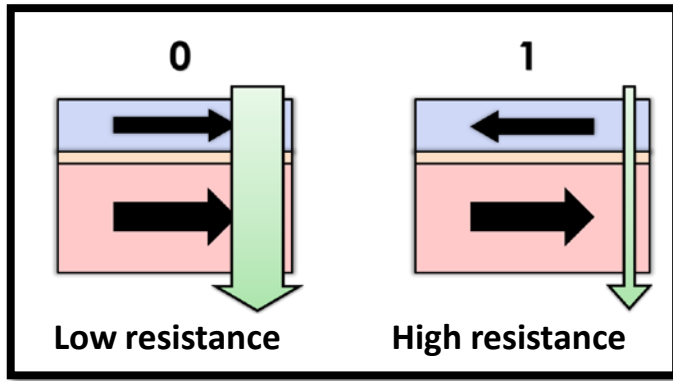
Weight: 350 Kg, Current: 70 A



$$B = \mu n I$$



Magnetic tunnel junction: two FM electrodes separated by an insulating oxide

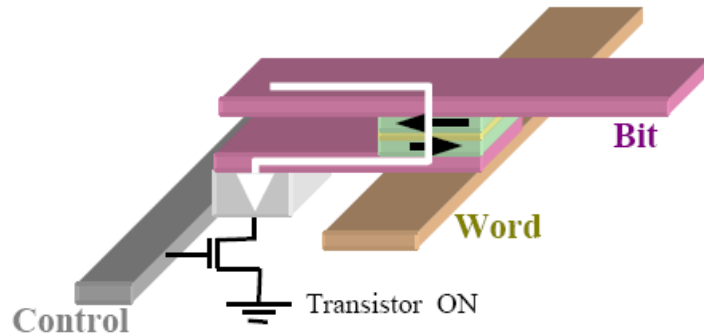


“Universal memory”

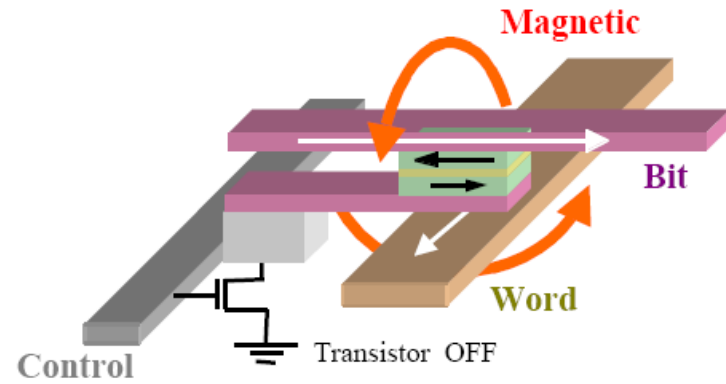
**Fast
Dense
Non-volatile**

Field-induced magnetization switching

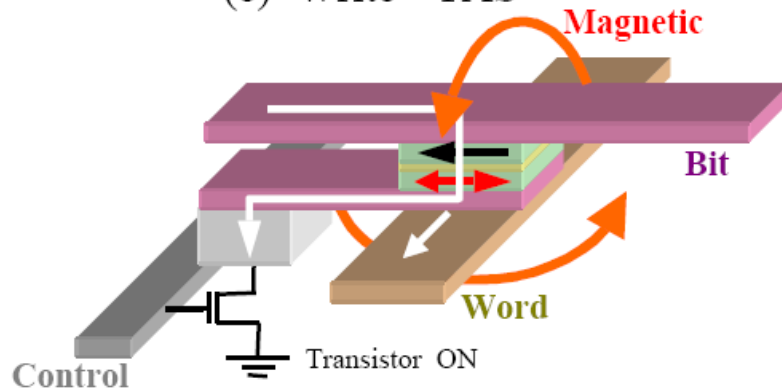
(a) Read



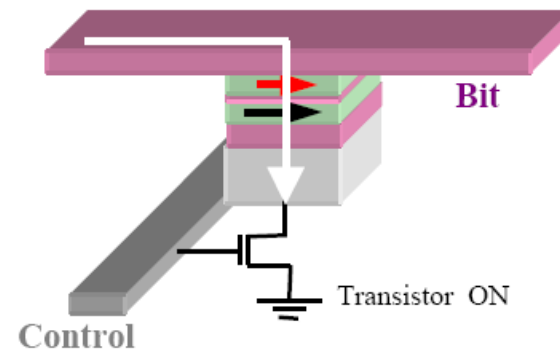
(b) Write - FIMS



(c) Write - TAS



(d) Write - CIS



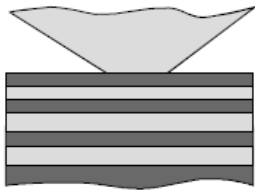
Thermally-assisted switching

Current-induced switching

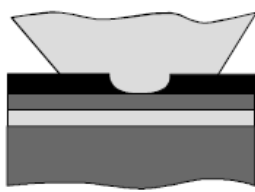
Dieny et al.,
Int. J. Nanotech.
2010

Theoretical prediction: Berger PRB 1996, Slonczewski, JMMM 1996

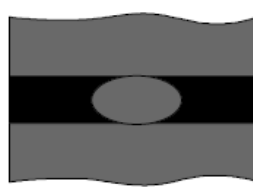
Mechanical
point contacts



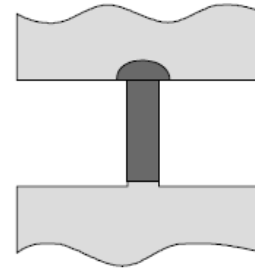
Lithographical
point contacts



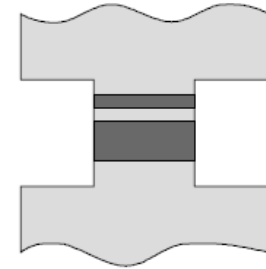
Manganite
trilayer junctions



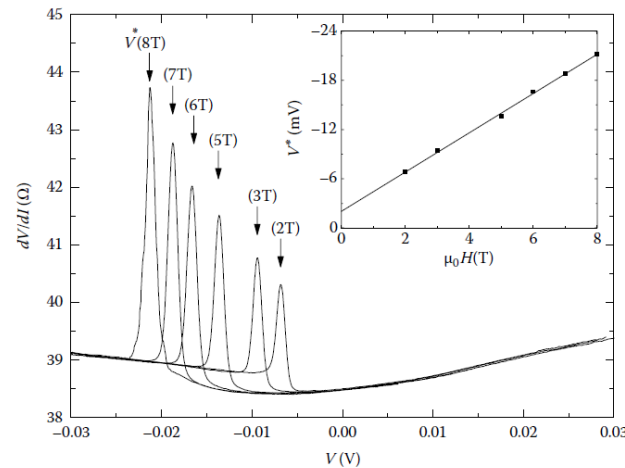
Electrodeposited
nanowires



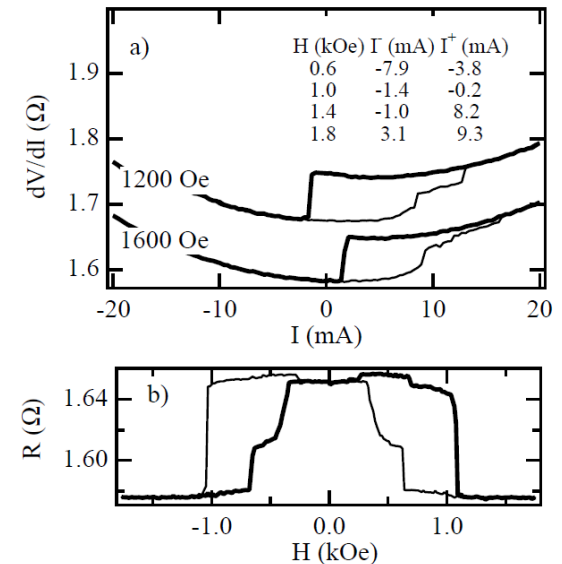
Lithographical
pillar devices



- Multilayer stacks
- GMR detection
- nm-sized contacts
- Large current density
 $\sim 10^8 \text{ A/cm}^2$
- Small Oe field
- Good thermal dissipation



Tsoi, et al., PRL 80, 4281, 1998



Katine et al., PRL 84, 3149 (2000)

- ❑ Key concepts in spin transport in FM/NM systems
- ❑ Interaction of a spin polarized current with a magnetic layer
- ❑ Spin transfer torque (STT): AD and FL components
- ❑ STT on domain walls
- ❑ Spin pumping
- ❑ STT-induced magnetization dynamics

- ❑ Spin-orbit coupling and spin-orbit torques (SOT)
- ❑ Spin Hall and Rashba effects
- ❑ SOT measurements
- ❑ Three-terminal SOT magnetic tunnel junctions
- ❑ Ultrafast SOT-induced switching
- ❑ Conclusions

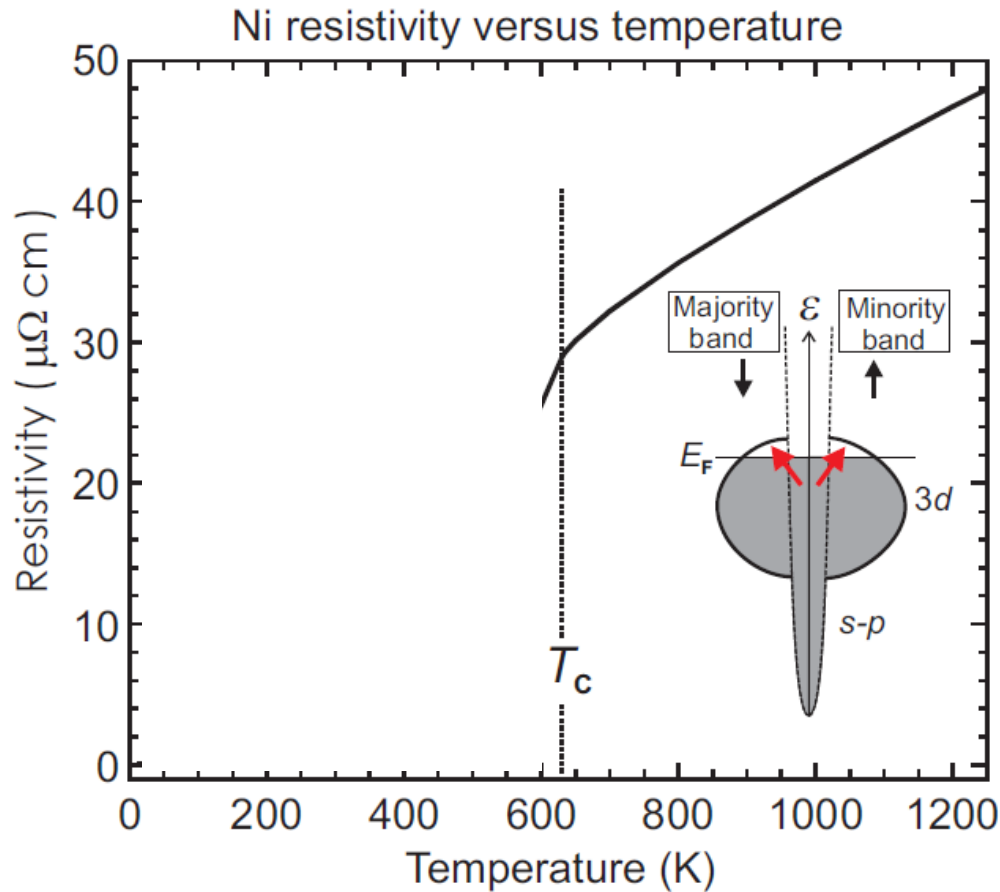
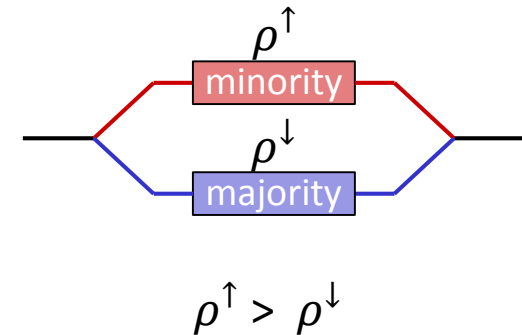
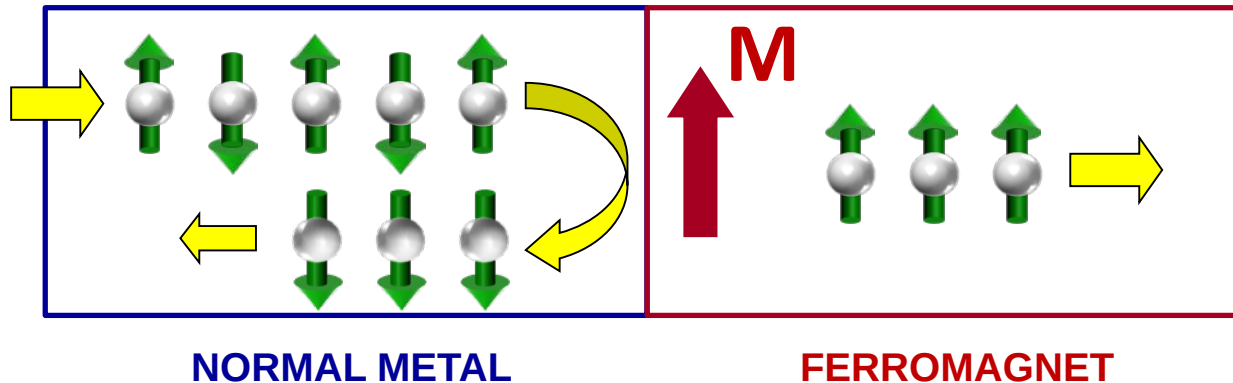


Figure
courtesy
of J. Stöhr

Mott's two current model

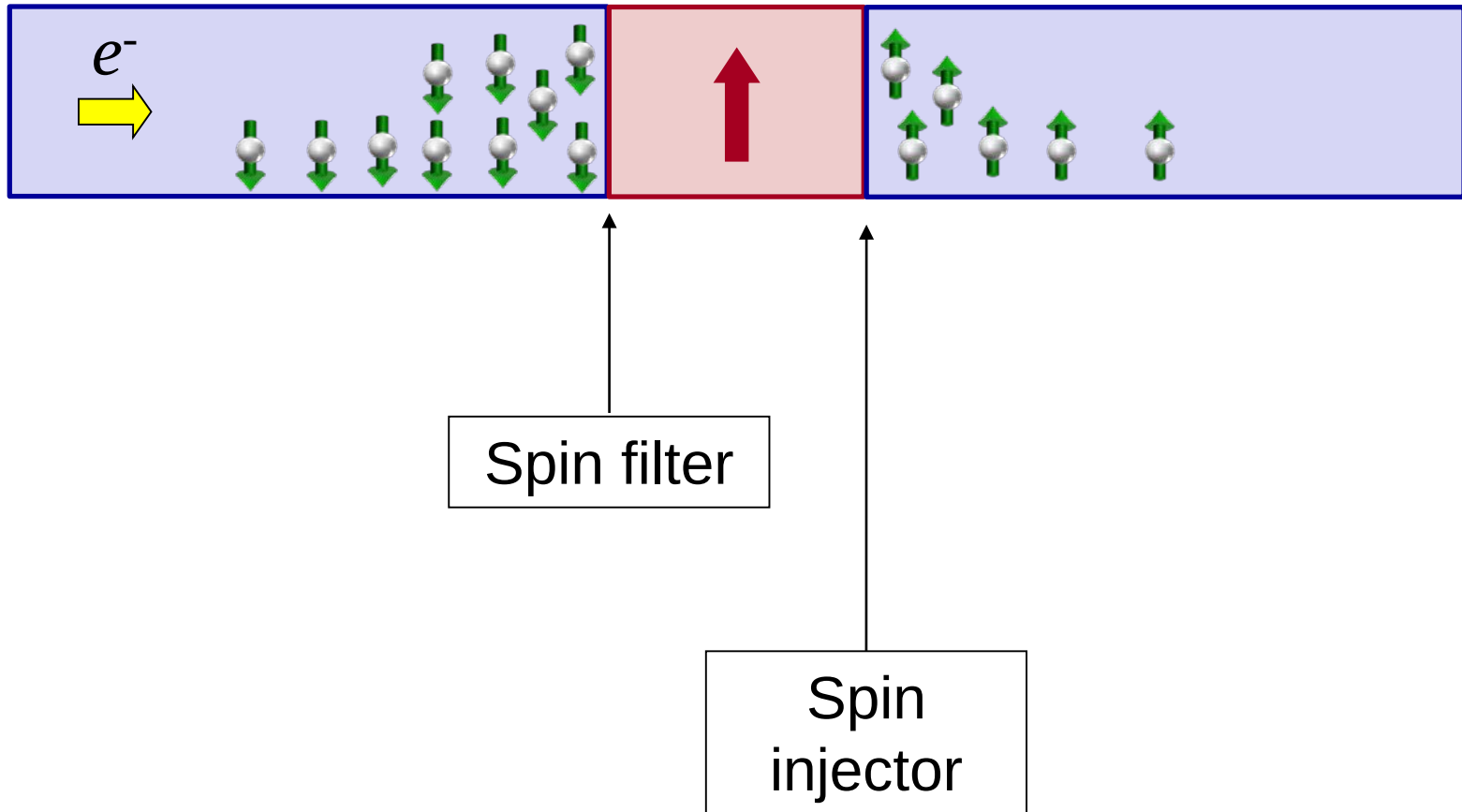


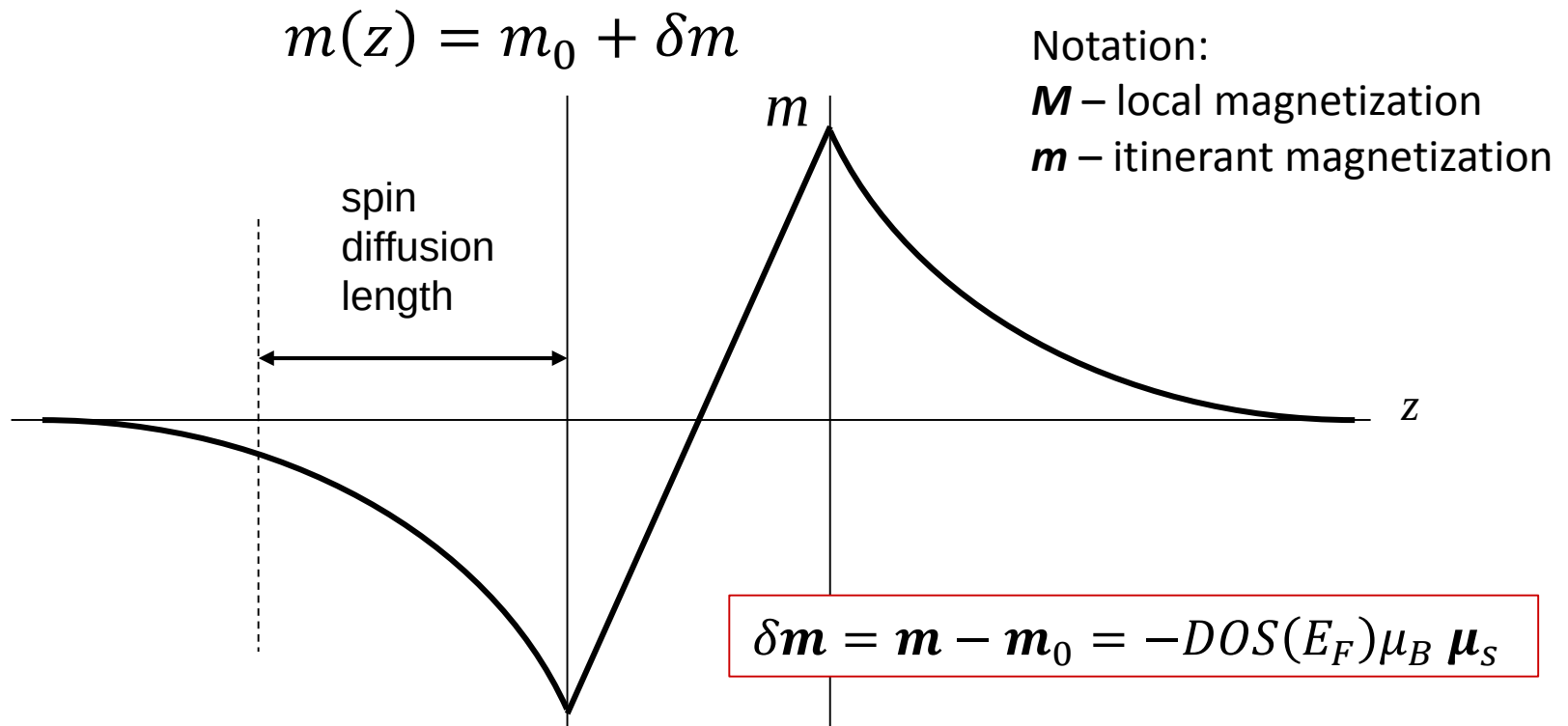
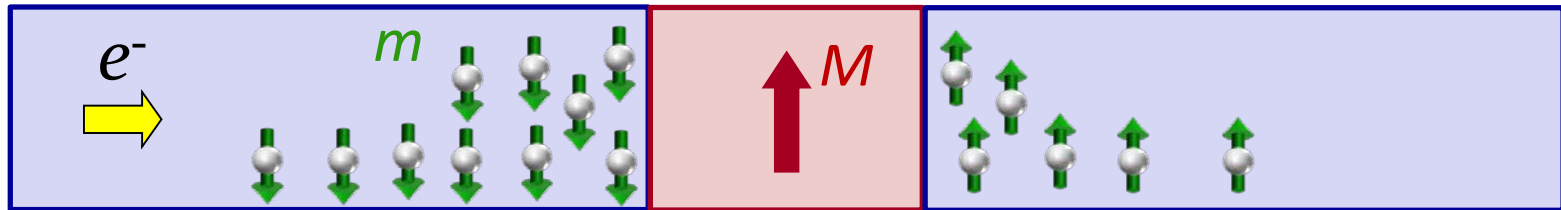
- The current flows independently in two spin channels -- **no spin flips** !
- The current below T_c becomes spin-polarized
- Minority band electrons scatter more readily from the s-p band to the d-band due to the availability of hole states in the minority d-band.



- “Majority” spins are preferentially transmitted.
- “Minority” spins are preferentially reflected.

Ferromagnets act as spin filters, even when very thin





Due to the conductivity mismatch between $\uparrow$ and $\downarrow$ spins, non-equilibrium spin polarization “accumulates” near the interfaces of FM and non-magnetic conductors.

$$\mathbf{Q} = n \frac{\hbar}{2} P \mathbf{v} \otimes \boldsymbol{\sigma} \quad \left[\frac{\hbar/2}{s \, m^2} \right]$$

$$\mathbf{j}_s = neP \mathbf{v} \otimes \boldsymbol{\sigma} \quad \left[\frac{e}{s \, m^2} = \frac{A}{m^2} \right]$$

n electron density

$e = |e|$ charge

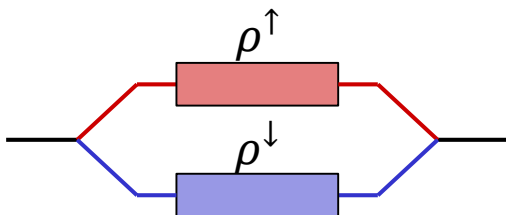
P spin polarization

$\mathbf{v}$ velocity

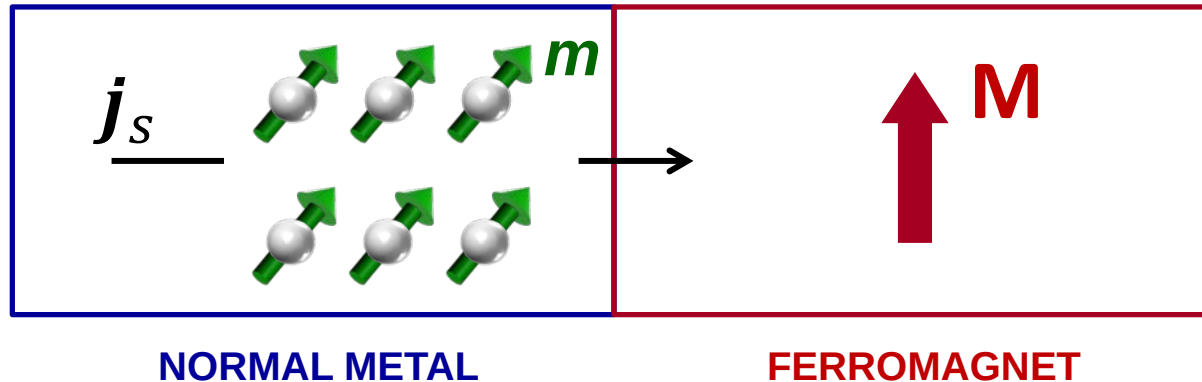
$\boldsymbol{\sigma} = (\sigma_x, \sigma_y, \sigma_z)$ vector of Pauli matrices

Two-current model:

$$\mathbf{j}_s = \mathbf{j}_c^\uparrow - \mathbf{j}_c^\downarrow$$



	Charge current	Spin current
Unpolarized current		0
Spin-polarized current		
Fully spin-polarized current		
Pure spin current	0	



A spin current $\mathbf{Q}$ (or $\mathbf{j}_s$) injected into a material corresponds to a magnetization entering and exiting the material:

$$\mathbf{m} = -\frac{\mu_B}{\hbar/2} \frac{\mathbf{Q}}{v} = -\frac{\mu_B}{e} \frac{\mathbf{j}_s}{v} \quad \left[\frac{A}{m} = \frac{\text{magnetic moment}}{\text{volume}} \right]$$

The divergence of the spin current corresponds to a change of magnetization:

$$\frac{\partial \mathbf{m}}{\partial t} = \frac{\mu_B}{\hbar/2} \nabla \cdot \mathbf{Q} = \frac{\mu_B}{e} \nabla \cdot \mathbf{j}_s \quad \left[\frac{A}{m \, s} \right]$$

$$H_{sd} = -J_{sd} \hat{\mathbf{m}} \cdot \hat{\mathbf{M}} \quad \left| \quad J_{sd} \text{ exchange coupling constant [energy]} \right.$$

Effective exchange field acting on $\mathbf{m}$: $\mathbf{B} = \frac{J_{sd}}{m} \hat{\mathbf{M}} \rightarrow$ Torque: $\mathbf{T} = J_{sd} \hat{\mathbf{m}} \times \hat{\mathbf{M}}$

Effective exchange field acting on $\mathbf{M}$: $\mathbf{B} = \frac{J_{sd}}{M} \hat{\mathbf{m}} \rightarrow$ Torque: $\mathbf{T} = J_{sd} \hat{\mathbf{M}} \times \hat{\mathbf{m}}$

Changes of $\mathbf{m}$ and $\mathbf{M}$ are related by $\frac{d\mathbf{m}}{dt} = -\frac{d\mathbf{M}}{dt}$ Action = Reaction !

