



Real-time Optimization for Power Distribution Systems

Adrian Hauswirth

Agenda

Introduction

Facts and terminology everyone should know about

Tutorial in control & optimization

Transmission system operations

Active distribution grids

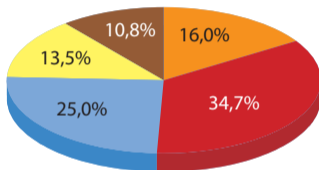
Research: combining control and optimization in a novel way

Conclusion

Electric Energy Supply

Swiss energy consumption by carrier (2015)

- Fossil fuels
- Gasoline
- Electricity
- Natural Gas
- Others

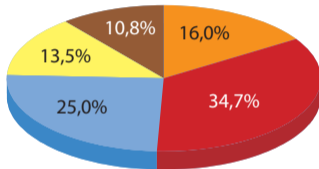


[BFE, Schweizerische Gesamtenergiestatistik 2015]

Electric Energy Supply

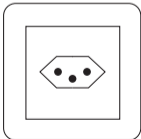
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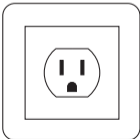


[BFE, Schweizerische Gesamtenergiestatistik 2015]

230V ~ 50Hz



120V ~ 60Hz



Power consumption

$$P(t) = V(t)I(t)$$

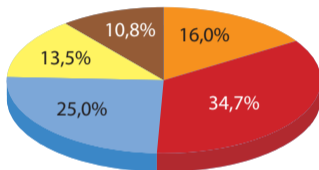
Electric energy consumption

$$E = \int_{t_0}^{t_1} P(t)dt$$

Electric Energy Supply

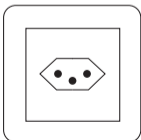
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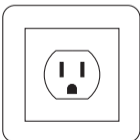


[BFE, Schweizerische Gesamtenergiestatistik 2015]

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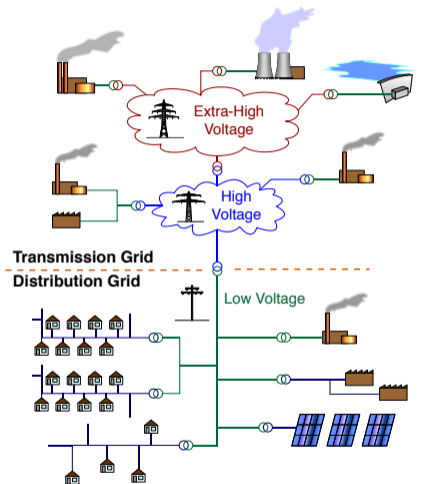


Power consumption

$$P(t) = V(t)I(t)$$

Electric energy consumption

$$E = \int_{t_0}^{t_1} P(t)dt$$



[Wikipedia, MBizon, 2010]

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Fact 1:**Capacity \neq Flexibility****signs of inflexibility:**

- price volatility, negative market prices
- significant renewable energy curtailment
- balancing violations, frequency excursions, etc.

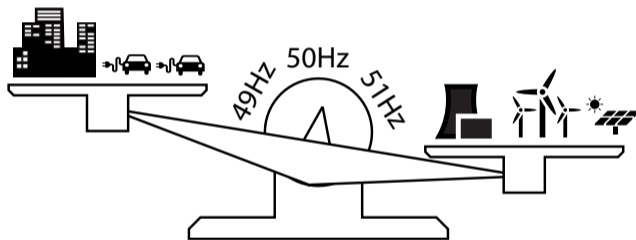
increasing flexibility:

- interconnected systems
- fast generators, flexible loads, storage
- market design, communication infrastructure

Assumption 1

Enough capacity & flexibility such that demand can be met at all times.

