

# **Chapter 3: Exosolar Planets**

Part 1: Clever techniques for  
detecting extrasolar planets and  
planetary systems

## Detection of extrasolar planets: what's the problem?

Nearest stars are about 50,000 times further away than Jupiter – i.e. about  $3 \times 10^9$  fainter in brightness.

[In astronomical magnitudes,  $m = -2.5 \log f + \text{const.}$ ]

$$m_{\text{Jupiter}} \sim -2 \rightarrow m_{\text{planet}} \sim 21.6 \quad (\text{this is easy!})$$

Angular separation of Jupiter-Sun at nearest star is about 4 arcsec (should also be easy!)

## Brightness of extrasolar planets

Planets will shine by both reflected (sun-)light and thermal emission. Assuming an albedo of  $a$  and a radius  $r$  of the planet at an orbital distance  $D$  from a star with radius  $R_s$  and temperature  $T_s$ , and neglecting non-stellar heat sources:

Reflected sunlight: 
$$L_p = a 4\pi R_s^2 \sigma T_s^4 \frac{2\pi r^2}{4\pi D^2} = L_s a \frac{r^2}{2D^2}$$

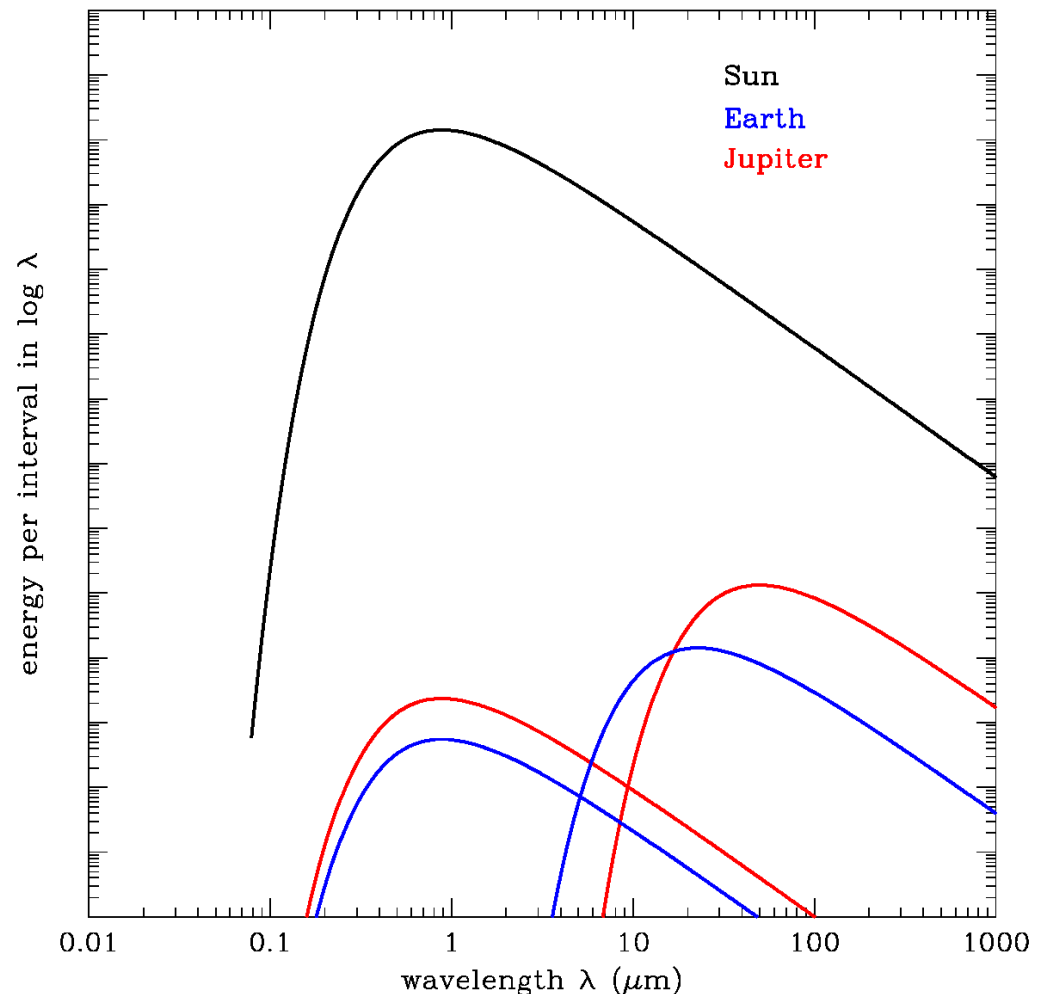
Self-emission: 
$$L_p = (1 - a) L_s \frac{r^2}{2D^2} = (1 - a) 4\pi R_s^2 \sigma T_s^4 \frac{r^2}{2D^2}$$

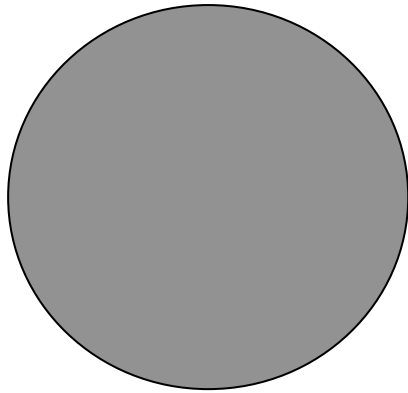
$$T_p = \sqrt[4]{\frac{L_p}{4\pi\sigma r^2}} = T_s (1 - a)^{1/4} \sqrt{R_s / 2D}$$

|         | radius              | distance               | $r^2/2D^2$            |
|---------|---------------------|------------------------|-----------------------|
| Earth   | $6.3 \times 10^6$ m | $1.6 \times 10^{11}$ m | $7.8 \times 10^{-10}$ |
| Jupiter | $7.1 \times 10^7$ m | $7.8 \times 10^{11}$ m | $4.1 \times 10^{-9}$  |
| Sun     | $7.0 \times 10^8$ m | ---                    | ---                   |

### Looking at the Earth and Jupiter from far away: The problem is the Sun

- Brightness contrast relative to Sun is  $\sim 10^9$  at  $\lambda < 1 \mu\text{m}$ , and still  $10^5$  at  $\lambda \sim 100 \mu\text{m}$
- Note: The Earth is brighter than Jupiter at  $10 \mu\text{m}$ !





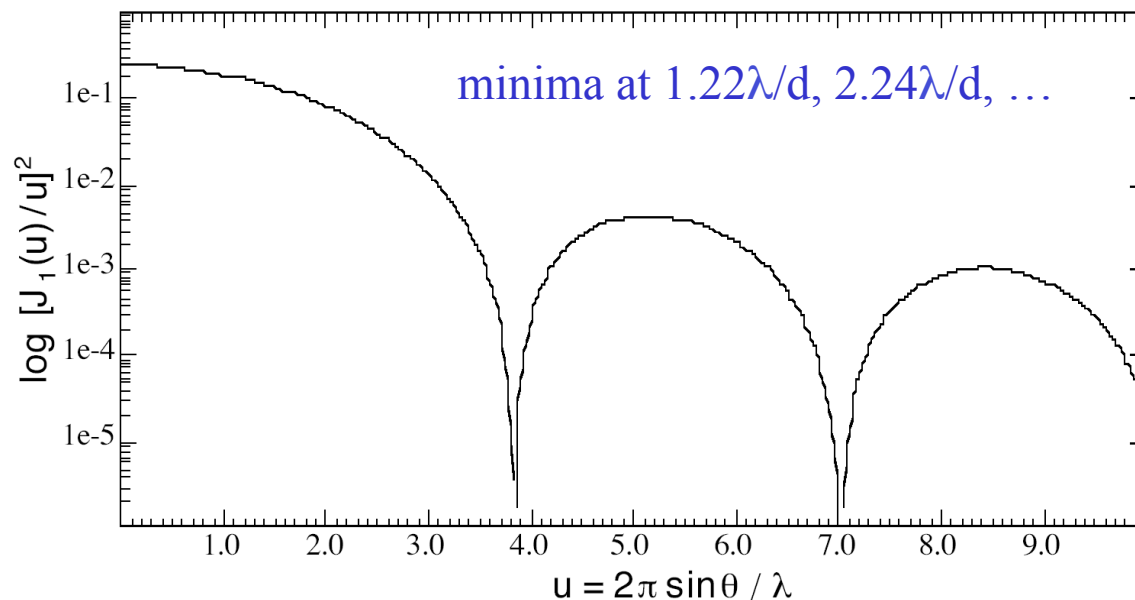
Diffraction from ideal telescope aperture:

Point spread function of telescope (image of point source) is Fourier transform of entrance aperture:

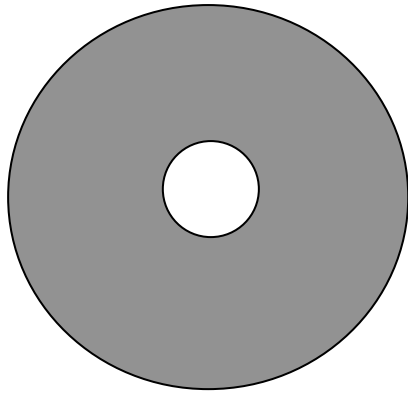
For an idealised perfectly circular aperture:

$$I(\theta) = I_0 \left( \frac{2J_1(u)}{u} \right)^2 \quad u = 2\pi\theta / \lambda$$

$J_1 = 1^{\text{st}}$  order Bessel function of first kind



84% of energy within a diameter of  $1.22\lambda/d$  ( $\sim 0.015$  arcsec for 8 m telescope at visible wavelengths 550 nm), but scattered light decreases slowly with radius



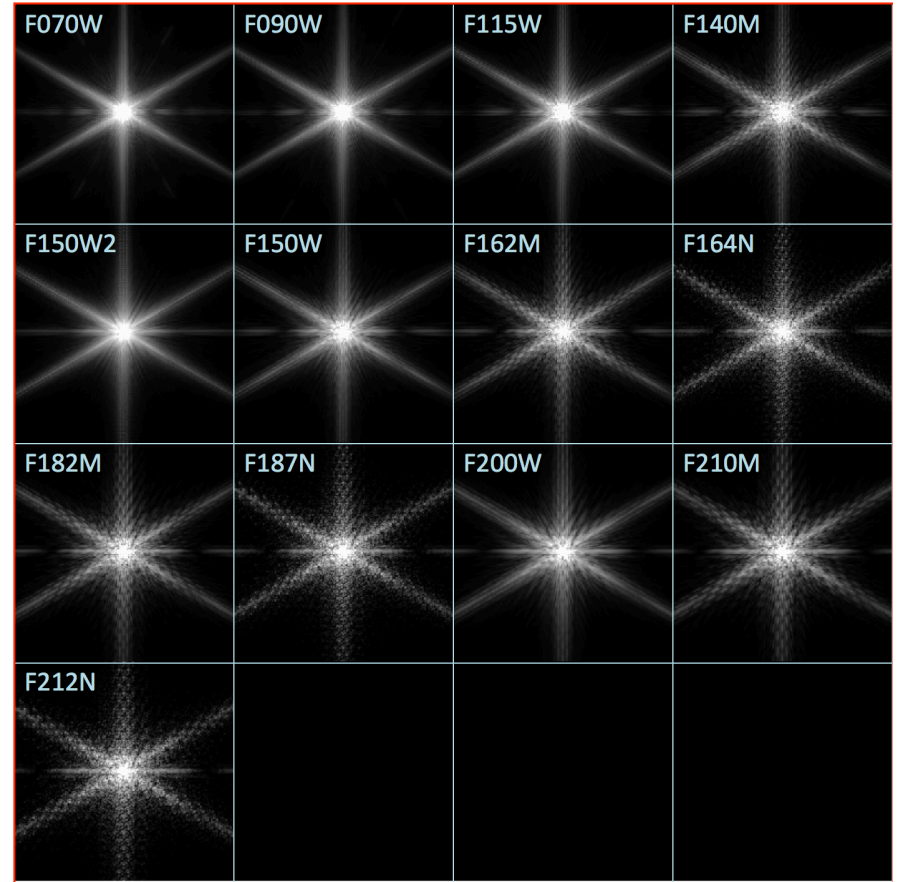
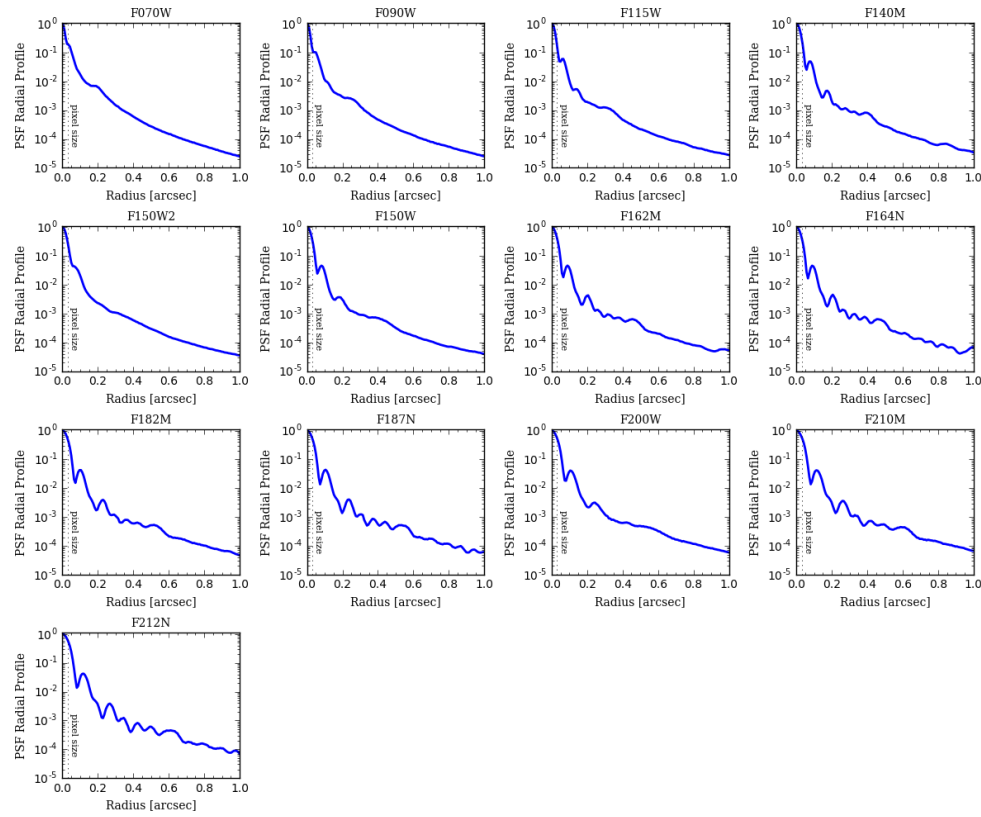
In practice it is even worse