Conservation of angular momentum

Note: This is exact if spin relaxation and spin-orbit coupling are neglected, i.e., assuming weak spin-lattice interactions compared to electron-electron interactions

$$\mathbf{T} = J_{sd} \hat{\mathbf{M}} \times \hat{\mathbf{m}} \quad \text{Torque on } \mathbf{M} \text{ due to the } sd \text{ exchange interaction}$$

$$\mathbf{m} = \mathbf{m}_0 + \delta \mathbf{m} \quad \left| \begin{array}{l} \mathbf{m}_0 \text{ equilibrium magnetization of conduction electrons, } \mathbf{m}_0 \parallel \mathbf{M} \\ \delta \mathbf{m} = -DOS(E_F) \mu_B \boldsymbol{\mu}_s \text{ nonequilibrium magnetization} \end{array} \right.$$

Assuming $|\mathbf{M}| = \text{const.}$, the only component of $\mathbf{m}$ that gives a torque is $\delta \mathbf{m}_\perp$

$$\delta \mathbf{m}_\perp = a_j \mathbf{M} \times \mathbf{m} + b_j (\mathbf{M} \times \mathbf{m}) \times \mathbf{M} \quad \left| \begin{array}{l} a_j, b_j \text{ parameters that depend on the current,} \\ \text{magnetization, NM/FM geometry and materials} \end{array} \right.$$

$$\mathbf{T} \sim \mathbf{M} \times \delta \mathbf{m}_\perp = a_j \mathbf{M} \times (\mathbf{M} \times \mathbf{m}) + b_j \mathbf{M} \times \mathbf{m}$$

"In-plane torque"

"Spin transfer torque"

"Slonczewski torque"

"Antidamping torque"

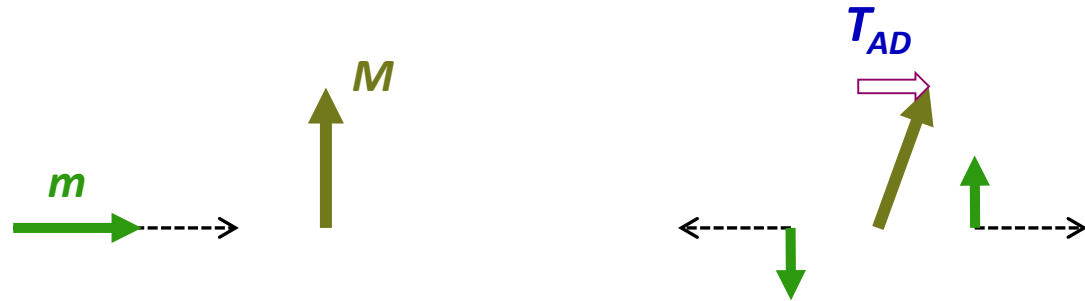
"Out-of-plane torque"

"Perpendicular torque"

"Effective field"

"Field-like torque"

AD torque

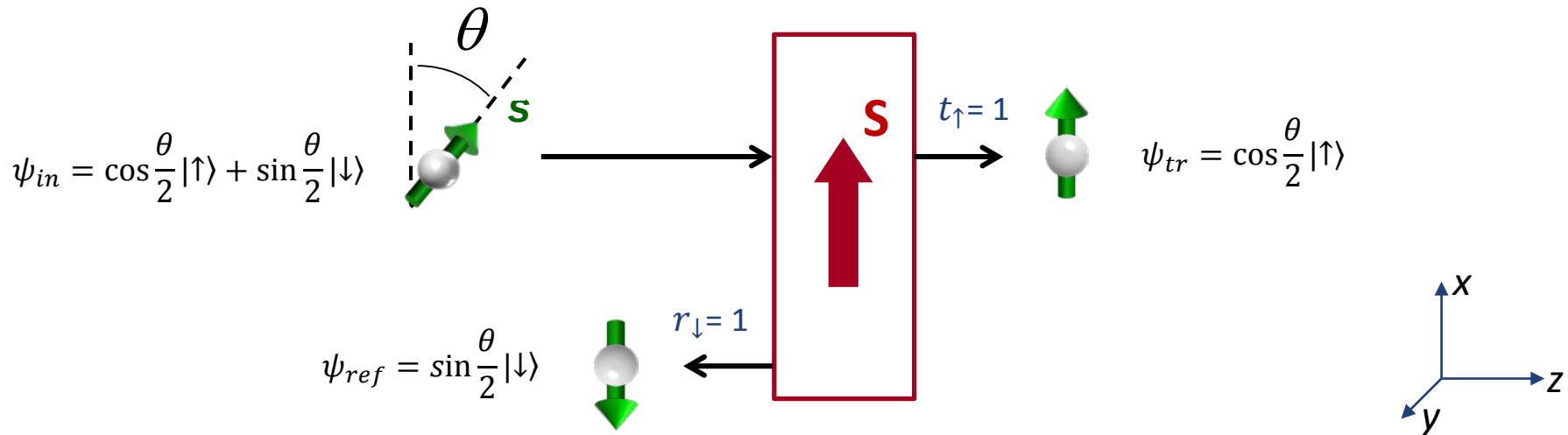


Absorption of the transverse part of the spin current
Rotates M towards the direction of m

FL torque

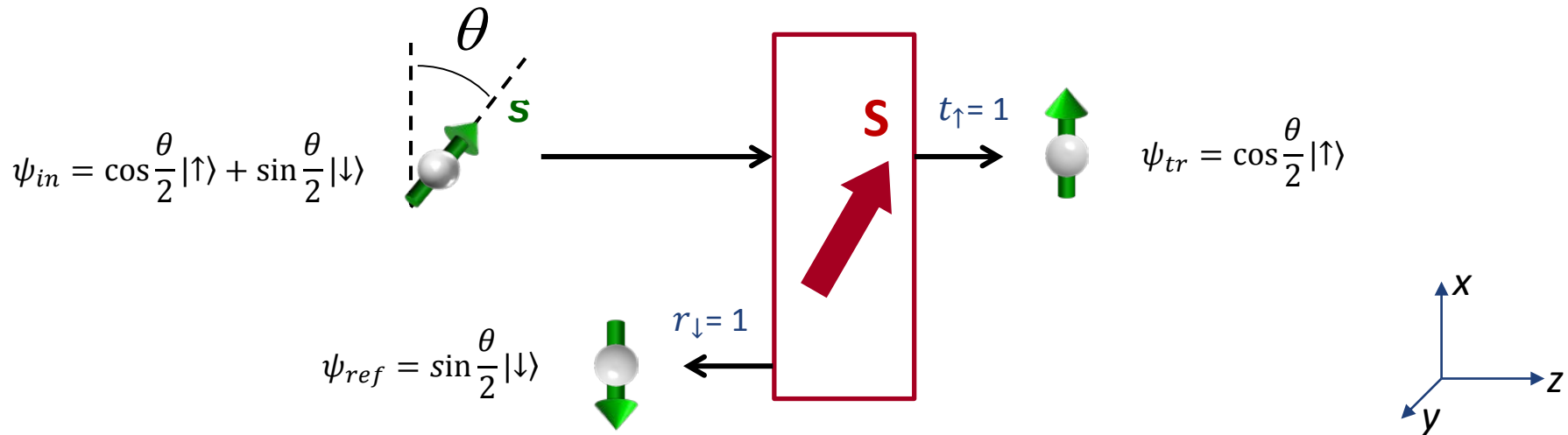


Precession of M about the exchange field created by m



Initial state	Final state		$\Delta \mathbf{s} = \mathbf{s}_f - \mathbf{s}_i$
$\langle s_x^{in} \rangle = \frac{\hbar}{2} \sin\theta$	$\langle s_x^{tr} \rangle = 0$	$\langle s_x^{ref} \rangle = 0$	$\Delta s_x = -\frac{\hbar}{2} \sin\theta$
$\langle s_z^{in} \rangle = \frac{\hbar}{2} \cos\theta$	$\langle s_z^{tr} \rangle = \frac{\hbar}{2} \cos^2\frac{\theta}{2}$	$\langle s_z^{ref} \rangle = -\frac{\hbar}{2} \sin^2\frac{\theta}{2}$	$\Delta s_z = 0$

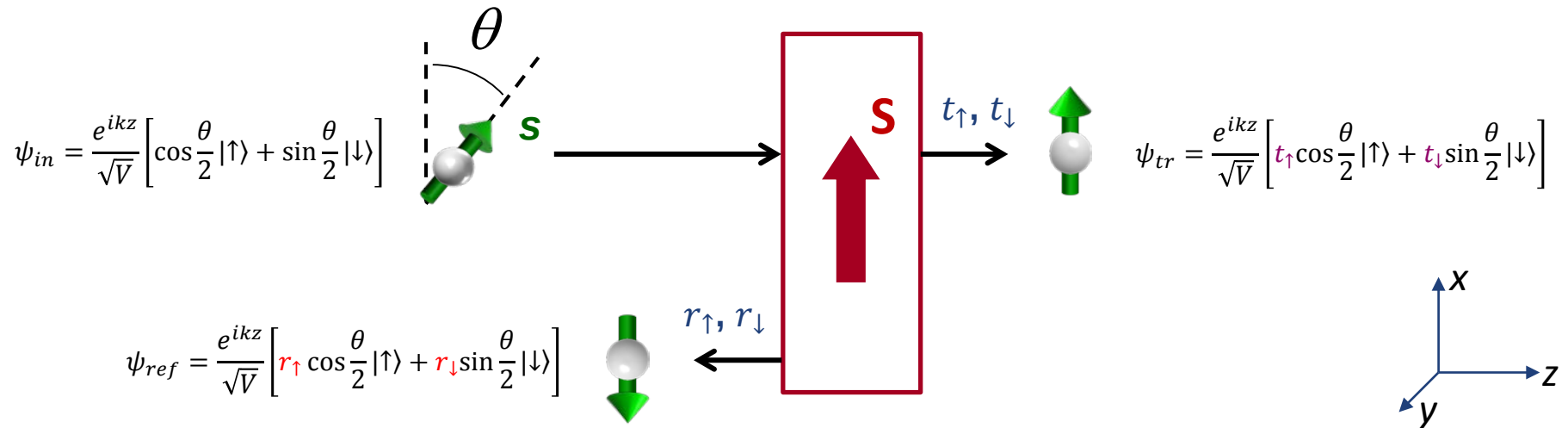
Conservation of angular momentum: $\Delta \mathbf{s} + \Delta \mathbf{S} = 0 \Rightarrow \Delta S_x = +\frac{\hbar}{2} \sin\theta$



$$\Delta \mathbf{S}_x = +\frac{\hbar}{2} \sin\theta \hat{x} = \frac{\hbar}{2} \mathbf{S} \times \underbrace{(\mathbf{S} \times \mathbf{s})}_{\sin\theta}$$

Change of total moment of magnetic layer: $\Delta \mathbf{M} V = \frac{\hbar}{2} |\gamma| \hat{\mathbf{M}} \times (\hat{\mathbf{M}} \times \hat{\mathbf{m}})$...per incident electron

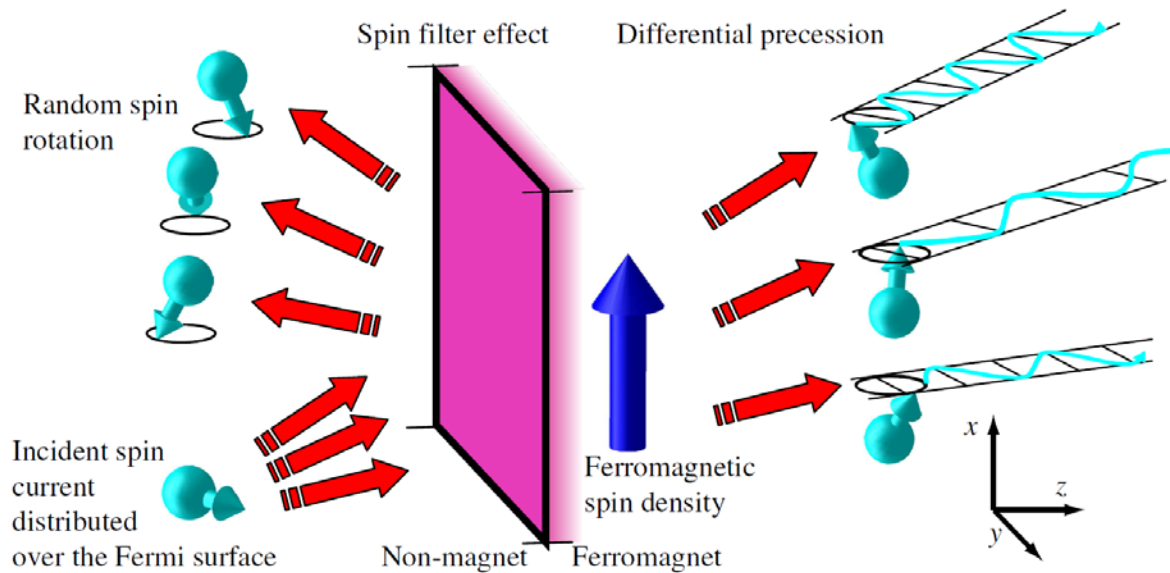
For a continuous current: $\frac{d\mathbf{M}}{dt} = \frac{\hbar |\gamma|}{2 V} \hat{\mathbf{M}} \times (\hat{\mathbf{M}} \times \hat{\mathbf{m}}) \frac{I}{e} = \boxed{\frac{I \hbar |\gamma|}{2 e M_s^2 V} \mathbf{M} \times (\mathbf{M} \times \hat{\mathbf{m}})}$



$$\mathbf{Q} = \frac{\hbar^2}{2m} \text{Im}\{\psi^* \boldsymbol{\sigma} \otimes \nabla \psi\} \rightarrow \mathbf{Q}_{in} = \frac{\hbar^2 k}{2mV} [\sin \theta \hat{\mathbf{z}} + \cos \theta \hat{\mathbf{x}}], \quad \text{etc.}$$

$$\mathbf{T}_{st} = (\mathbf{Q}^{in} + \mathbf{Q}^{ref} - \mathbf{Q}^{tr}) \cdot A = \frac{A \hbar^2 k}{V 2m} \sin \theta \left[\underbrace{(1 - \text{Re}\{t_{\uparrow} t_{\downarrow}^* + r_{\uparrow} r_{\downarrow}^*\})}_{\text{In-plane torque}} \hat{\mathbf{z}} + \underbrace{\text{Im}\{t_{\uparrow} t_{\downarrow}^* + r_{\uparrow} r_{\downarrow}^*\}}_{\text{Out-of-plane torque}} \hat{\mathbf{y}} \right]$$

- $\mathbf{T}_{st} \perp \hat{\mathbf{x}}$ - The torque is perpendicular to the magnetization
- $\mathbf{T}_{st} = 0$ if $t_{\uparrow} = t_{\downarrow}, r_{\uparrow} = r_{\downarrow}$ (no spin filter effect)
- $\mathbf{T}_{st} = 0$ if $\theta = 0, \pi$
- The in-plane and out-of-plane torque components depend on the real and imaginary values of the reflection and transmission coefficients



M. D. Stiles and J. Miltat,
Topics in App. Phys. 101,
225 (2006).

1. **Spin filter effect:** spin-dependent reflection and transmission at NM/FM interface, reduces the transverse spin components of reflected and transmitted electrons.
2. **The spin rotates upon reflection:** $r_{\uparrow\downarrow}^* = |r_{\uparrow\downarrow}^*|e^{i\Delta\phi}$. The relative phase $\Delta\phi$ of the reflected transverse components varies significantly over the Fermi surface. The reflected transverse spin averages out when summing over the electron distribution (classical dephasing).
3. **Spatial precession of the transmitted spins in the FM.** Spin-up and spin-down components have the same total energy E_F , but different kinetic energy $\Rightarrow k_{\uparrow} \neq k_{\downarrow}$, leading to a space-dependent phase difference $e^{i(k_{\uparrow}-k_{\downarrow})z}$ as the electron penetrates into the FM. The precession frequency is different for electrons from different portions of the Fermi surface, hence complete cancellation of the transverse spin occurs after propagation into the FM by a few lattice constants.

- If the cancellation of the transverse component of $\mathbf{Q}^{ref}$ and $\mathbf{Q}^{tr}$ is complete, $\mathbf{Q}_{\perp}^{in}$ is absorbed at or near the interface, leading to

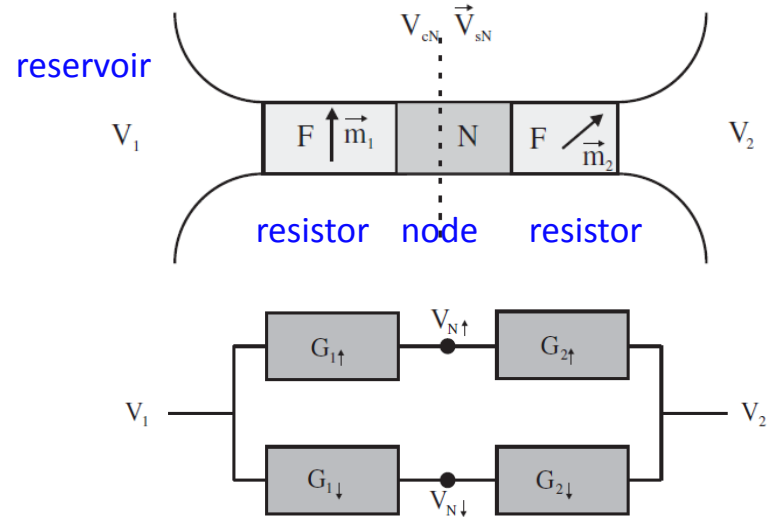
$$\mathbf{T}_{st} = (\mathbf{Q}^{in} + \mathbf{Q}^{ref} - \mathbf{Q}^{tr}) \cdot A\hat{\mathbf{z}} \approx \mathbf{Q}_{\perp}^{in} \cdot A\hat{\mathbf{z}} = \mathbf{T}_{AD}$$

The torque is AD-like and proportional to the transverse part of the incident spin current.

- If the transverse component of $\mathbf{Q}^{ref}$ and $\mathbf{Q}^{tr}$ does not average out, as is the case in very thin FM layers, a small amount of precession of the reflected and transmitted spins leads to a finite FL torque and

$$\mathbf{T}_{st} = \mathbf{T}_{AD} + \mathbf{T}_{FL}$$

- The relative importance of the spin transfer mechanisms 1-3 depends on materials pair and crystal structure.
- In metallic spin valves (CPP geometry), $\mathbf{T}_{FL}$ is typically less than 5% of $\mathbf{T}_{AD}$.
- In MTJs, averaging is not so effective due to k-selection, $\mathbf{T}_{FL}$ can be ~30% of $\mathbf{T}_{AD}$.



- Generalization of the two-channel series resistor model to multilayer structures and noncollinear magnetization
- Similar to drift-diffusion theory but neglects the spatial dependence of the chemical potential within the layers (nodes).
- Practical for treating interface effects and complex device structures.

A. Brataas, Yu. V. Nazarov, and G. E. W. Bauer, PRL 84, 2481 (2000).

A. Braatas, G.E.W. Bauer, and P.J. Kelly, Phys. Rep. 427, 157 (2006).

$$\mathbf{j}_s = \underbrace{(j_{\uparrow} - j_{\downarrow})\hat{\mathbf{M}}}_{\text{Bare spin current determined by spin dep. conductivity}} - \underbrace{\frac{2}{e} \text{Re}\{G_{\uparrow\downarrow}\} \hat{\mathbf{M}} \times (\hat{\mathbf{M}} \times \boldsymbol{\mu}_s) - \frac{2}{e} \text{Im}\{G_{\uparrow\downarrow}\} \hat{\mathbf{M}} \times \boldsymbol{\mu}_s}_{\text{Spin current absorbed by the ferromagnet}}$$

$$G_{\uparrow\downarrow} = \frac{e^2}{h} \sum_{n \in NM} \left[1 - \sum_{m \in NM} r_{\uparrow}^{nm} (r_{\downarrow}^{nm})^* \right]$$

- Spin mixing conductance: relevant for transport at interfaces when the spin accumulation $\mathbf{m}$ and magnetization $\mathbf{M}$ are not collinear

$$G_{\uparrow} = \frac{e^2}{h} \sum_{n \in NM} \sum_{m \in FM} |t_{\uparrow}^{nm}|^2$$

$$G_{\downarrow} = \frac{e^2}{h} \sum_{n \in NM} \sum_{m \in FM} |t_{\downarrow}^{nm}|^2$$

Majority and minority conductances describe electrons going from one material to another

$$G_{\uparrow\downarrow} = \frac{e^2}{h} \sum_{n \in NM} \left[1 - \sum_{m \in NM} r_{\uparrow}^{nm} (r_{\downarrow}^{nm})^* \right]$$

Describes a spin current absorbed by the FM, hence the behavior of the spins in the NM that are perpendicular to the magnetization of the FM

$Re\{G_{\uparrow\downarrow}\}$ Spin current aligned with the transverse part of μ_s in the NM

$Im\{G_{\uparrow\downarrow}\}$ Spin current perpendicular to both μ_s and $\mathbf{M}$

Both spin current components $Re\{G_{\uparrow\downarrow}\}$ and $Im\{G_{\uparrow\downarrow}\}$ are absorbed in the FM, leading to the spin torque

$$\tau_{ST} = \frac{\hbar}{2e} \mathbf{j}_s^{abs} = \frac{\hbar}{e^2} \left[Re\{G_{\uparrow\downarrow}\} \widehat{\mathbf{M}} \times (\widehat{\mathbf{M}} \times \mu_s) + Im\{G_{\uparrow\downarrow}\} \widehat{\mathbf{M}} \times \mu_s \right]$$

[torque / unit area]

$$G_{\uparrow\downarrow} = \frac{e^2}{h} \sum_{n \in NM} \left[1 - \sum_{m \in NM} r_{\uparrow}^{nm} (r_{\downarrow}^{nm})^* \right] \quad \left[\frac{I}{V} = \Omega^{-1} \right]$$

More often $G_{\uparrow\downarrow}$ is given as $\frac{j}{V}$ [$\Omega^{-1}m^{-2}$]; typically $G_{\uparrow\downarrow} = 1 \times 10^{15} \Omega^{-1}m^{-2}$ (e.g., Pt/NiFe)

TABLE I. Interface conductances in units of $10^{15} \Omega^{-1}m^{-2}$.

Xia et al., PRB 65, 220401 (2002)

System	Interface	G^{maj}	G^{min}	$\text{Re}G^{mix}$	$\text{Im}G^{mix}$
Cu/Co(111)	Clean	0.42	0.36	0.41	0.009

~ 0
 due to spin filter and dephasing

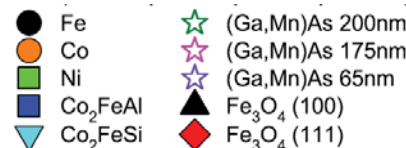
$\sim$ number of conducting channels

$$\frac{G_{\uparrow\downarrow}}{G_0/2} = \frac{G_{\uparrow\downarrow}}{e^2/h} \leftarrow \text{Quantum of conductance per spin channel}$$

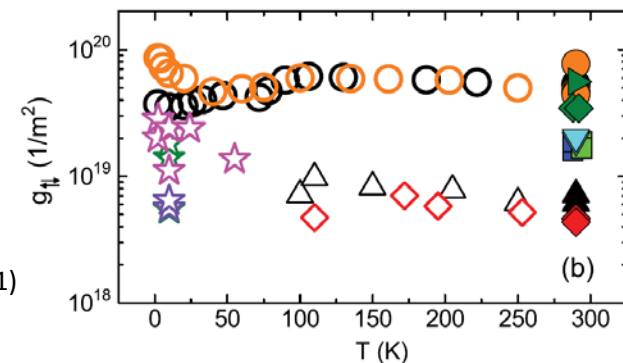
$$\sim 1 \times 10^{15} \Omega^{-1}m^{-2} \times 25.8 \text{ k}\Omega$$

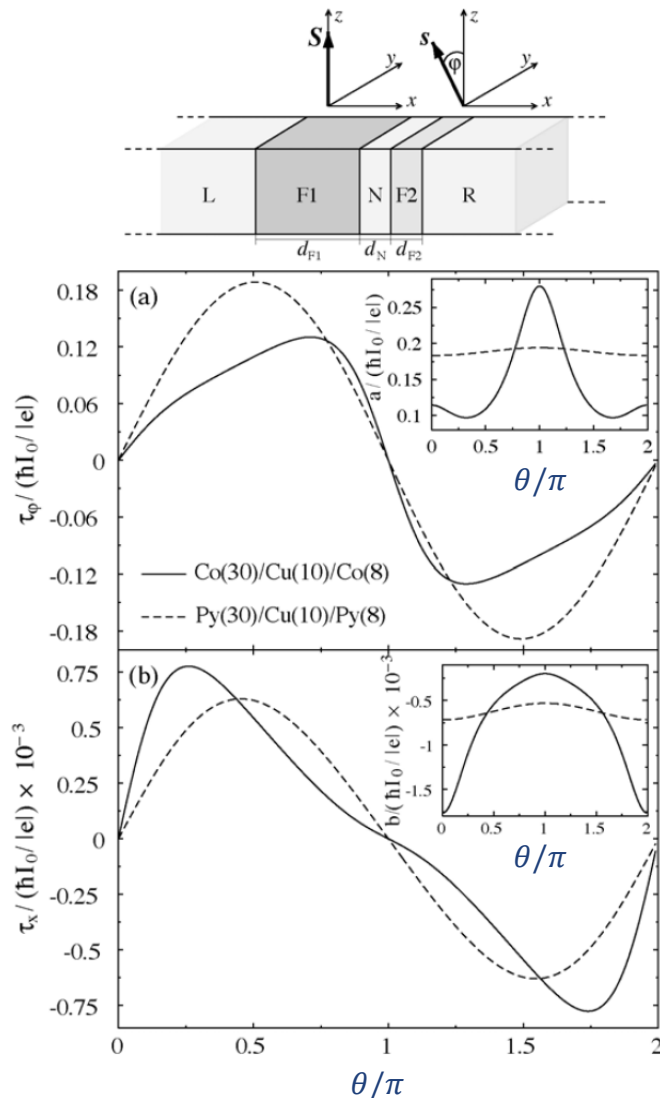
$$\approx 3 \times 10^{19} m^{-2}$$

N.B. # atoms in a monolayer film:
 $\approx 10^{19} m^{-2}$



Spin pumping & ISHE
 Czeschka et al., PRL 107, 046601 (2011)

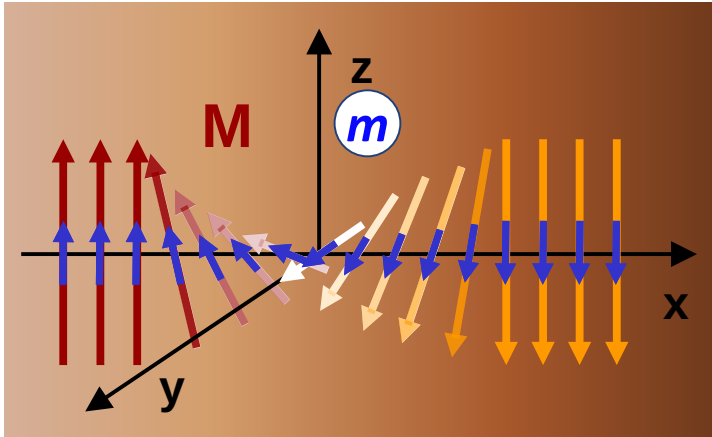
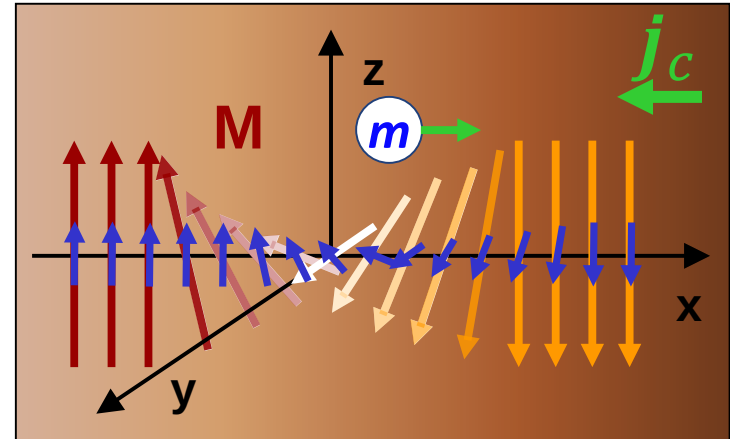




- The spin current and the coefficients a_j and b_j depend on the angle between $\mathbf{m}$ and $\mathbf{M}$ due to the influence of the longitudinal spin accumulation on spin transport

$$\mathbf{T}_{AD} = a_j(\theta) \mathbf{M} \times (\mathbf{M} \times \mathbf{m})$$

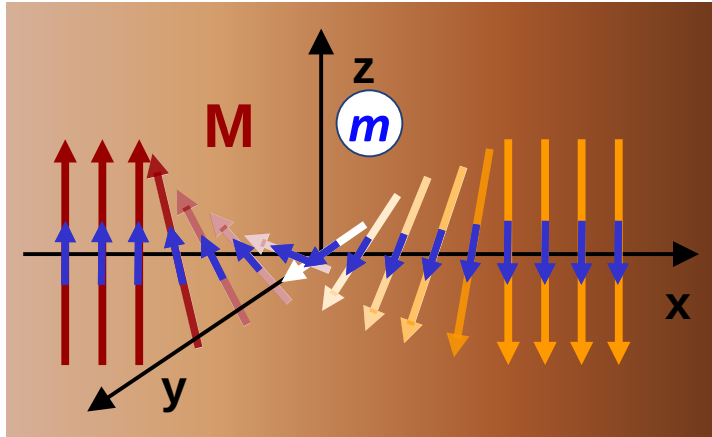
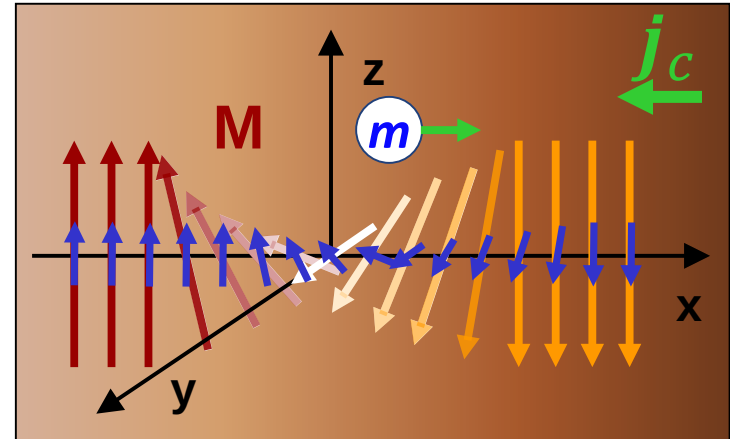
$$\mathbf{T}_{FL} = b_j(\theta) \mathbf{M} \times \mathbf{m}$$