[NREL, "Flexibility in 21st Century Power Systems," 2014]

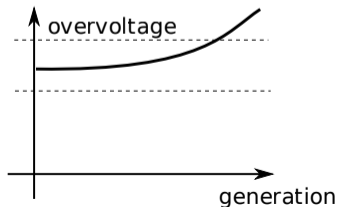
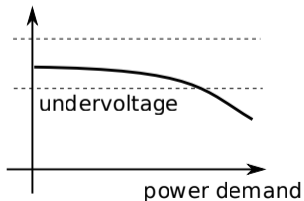
Fact 2:**supply \neq demand \rightarrow frequency deviation****Assumption 2**

The power system is stabilized and operates in steady-state, i.e., at 50Hz.

Terminology

congestion → **cascading line failures**
(overloaded transmission lines)

under-/overvoltage → **voltage collapse**



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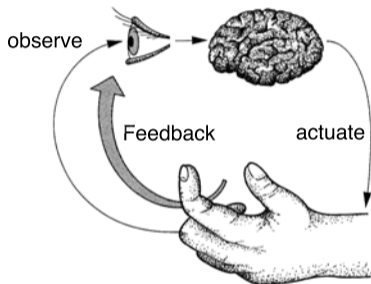
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Primer in Control Engineering

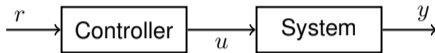


[Longchamp, 1995]

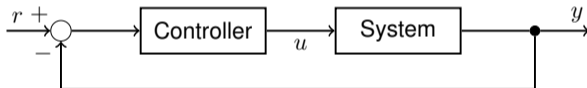
Feedback control can achieve:

- **no steady-state error**, i.e., $r(t) = y(t)$ for $t \rightarrow \infty$
- **stability**: output y remains bounded (for bounded input r)
- **robustness**: reduce influence of model uncertainties

open-loop system (feedforward control):



closed-loop system (feedback control):



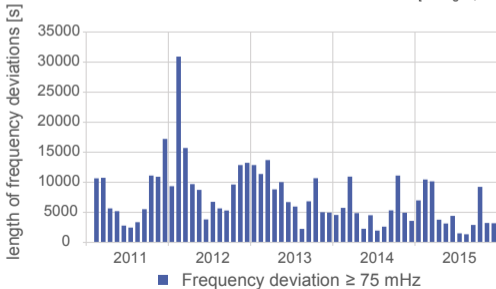
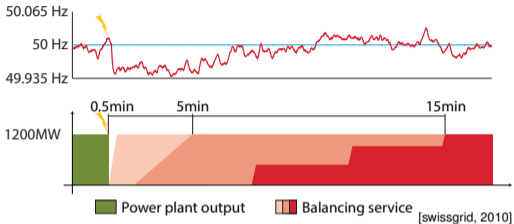
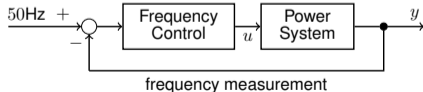
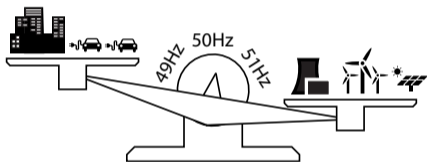
r reference value

u control signal

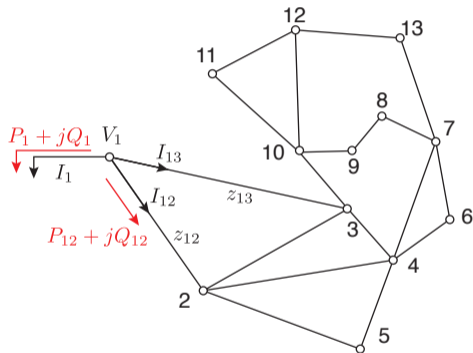
y output signal

Example: Frequency Control in Power Systems

supply \neq demand \rightarrow freq deviation



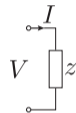
Steady-state AC power flow model



V_k nodal voltage
 I_k current injection
 P_k, Q_k power injections

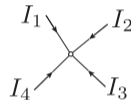
z_{kl} line impedance
 I_{kl} line current
 P_{kl}, Q_{kl} power flow