- “On-axis” telescopes usually have central obstruction of some kind for mechanical design reasons
- Imperfections in optics throw light to large angles

Plus:

- Phase errors across the aperture due to variations in atmospheric refractive index (for ground-based telescope at optical wavelengths) produce approximately gaussian images of typical FWHM  $\sim 0.5-1.2$  arcsec  $\sim 30 \times$  diffraction limit

# Even telescopes in space have complex point-spread-functions (PSF), e.g. JWST



# Exo-solar planet detection: how to do it?

## **A: Indirect detection (does not detect the light from planet)**

1. Radial velocity measurements (and pulsar timing)
2. Astrometric searches
3. Transits
4. Gravitational lensing

## **B: Direct searches (does detect the light from the planet)**

Use different approaches to subtract the dominant star-light

1. Coronagraphy
2. Adaptive optics
3. Polarimetry and/or spectral chopping
4. Interferometry and nulling interferometry

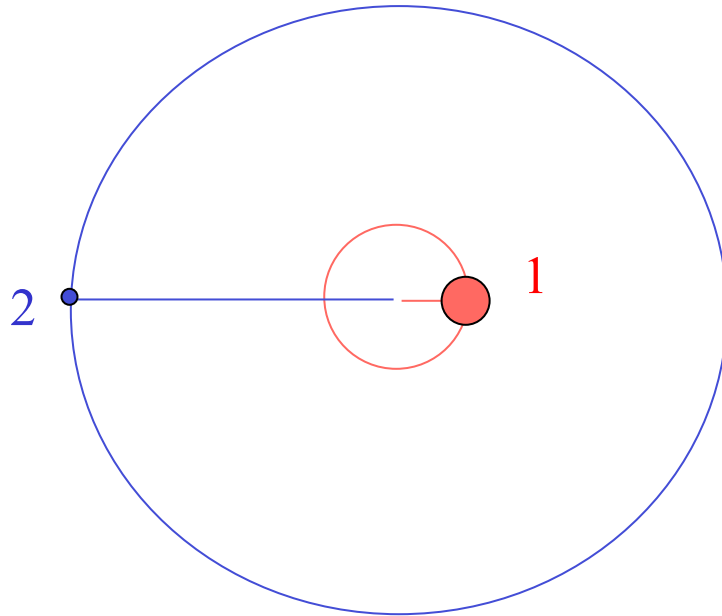


## 1. Doppler (radial velocity) methods

Simple two-body problem in Newtonian gravity: both bodies orbit their common center of mass → detectable shifts in radial velocity (and/or astrometric position on sky) during orbit.

High stability high resolution spectrographs can measure radial velocities of bright stars at the < 1 m/s level through Doppler shift of wavelengths:

$$\frac{v_r}{c} = \frac{\lambda_{obs} - \lambda_{rest}}{\lambda_{rest}} = \frac{\Delta\lambda}{\lambda}$$



$$\frac{v_1^2}{r_1} = \frac{Gm_2}{(r_1 + r_2)^2}$$

$$m_1 r_1 = m_2 r_2$$

$$2\pi r_1 = v_1 P$$

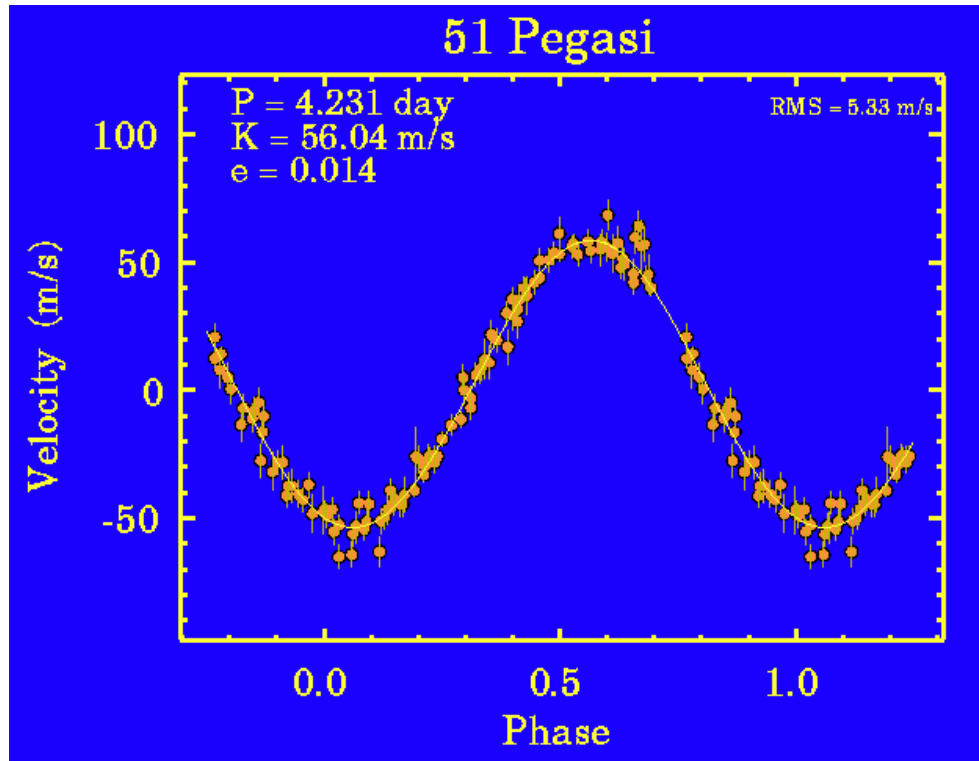
$$m_2 = m_1^{2/3} \left( \frac{P}{2\pi G} \right)^{1/3} v_1$$

We know  $m_1$  from the type of star

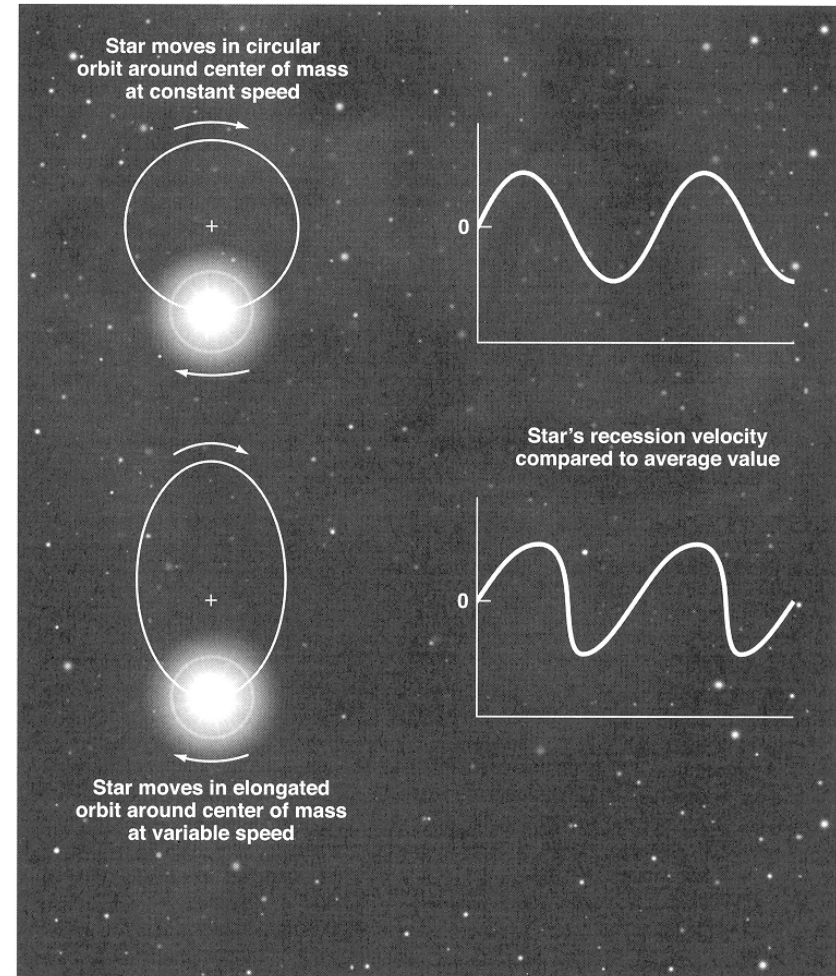
$$v_r = v_1 \sin i$$

We don't *a priori* know the inclination of the orbit w.r.t. the line of sight, and measure only the radial component  $v_r$  (relative to us) of  $v_1$ , so the measurement is actually of  $m_2 \sin i$ . A lower limit on  $m_2$  is obtained with  $\sin i = 1$ .

# 51 Peg discovered 1995 by Mayor and Queloz (Geneva)



Circular orbits give sinusoidal wave  $v_r(t)$



Eccentric orbits give distorted wave

What about the observability (to others!) of our own Solar System?

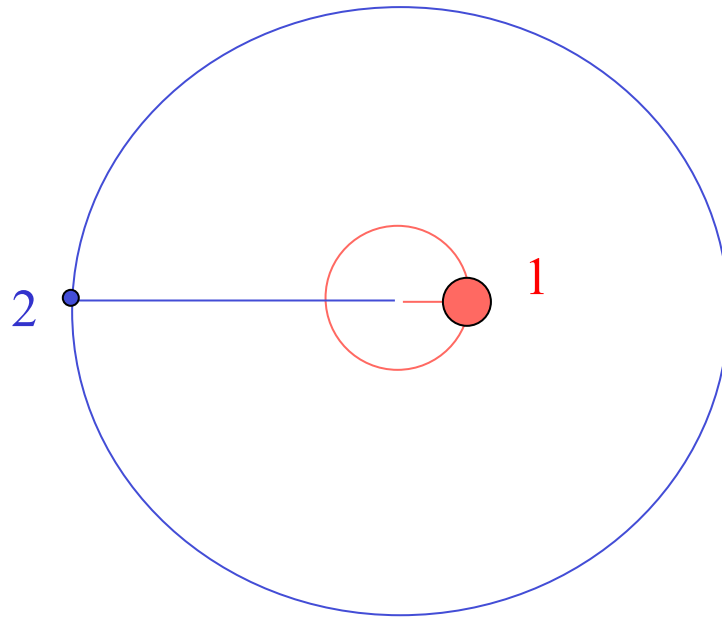
$$v_1 = v_2 \frac{m_2}{m_1}$$

|         | $v_2$                | $m_2/m_{\text{sun}}$ | $v_1$                |
|---------|----------------------|----------------------|----------------------|
| Earth   | 30 kms <sup>-1</sup> | $3.0 \times 10^{-6}$ | 0.1 ms <sup>-1</sup> |
| Jupiter | 13 kms <sup>-1</sup> | $1.0 \times 10^{-3}$ | 13 ms <sup>-1</sup>  |

For a given  $m_1$ , easier detection for higher  $m_2$ , and smaller  $r$ , i.e. smaller  $P (\propto r^{-1/2})$ .

Note: in principle the signal  $\Delta v$  is independent of the distance to system (but of course the target star is fainter at larger distances so it is harder to measure  $v$ )

## 2. Closely related: timing methods



Precise clocks in orbit change speed for distant observers (can think of either as Doppler shift during approach/recession or as light travel time across the orbit)

- $\Delta(\text{rate})/\text{rate} \sim v_r/c$
- $\Delta t \sim r/c$

Same  $\sin i$  inclination effects as before

Aside: this is effectively the same method as Römer used to determine speed of light using Jupiter's moons as "clocks" in 1676

## Observability for timing methods for the central object

$$\Delta t = \frac{r_2}{c} \frac{m_2}{m_{star}}$$

|         | $r_2$            | $m_2/m_{sun}$        | $\Delta t$           |
|---------|------------------|----------------------|----------------------|
| Earth   | 8 light minutes  | $3.0 \times 10^{-6}$ | 1.4 msec over 1 year |
| Jupiter | 40 light minutes | $1.0 \times 10^{-3}$ | 2.4 s over 12 years  |

Pulsars: rapidly rotating neutron stars ( $M \sim 1 M_{\odot}$ ,  $r \sim 10$  km,  $P \sim$  few ms – few s)

PSR 1257+12 (1992): Three roughly one Earth-mass “planets” orbiting a spinning neutron star at 0.2-0.5 AU (plus possible 35 AU Saturn-mass object): Life?

- No light
- Hazardous radiation
- SN explosion few million years ago

## 2. Astrometric methods

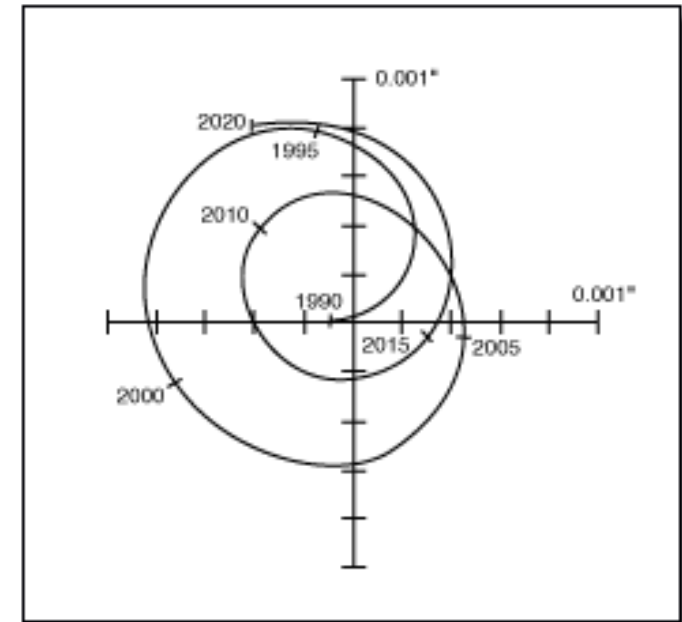
Motion of star around center of mass produces change in position on sky (superimposed on any systematic motion due to stars velocity through space).