$I = 0$  $I \neq 0$ 

$$\mathbf{Q} = -\frac{\hbar}{2e} \mathbf{j}_c \otimes \hat{\mathbf{m}} \approx -\frac{\hbar}{2e} \mathbf{j}_c \otimes \hat{\mathbf{M}}$$

$$\nabla \cdot \mathbf{Q} = -\frac{\hbar}{2e} j_c \frac{\partial \hat{\mathbf{M}}}{\partial x}$$

$$t_{st} \approx -\nabla \cdot \mathbf{Q}$$

$I = 0$  $I \neq 0$ 

$$\delta \mathbf{m}_{\perp} \sim \mathbf{M} \times \frac{\partial \mathbf{M}}{\partial x} + \frac{\partial \mathbf{M}}{\partial x}$$

$$t_{st} \sim \mathbf{M} \times \delta \mathbf{m}_{\perp} = -\frac{\mu_B P}{e M_S^3} \mathbf{M} \times [\mathbf{M} \times (\mathbf{j}_c \cdot \nabla) \mathbf{M}] - \frac{\mu_B P}{e M_S^2} \beta \mathbf{M} \times (\mathbf{j}_c \cdot \nabla) \mathbf{M}$$

"Adiabatic torque" "Non-adiabatic torque"

$$\mathbf{t}_{st} = -\frac{\mu_B P}{e M_S^3} \mathbf{M} \times [\mathbf{M} \times (\mathbf{j}_c \cdot \nabla) \mathbf{M}] - \frac{\mu_B P}{e M_S^2} \beta \mathbf{M} \times (\mathbf{j}_c \cdot \nabla) \mathbf{M}$$

$$\mathbf{H}_{ad} \sim \mathbf{M} \times (\mathbf{j}_c \cdot \nabla) \mathbf{M}$$

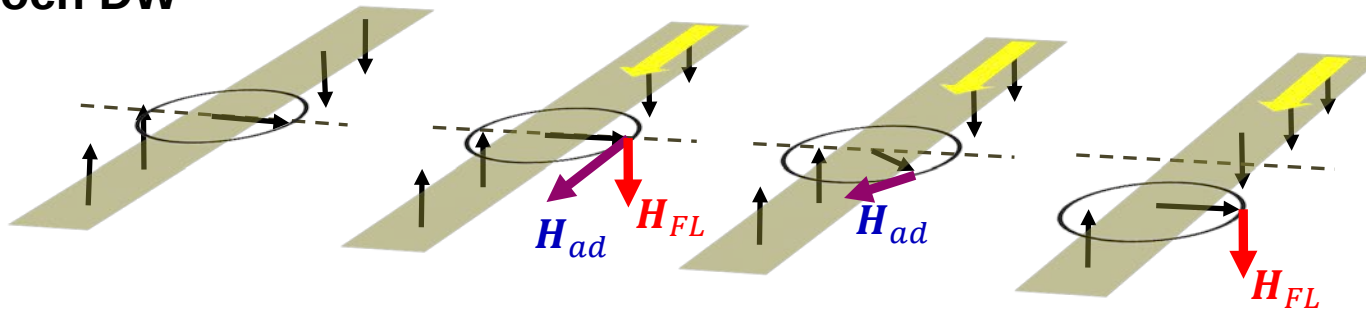
$$\mathbf{H}_{FL} \sim \beta (\mathbf{j}_c \cdot \nabla) \mathbf{M}$$

Bloch DW

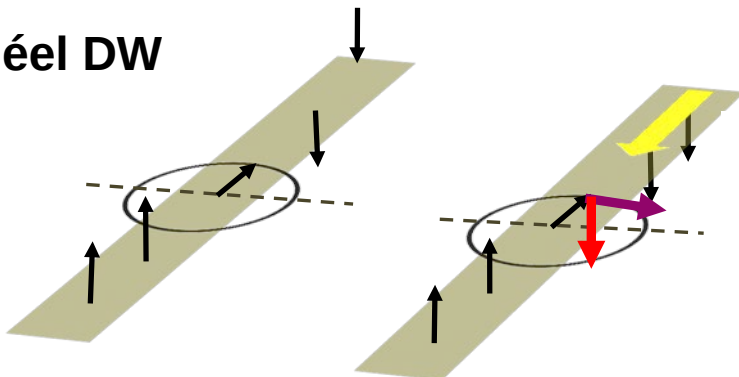
electric current

distorts DW

moves DW



Néel DW

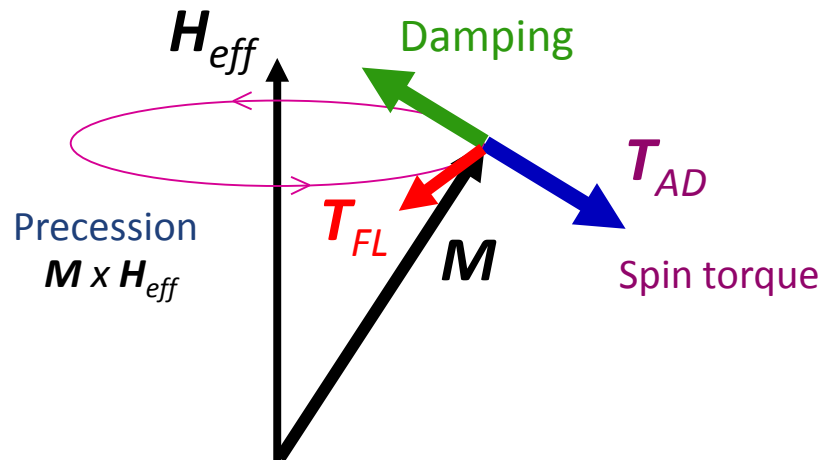


- The FL torque induces an effective field along the easy axis of the magnetization
- In the low current (non turbulent) regime, the DW velocity depends on $\mathbf{H}_{FL}$

A spin current moves the magnetization



Magnetization motion induces a spin current



$$\frac{d\vec{M}}{dt} = -\gamma \vec{M} \times \vec{H}_{eff} + \boxed{\frac{\alpha}{M} \vec{M} \times \frac{d\vec{M}}{dt}}$$



Damping term



Dissipation of angular momentum



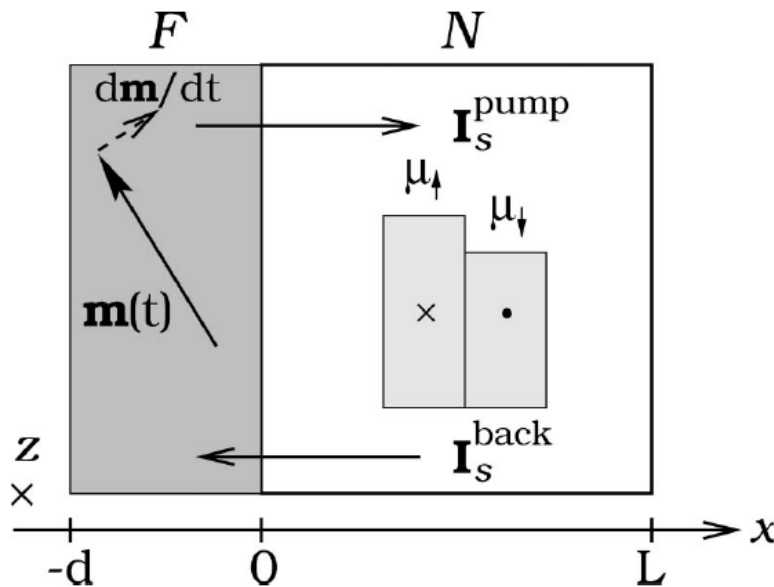
Transferred to conduction electrons



Generation of **spin current** ($\mu_{\uparrow} \neq \mu_{\downarrow}$)

Y. Tserkovnyak et al., PRL 88, 117601 (2002).

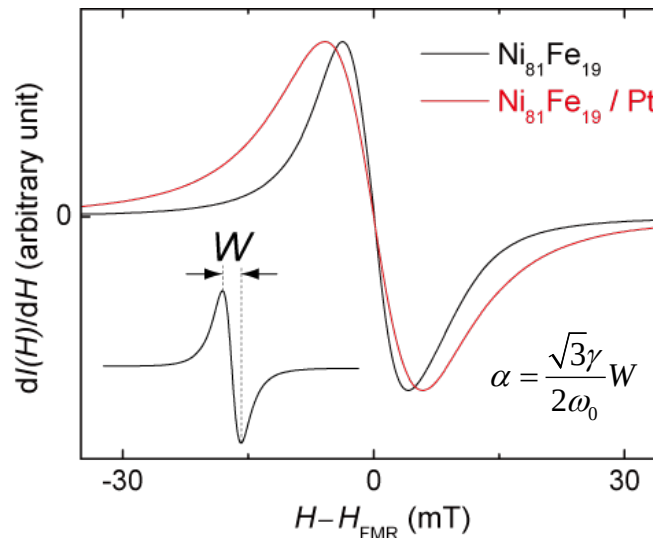
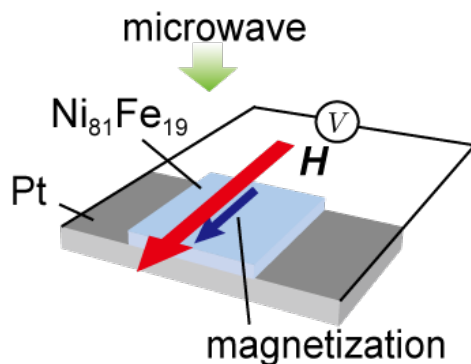
S. Mizukami et al., PRB 66, 104413 (2001); R. Urban et al., PRL 87, 217204 (2001).



$$\mathbf{j}_s = \frac{\hbar}{e} \left[\text{Re}\{G_{\uparrow\downarrow}\} \left(\hat{\mathbf{M}} \times \frac{d\hat{\mathbf{M}}}{dt} \right) + \text{Im}\{G_{\uparrow\downarrow}\} \frac{d\hat{\mathbf{M}}}{dt} \right]$$

- The spin current pumped out of the FM is perpendicular to $\mathbf{M}$
- STT and spin pumping are reciprocal effects, governed by the same conductance parameters

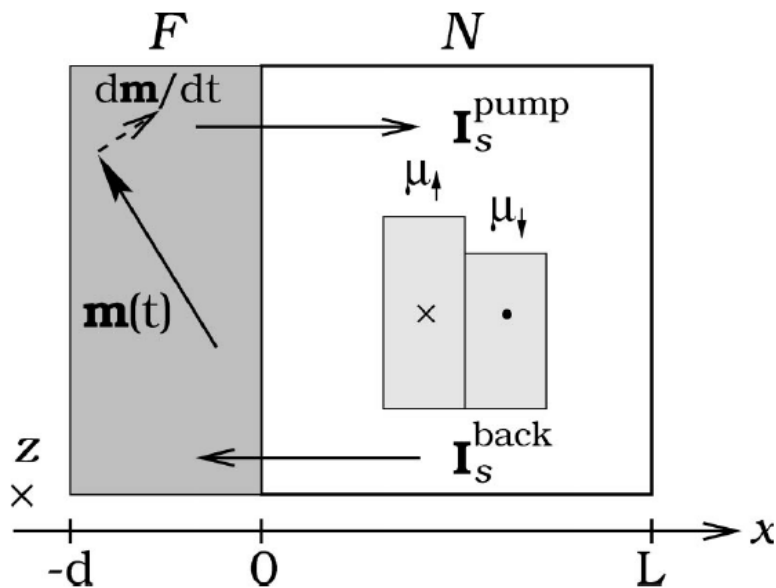
Y. Tserkovnyak et al., PRB 66, 224403 (2002)



$$\alpha = \alpha_0 + \alpha'$$

$$\alpha' \sim G_{\uparrow\downarrow}$$

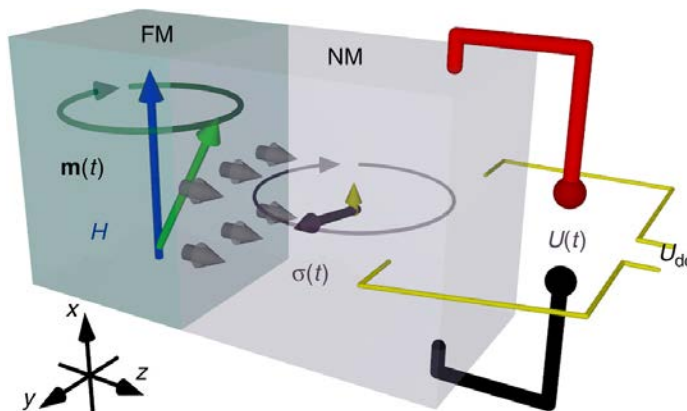
Ando et al.,
PRL 101, 036601
(2008)



$$\mathbf{j}_s = \frac{\hbar}{e} \left[\text{Re}\{G_{\uparrow\downarrow}\} \left(\hat{\mathbf{M}} \times \frac{d\hat{\mathbf{M}}}{dt} \right) + \text{Im}\{G_{\uparrow\downarrow}\} \frac{d\hat{\mathbf{M}}}{dt} \right]$$

- The spin current pumped out of the FM is perpendicular to $\mathbf{M}$
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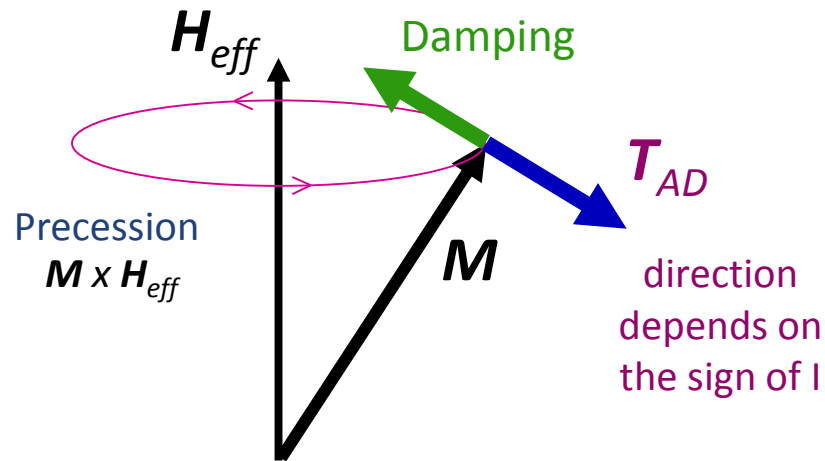
Y. Tserkovnyak et al., PRB 66, 224403 (2002)



$$V_{\text{ISHE}} \sim \mathbf{j}_s \times \boldsymbol{\sigma}$$

D. Wei et al., Nat. Comm. 5, 3768 (2014)

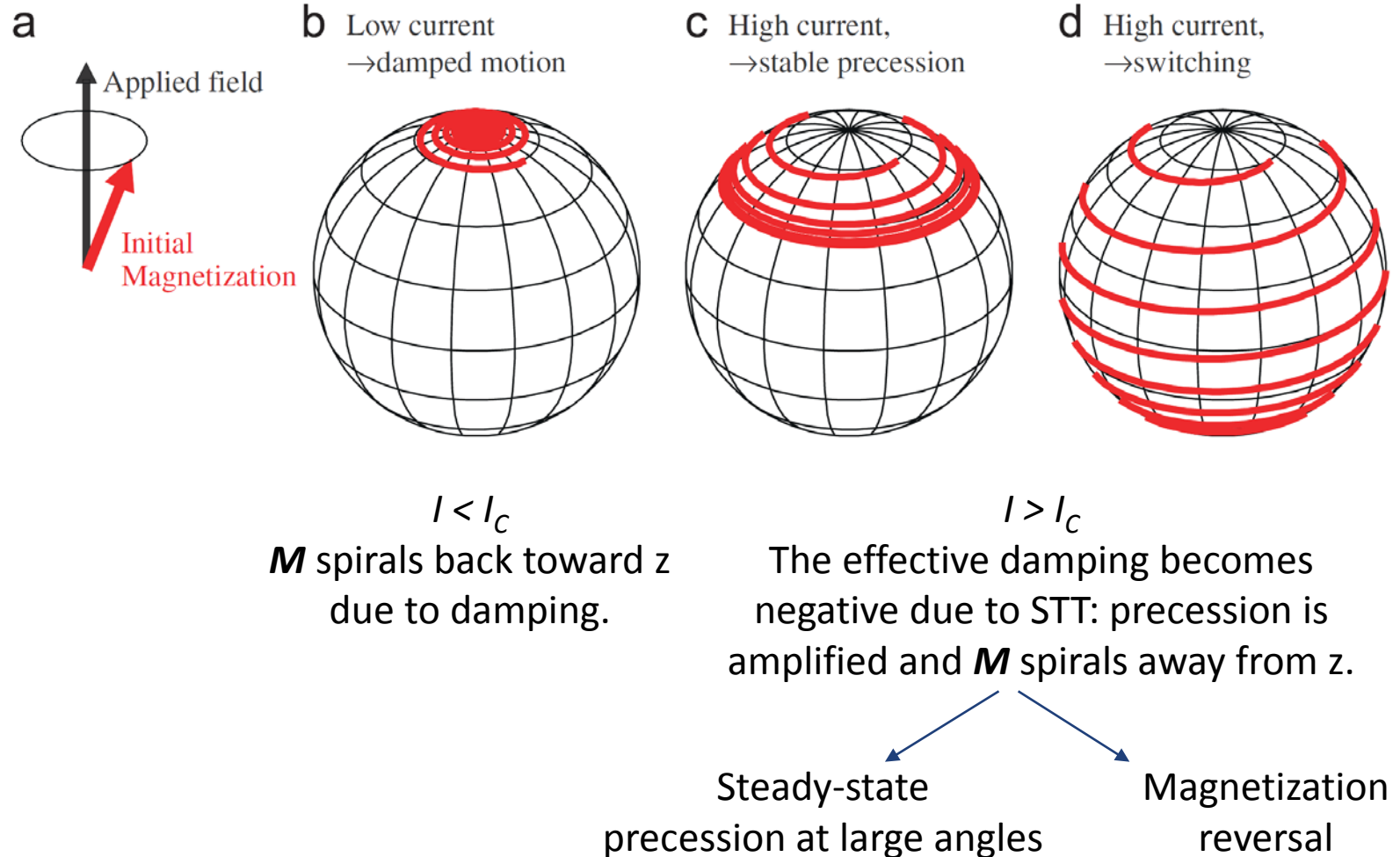
M. Weiler et al., PRL 113, 157204 (2014)



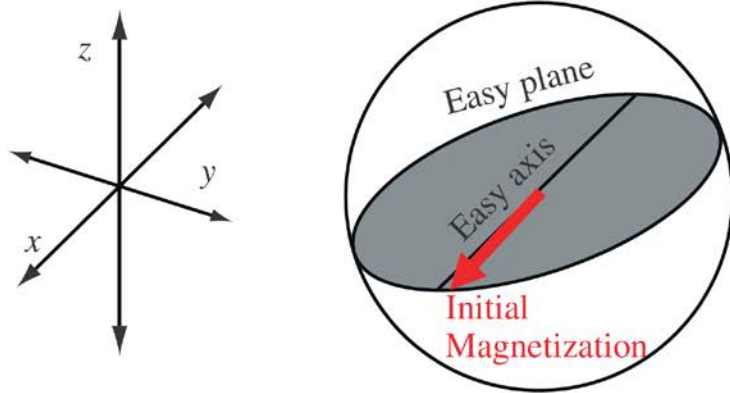
$$\frac{d\vec{M}}{dt} = -\gamma \vec{M} \times \vec{H}_{eff} + \frac{\alpha}{M} \vec{M} \times \frac{d\vec{M}}{dt} + \eta(\theta) \frac{\mu_B I}{eV} \hat{M} \times (\hat{M} \times \hat{m})$$

- AD spin torque added to LLG equation for $\vec{M}$
- Dynamics of spin accumulation ($\vec{m}$) much faster than $\vec{M}$
- Macrospin approximation or micromagnetic simulations

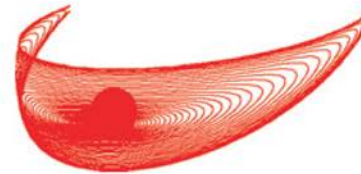
Magnetization in a perpendicular field



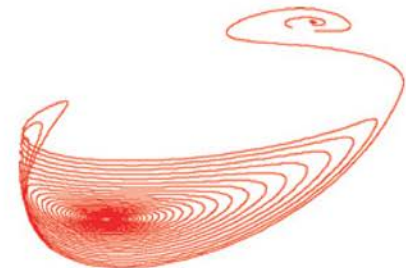
Thin film with easy axis along x, hard axis along z



Stable precession



Switching

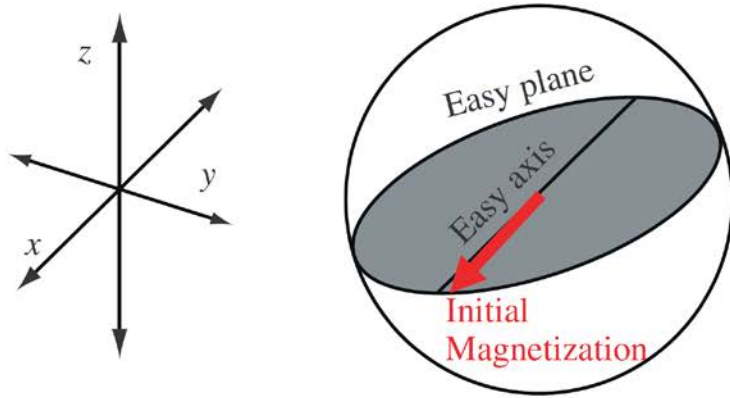


- The critical switching current is reached when the energy lost due to damping is overcome by the energy gained by STT in each cycle
- Generally, due to the larger amount of spin accumulation in the AP state

$$I_C = \frac{2e}{\hbar} \frac{\alpha}{\eta(\theta_0)} V \mu_0 M_s \left(H + H_k + \frac{1}{2} M_s \right)$$

$$I_{AP \rightarrow P} < I_{P \rightarrow AP}$$

Thin film with easy axis along x, hard axis along z



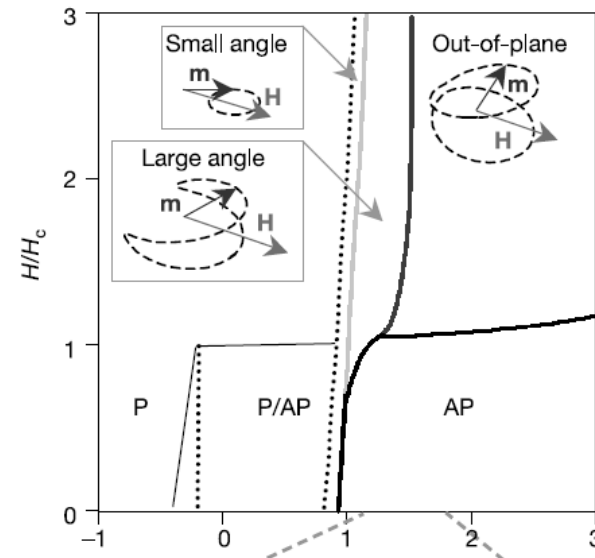
Stable precession

A 3D plot showing a red, teardrop-shaped surface representing the stable precession of the magnetization vector. A red dot is at the center of the base of the teardrop.

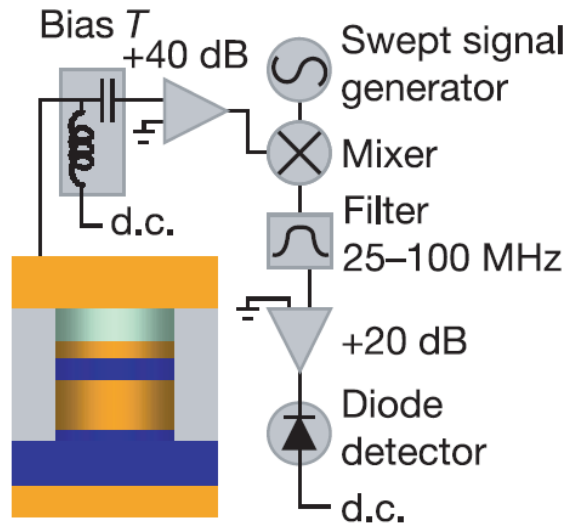
Switching

A 3D plot showing a red, teardrop-shaped surface representing the switching of the magnetization vector. The surface is elongated and spiraling, indicating a transition state.

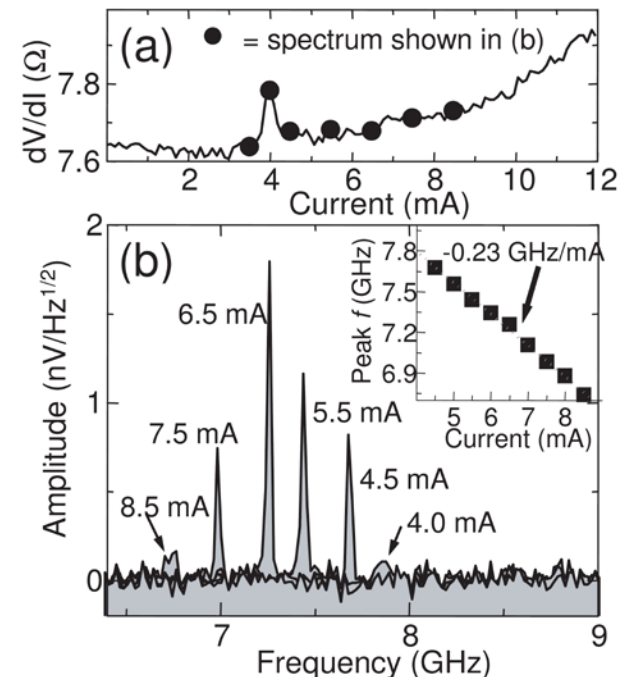
- Different static magnetic states and stationary precessional modes can be reached depending on current and applied field



DC current → Precession → GMR changes at MW frequency → MW voltage at contacts



Kiselev et al., Nature 425, 380 (2003)



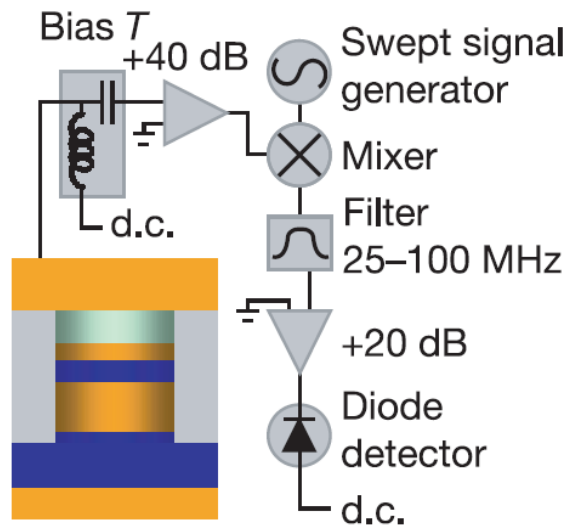
Differential resistance vs I

MW voltage vs I and f

Rippard et al., PRL 92, 027201 (2004)

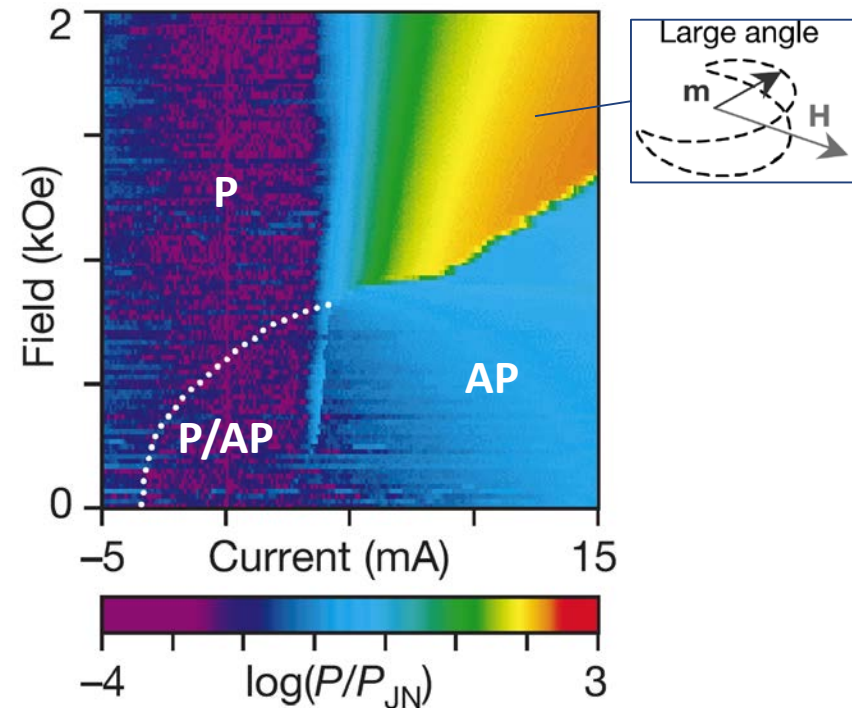
External fields favors P configuration, current favors AP → steady state oscillations

DC current $\rightarrow$ Precession $\rightarrow$ GMR changes at MW frequency $\rightarrow$ MW voltage at contacts