Ohm's Law



$$V = zI$$

Current Law



$$0 = I_1 + \dots + I_k$$

AC power

$$S = P + jQ = VI^*$$

AC power flow equations

$$S_k = \sum_{l \in N(k)} \frac{1}{z_{kl}} V_k (V_k^* - V_l^*) \quad \forall k \in \mathcal{N}$$

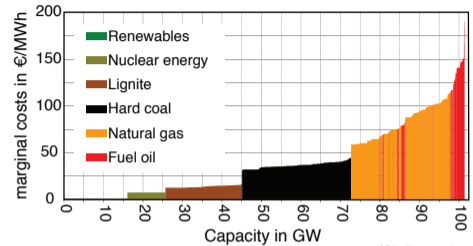
(all variables and parameters are \mathbb{C} -valued)

Power system optimization

minimize $\phi(x)$

subject to $x \in \mathcal{X}$

$\phi : \mathbb{R}^n \rightarrow \mathbb{R}$ objective function
 $\mathcal{X} \subset \mathbb{R}^n$ constraint set

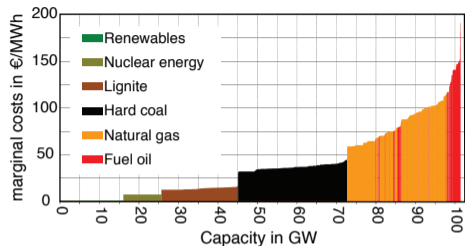


[Cludius et al., 2014]

Power system optimization

$$\begin{aligned} & \text{minimize} && \phi(x) \\ & \text{subject to} && x \in \mathcal{X} \end{aligned}$$

$\phi : \mathbb{R}^n \rightarrow \mathbb{R}$ objective function
 $\mathcal{X} \subset \mathbb{R}^n$ constraint set



[Cludius et al., 2014]

(simple) Optimal Power Flow (OPF) problem

- minimize cost of generation
- respect generation capacity
- satisfy AC power flow laws
- no over-/under-voltage
- no congestion

$$\begin{aligned} & \text{minimize} && \sum_{k \in \mathcal{N}} \text{cost}_k(P_k^G) \\ & \text{subject to} && P^G + jQ^G = P^L + jQ^L + \text{diag}(V)Y^*V^* \\ & && \underline{p}_k \leq P_k^G \leq \bar{p}_k, \quad \underline{q}_k \leq Q_k^G \leq \bar{q}_k && \forall k \in \mathcal{N} \\ & && \underline{v}_k \leq V_k \leq \bar{v}_k && \forall k \in \mathcal{N} \\ & && |P_{kl} + jQ_{kl}| \leq \bar{s}_{kl} && \forall \{k, l\} \in \mathcal{E} \end{aligned}$$

Y admittance matrix, P_k^G, Q_k^G power generation, P_k^L, Q_k^L load, $\{\underline{v}_k, \bar{v}_k, \dots\}$ nodal limits, \bar{s}_{kl} line flow limit

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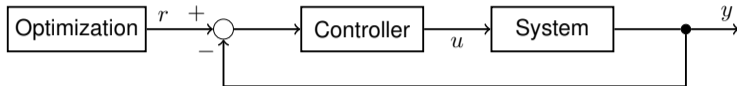
Transmission system operations

Active distribution grids

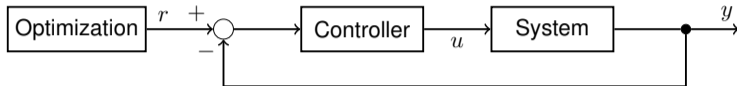
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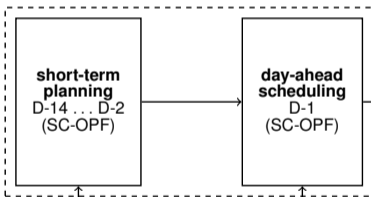
Optimization and control in power system operations



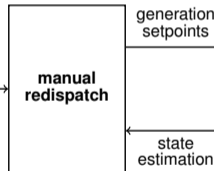
Optimization and control in power system operations