(Note center of mass of Sun-Jupiter system is  $0.9 R_{\text{sun}}$  from the center of the Sun)

## Observability for astrometric methods

Note: Angular displacement decreases with the distance to the star as  $d^{-1}$

$$\Delta\theta = \frac{r_2}{d} \frac{m_2}{m_{star}}$$



Astrometric displacement of the Sun due to Jupiter as seen from 10 parsecs.

| Assume<br>$d = 10\text{pc}$ | $r_2$   | $m_2/m_{\text{Sun}}$ | $\Delta\theta$         |
|-----------------------------|---------|----------------------|------------------------|
| Earth                       | 1 A.U.  | $3.0 \times 10^{-6}$ | $0.3 \mu\text{arcsec}$ |
| Jupiter                     | 12 A.U. | $1.0 \times 10^{-3}$ | $0.1 \text{ marcsec}$  |



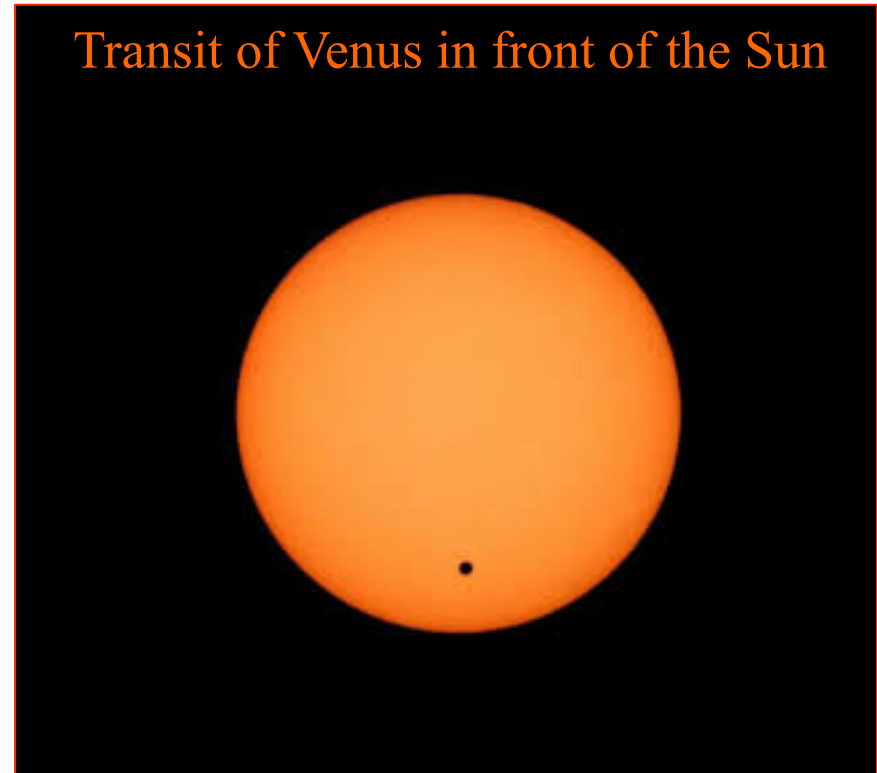
### 3. Occultations

Jupiter has  $0.1 \times$  radius of Sun, i.e. 1% of area. When Jupiter passes in front of Sun (for an extrasolar observer) the brightness of Sun drops by 1% for  $\sim 15$  hours

→ monitor large numbers of stars  
hoping for occultations

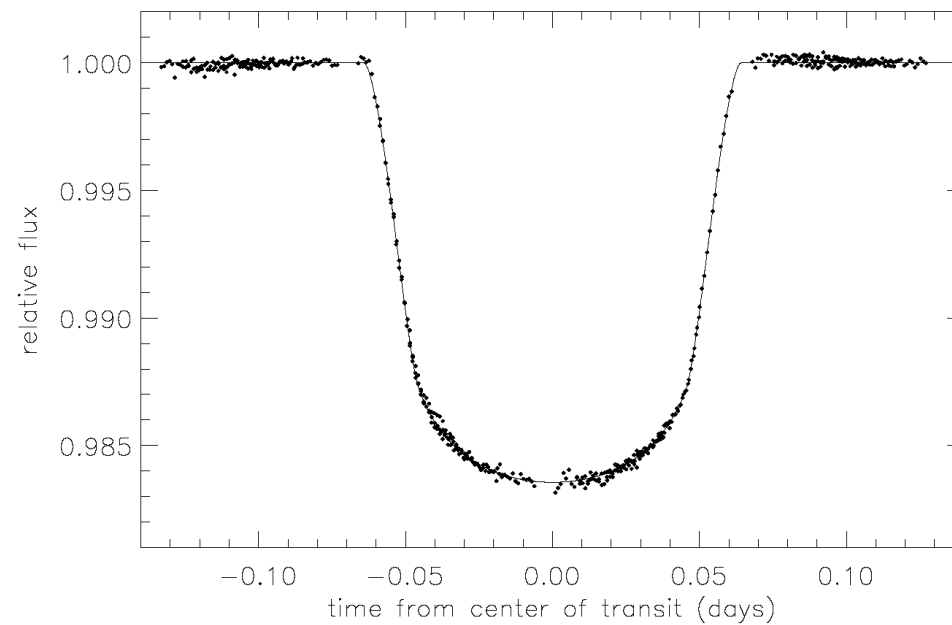
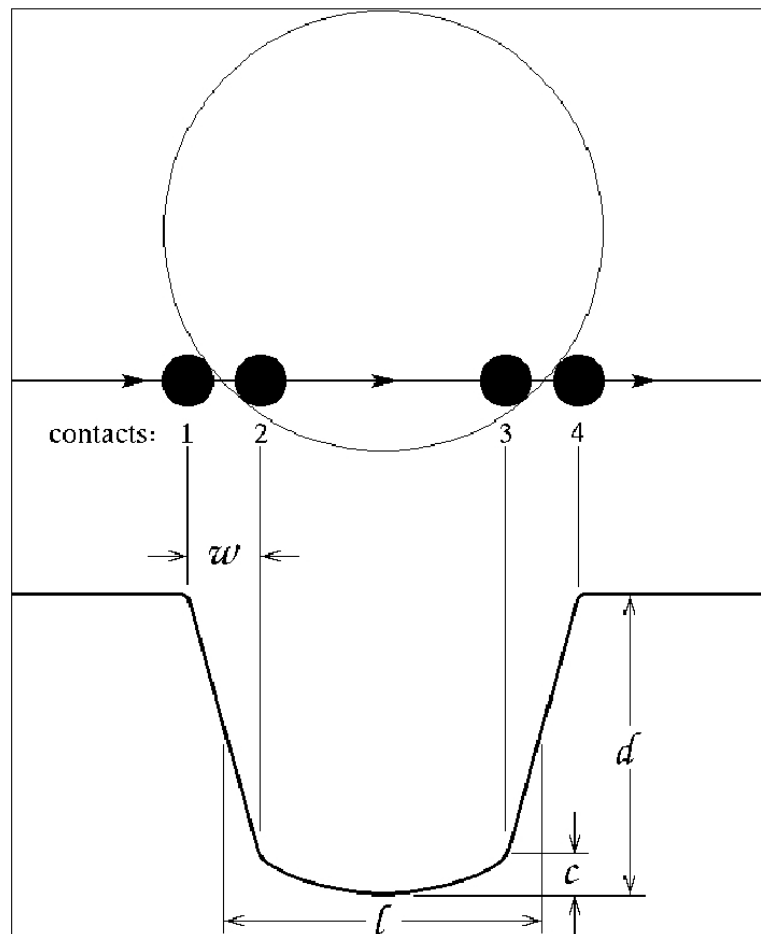
or

→ focus on known RV systems at the phase when  $v_r \sim 0$

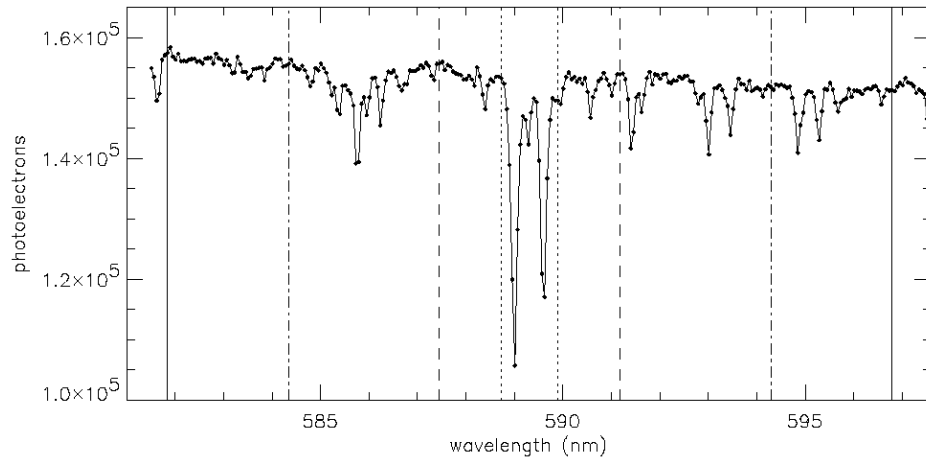


Note: occultations will only occur if  $\sin i \sim 1$  (i.e.  $i \sim 90^\circ$ ) making a real  $m_2$  measurement out of the  $m_2 \sin i$ . Also, the occultation gives size of the planet (assuming size of star is known) and therefore can give the density of the planet.

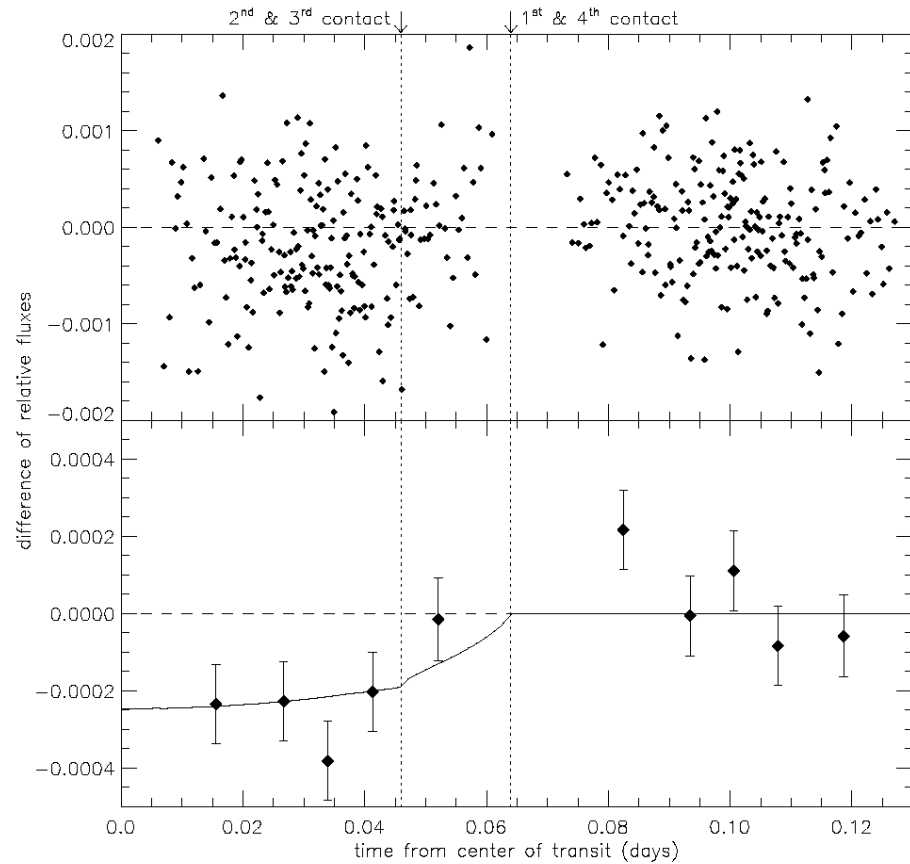
Note: Also, there will be a much smaller drop when the planet passes behind the star and we lose the planet's own light (therefore best done in infrared where contrast in brightness is smaller)



If the planet has a “transparent” atmosphere with absorption lines, then the planet will be effectively bigger at the wavelengths of the absorption lines, blocking more light → “transit absorption spectroscopy”



e.g. first detection of Na absorption in atmosphere of a transiting planet

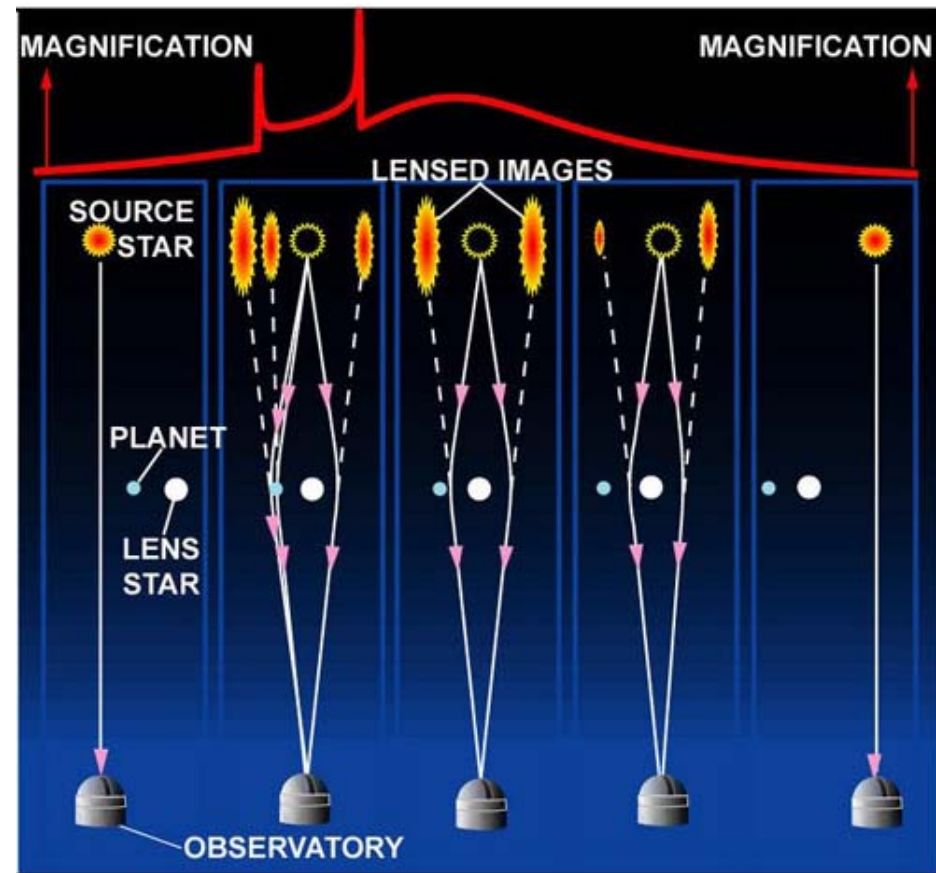
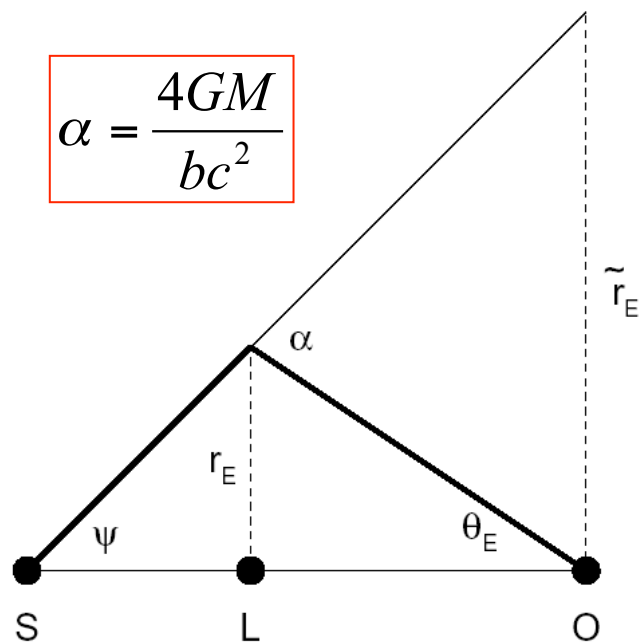