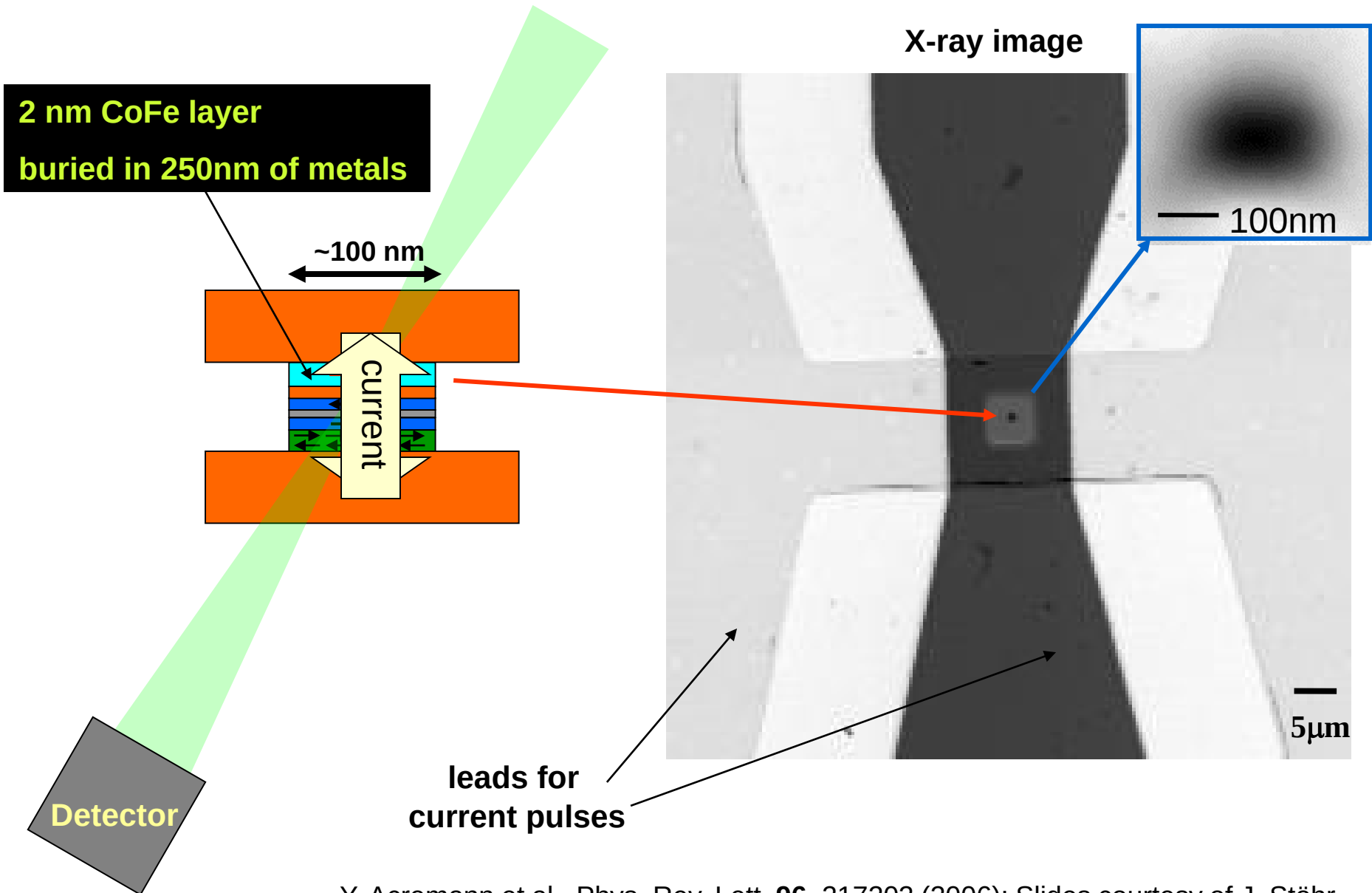


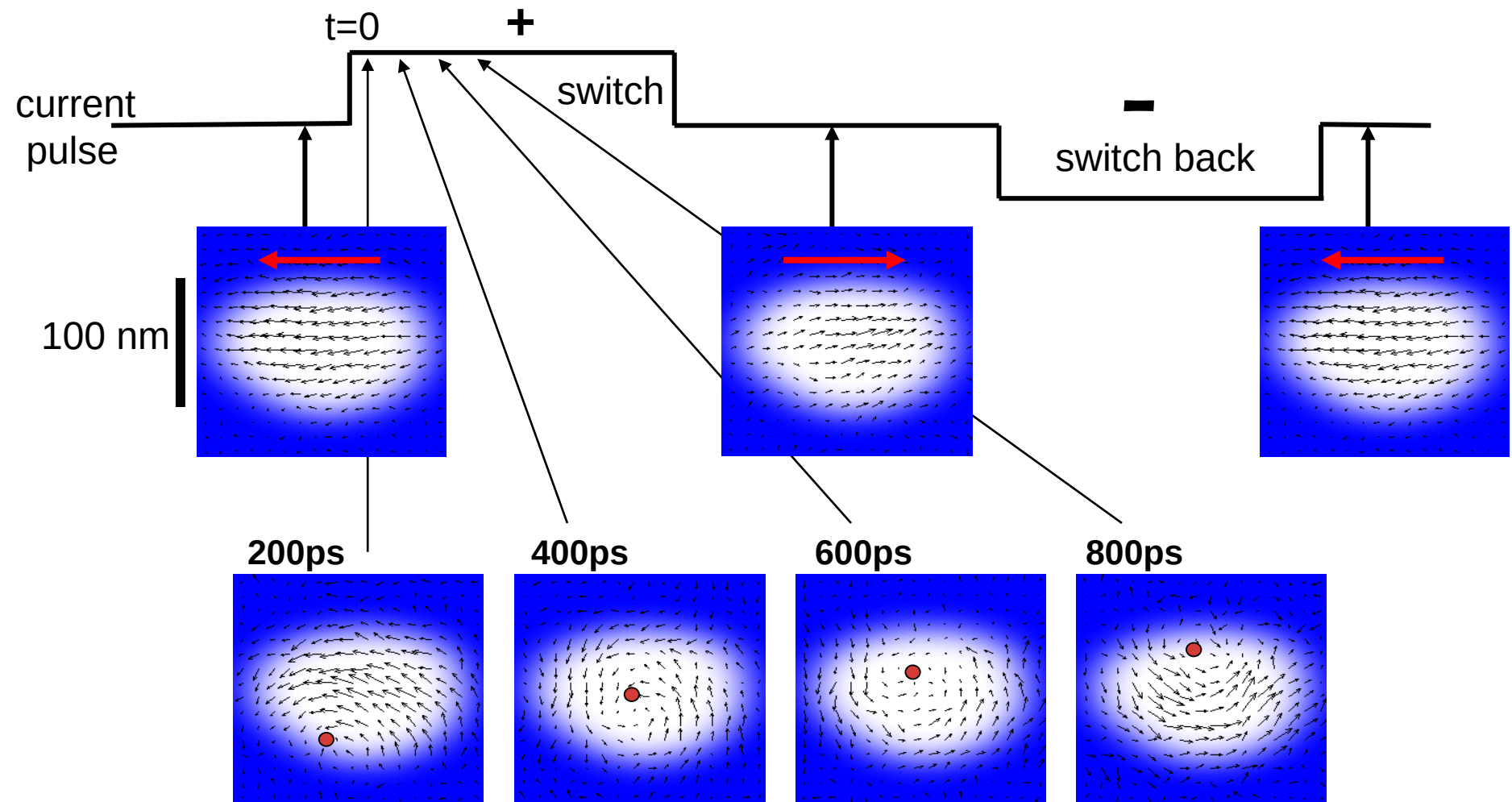
Kiselev et al., Nature 425, 380 (2003)

MW power versus I and H
applied along the in-plane easy axis.



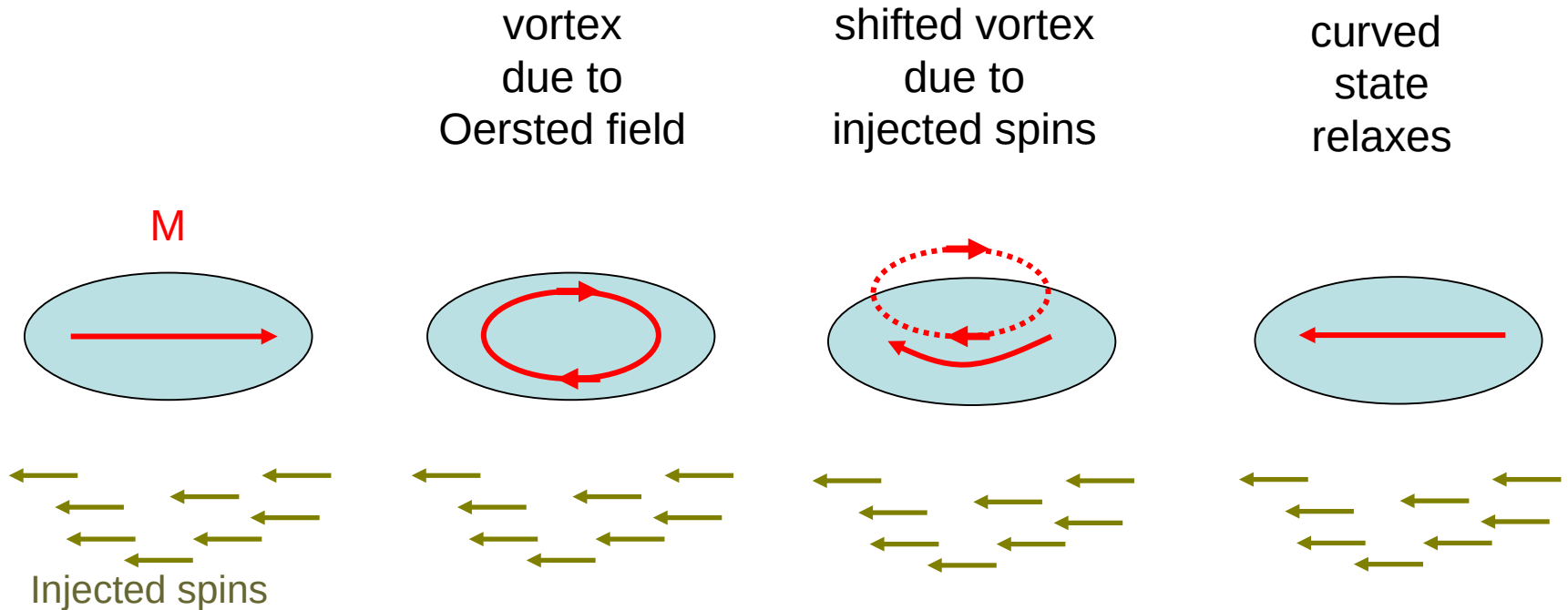
- Nanoscale oscillator or MW source with tunable frequency for on-chip applications
- MW power scales with MR (larger in MTJ)
- Nonlinear coupling between amplitude and frequency leads to f fluctuations and broadens the linewidth



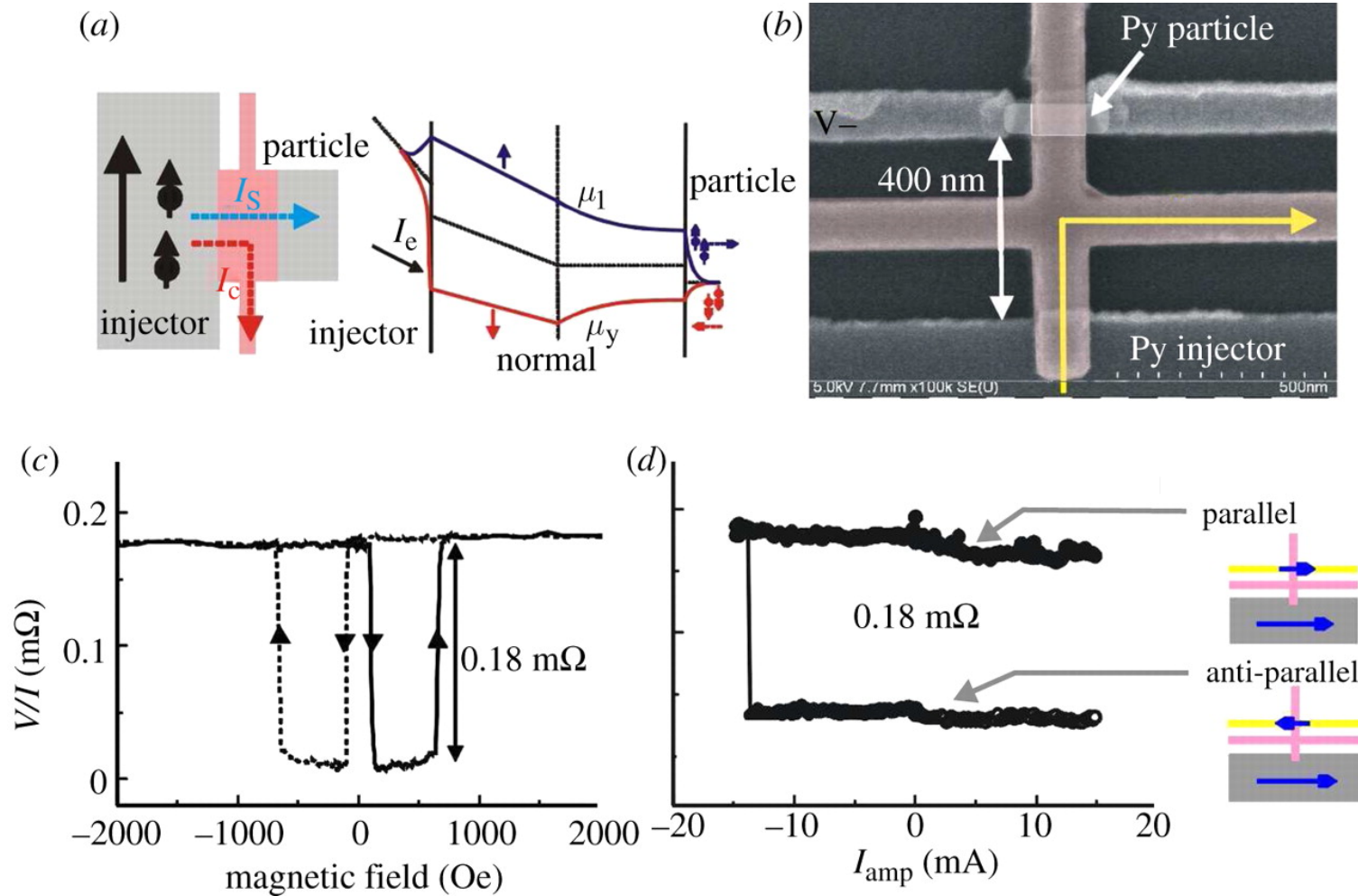


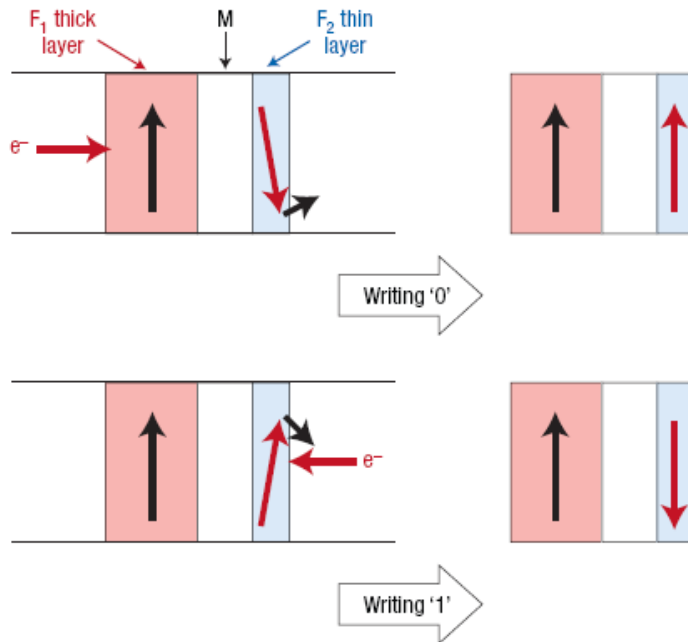
Y. Acremann et al., Phys. Rev. Lett. **96**, 217202 (2006)

J. P. Strachan et al., Phys. Rev. Lett. **100**, 247201 (2008)



- Vortex breaks the symmetry, starts process
- Spin current transfers angular momentum, drives switching
- Switching speed 200 m/s ($\sim$ speed of sound)

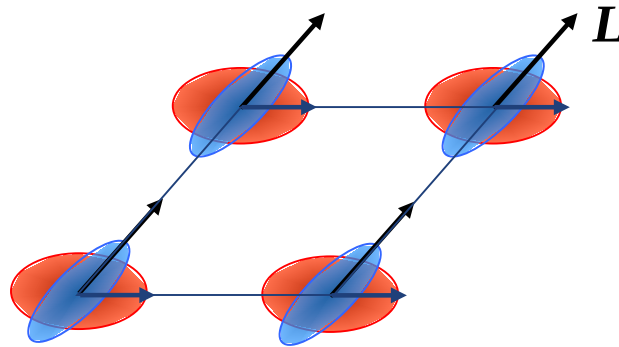




- Spin current generated by the spin-transfer effect from a FM “polarizer” layer or magnetic domain
- Can be used to switch a “free” FM layer, move DWs, or induce sustained oscillations
- It works in metallic spin valves (FM/NM/FM) as well as in magnetic tunnel junctions (FM/oxide/FM)

- Charge and spin transport channels overlap: other device geometries are possible
- Requires at least two FM layers in CPP geometry
- DW motion requires large current density
- $T \sim \sin\theta_0 \sim \theta_0$ implies large and unpredictable incubation time to initiate switching

Fundamental link between charge and spin



$$\mathcal{H} = \sum_i \left(\frac{\vec{p}_i^2}{2m} + V(\vec{r}_i) \right) + \frac{1}{2} \sum_{i \neq j} \frac{e^2}{|\vec{r}_i - \vec{r}_j|} + \mu_B B \frac{1}{\hbar} \sum_i (\ell_{z,i} + 2 s_{z,i})$$

$$\mathcal{H}_{\ell s} = \sum_i \zeta(\vec{r}_i) \vec{\ell}_i \vec{s}_i$$

	Energy (eV/atom)
Cohesive energy	5.5
Local moment formation	1.0
Alloy formation	0.5
Exchange	0.2
Structural relaxation	0.05
Spin-orbit coupling	0.03-0.08

- Magnetocrystalline anisotropy

$$E(\theta) = K_u \sin^2 \theta$$

- Antisymmetric exchange

$$H_{DM} = D_{ij} (\mathbf{S}_i \times \mathbf{S}_j)$$

- Magnetic damping

$$\frac{d\vec{M}}{dt} \sim \frac{\alpha}{M} \vec{M} \times \frac{d\vec{M}}{dt}$$

- Anisotropic magnetoresistance

$$R(\theta) = R_{\perp} + (R_{//} - R_{\perp}) (\hat{\mathbf{j}} \cdot \hat{\mathbf{M}})$$

- Anomalous Hall effect

$$R_H = R_0 + R_a (\hat{\mathbf{j}} \times \hat{\mathbf{M}})$$

- Spin Hall effect

$$j_i^k = \sigma_{ij}^k E_j$$

- Rashba effect

$$H_R = \alpha_R (\sigma_x k_y - \sigma_y k_x)$$

- Dresselhaus effect

$$H_D = \beta (\sigma_x k_x - \sigma_y k_y)$$

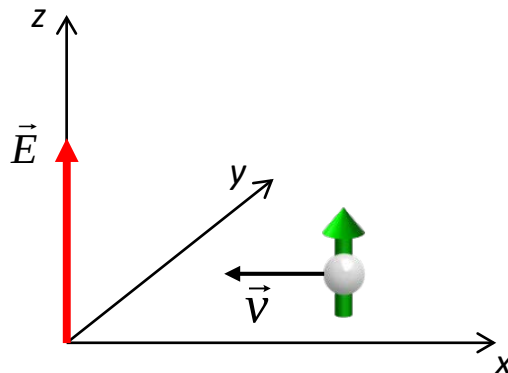
Schrödinger-Pauli Hamiltonian:

$$H = \frac{1}{2m} \left[\vec{p} + \frac{e}{c} \vec{A}(\vec{r}, t) \right]^2 - e\phi(\vec{r}, t) + \frac{e\hbar}{2mc} \vec{\sigma} \cdot \vec{B}(\vec{r}, t)$$

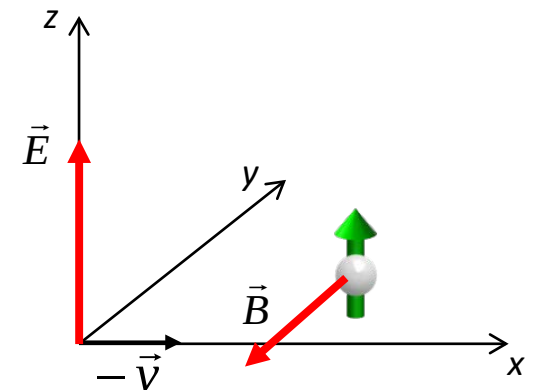
Relativistic effect: **magnetic field due to spin-orbit coupling**

$$\vec{B}_{eff}(\vec{k}) = \frac{1}{2c^2} \vec{E} \times \vec{v}$$

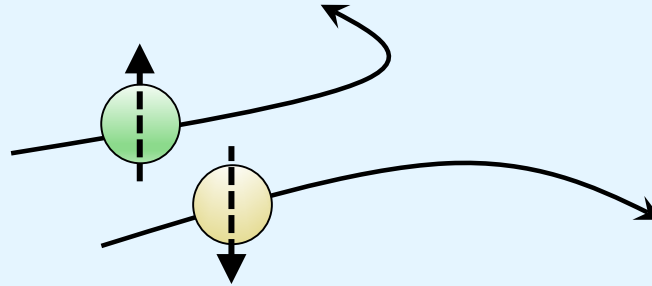
Laboratory
reference
frame



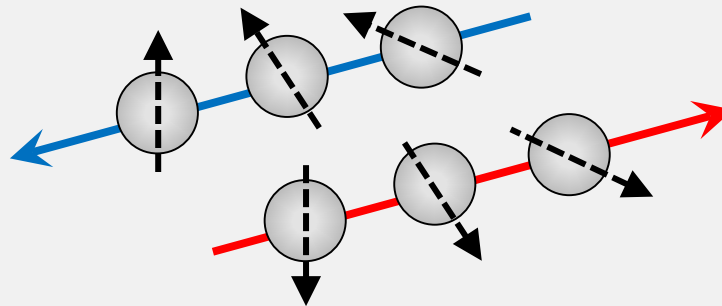
Electron's
rest
frame



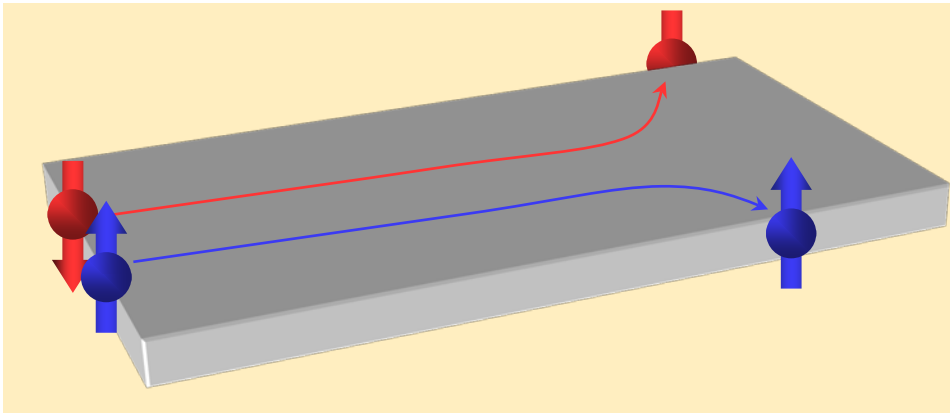
Spin-dependent scattering



Spin rotation



Spin-dependent scattering gives rise to
transverse spin imbalance
of charge currents

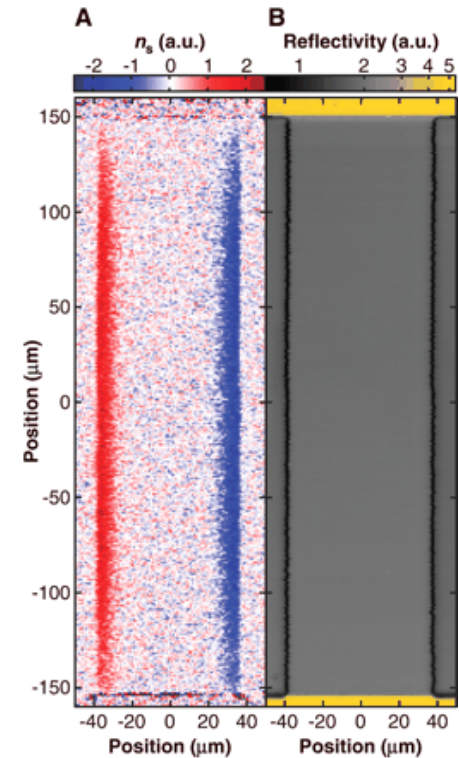


M. I. Dyakonov and V. I. Perel, JETP Lett. **13**, 467 (1971);

J. E. Hirsch, Phys. Rev. Lett. **83**, 1834 (1999)

Reviews: Sinova et al., arXiv:1411.3249

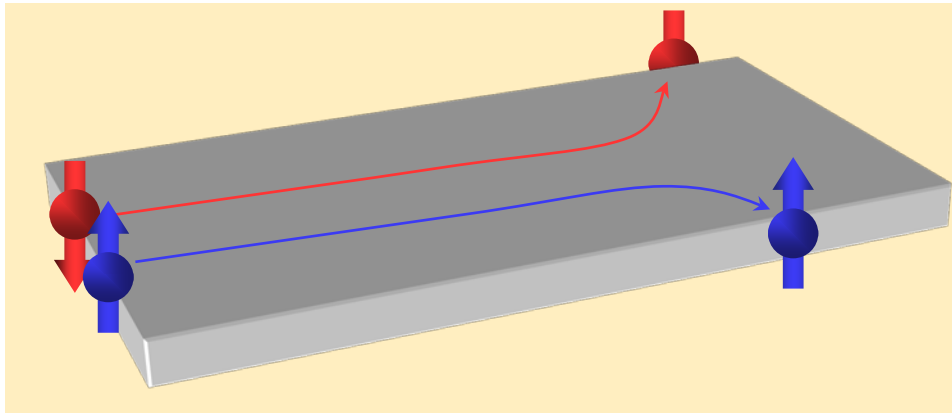
Hoffmann, IEEE Transactions on Magnetics, 2013



Direct observation in GaAs
with optical detection

Y. K. Kato et al., Science **306**, 1910 (2004)

Spin-dependent scattering gives rise to
transverse spin imbalance
of charge currents