Optimization stage

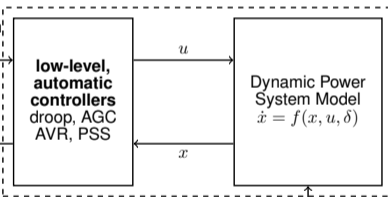


schedule



Steady-state model

$h(x, \delta) = 0$ (AC power flow)

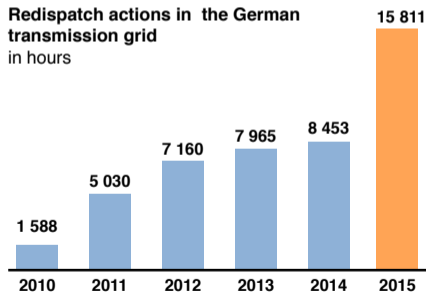


prediction (load, generation, downtimes)

δ

National & international redispatch

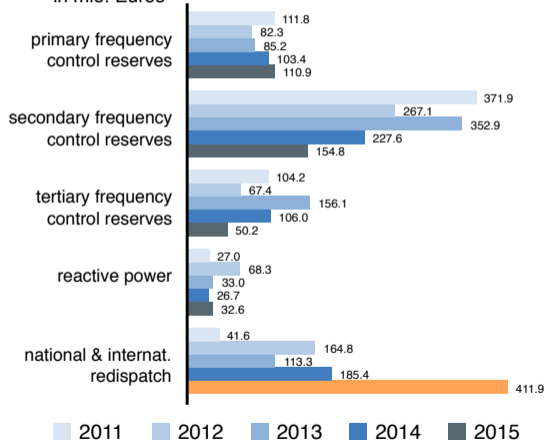
- in case of unforeseen congestion or voltage problems
- (manually) dispatched on a 15-minute timescale



[Bundesnetzagentur, Monitoringbericht 2016]

Cost of ancillary services of German TSOs

in mio. Euros



[Bundesnetzagentur, Monitoringbericht 2016]

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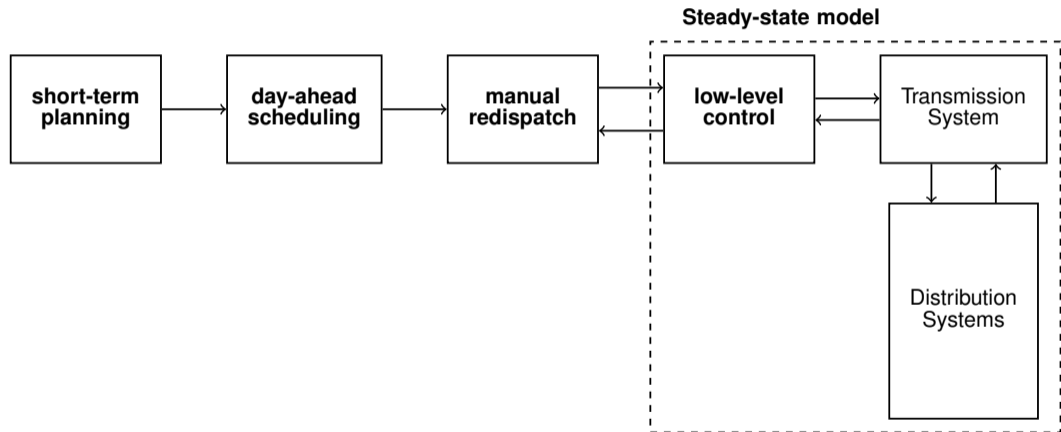
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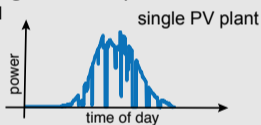
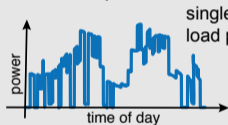
Traditional distribution grids