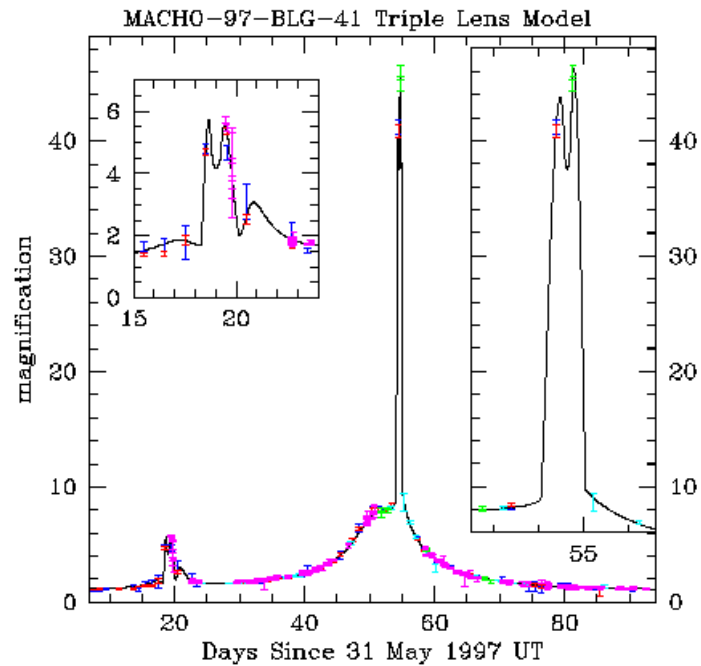
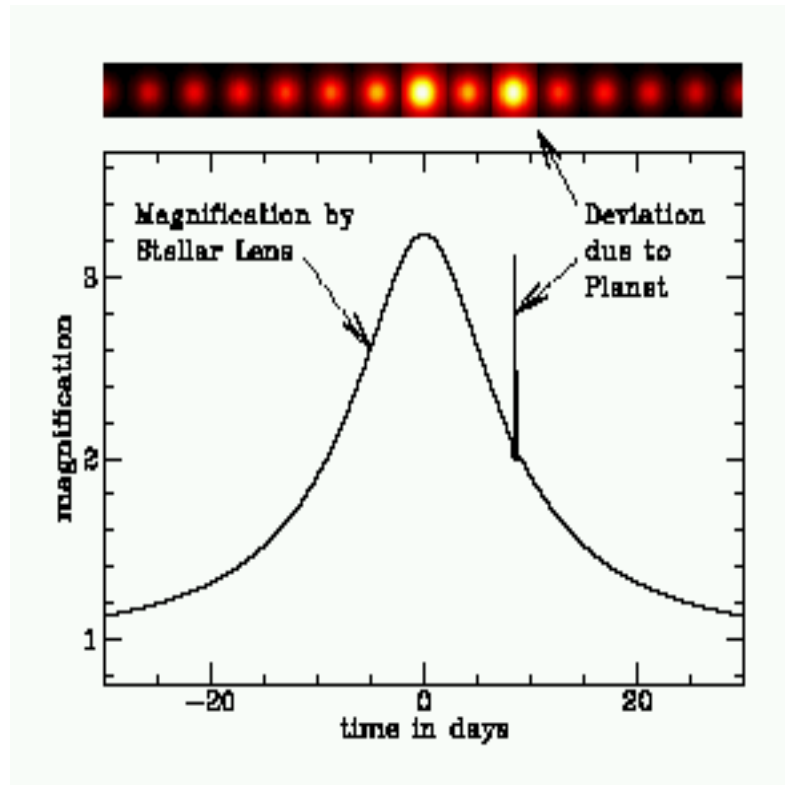
## 4. Gravitational lensing

Planets passing in front of background stars can produce gravitational lensing effects, i.e. brightening of the background star.

Light passing at distance  $b$  from point mass  $M$  is deflected through angle  $\alpha$

$$\alpha = \frac{4GM}{bc^2}$$





Again, you must monitor a huge number of stars for a long period of time to see lensing by foreground star, some fraction of which may have planet if you are lucky.

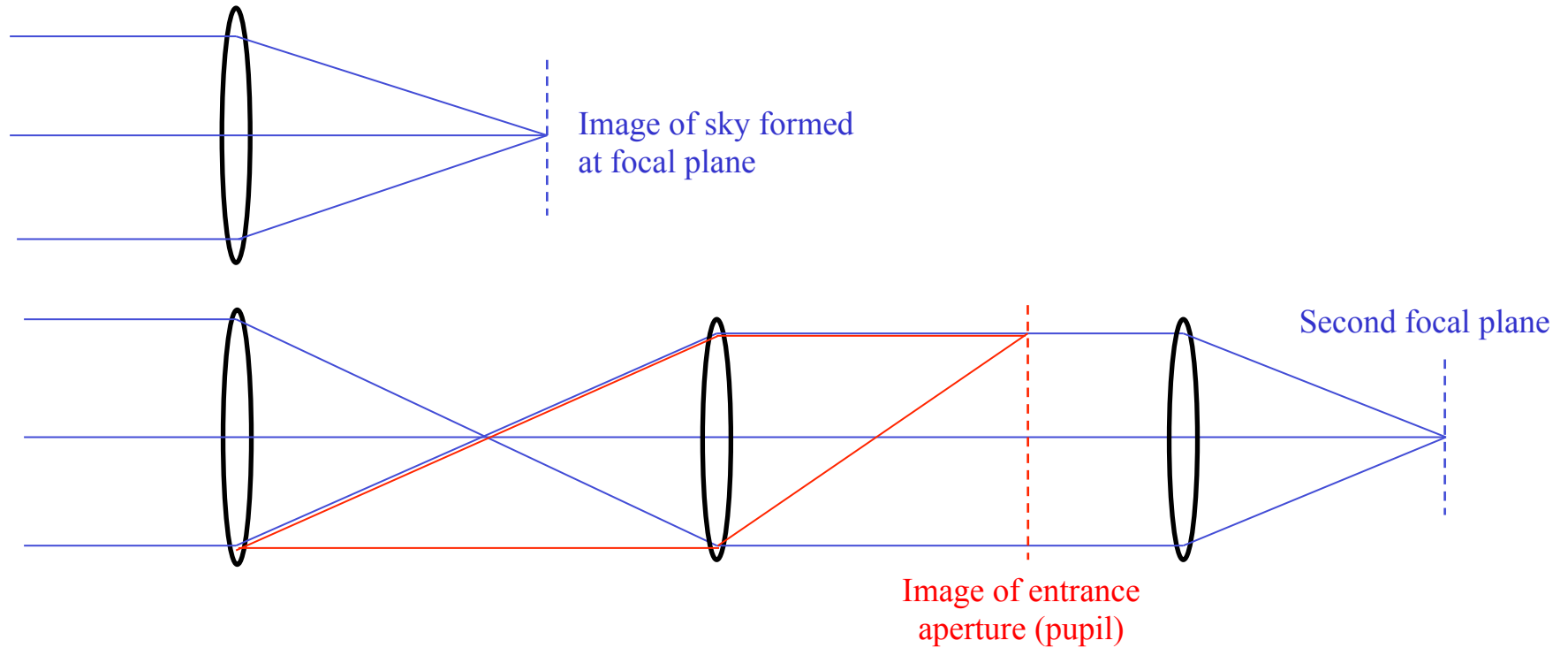
→ Monitor either huge number of stars in central region of our Galaxy or look at a nearby stellar system like the Large Magellanic Cloud (LMC).

## **B: Direct searches**

Potential approaches to try to reduce the dominant starlight so as to detect light from the planet

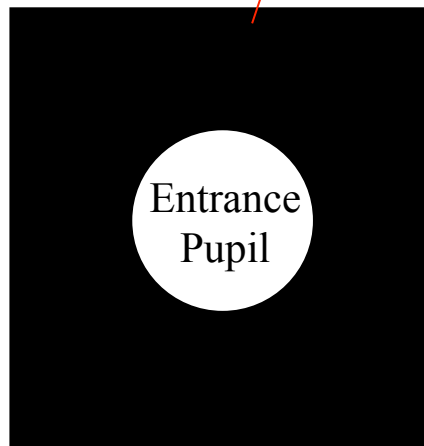
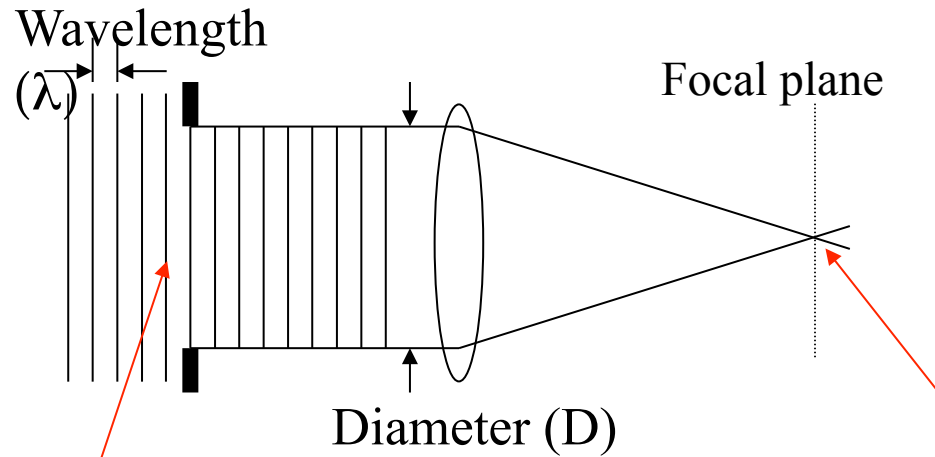
1. Coronagraphy
2. Adaptive optics
3. Polarimetry and/or spectral chopping
4. Interferometry and nulling interferometry

## Simple optics: (doesn't matter whether lenses or mirrors)



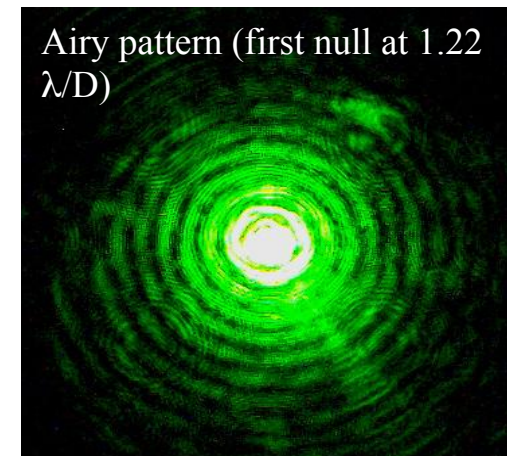
Key point: at various points through the optical system there are “images” of the different optical elements. This includes “images” of the atmosphere at different altitudes above the telescope

# Fourier Optics: The classical circular aperture



Fourier optics:

The image in the focal plane is the spatial Fourier transform of the entrance field





# Coronagraphics: The simple Lyot camera

Telescope Pupil  
Evenly Illuminated



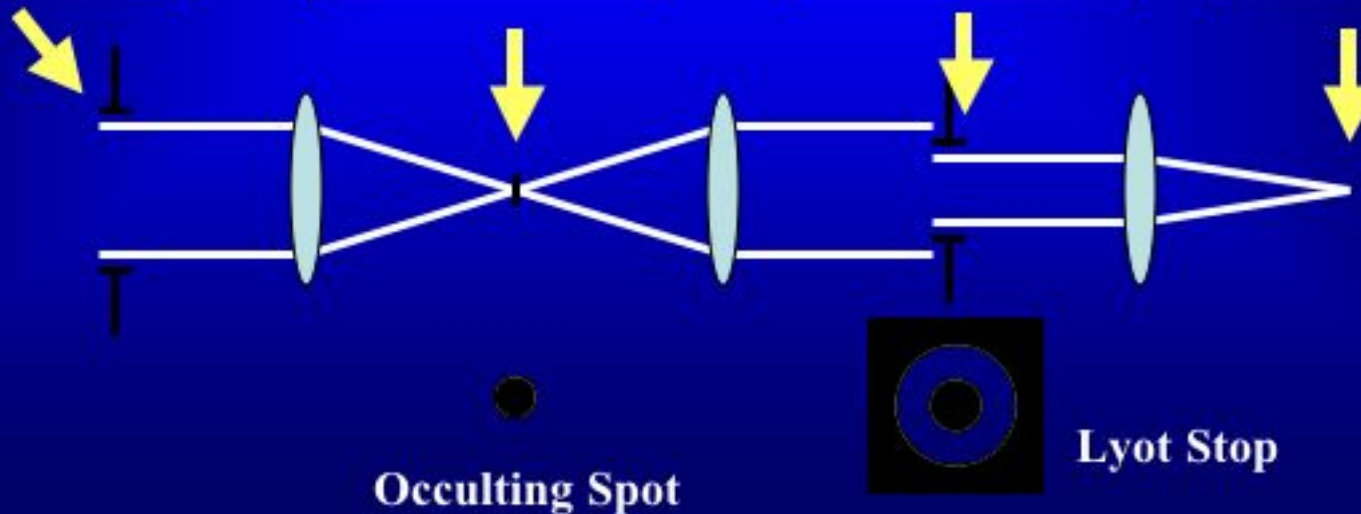
Image is made (top)  
And occulted (bottom)



Pupil is reimaged (top)  
And partially blocked (bottom)

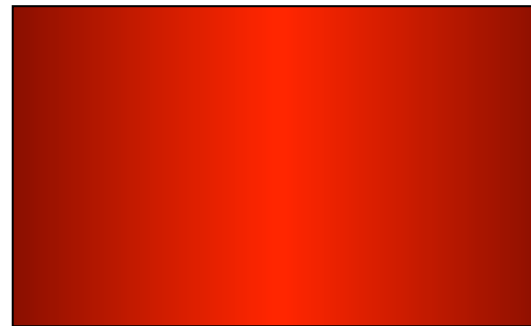
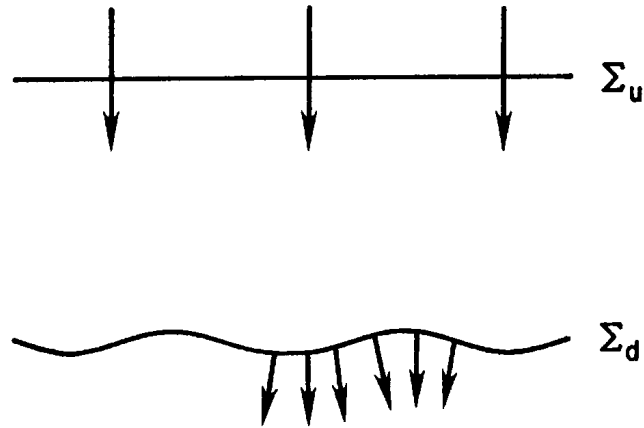


The Final image after  
Coronagraph has only  
1.5% of the original  
Starlight.