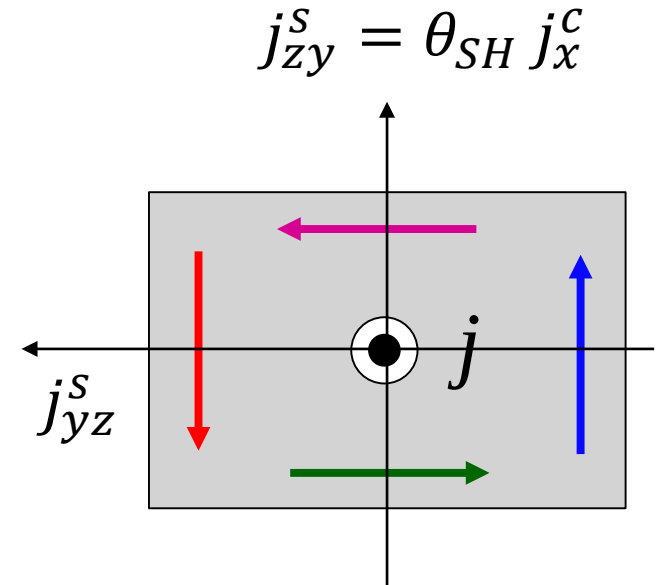


M. I. Dyakonov and V. I. Perel, JETP Lett. **13**, 467 (1971);

J. E. Hirsch, Phys. Rev. Lett. **83**, 1834 (1999)

Reviews: Sinova et al., arXiv:1411.3249

Hoffmann, IEEE Transactions on Magnetism, 2013



$$\theta_{SH} = \frac{j_c}{j_s} = \frac{\sigma_{xx}}{\sigma_{yx}^{SH}}$$

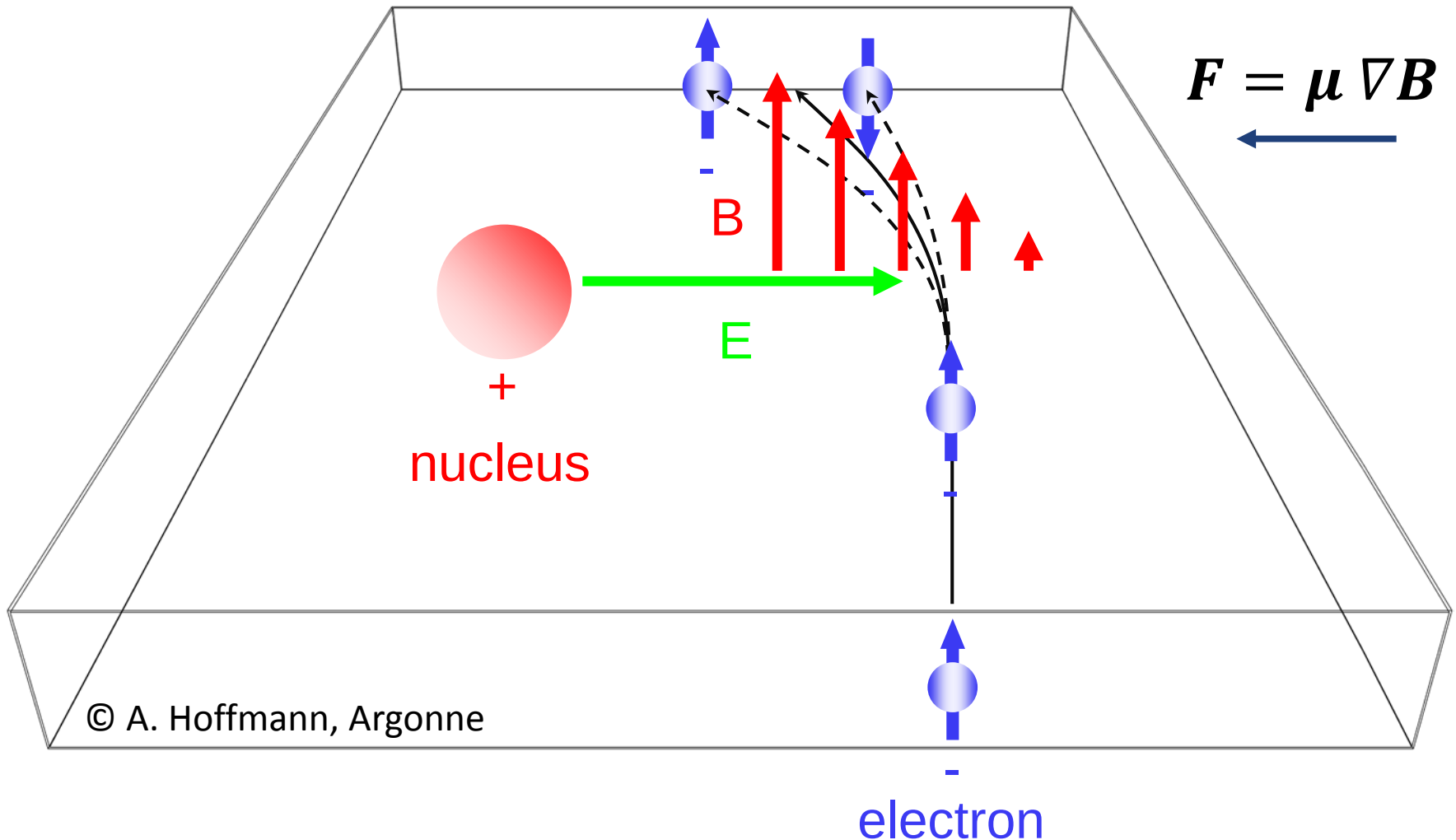
$$\theta_{SH}(\text{Pt}) = 0.0037 \quad \rightarrow \quad 0.08 \quad \rightarrow \quad \geq 0.2$$

T. Kimura et al.,
PRL 98, 156601 (2007)

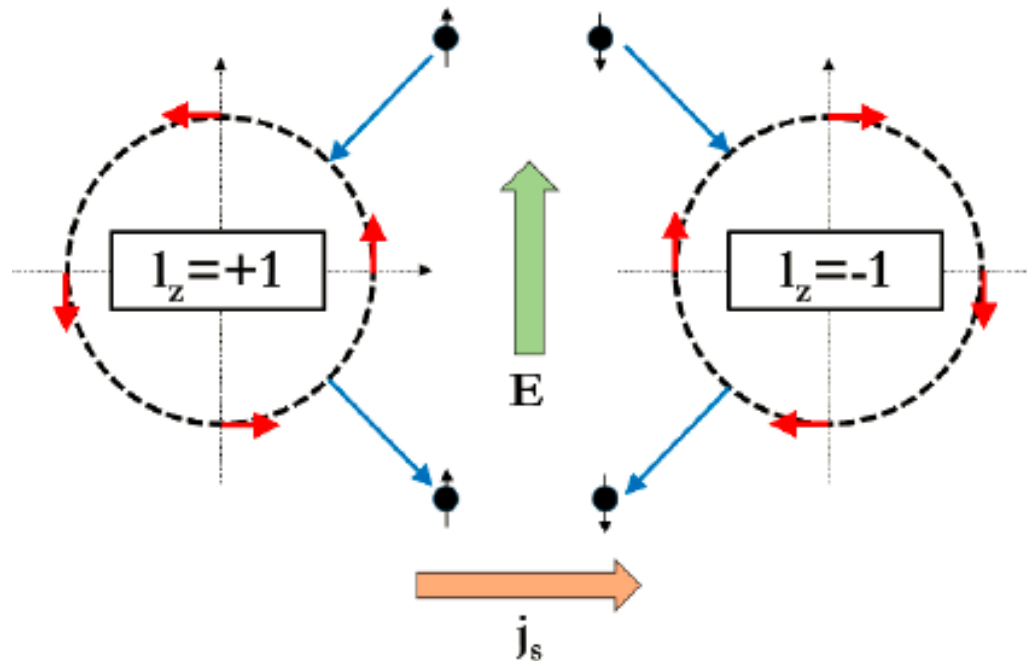
E. Saitoh et al.,
APL 88, 182509 (2006)

K. Ando et al.,
PRL 101, 036601 (2008)

M.H. Nguyen et al.,
arXiv:1504.02806



© A. Hoffmann, Argonne



PhD thesis
Marc Drouard

- E-field induced hopping of spin up (down) electrons between sd-states with plus (minus) orbital moment according to 3rd Hund's rule
- Electron acquire a finite amount of orbital angular momentum that is spin dependent

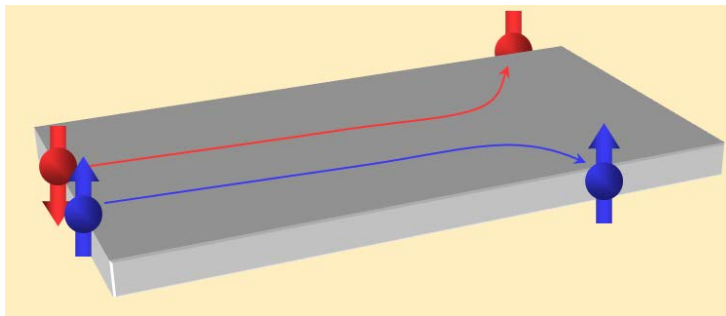
$$\dot{\mathbf{x}} = \frac{1}{\hbar} \frac{\partial E_n(\mathbf{k})}{\partial \mathbf{k}} + \underbrace{\dot{\mathbf{k}} \times \mathbf{B}_n(\mathbf{k})}_{\text{Anomalous velocity}}$$

SHE

Charge Current



Transverse spin imbalance

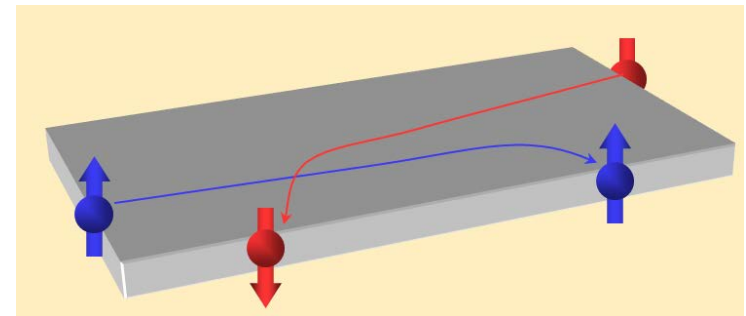


ISHE

Spin Current



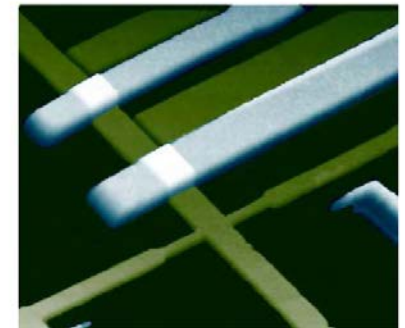
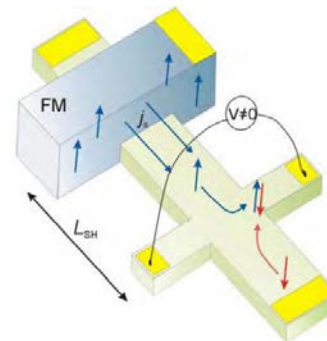
Transverse charge imbalance

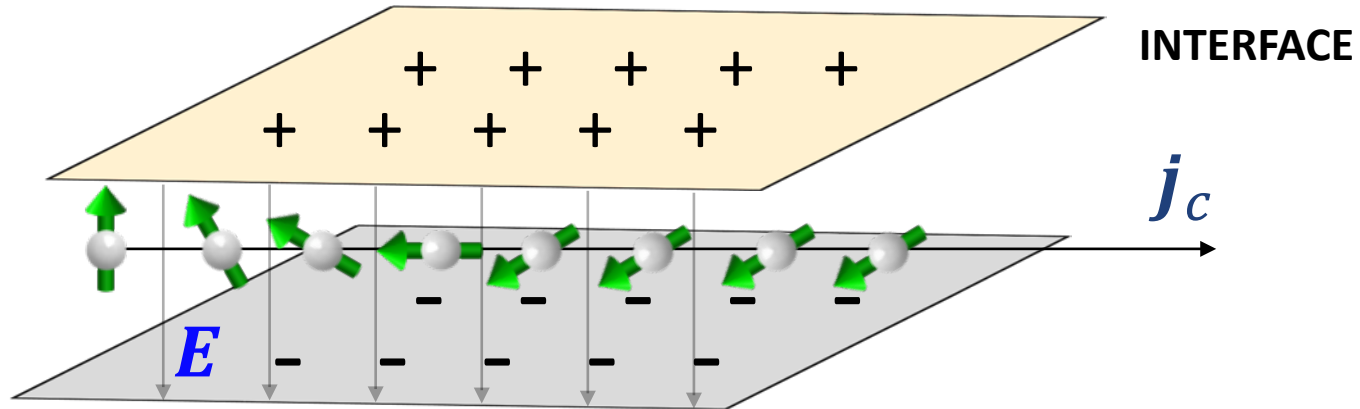


Optical spin excitation: Bakun et al.,
Sov. Phys. JETP Lett. 40, 1293 (1984)

Non local transport: Valenzuela and
Tinkham, Nature 442, 176 (2006).

Spin pumping: Saitoh et al., APL 88,
182509 (2006)





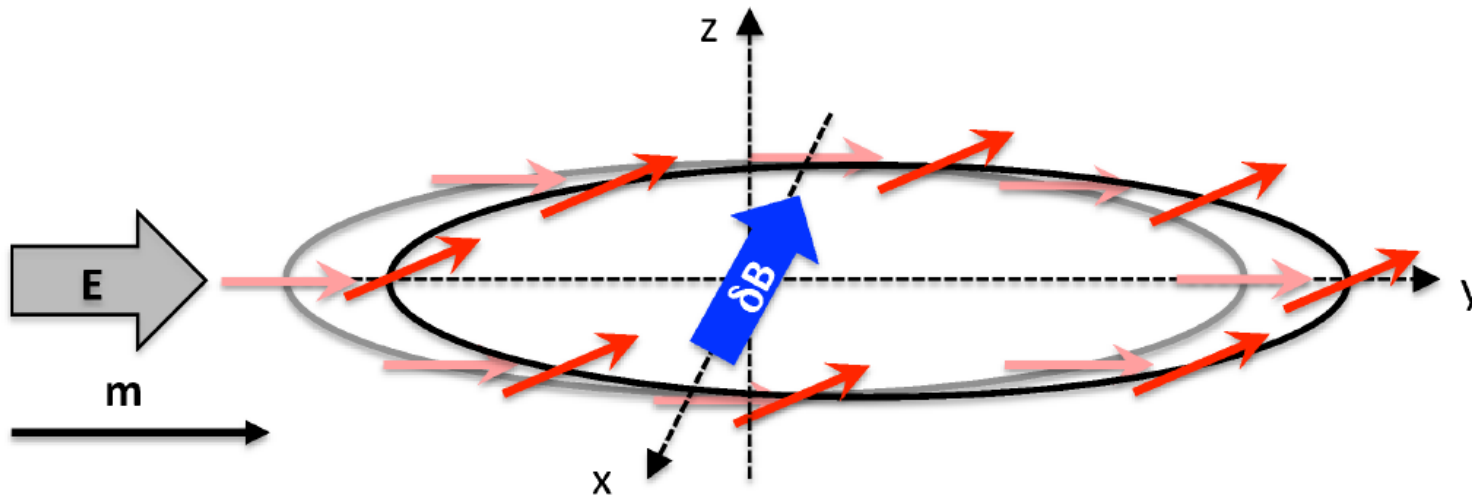
Conduction electrons moving in an uncompensated $\mathbf{E}$ field at interfaces: $\mathbf{B} \sim \mathbf{v} \times \mathbf{E} \sim \mathbf{j}_c \times \hat{\mathbf{z}}$

$$\mathbf{B}_R = \frac{\alpha_R}{2\mu_B^2} (\mathbf{j}_c \times \hat{\mathbf{z}})$$

$$\delta m_y = \frac{\mu_B m_e^* \alpha_R}{e\hbar E_F} j_c$$

The Rashba field induces a homogenous spin polarization in-plane, perpendicular to the current.

“Edelstein effect” or “Inverse spin galvanic effect” or “Rashba effect”



$$\delta m_z \sim \frac{\alpha_R}{J_{sd}} j_c$$

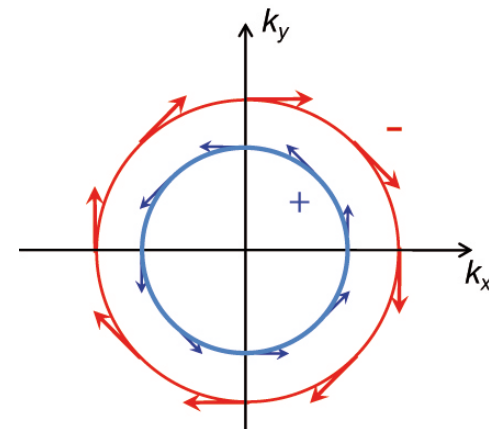
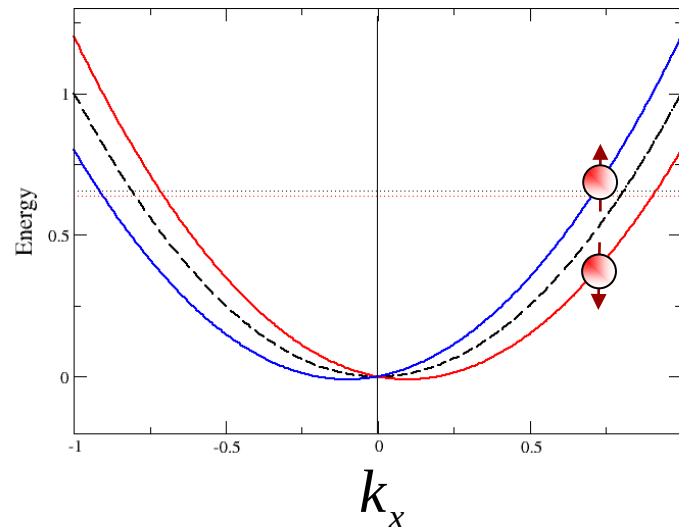
- Displacement of the Fermi surface → nonequilibrium spin-orbit field $\delta B \parallel x$
 - spin precession around δB produces a stationary spin density along z

2D electron gas with
structure inversion asymmetry

$$H = -\frac{\hbar^2 k^2}{2m} + \alpha_R (\sigma_x k_y - \sigma_y k_x)$$

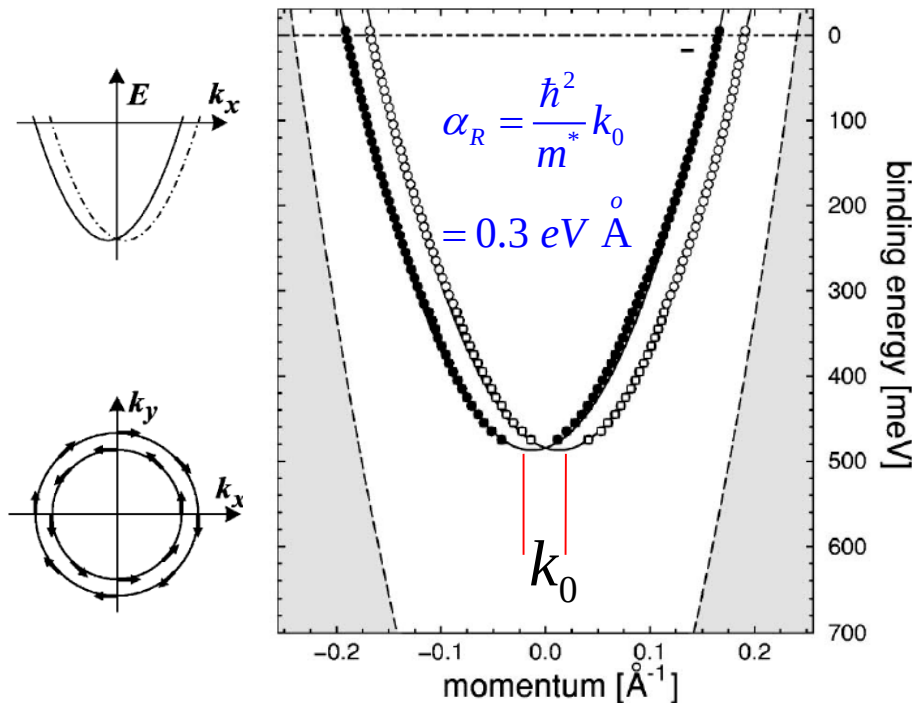
Spin-split energy bands
In the absence of local moments

$$E_{+(-)}(k) = \frac{\hbar^2}{2m} k^2 + (-) \cdot \alpha_R k$$



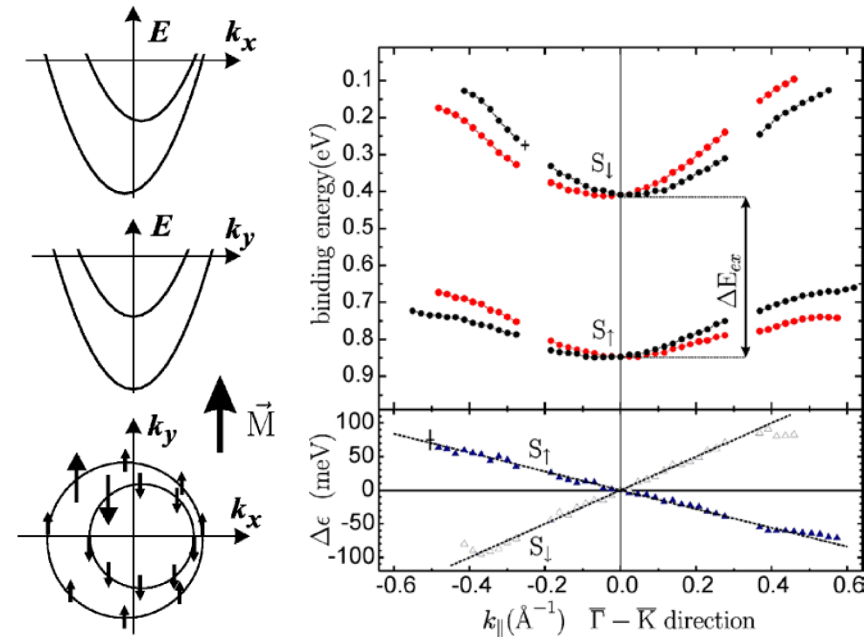
Fermi surface

Au(111)

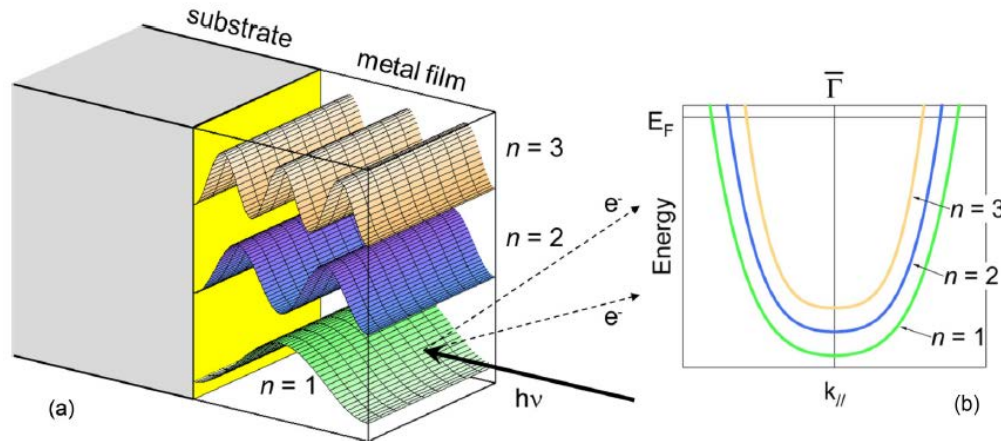


Reinert et al.,
PRB 63, 115415 (2001)

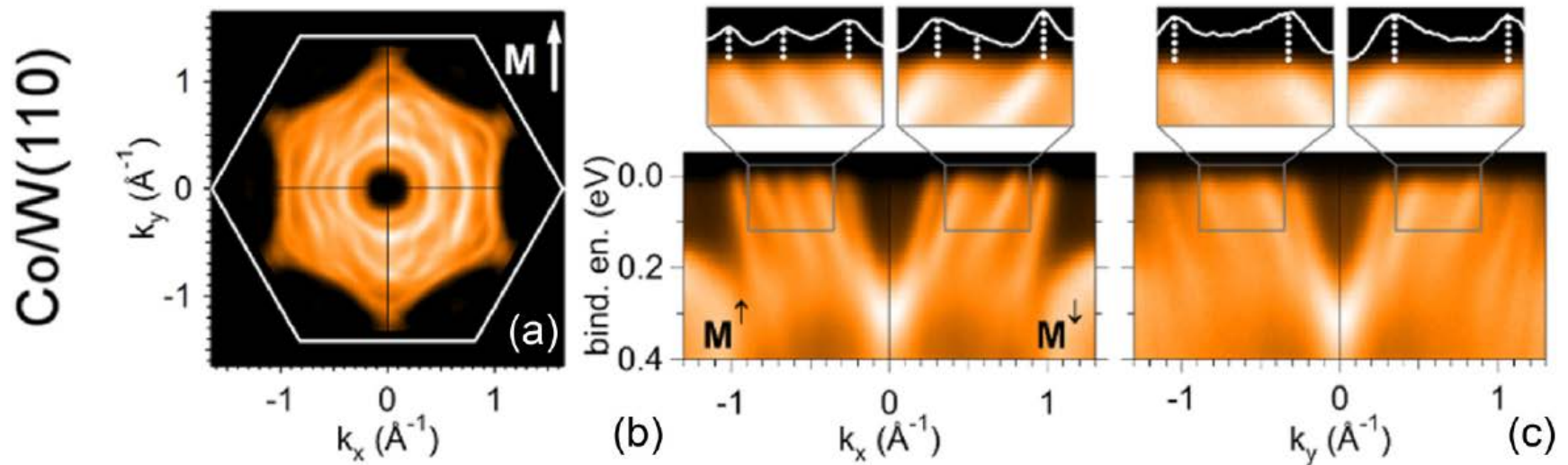
Gd(0001)



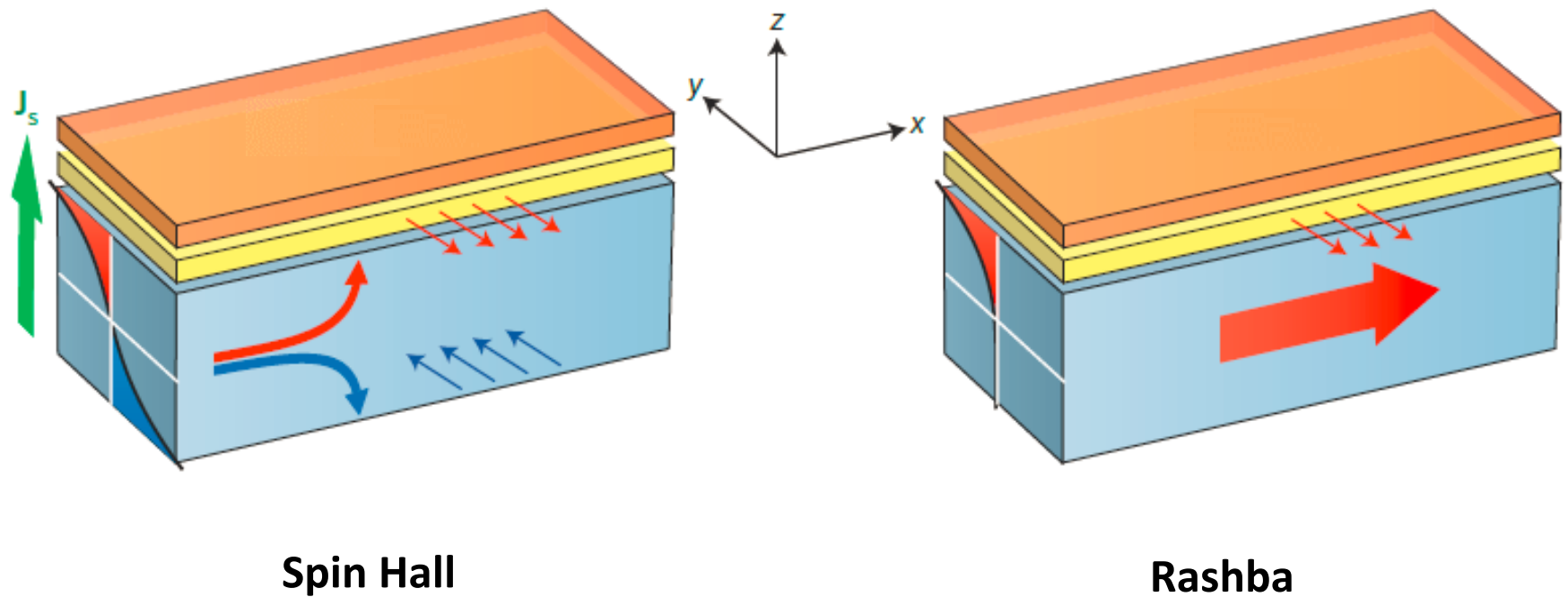
Krupin et al.,
PRB 71, 201403(R) (2005)

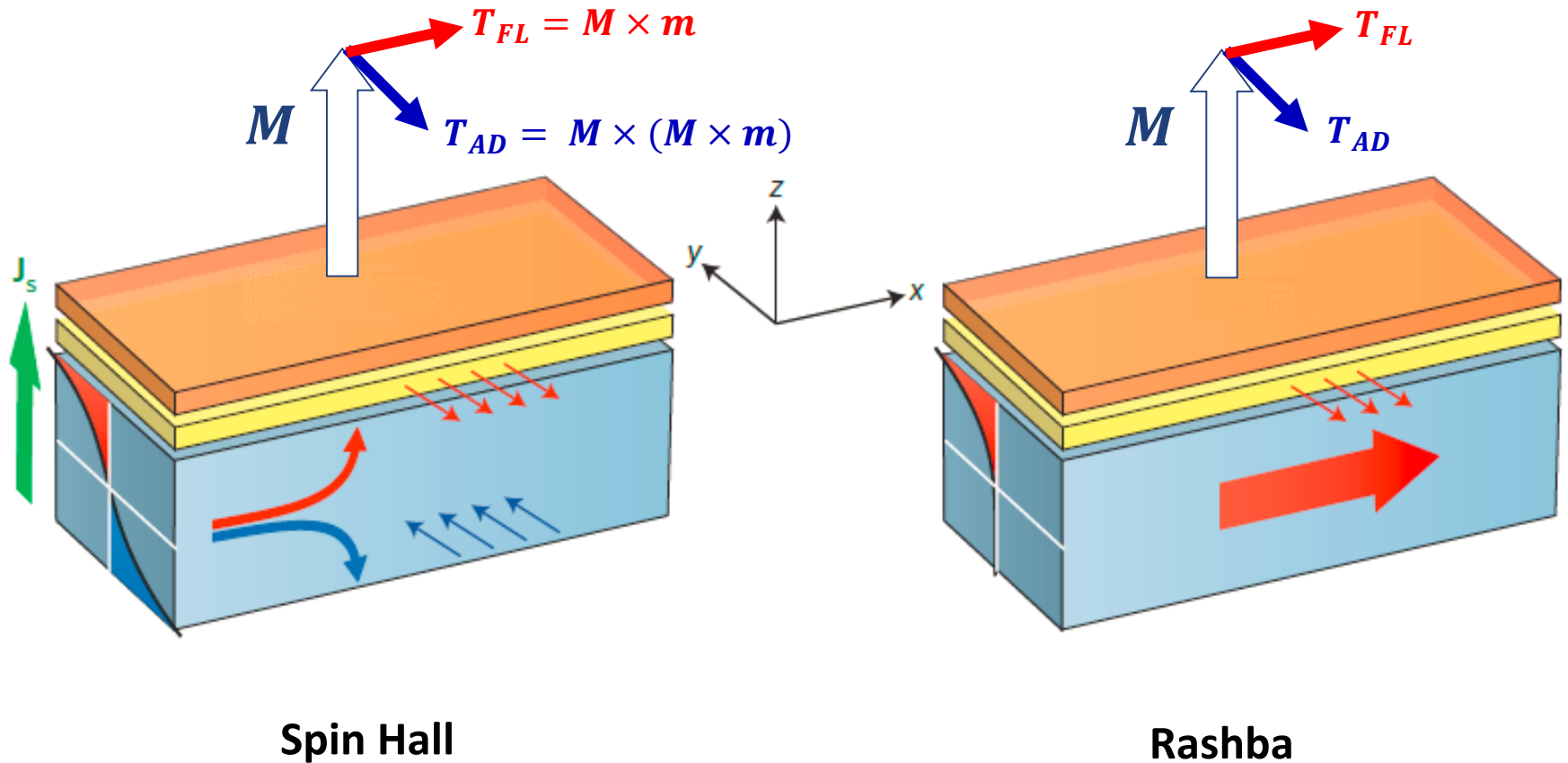


Moras et al.,
PRB 91, 195410 (2015)



QW states of 15 ML-thick Co films on W(110) display both exchange and Rashba splitting





Manchon and Zhang, PRB 2009; Garate and Mac Donald, PRB 2009; Matos-Abiague and Fabian, PRB 2009;
 van der Bijl and Duine, PRB 2012; Haney et al., PRB 2013; Hang Li et al., arXiv:1501.03292, ...