Distribution grids with high renewable penetration

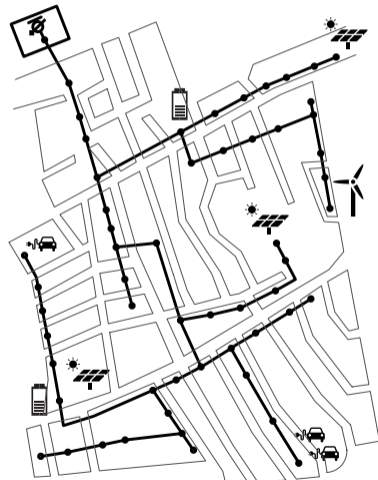
Challenges

- congestion (in urban grids)
- under-/over-voltage (in rural grids)
- hard to predict individual load/generation profiles



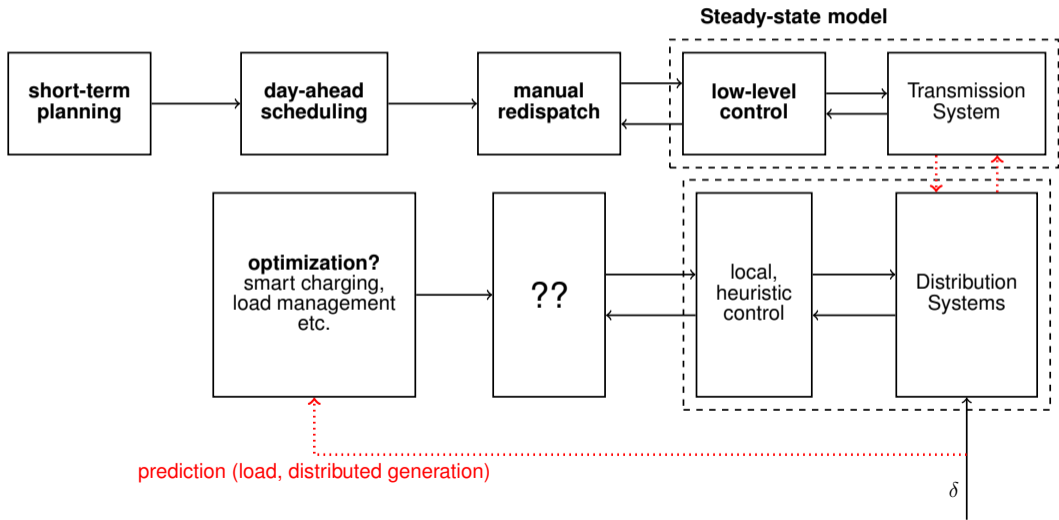
Opportunities

- new degrees of freedom (flexibility!)
- fast, inverter-based actuation
- inexpensive, reliable communication

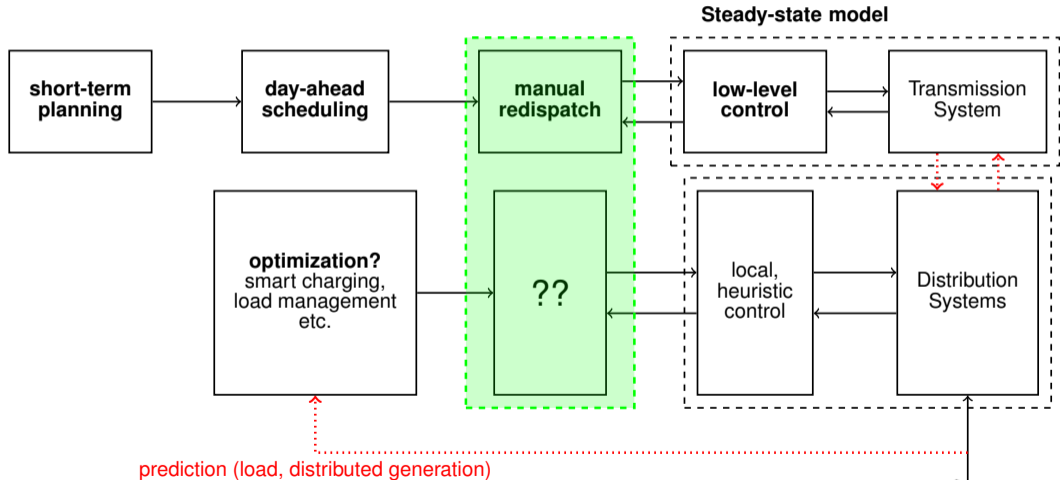


[IEEE 123 bus test feeder]