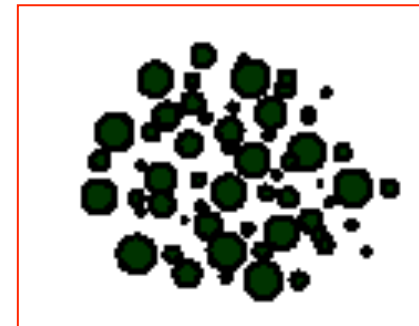
## 2. Adaptive Optics

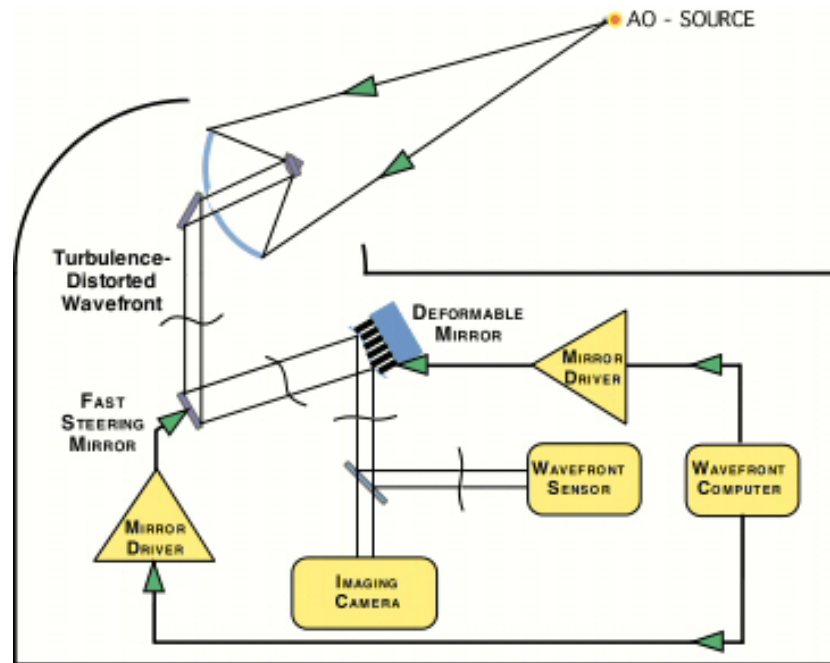
Spatial variations in the refractive index in the atmosphere above the telescope introduce rapidly varying wavefront distortions (phase variations) on a timescale of  $\sim 10$  ms.



Observed with small aperture telescope  $\rightarrow$  angled wavefront produces 10 msec image motion and brightness variations

With large aperture telescope  $\rightarrow$  distorted wavefront produces multiple rapidly moving images (“speckles”)

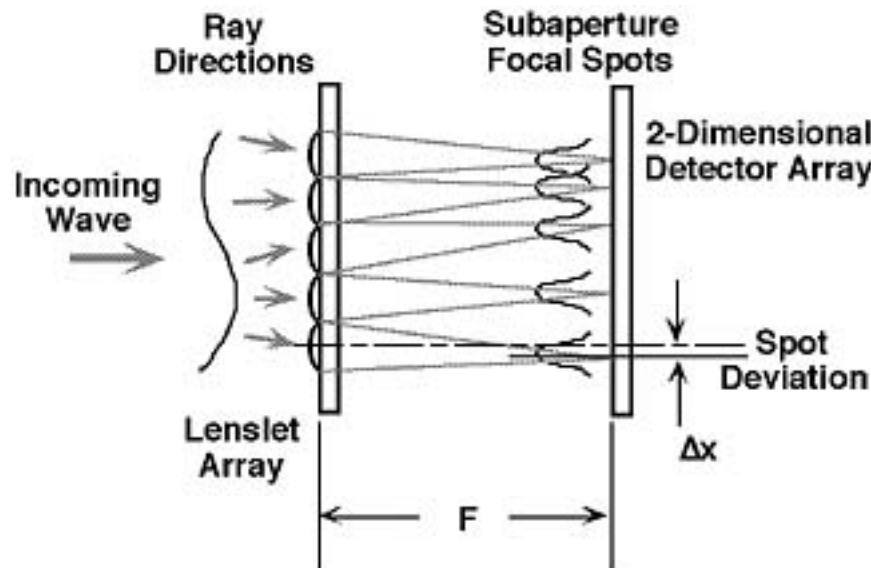




Generic adaptive optics system optical layout: A deformable mirror that is conjugated to the entrance pupil (or better, to the relevant height in the atmosphere) corrects the phase errors.

Must work at kHz rate.

How to measure phase distortions of the wavefront?  
Wavefront sensing (e.g. Shack-Hartmann method)

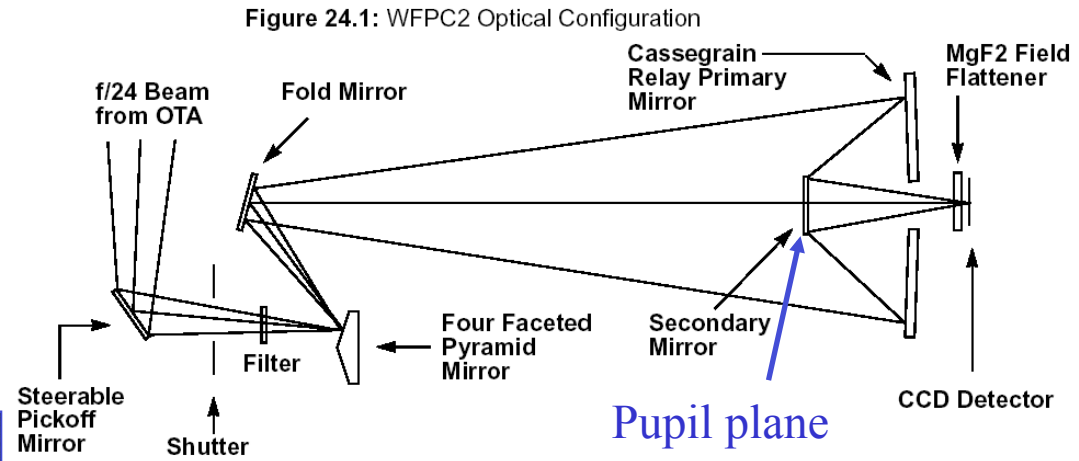


Position of image in sub-pupil gives the phase gradient of the wavefront

AO system

# As an aside: correction of primary mirror aberration on Hubble Space Telescope

HST's primary mirror had gross curvature error: spherical aberration = different annuli on mirror have different focal lengths

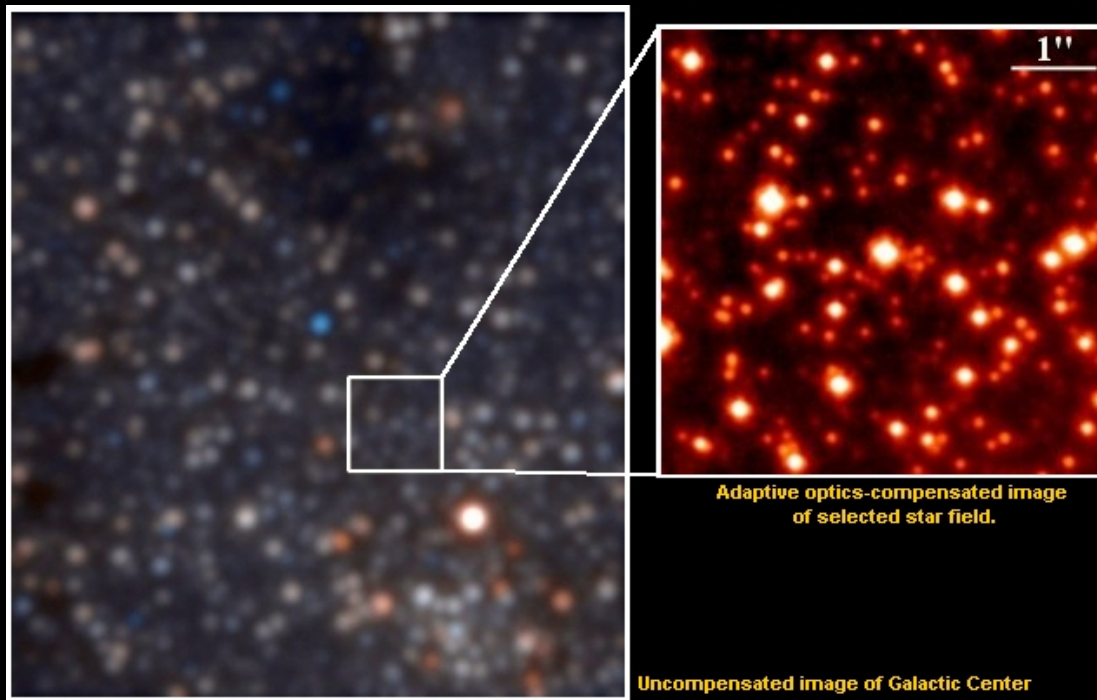


Wide Field Planetary Camera 1

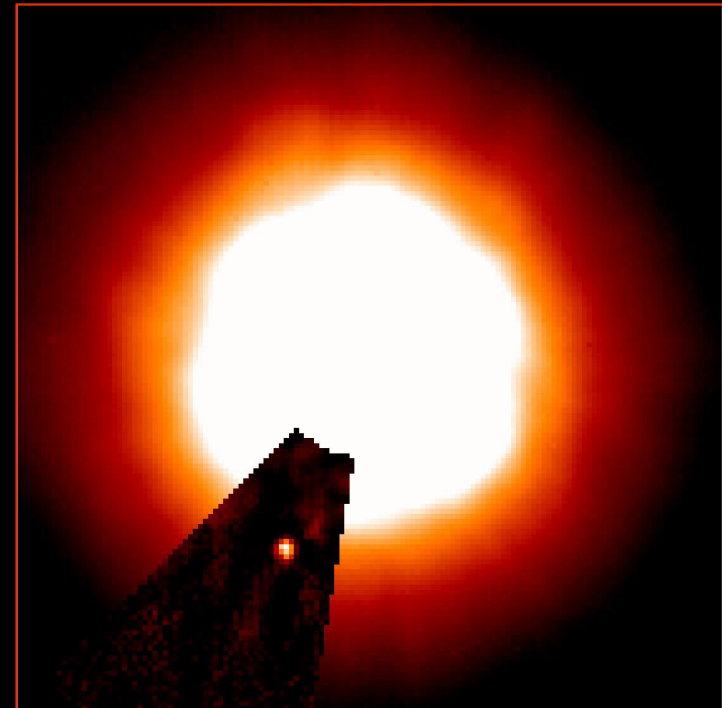


Wide Field Planetary Camera 2

HST aberration correction



AO image of Galactic Center

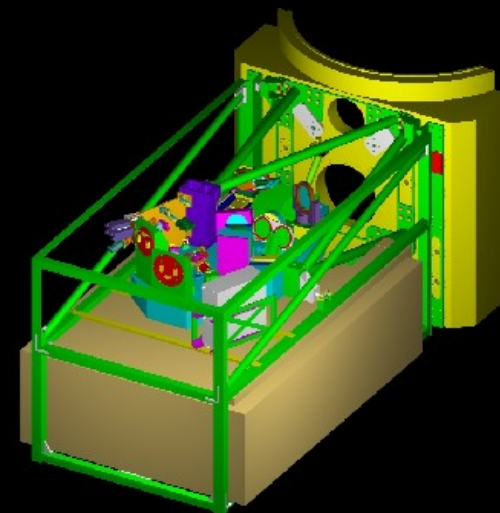


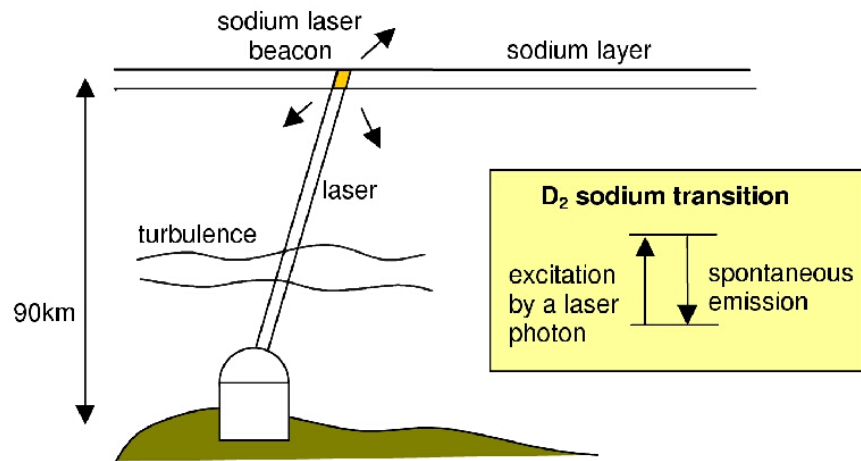
$65 M_{\text{Jupiter}}$  brown dwarf 0.8 arcsec from 5 mag star