“You like potato and I like pothato,,



$$T_{AD} = \mathbf{M} \times (\mathbf{M} \times \mathbf{m})$$

“Spin Hall torque”

“Spin transfer torque”

“Slonczewski torque”

$$T_{FL} = \mathbf{M} \times \mathbf{m}$$

“Spin orbit torque”

“Spin orbit field”

“Rashba torque”

Antidamping and field-like spin-orbit torques (SOT)

Dilute magnetic semiconductors:

Bernevig and Vafeek, PRB **72**, 033203 (2005)

Yang et al., APL **89**, 132112 (2006)

Chernyshov et al., Nat. Phys. **5**, 656 (2009).

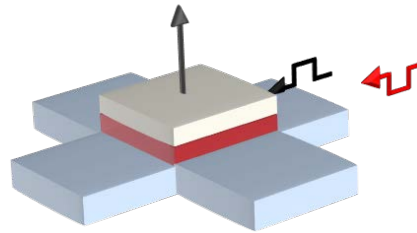
Metal layers:

Manchon and Zhang, Phys. Rev. B **78**, 212405 (2008)

Obata and Tatara, PRB **77**, 214429 (2008)

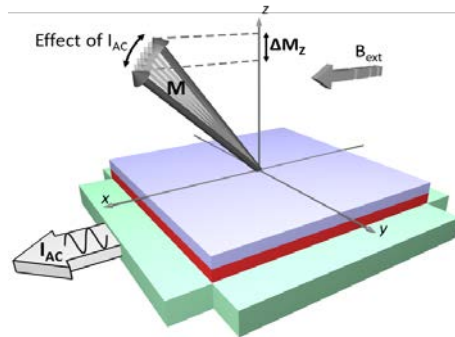
Garate and Mac Donald, PRB **80**, 134403 (2009)

Magnetization switching:



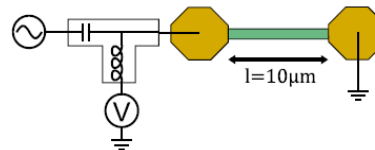
Miron et al.,
Nat. Mater. 2010; Nature 2011

AC Hall voltage and AMR modulation



Pi et al., APL 2010;
Garello et al., Nat. Nanotech. 2013;
Kim et al., Nat. Mater. 2013
...

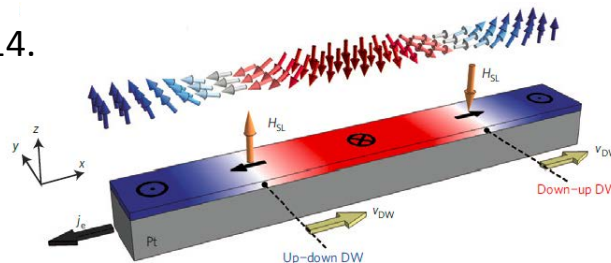
Spin-torque FMR:
(Resonant AC current excitation
AMR readout)



Liu et al., PRL 2011
Fang et al., Nat. Nanotech. 2011

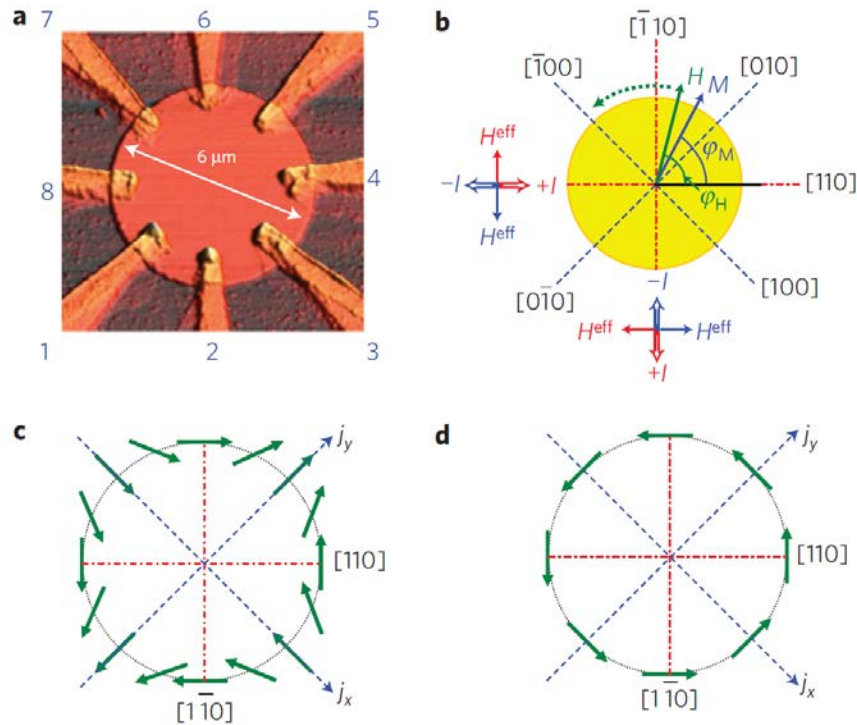
MOKE Fan et al., Nat. Comm. 2014.

Domain wall motion

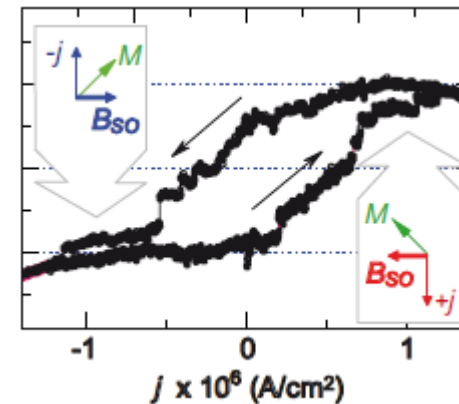


Emori et al., Nat. Mater. 2013
Ryu et al., Nat. Nanotech. 2013
Haazen et al., Nat. Mater. 2013

Ferromagnetic Semiconductor with Zinc-Blende symmetry

Ga_{1-x}Mn_xAs (6 nm)/GaAs(100)

T = 40 K



$$\Omega_D \propto k^3$$

Dresselhaus term

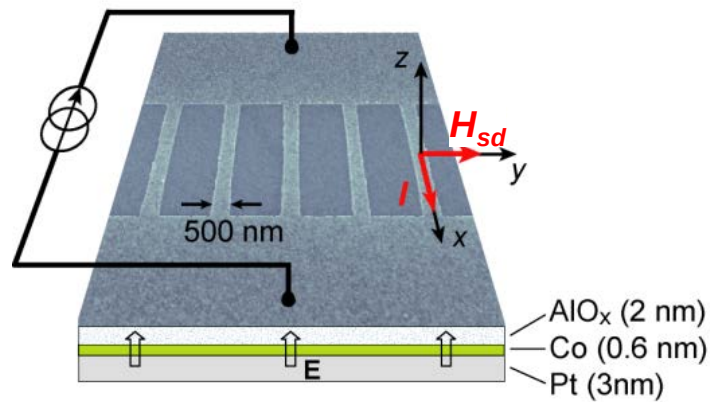
$$\Omega_\varepsilon = C \Delta \varepsilon(k_x, -k_y, 0)$$

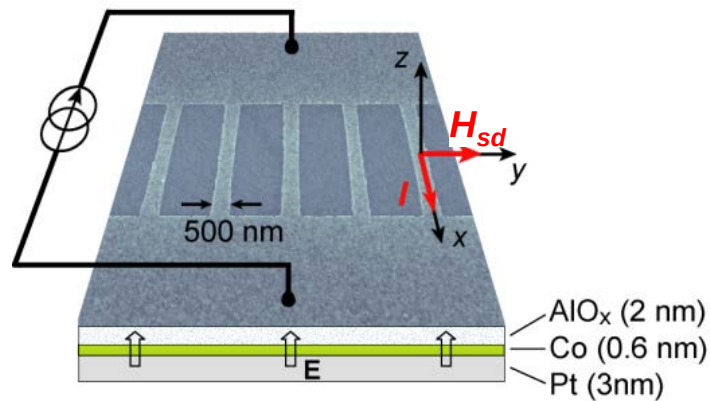
Strain

$$\Omega_R = \alpha_R(-k_y, k_x, 0)$$

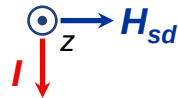
Rashba

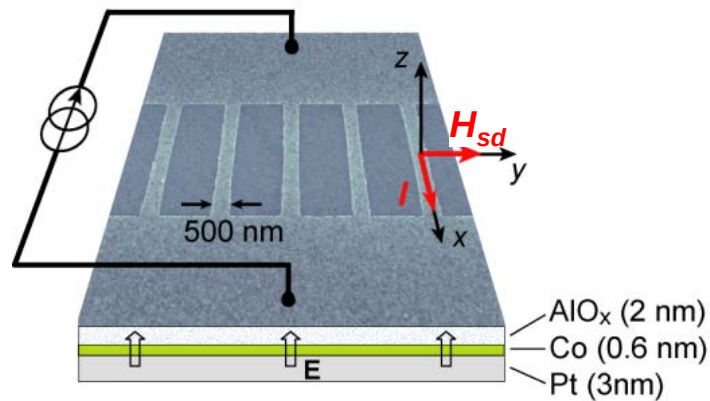
Chernyshov et al., Nature Phys. 5, 656 (2009).





- Pulse amplitude = 7.8×10^7 A/cm²
- Pulse length = 100 ns
- $H_{\text{ext}} = \pm 475$ Oe

 $H_{\text{ext}} = 0$  $H_{\text{ext}} \rightarrow$  $H_{\text{ext}} \leftarrow$



- Pulse amplitude = 7.8×10^7 A/cm²
- Pulse length = 100 ns
- $H_{ext} = \pm 475$ Oe

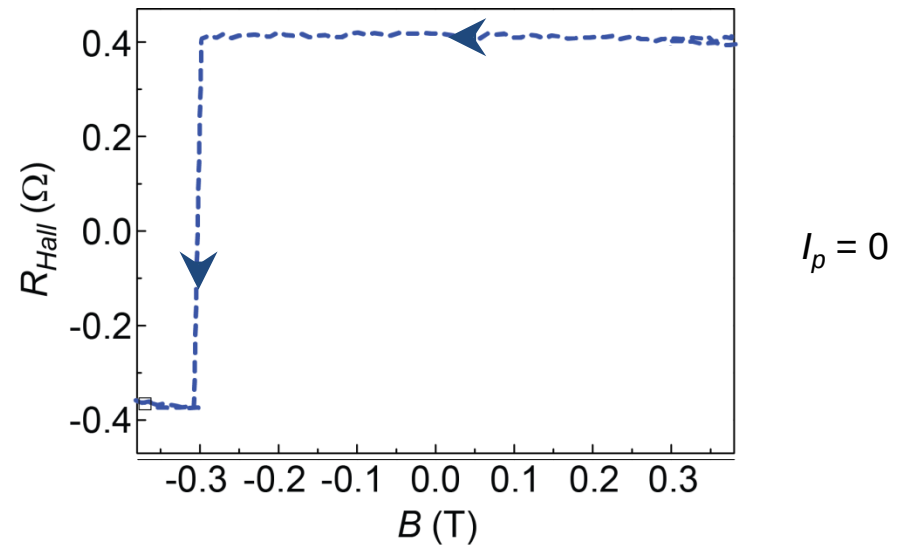
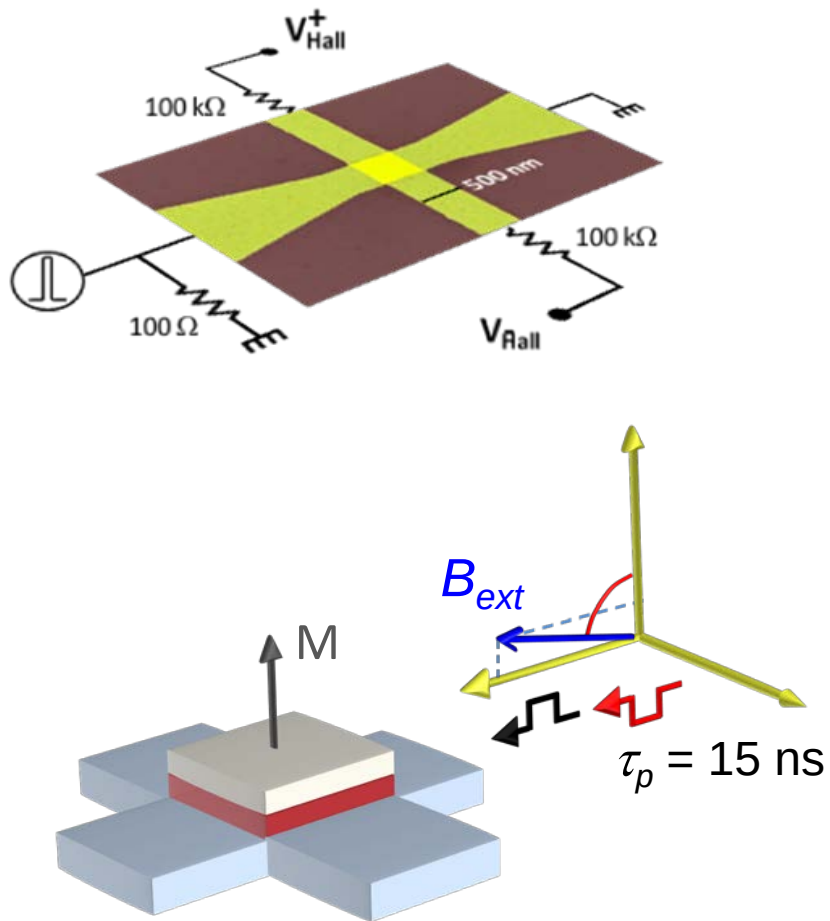
$$\mathbf{B}^\perp \sim \mathbf{y}$$

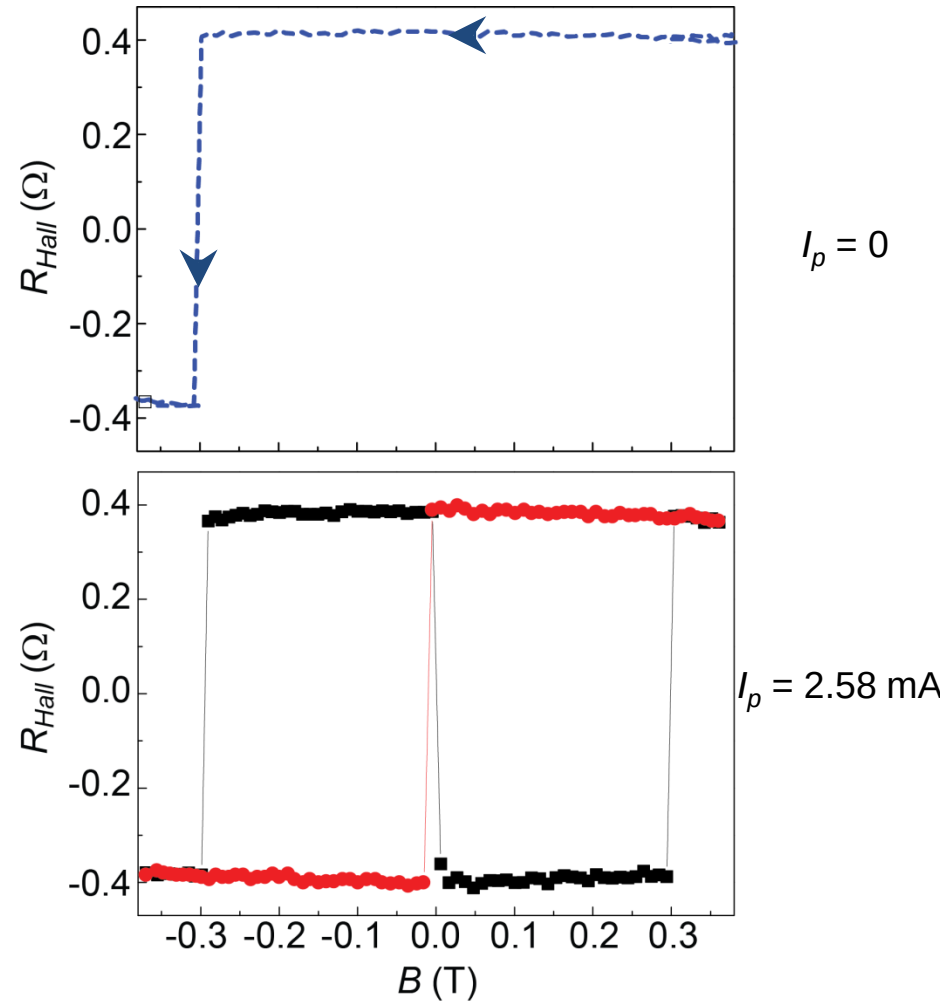
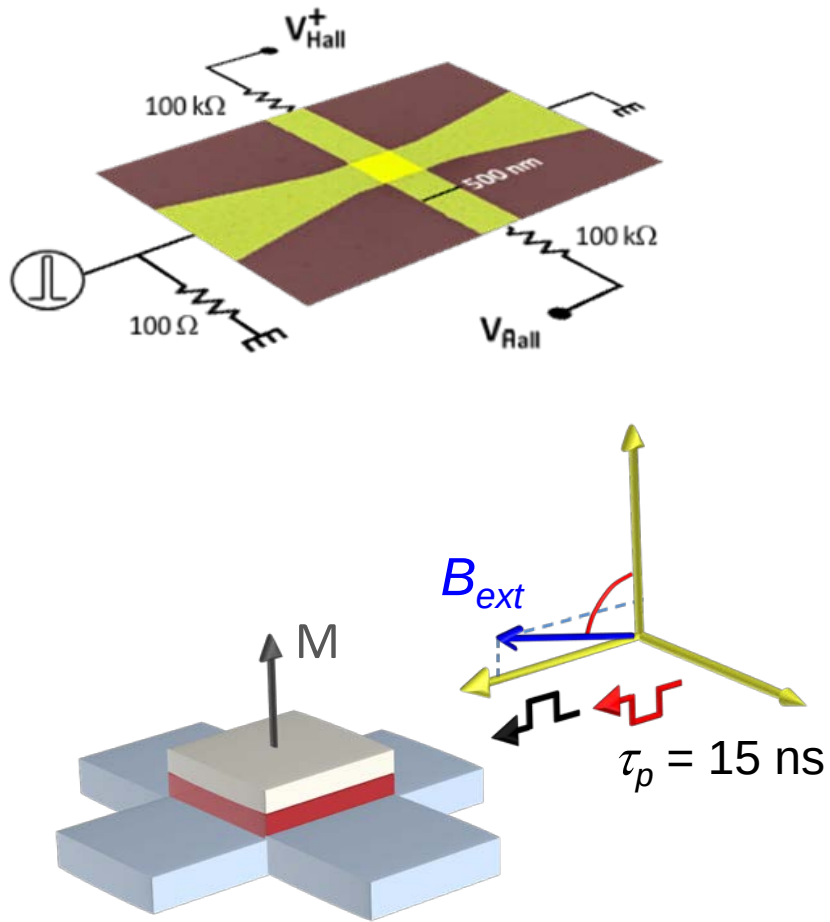
Transverse field

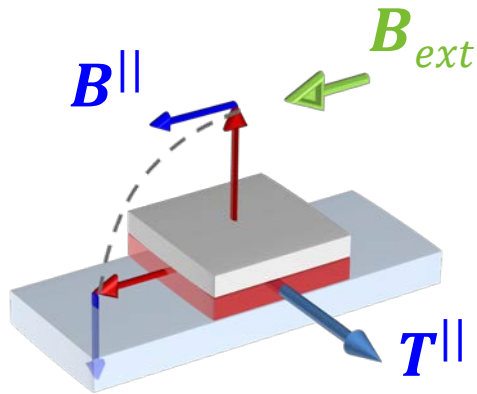


$$\mathbf{T}^\perp \sim (\mathbf{M} \times \mathbf{y})$$

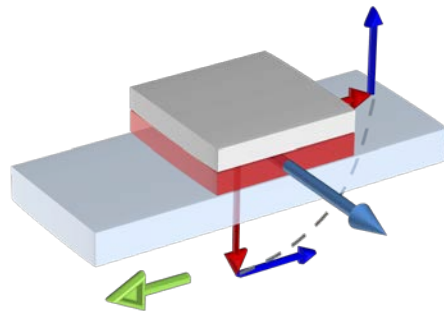
Field-like torque







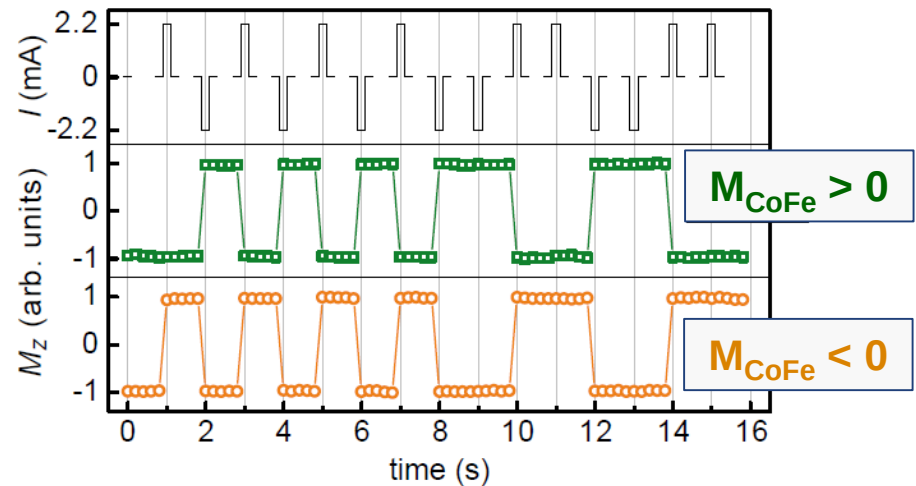
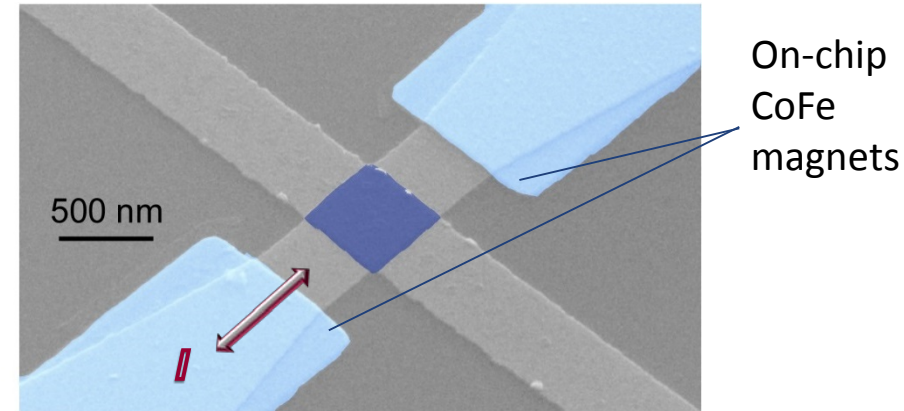
“up” – *unstable*



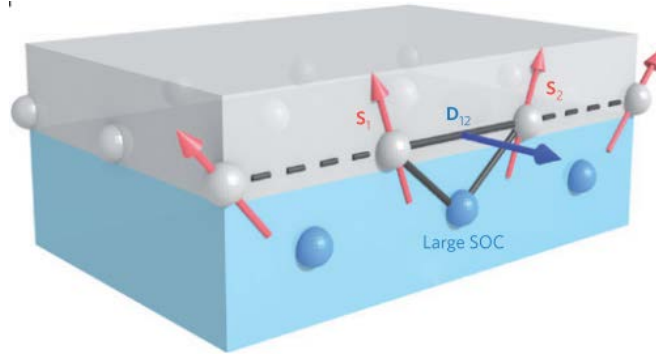
“down” – *stable*

$$B_{\parallel} \sim \mathbf{M} \times \mathbf{y} \quad \text{Longitudinal field}$$

$$T_{\parallel} \sim \mathbf{M} \times (\mathbf{M} \times \mathbf{y}) \quad \text{AD-like torque}$$



Miron et al., *Nature* **476**, 189 (2011)



$$H_{DM} = D_{ij} (\mathbf{S}_i \times \mathbf{S}_j)$$

Infinite stripe: $D < D_c = \sqrt{A/K}$

collinear



Infinite stripe: $D > D_c$

spiral



Finite stripe: $D < D_c$

canted



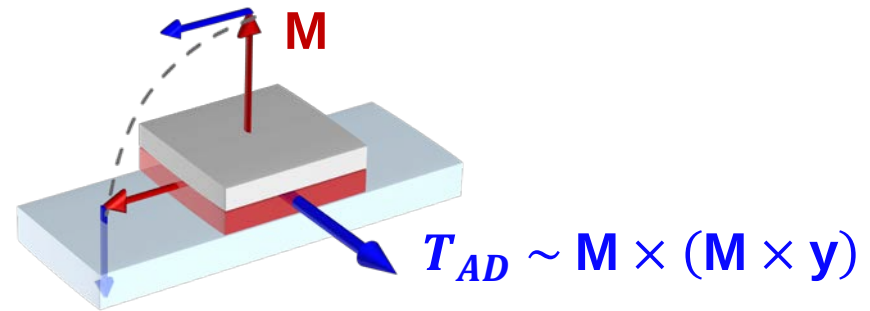
LETTER Miron et al., *Nature* **476**, 189 (2011)

doi:10.1038/nature10309

Perpendicular switching of a single ferromagnetic layer induced by in-plane current injection

“The symmetry of the switching field is consistent with the spin accumulation induced by the Rashba interaction, as well as with the torque induced by the spin Hall effect in the Pt layer”

“...The switching efficiency increases with the oxidation of the Al layer, suggesting that the Rashba interaction has a key role in the reversal mechanism.”