The future of active distribution systems



The future of active distribution systems



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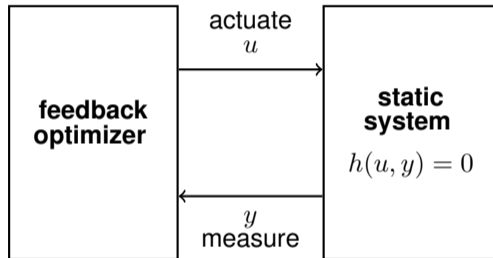
Research: combining control and optimization in a novel way

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Research: “feedback optimization”

Optimization problem

$$\begin{aligned} &\text{minimize} && f(u, y) \\ &\text{subject to} && h(u, y) = 0 \\ & && u \in \mathcal{U} \\ & && y \in \mathcal{Y} \end{aligned}$$



- no need to solve optimization problem numerically
- algebraic system constraint enforced automatically
- relies static system (or asymptotically stability with fast settling time)

The intuition behind feedback optimization

Update *control variables*

$$u^{k+1} = u^k + \Delta u,$$

measurements adapt to

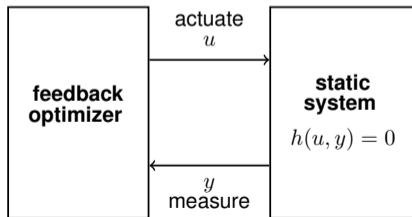
$$y^{k+1} \approx y^k + \Delta y$$

where $[\Delta u \quad \Delta y] \in \ker Dh(u^k, y^k)$.

Main Idea: Choose Δu such that $[\Delta u \quad \Delta y]$ is a *descent direction* that is feasible w.r.t. \mathcal{U} and \mathcal{Y} .

Optimization Problem

$$\begin{aligned} &\text{minimize} && f(u, y) \\ &\text{subject to} && h(u, y) = 0 \\ &&& u \in \mathcal{U} \\ &&& y \in \mathcal{Y} \end{aligned}$$



Related work

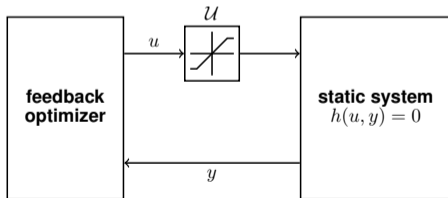
Dynamical systems that solve optimization problems:

- **Isospectral flows** on matrices
Applications: sorting lists, computing eigenvalues, solve LPs
[Brockett 1988], [Bloch 1990], [Helmke and Moore 1994]
- **Arrow-Hurwicz-Uzawa flows** for “soft-constrained” strongly-convex optimization problems
Applications: distributed consensus-based optimization
[Arrow et al. 1958], [Kose 1956], [Feijer and Paganini 2010], [Cherukuri et al. 2016], [Simpson 2016]
- **Projected dynamical systems** for “hard-constrained” convex optimization problems
Applications: variational inequalities
[Nagurney and Zhang 1996], [Heemels et al. 2000], [Cojocaru 2006]

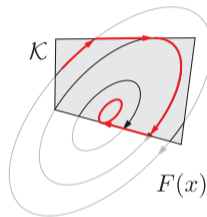
Projected dynamical systems for feedback optimization

Feedback optimization with saturation:

$$\begin{aligned} & \text{minimize} && f(u, y) \\ & \text{subject to} && h(u, y) = 0 \\ & && u \in \mathcal{U} \\ & && y \in \mathcal{Y} \end{aligned}$$



Projected dynamical systems:



Initial value problem:

$$\dot{x} = \Pi_{\mathcal{K}}(x, F(x)), \quad x(0) = x_0$$

where $\Pi_{\mathcal{K}}(x, v) \in \arg \min_{w \in T_x \mathcal{K}} \|v - w\|$.