AO systems in practice:

We need a bright source to use for the kHz wavefront sensing:

- Self-referencing
- Bright star within “isoplanetic patch”
- Artificial guide stars (e.g. Na laser)





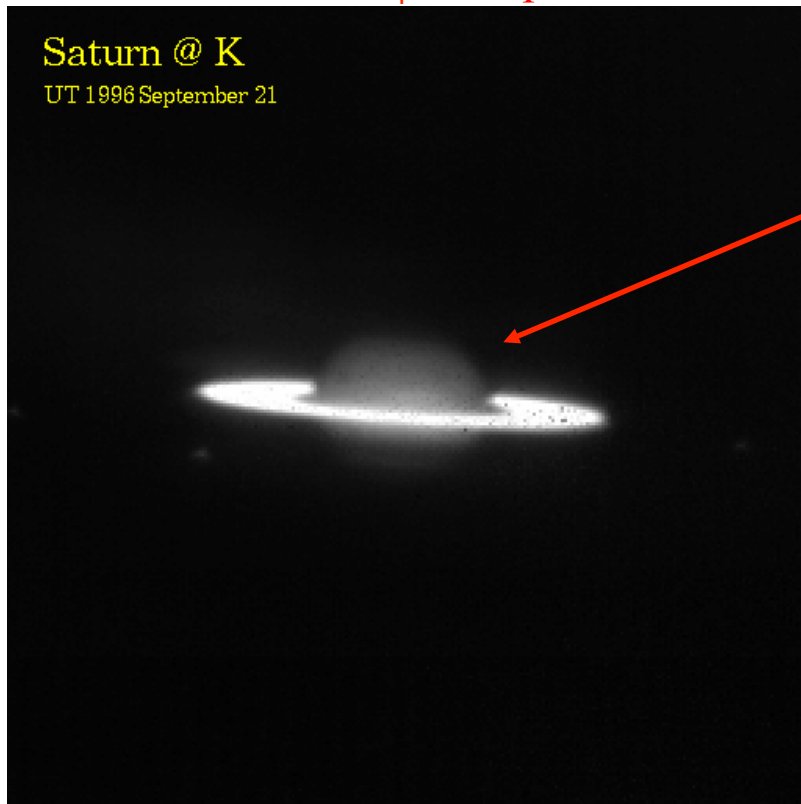
Artificial laser stars for adaptive optics using Na in upper atmosphere to produce artificial “star”



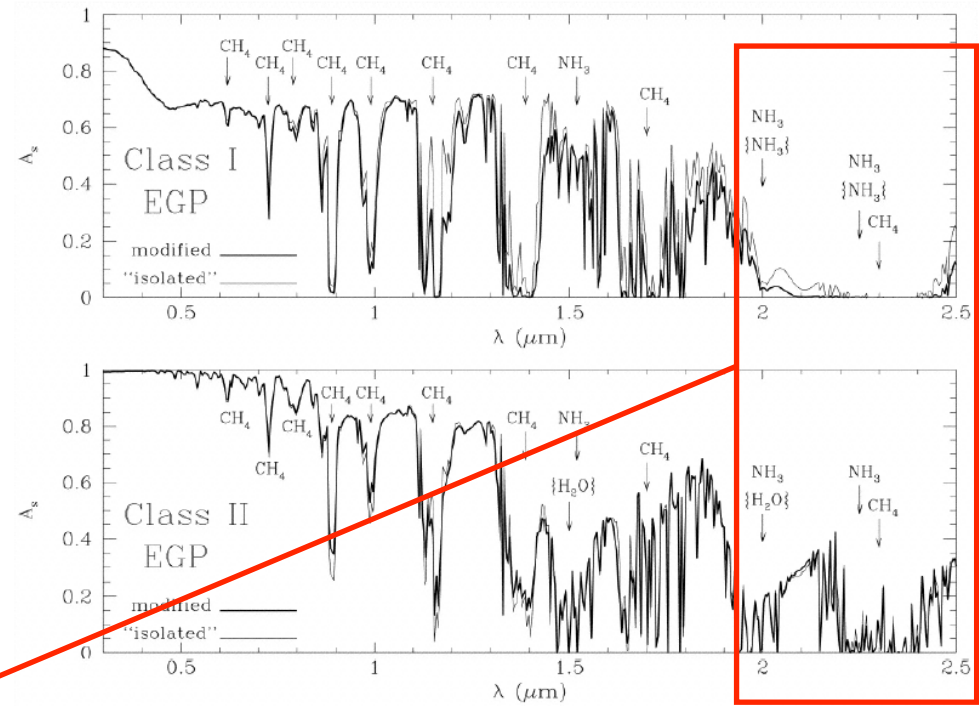
### 3(a) Spectral subtraction

Simultaneous differential “on-off” imaging at two wavelengths at which planet and star are expected to have different relative brightnesses

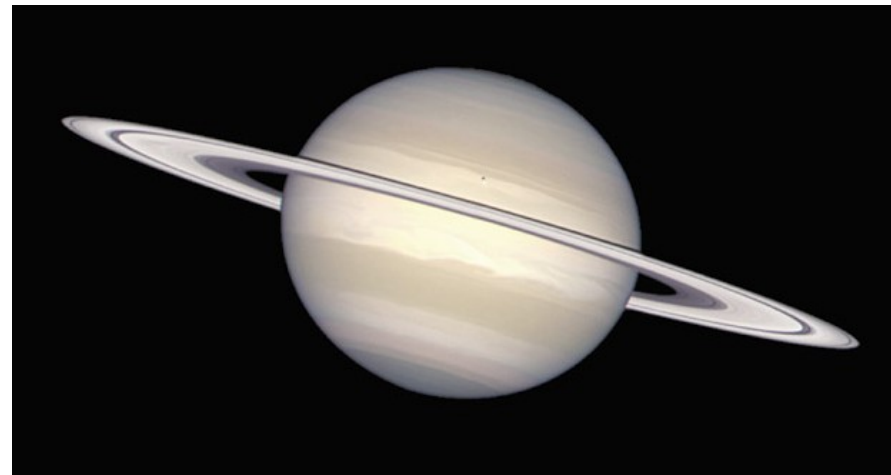
2  $\mu\text{m}$ : atmospheric albedo very low due to  $\text{CH}_4$  absorption



Methane differencing



Visible light: uniform albedo



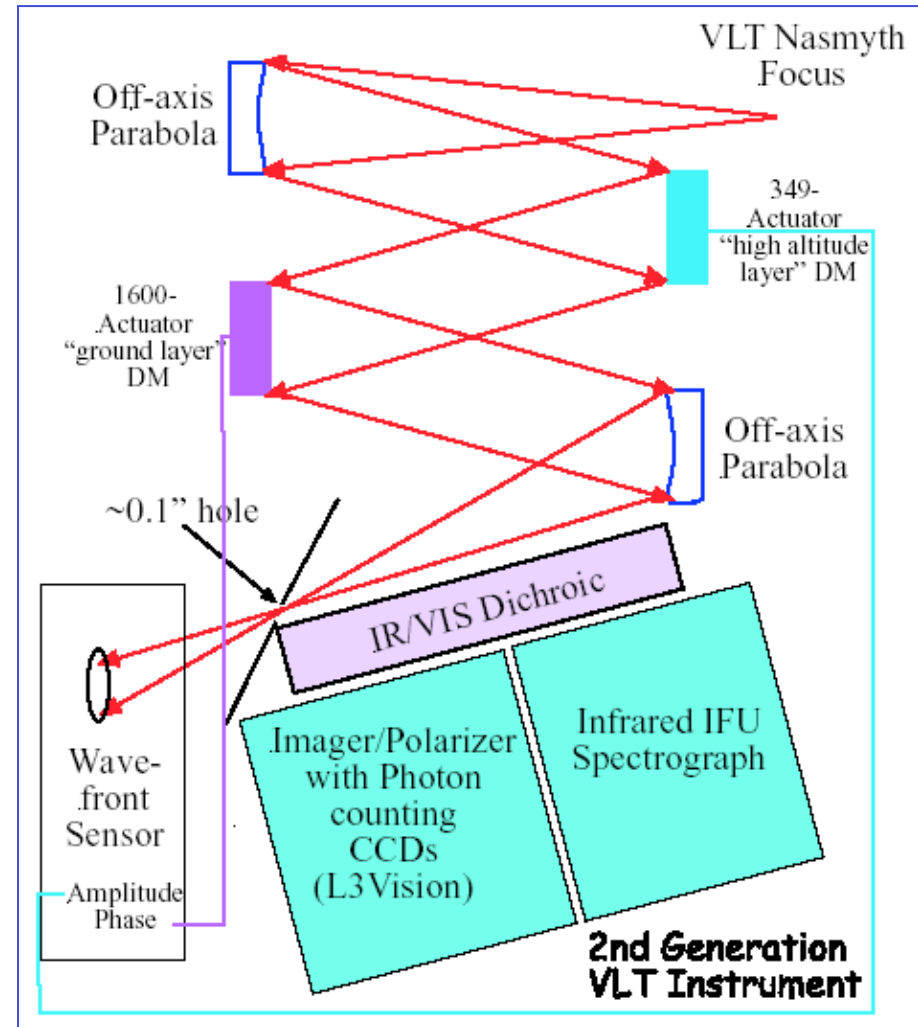
### 3(b) Differential polarimetric imaging

If the central star and planet (or dust disk) have different polarizations, then one can effectively remove the star-light.

SPHERE “planet-finder” instrument for European VLT combines

- High order multi-layer adaptive optics
- Differential infrared imaging on-off spectral features
- Differential polarimetric imaging

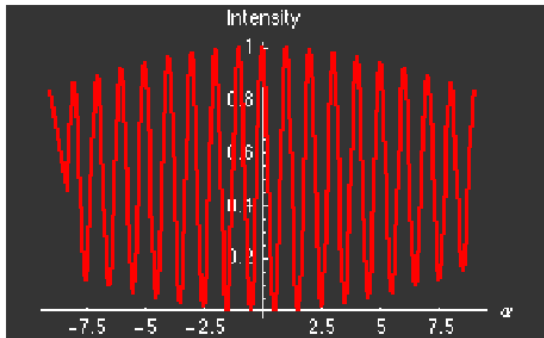
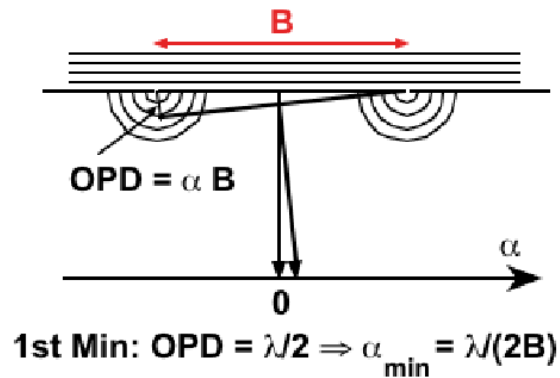
### SPHERE





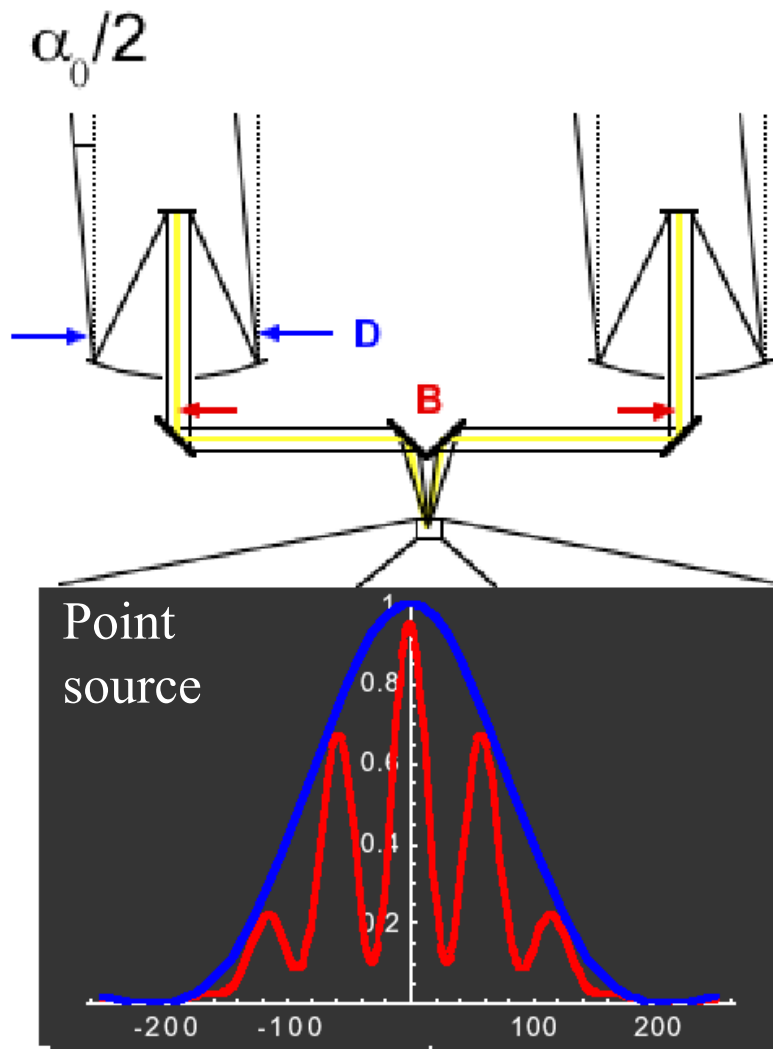
## 4. Interferometry

### Young's Two-Pinhole Experiment

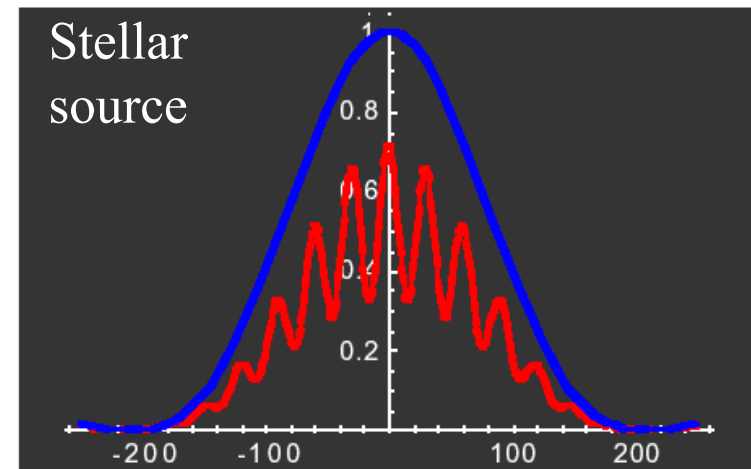


- Light source at infinity
- Intensity pattern =  $1 + \cos(2\pi\alpha B/\lambda)$ , where  $\alpha B$  is the Optical Path Difference (OPD)
- When  $OPD >$  coherence length, fringes disappear
- Light source at angle  $\alpha_0$  shifts fringe pattern spatially