Equivalent spin Hall angle:

$$\theta_{SH}^{eff} = 0.16$$

PRL **109**, 096602 (2012)

PHYSICAL REVIEW LETTERS

week ending
31 AUGUST 2012

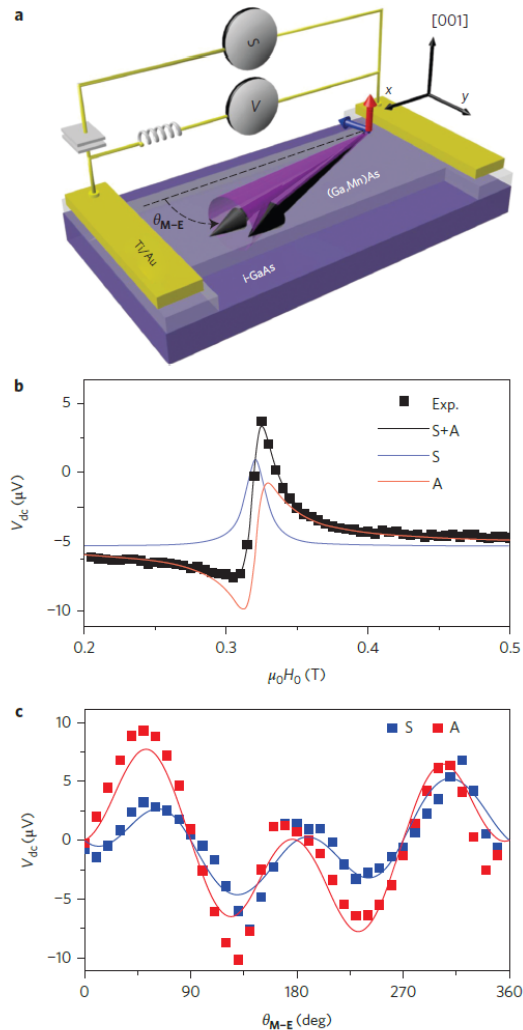
Current-Induced Switching of Perpendicularly Magnetized Magnetic Layers Using Spin Torque from the Spin Hall Effect

Luqiao Liu,¹ O.J. Lee,¹ T.J. Gudmundsen,¹ D.C. Ralph,^{1,2} and R. A. Buhrman¹

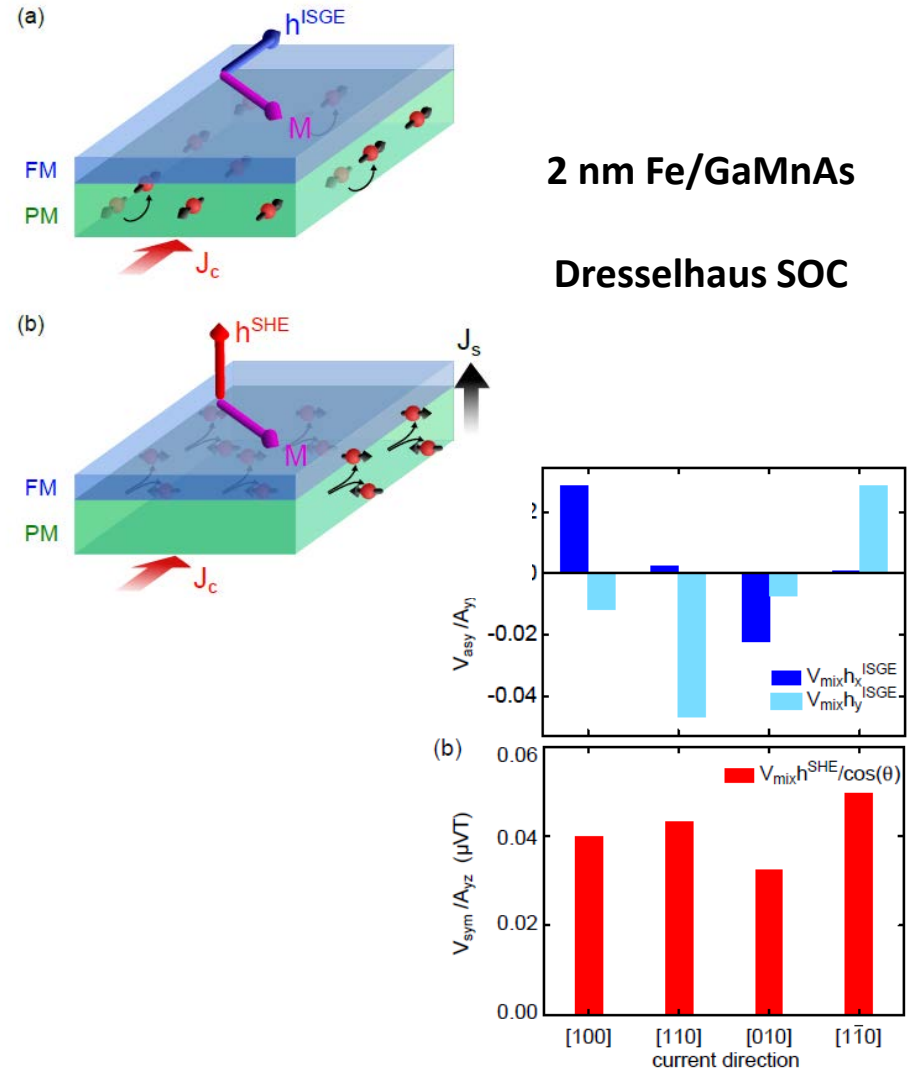
Same system: Pt(2nm)/Co(0.6nm)/AlOx(2nm)

Conclusion: pure “bulk” spin Hall effect; no observation of field-like torque

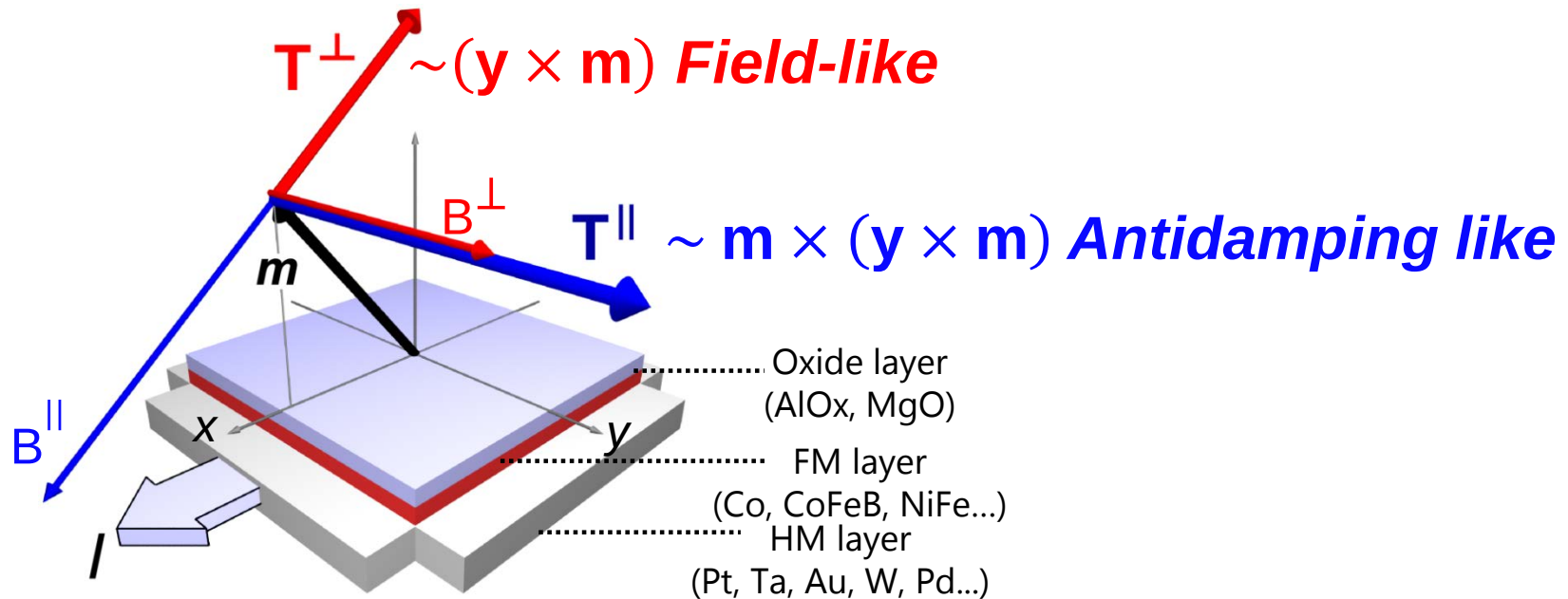
Single layer GaMnAs



Kurebayashi et al., Nat. Nanotech. 9, 211 (2014)



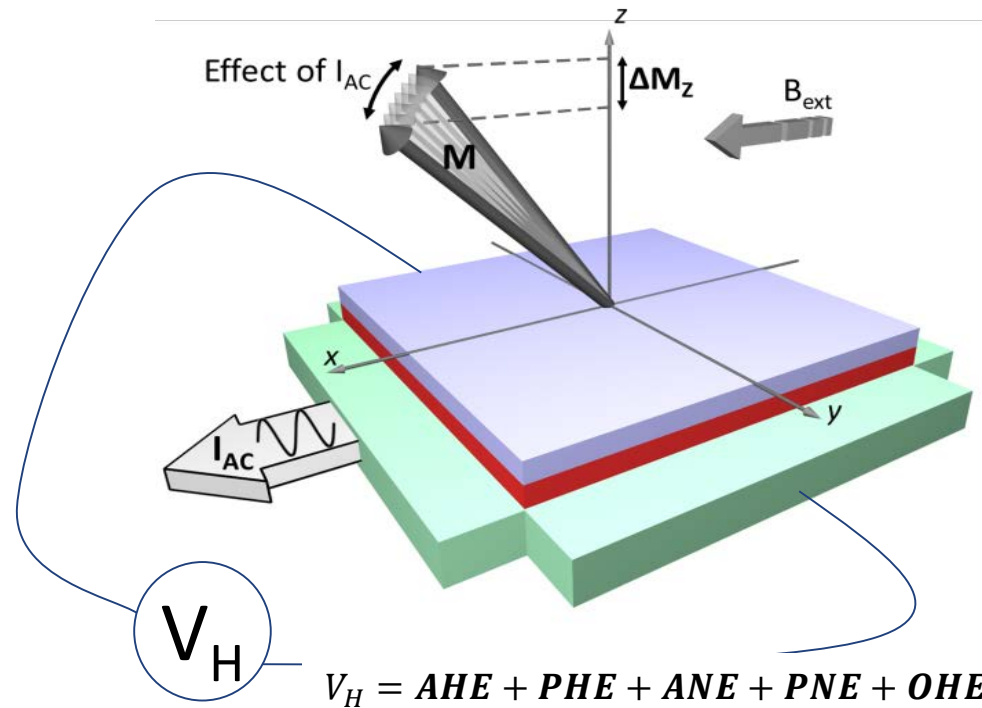
Skinner et al., Nat. Comm. 6, 6730 (2015)



A linear response analysis of the spin accumulation to an E -field compatible with the symmetry of the trilayer leads to additional torque terms, depending on the magnetization orientation:

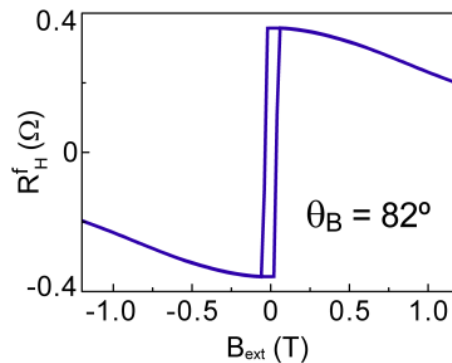
$$\mathbf{T}^{\perp} = (\mathbf{y} \times \mathbf{m}) [T_0^{\perp} + T_2^{\perp} (\mathbf{z} \times \mathbf{m})^2 + T_4^{\perp} (\mathbf{z} \times \mathbf{m})^4] + \mathbf{m} \times (\mathbf{z} \times \mathbf{m}) (\mathbf{m} \cdot \mathbf{x}) [T_2^{\perp} + T_4^{\perp} (\mathbf{z} \times \mathbf{m})^2]$$

$$\mathbf{T}^{\parallel} = \mathbf{m} \times (\mathbf{y} \times \mathbf{m}) T_0^{\parallel} + (\mathbf{z} \times \mathbf{m}) (\mathbf{m} \cdot \mathbf{x}) [T_2^{\parallel} + T_4^{\parallel} (\mathbf{z} \times \mathbf{m})^2]$$



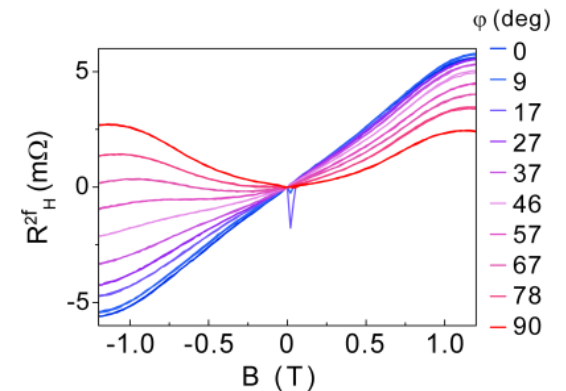
1st harmonic
Hall resistance

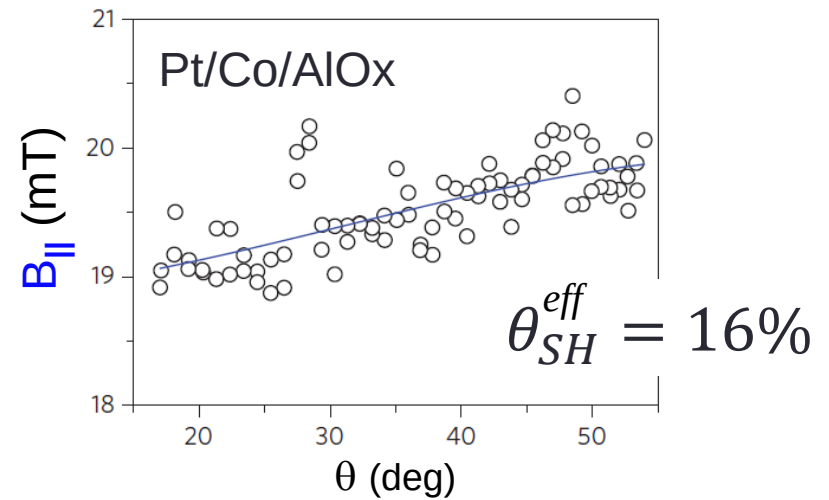
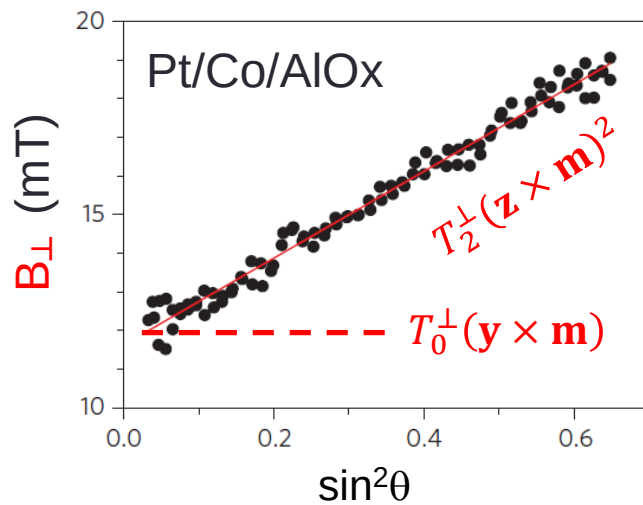
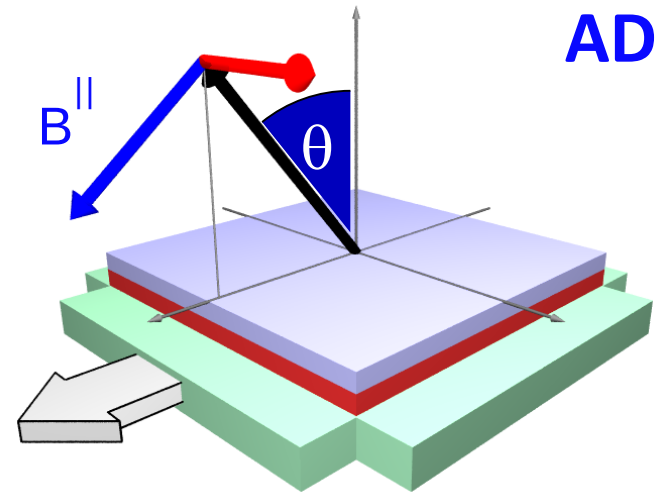
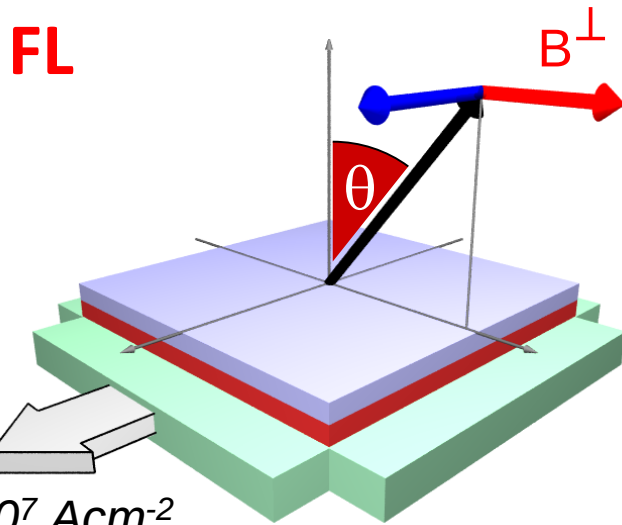
M vs B_{ext}

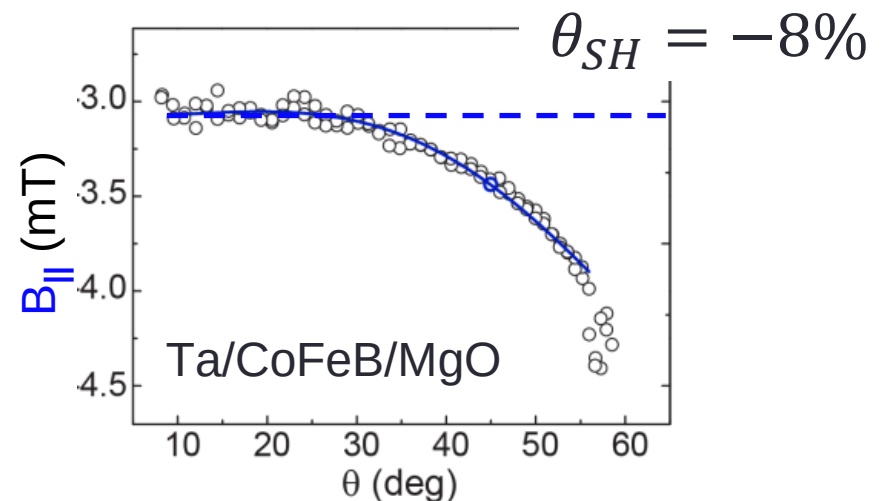
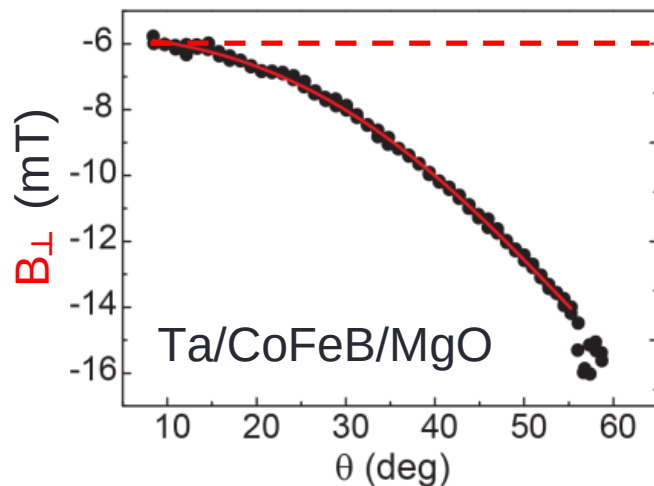
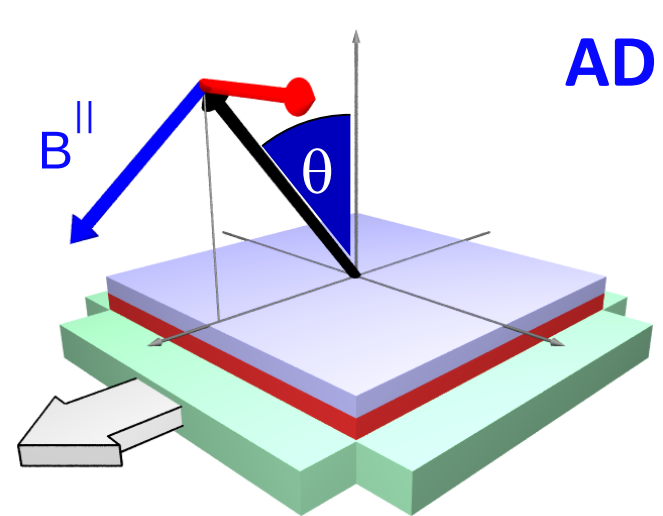
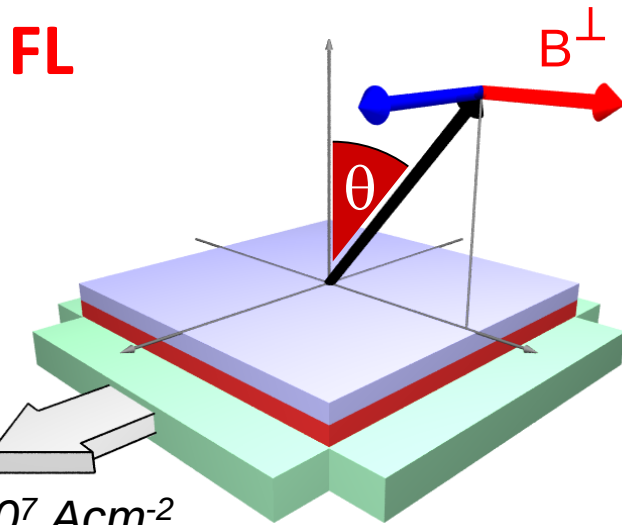


2nd harmonic
Hall resistance

M vs I_{ac}

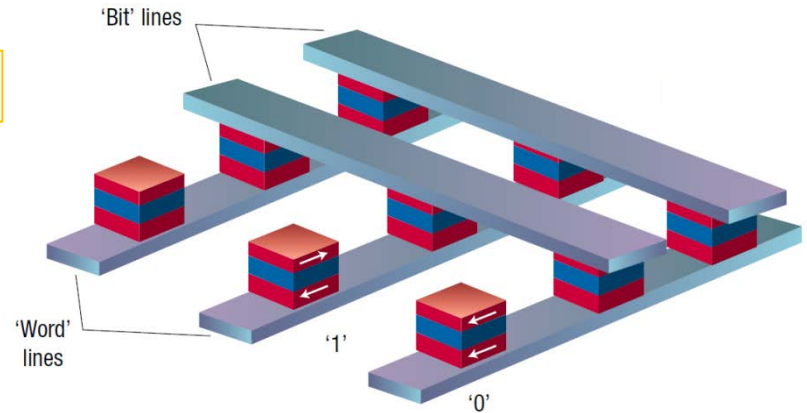




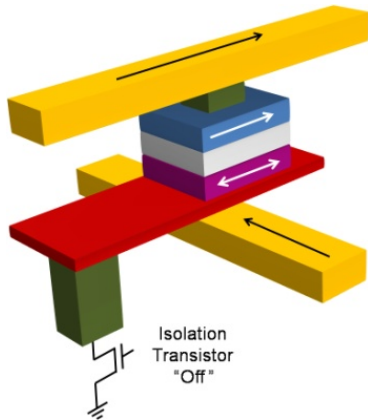


“universal memory”: rapid / dense / non-volatile

- Reading – TMR
- Writing:

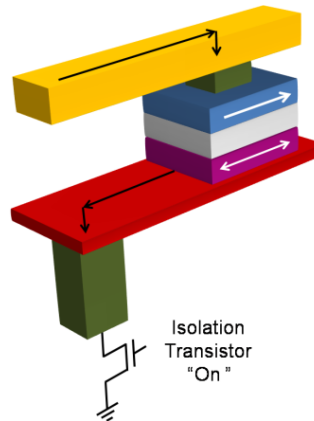


magnetic field



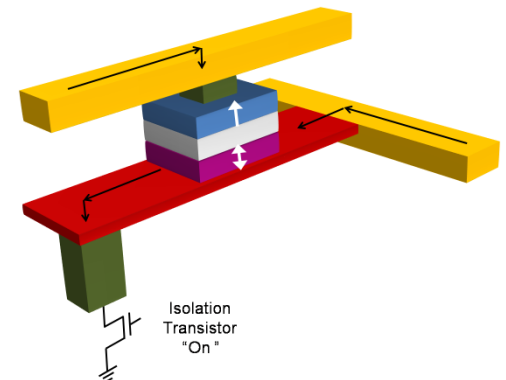
+ high endurance
— limited scalability

spin transfer (STT)



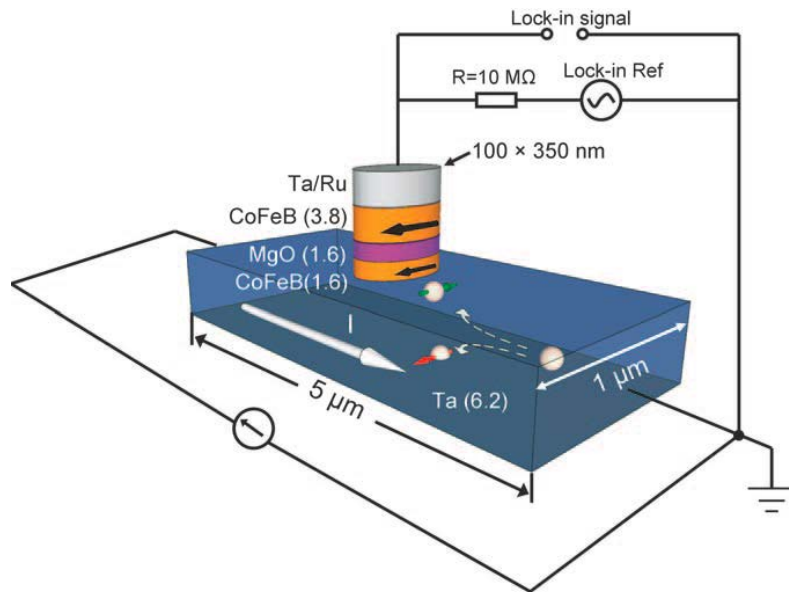
— limited endurance
+ high scalability

spin-orbit torque (SOT)



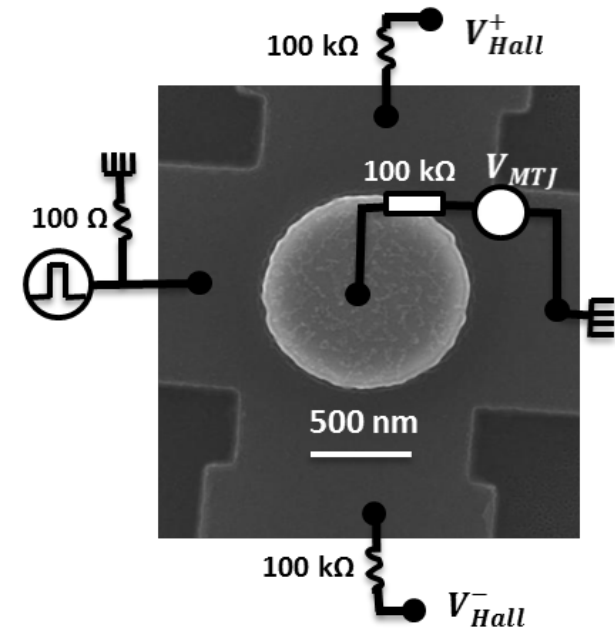
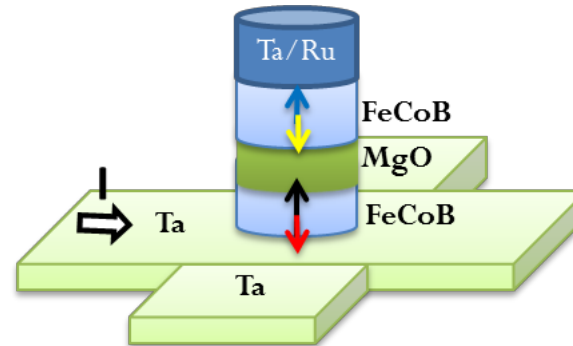
+ high endurance
+ high scalability

In-plane MTJ



Liu et al., Science **336**, 555 (2012)