$F : \mathbb{R}^n \rightarrow \mathbb{R}^n$ vector field, $\mathcal{K} \subset \mathbb{R}^n$ closed domain, $T_x \mathcal{K}$ tangent cone at x

Projected gradient descent

To find minimum on ϕ on a nonconvex \mathcal{K} follow negative gradient vector field:

$$\dot{x} = \Pi_{\mathcal{K}}(x, -\text{grad}\phi(x)), \quad x(0) = x_0.$$

- Does a solution trajectory exist? Is it unique? (yes, if \mathcal{K} is convex, otherwise *unknown*)
- Are solution trajectories (asymptotically) stable?
- Do solution trajectories converge to a minimizer of ϕ ?

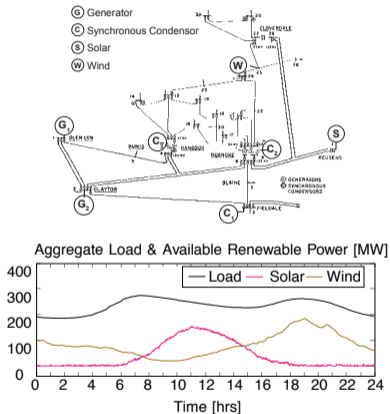
Corollary [AH et al. 2016] (simplified)

Let $x : [0, \infty) \rightarrow \mathcal{K}$ be a (Carathéodory-)solution of

$$\dot{x} = \Pi_{\mathcal{K}}(x, -\text{grad}\phi(x)) \quad x(0) = x_0.$$

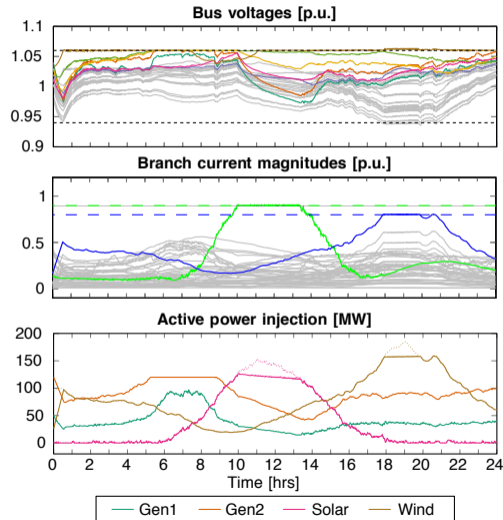
Then, if ϕ has compact level sets on \mathcal{K} sets $x(t)$ will converge to a critical point x^* of ϕ on \mathcal{K} . Furthermore, if x^* is asymptotically stable then it is a local minimizer of ϕ on \mathcal{K} .

Tracking OPF solution despite intermittency



Controller: Penalty + Saturation

A. Hauswirth, S. Bolognani, F. Dörfler and G. Hug, "Online Optimization in Closed Loop on the Power Flow Manifold," Powertech Conference, 2017, *accepted*



Further topics

- **Distributed control/optimization:** reduce information exchange to neighbor-to-neighbor communication
[Bolognani et al. 2013], [Dall'Anese and Simmonetto 2016], [Li et al. 2014], [Gan and Low 2016], ...

Further desirable properties:

- **plug-and-play:** no tuning required, distributed performance certificates
- **privacy-preserving:** no need to share private information
- **incentive-compatible:** individual, rational choices lead to social optimum

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Summary

- **Energy transition** opens up new challenges in the operation of power systems at all grid levels.
- Optimization and control theory are essential for a safe and reliable power supply.
- New methods are required to robustly **stabilize & optimize** power grids under large uncertainty and **in real-time**.
- **Feedback optimization** is a new paradigm that tries to combine the advantages of both worlds.
- Simulations look promising, but the math behind is still active research.

Thanks

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Project students: Alessandro Zanardi
József Pázmány

Questions

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