## Aside: The Michelson stellar interferometer (1920) was used to measure stellar angular sizes

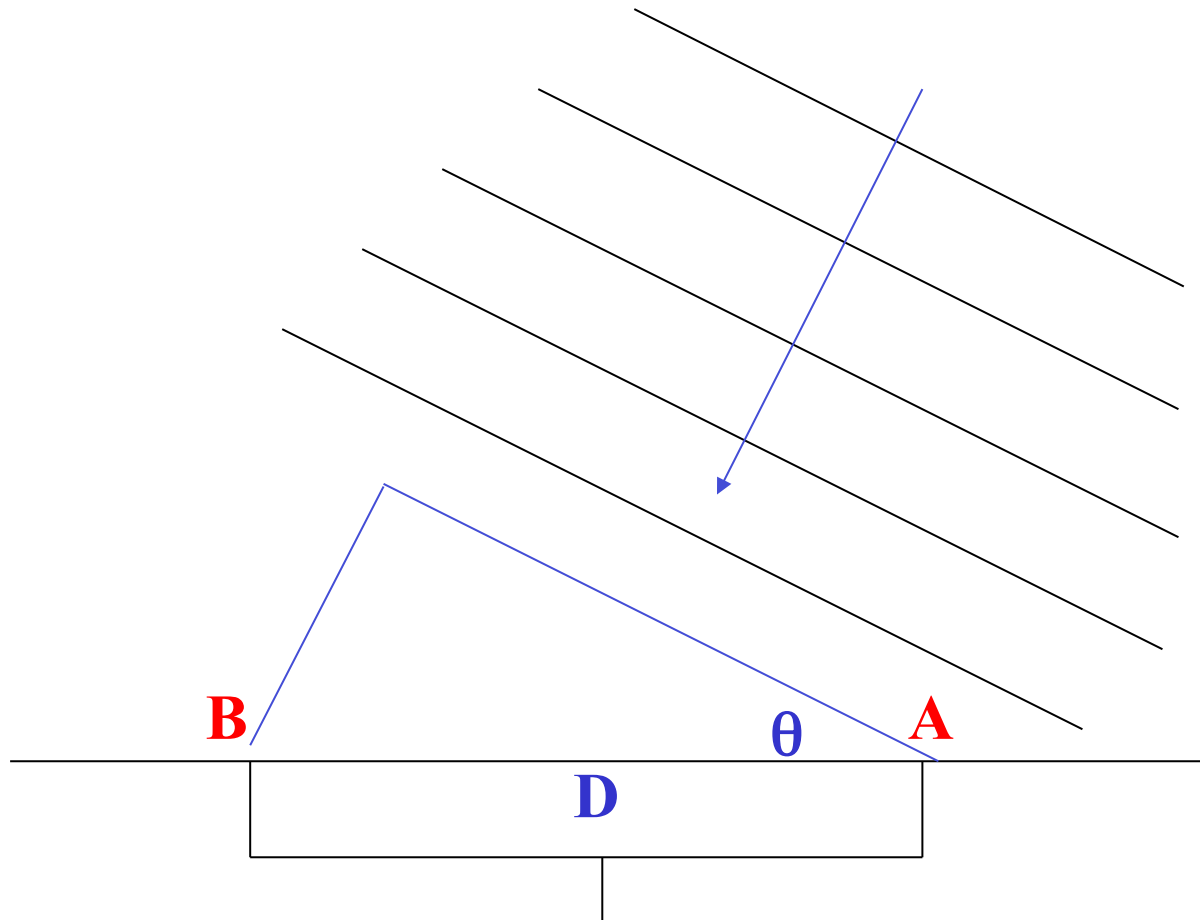


- Stellar source with angular diameter  $a_0$
- Add fringe patterns shifted by 0 to  $\pm a_0/2$ .
- This reduces the contrast of the fringe pattern depending on  $a_0$  and telescope separation  $B$



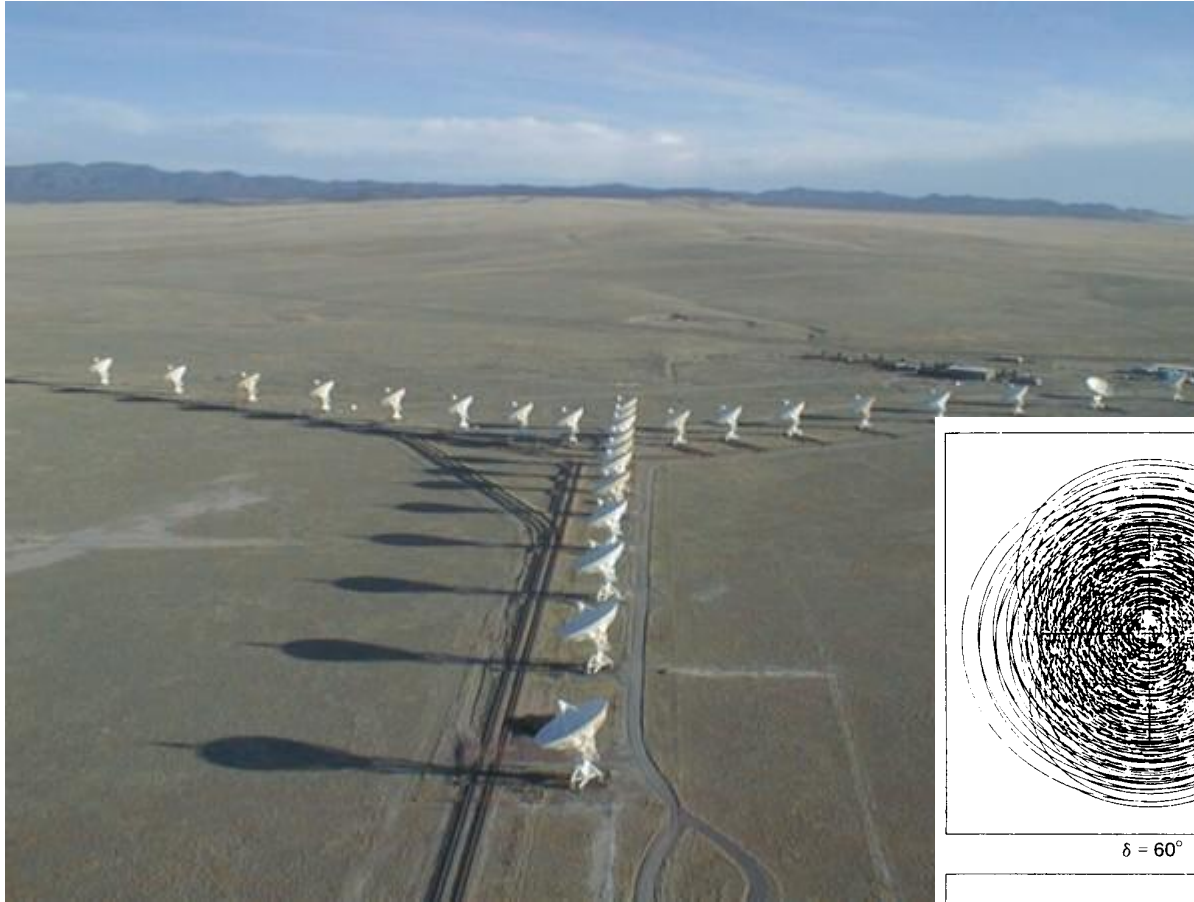
GENIE Workshop, Leiden, June 3-6, 2002

## Short aside: radio interferometry

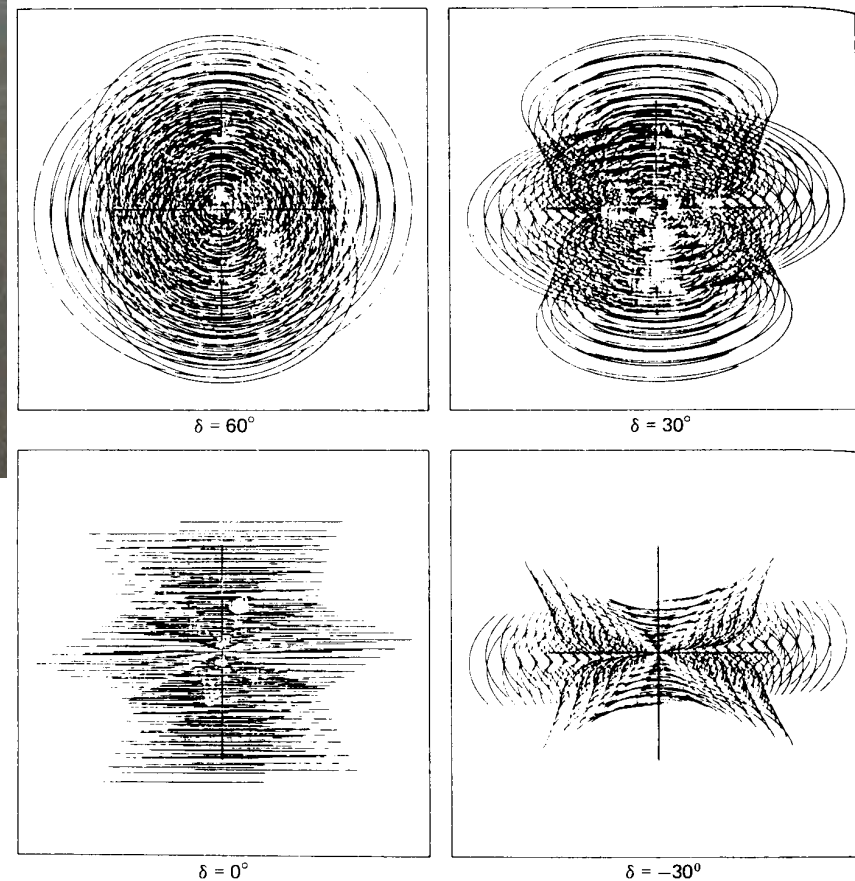


Net result: Two radio telescopes measure one Fourier component of the radio sky brightness

$$V_A \times V_B = \langle V_A \rangle \langle V_B \rangle \cos \phi ; \quad \phi = 2\pi D\theta/\lambda$$



Fourier plane coverage of VLA antennae (as Earth rotates)

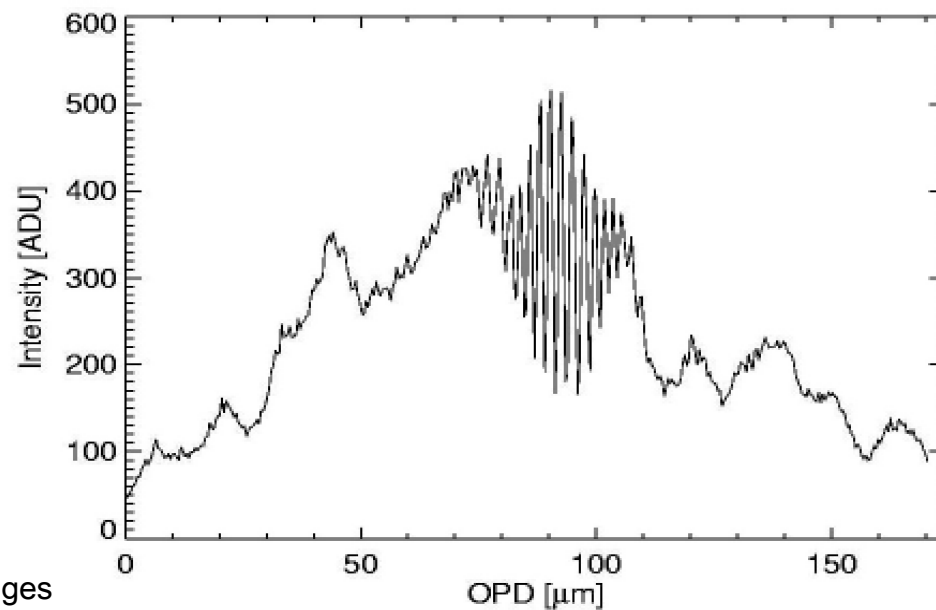


Very Large Array: combining all possible pairs samples the Fourier space quite well. This is the standard technique for making images at radio wavelengths.

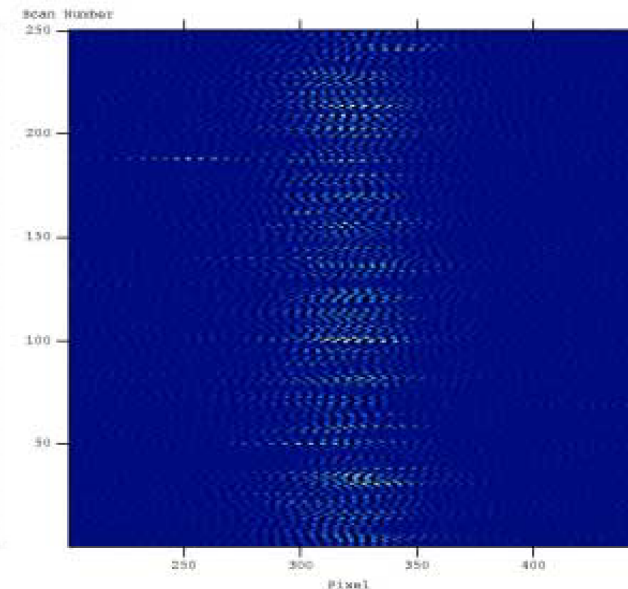
## This is much harder at optical wavelengths: Why?

- We cannot measure the phase of photons like in the radio (must allow the photons themselves to interfere rather than multiply voltage signals)
- There is a short coherence time for short  $\lambda$  photons
- Effects of rapid variation of atmospheric phase distortions

World leaders: 4x8m ESO VLT in Chile.