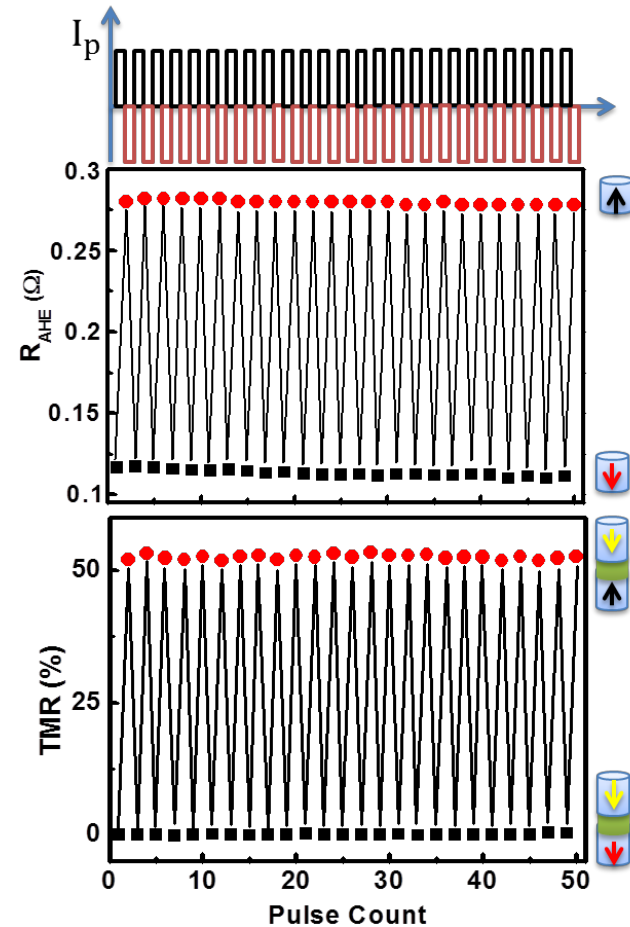
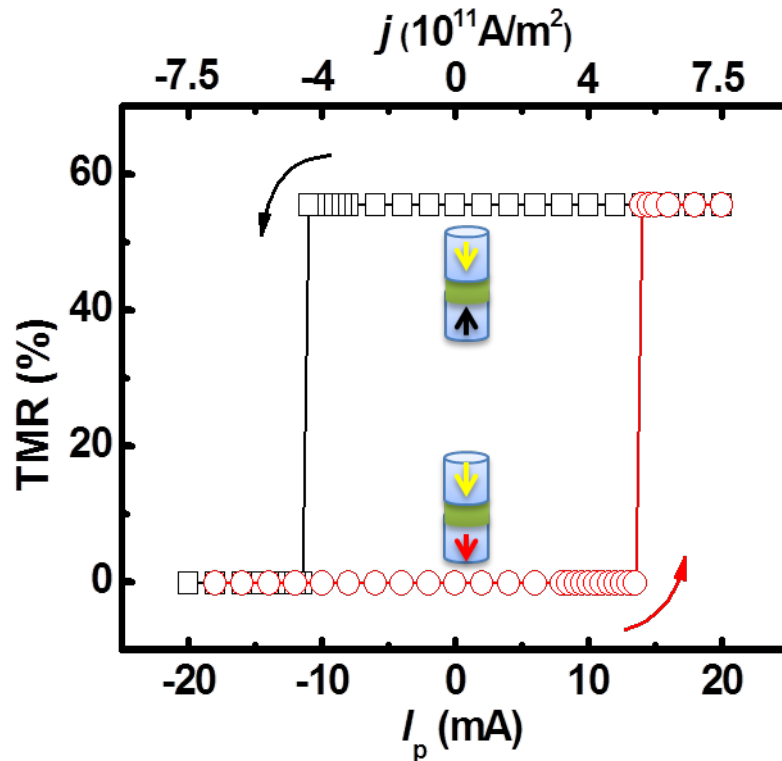
Perpendicular - MTJ



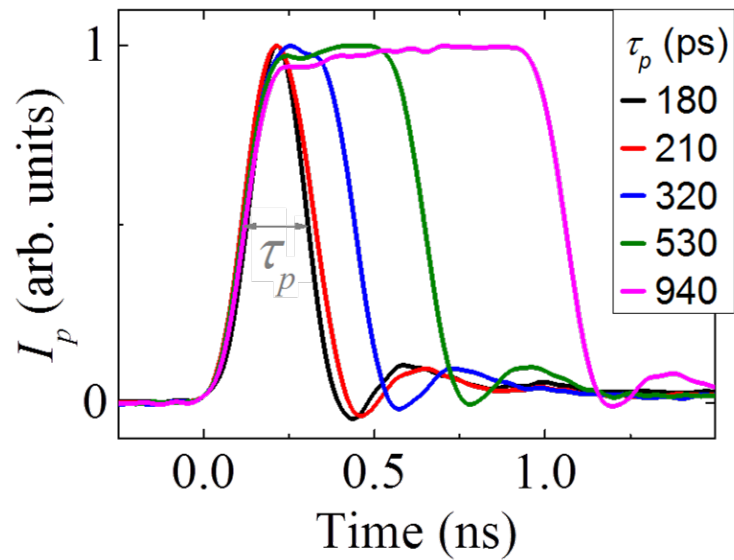
Cubukcu et al., APL **104**, 042406 (2014)

CURRENT DEPENDENCE

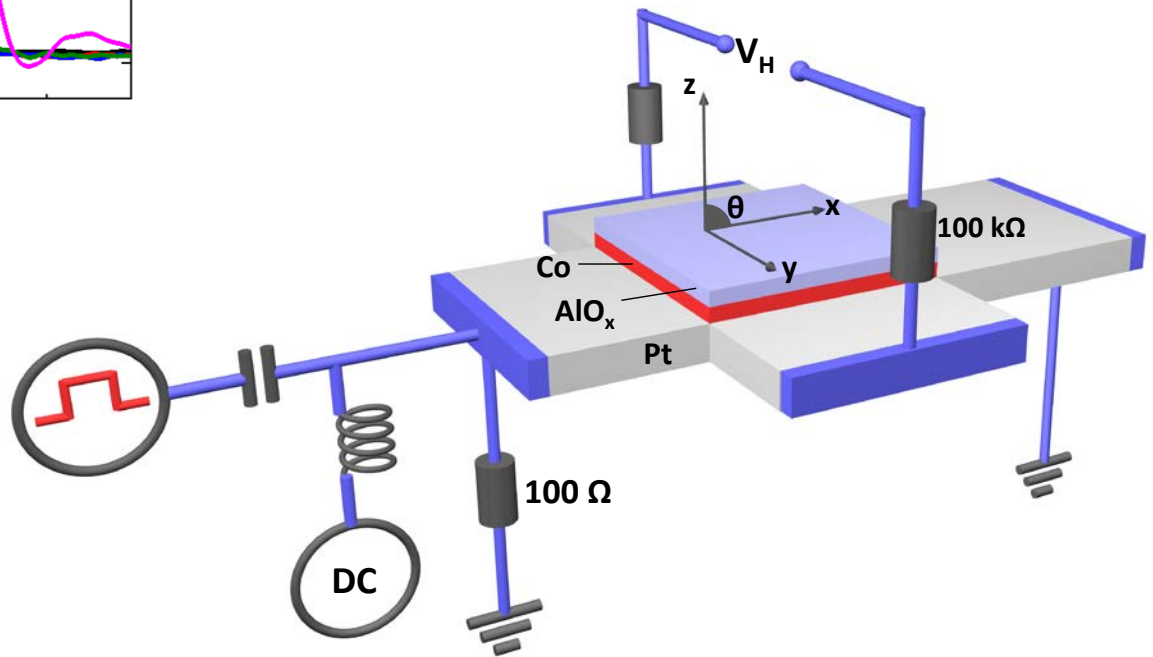
$$B_{\text{ext}} = 400 \text{ Oe}$$

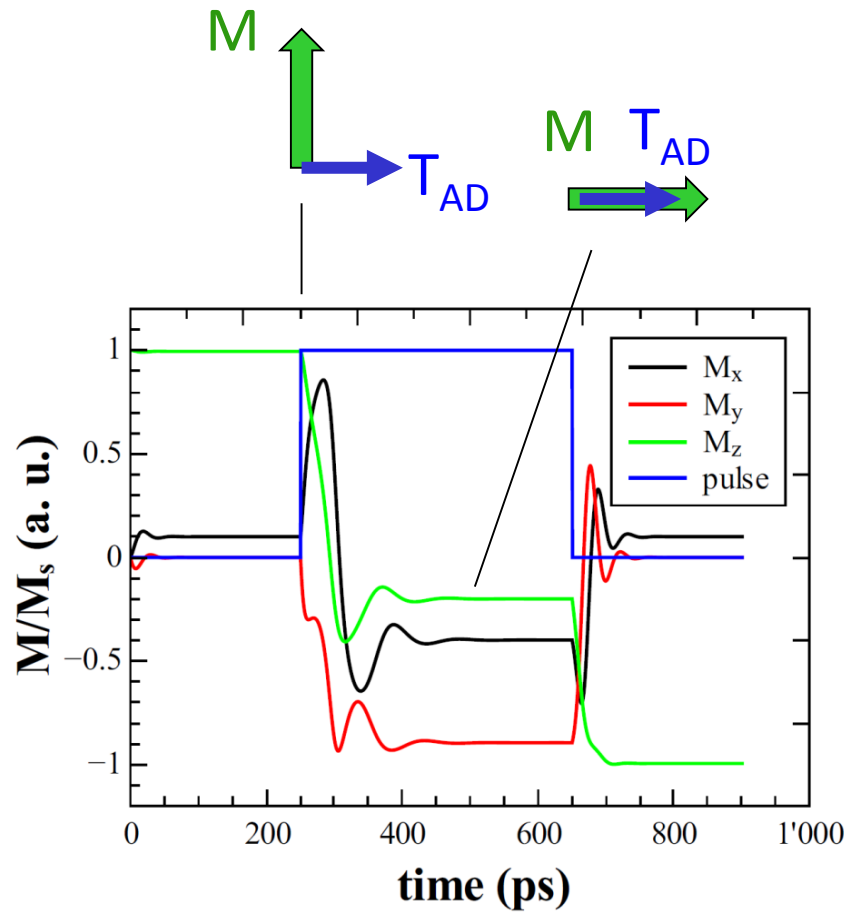


- Ta(20)/Fe₆₀Co₂₀B₂₀(1)/MgO/Fe₆₀Co₂₀B₂₀(1.5)/Ta(5)/Ru(7) annealed 1h at 240C
- TMR: 55%, RA = 1.15 k $\Omega \cdot \mu\text{m}^2$

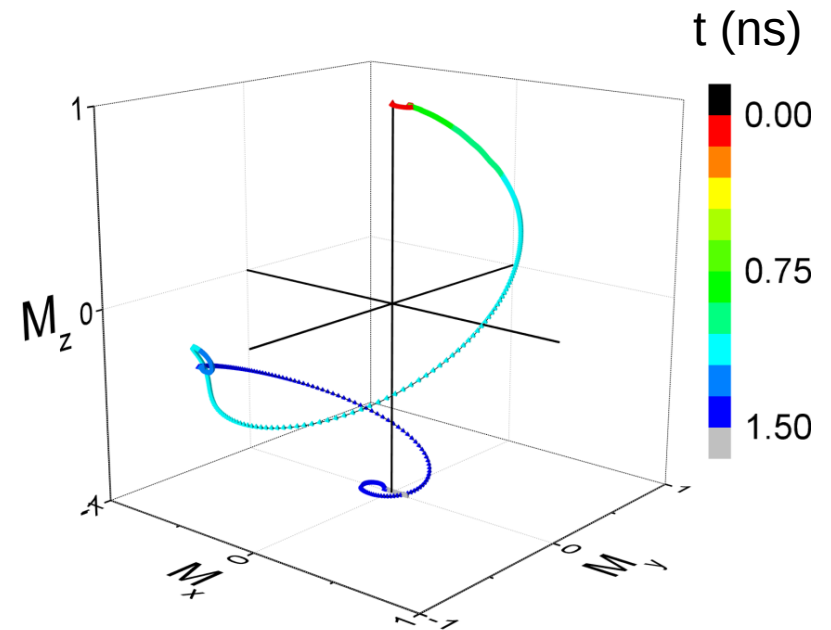


Pulser
(0.2 ns – 10 ms)





$$T_{AD} \sim 50 \text{ mT}/10^8 \text{ Acm}^{-2}$$

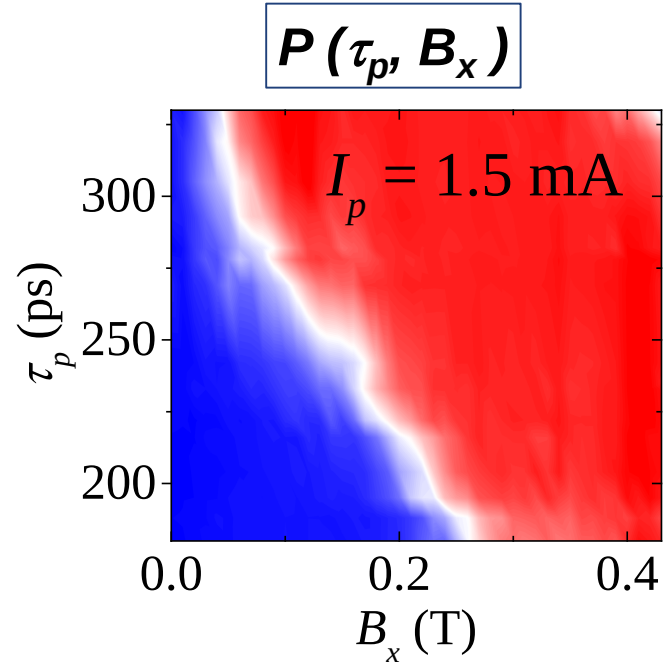
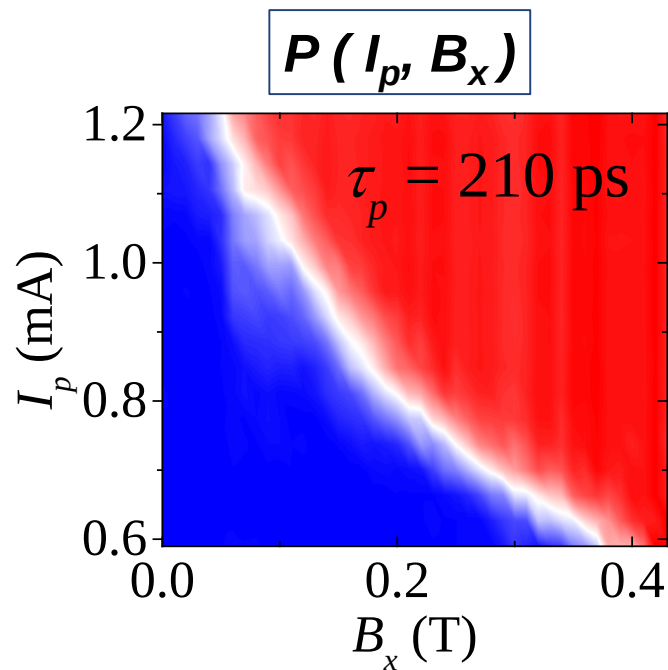
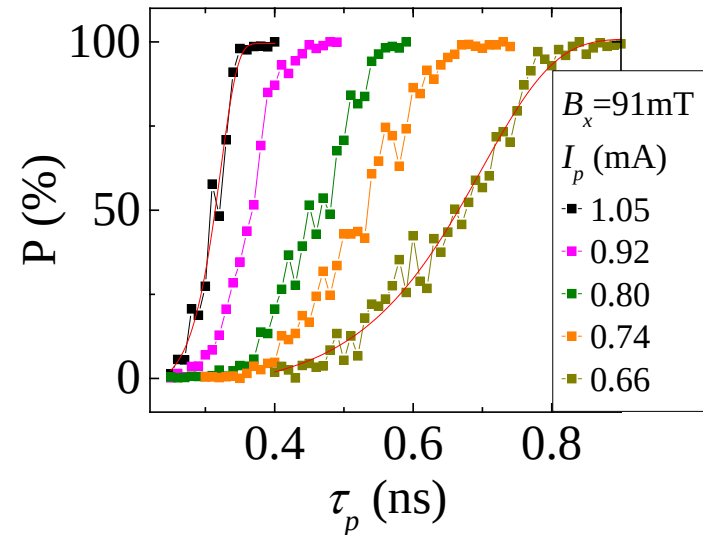
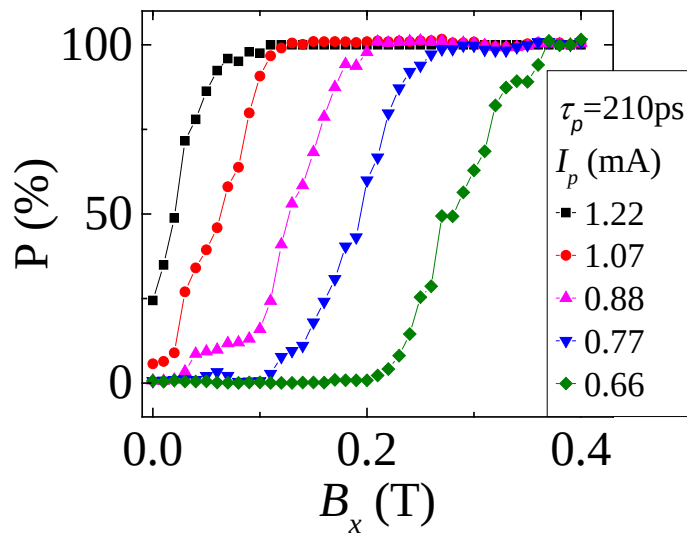


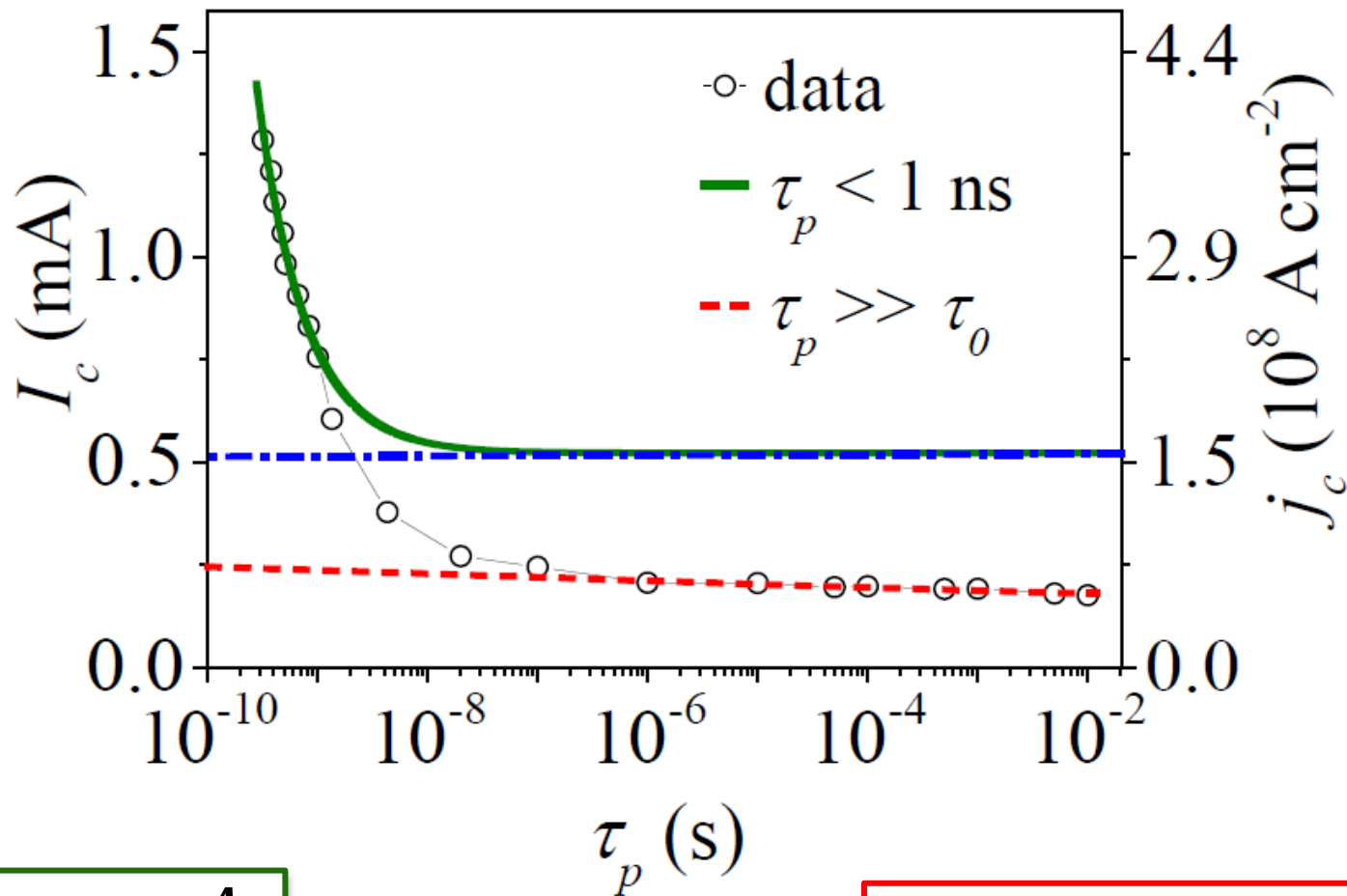
$$\alpha = 0.5$$

$$B_k = 1 \text{ T}$$

$$B_{\text{ext}} = 0.1 \text{ T}$$

$$J_p = 8 \cdot 10^8 \text{ Acm}^{-2}$$



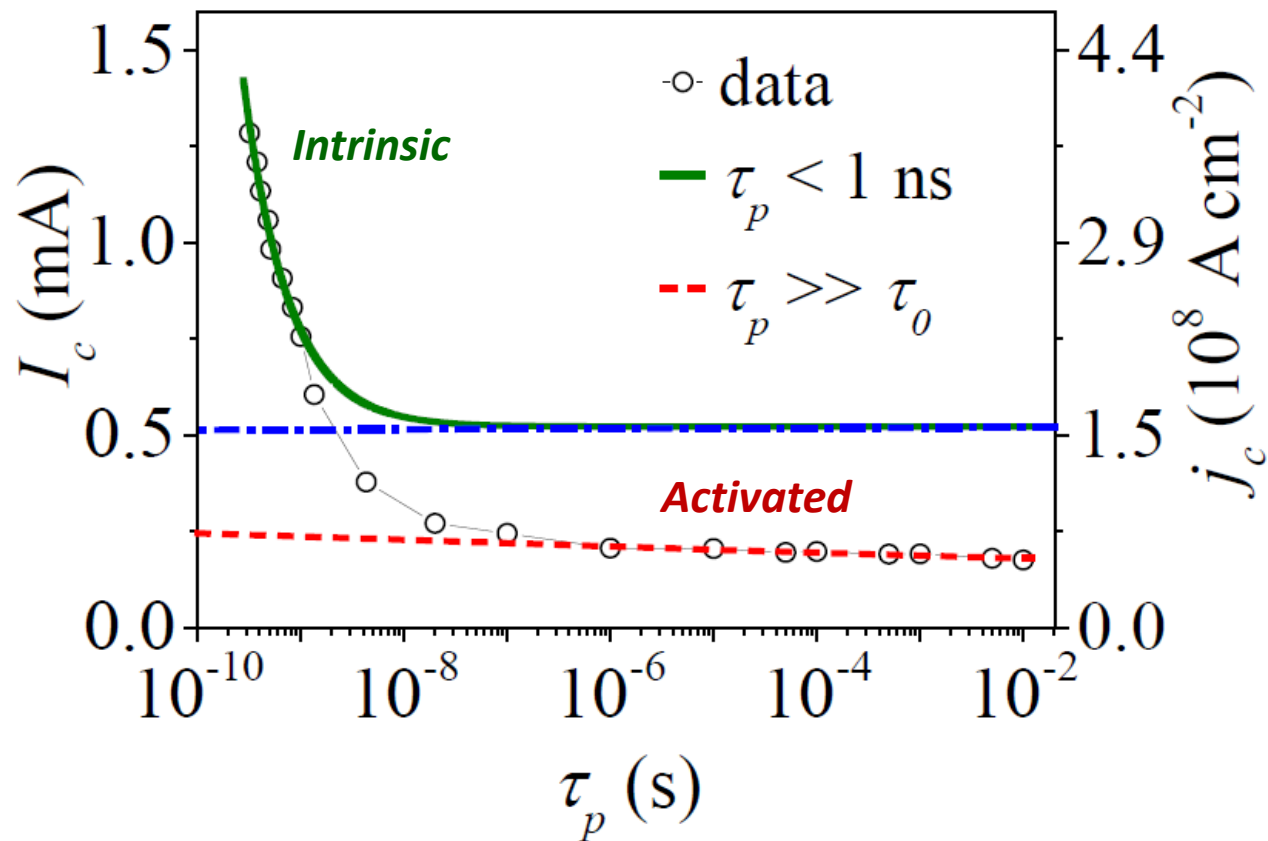


$$I_c = I_{c0} + \frac{A}{\tau_p}$$

intrinsic regime

$$I_c = I_{c0} \left(1 - \frac{k_b T}{E} \ln \tau_p / \tau_0 \right)$$

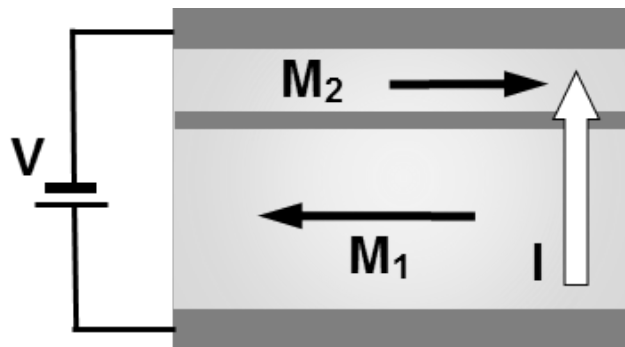
activated regime



- $\tau_p < 1 \text{ ns}$: Intrinsic short-time regime
- $\tau_p > 1 \text{ ns}$: Thermally activated
- Switching down to 180 ps
- Nonprecessional
- Incubation time ≈ 0

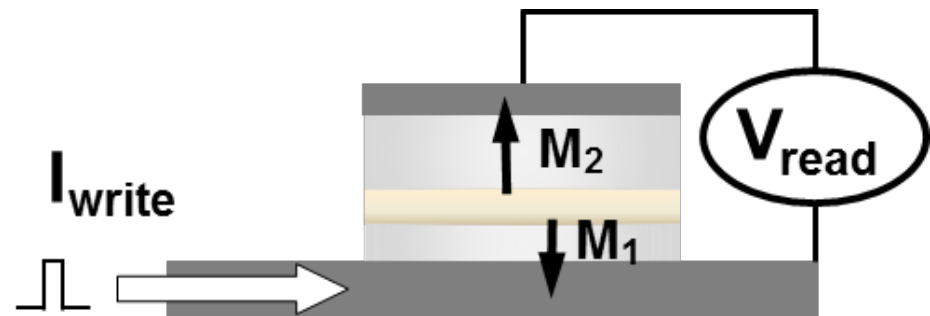
STT - MTJ

- ST by spin filtering
- Torque $\sim J_s = J \cdot \text{Polarization}$
- $J = I / \text{Transverse Area}$
- Incubation time $\sim 50 \text{ ps} + \text{jitter}$



SOT - MTJ

- ST by spin-orbit coupling
- Torque $\sim J_s = J \cdot \Theta_{\text{SH}}$
- $J = I / \text{Longitudinal Area}$
- No incubation time

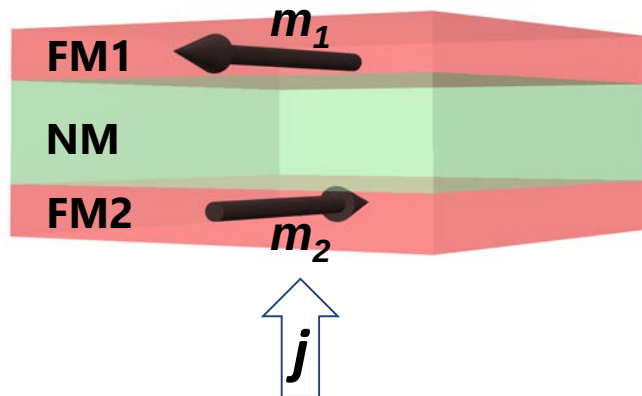


$$I_{c0}^{\text{SOT}} / I_{c0}^{\text{STT}} = \frac{1}{2\alpha} \frac{\eta}{\theta_{\text{SH}}^{\text{eff}}} \frac{t_{\text{FM}} + t_{\text{HM}}}{w}$$

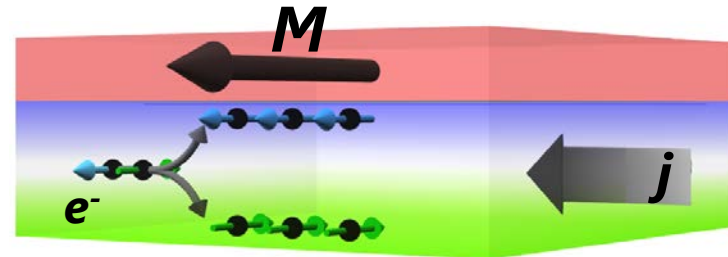
Spin transfer and spin-orbit coupling can be used to

- Generate spins. Spin injection
- Transport spins from the source
- Manipulate spins/macroscale
- Detect spins

STT and GMR



STT and USMR



Avci et al., Nat. Phys. 2015

Spin transfer and spin-orbit torques can be combined in devices

- ❑ Spin-orbit torques are very efficient to manipulate the magnetization of nanoscale magnets: Switching, spin waves, DW motion
- ❑ New type of devices are possible: 3-terminal MTJ, MW oscillators, logic gates
- ❑ Materials compatible with CMOS processing
- ❑ High coercivity, radiation hard magnetic bits
- ❑ MTJ stacks: 120-180 % TMR, 2-200 $\Omega \mu\text{m}^2$ RA
- ❑ Ultrafast switching (<200 ps), deterministic, bipolar

To do:

- ❑ Material optimization to obtain a larger SOT/current ratio and/or lower resistivity of write line.
- ❑ Scaling of MTJ devices below 40 nm
- ❑ Integrate in-plane bias field in MTJ stack or design structures that do not need a bias field
- ❑ And more...

Acknowledgments



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Mihai Miron

Olivier Boulle

Murat Cubucku

Marc Drouard

Stephane Auffret

Gilles Gaudin

Frank Freimuth

Yuriy Mokrousov

Stefan Blügel

S. Tibus

J. Langer