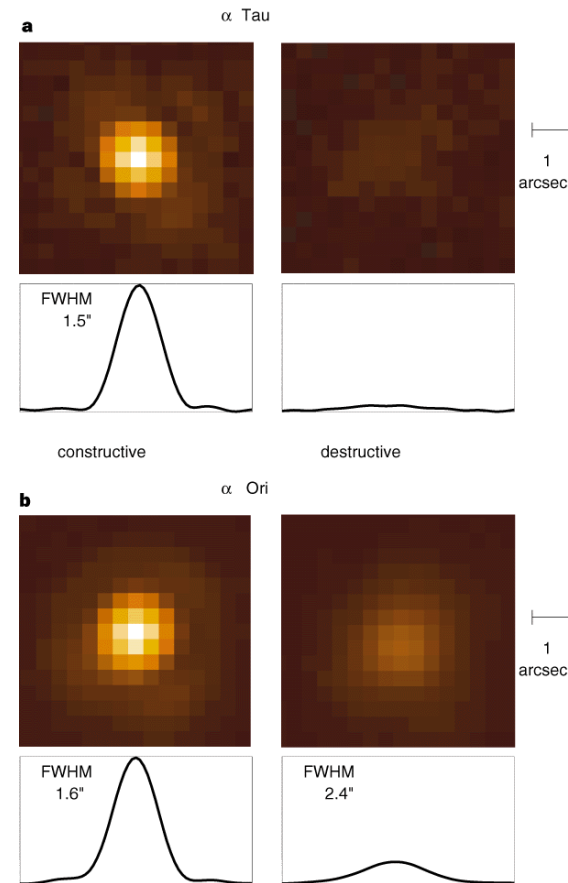
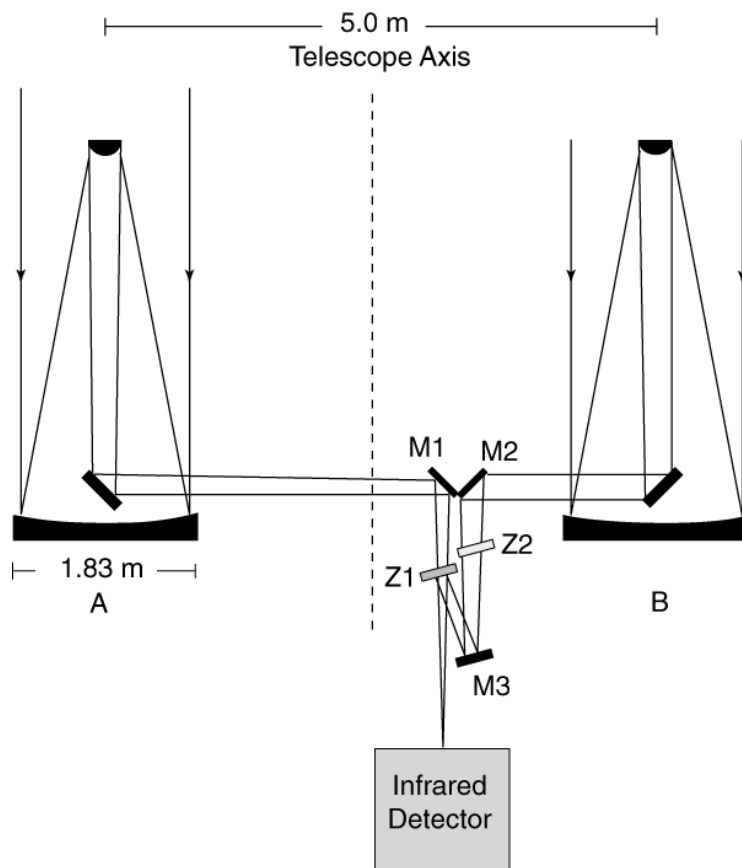


VLT fringes

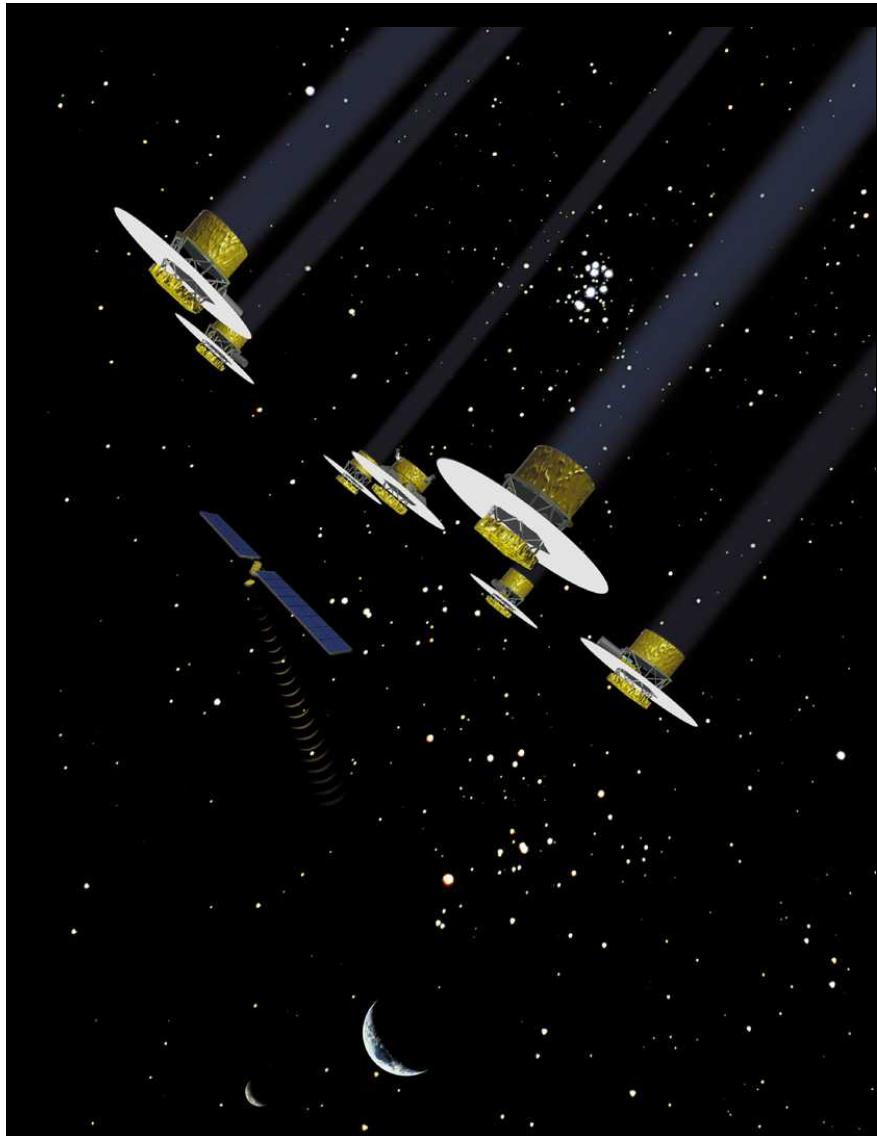


## Other clever techniques: Nulling interferometry

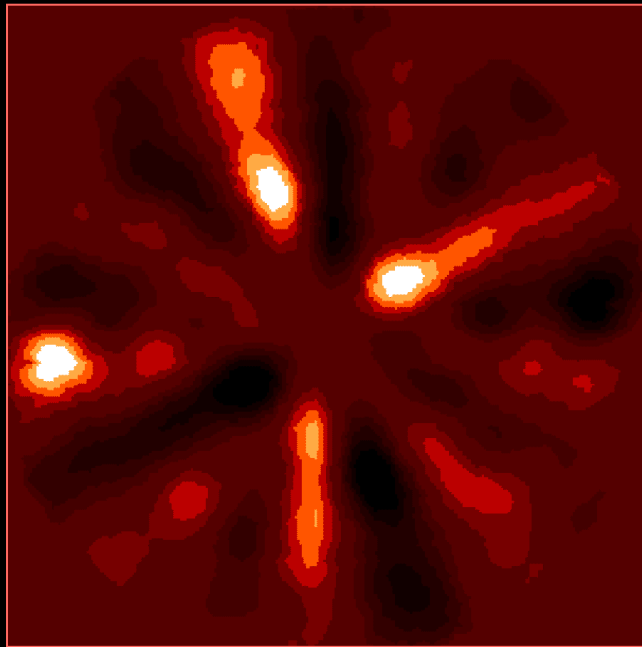
Take half of light and add  $\pm \pi$  phase. Central part of Airy disk is now a minimum and first maximum occurs where previously there was the first minimum:



Nulling interferometry

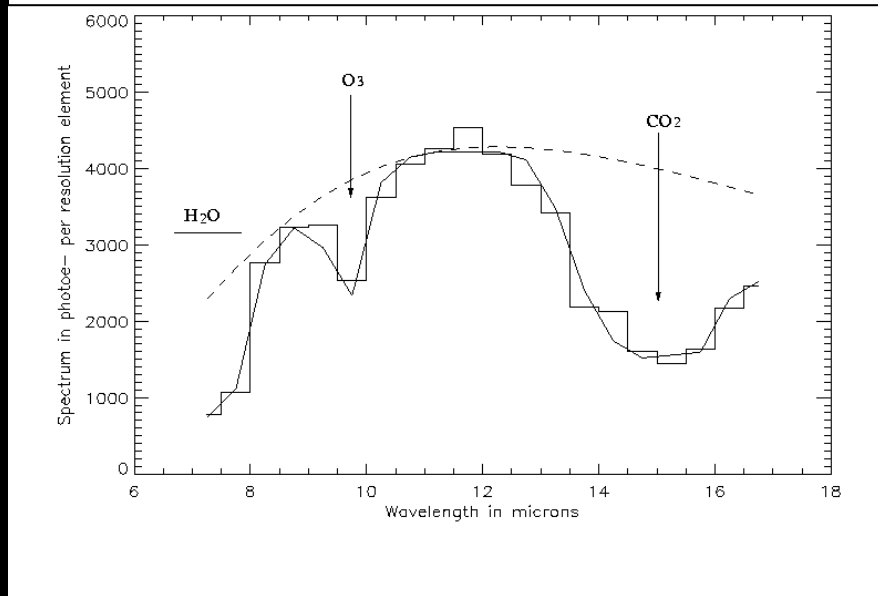


2007 Proposed ESA Darwin mission  
(no longer active due to cost)



Simulated  
Venus,  
Earth, Mars  
at 10 pc

Simulated Earth spectrum



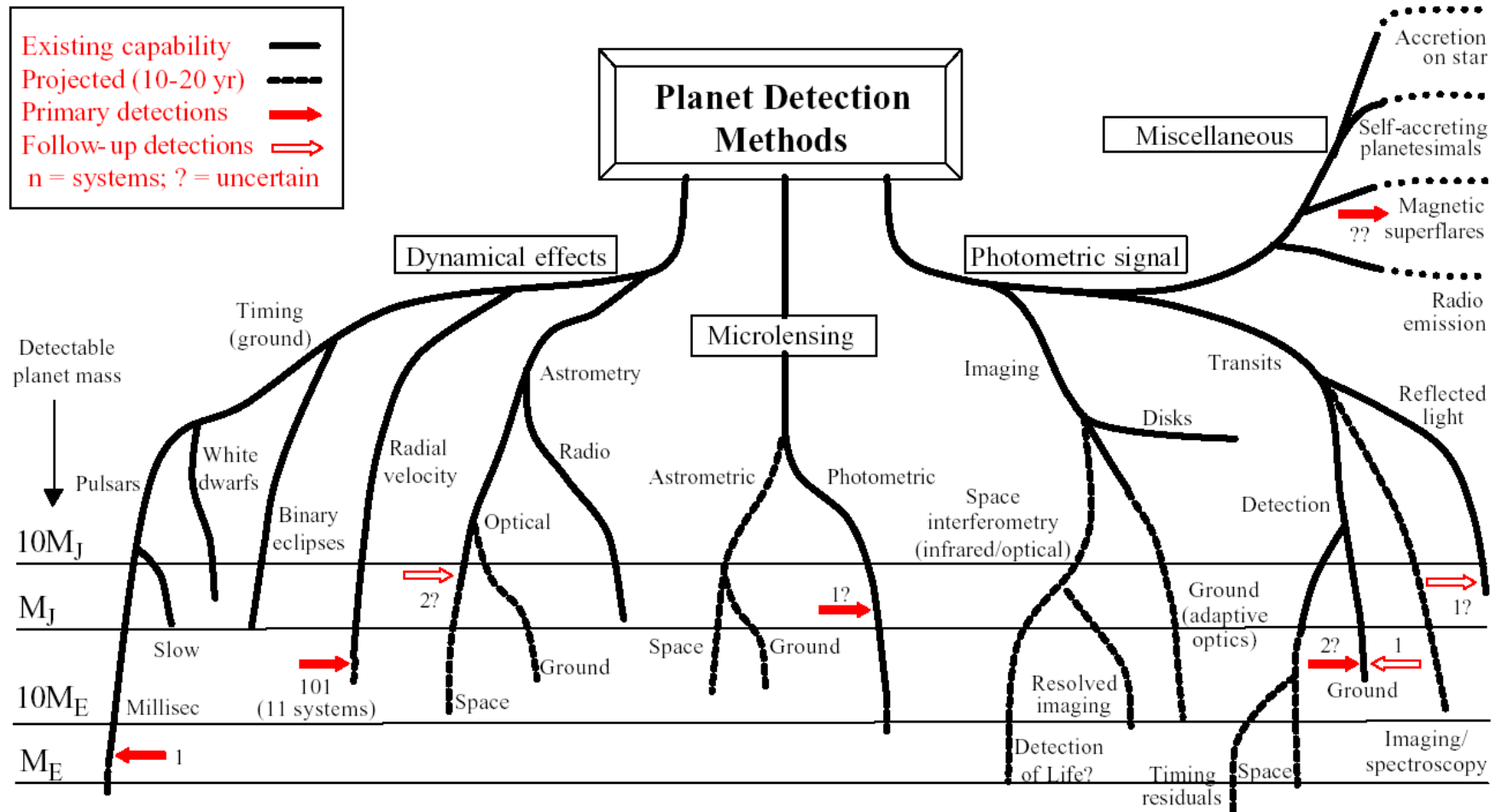


ESO 39m E-ELT artists impression: first light in 2025?



# Planet Detection Methods

Michael Perryman: Rep. Prog. Phys, 2000, 63, 1209 (updated Aug 2002)



Summary (Perryman tree)