ETH ZURICH

Simulating grating MOT designs

Author:

Johannes Eberle

Supervisors:

Gillenhaal BECK Prof. Dr. Jonathan HOME

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ETH zürich

Abstract

This report presents a simulation-based study aimed at determining the optimal parameters for a grating in a magneto-optical trap (MOT) for applications in trapped ion quantum computers. The study investigates the effects of different grating geometries and parameter configurations on the performance of the MOT.

Throughout the study, we have developed a code in a modular way, allowing for easy modifications and the addition of other grating geometries and analysis methods as needed.

By leveraging advanced simulation techniques, we have identified an optimal grating design that exhibits high grating efficiency while having minimal impact on the polarization of the laser source. Specifically, we have found a grating with cylindrical holes as unit cells that exhibits a high grating efficiency where 82.4% is emitted into the first order which is emitted at an azimuthal angle of 42.6°, while inducing only a slight change in polarization. The resulting ratio of the major to the minor axis in the polarization ellipse is r = 1.10. Additionally, we have found parameters for a blazed grating where 74% of the source power is emitted into a single order emitted at an azimuthal angle of 43.5°. In this case, the ratio of the major to the minor axis in the polarization ellipse is r = 1.3.

This finding is of importance for trapped ion quantum computers, as it provides a technique to transport ions from the source to the ion trap and eventually achieving higher ion loading efficiencies.

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1 Introduction

Trapped ion quantum computers have emerged as one of the leading platforms for realizing large-scale, fault-tolerant quantum computing. Central to the success of these systems is the precise control and manipulation of individual ions within an electromagnetic trap. One possible approach to achieving this involves utilizing a grating within the setup of the magneto-optical trap (MOT).

A grating MOT consists of two parts: the magnetic trapping and the optical trapping. To realize the latter, a diffraction grating is used which converts a single laser beam at normal incidence into several first order beams at an azimuthal angle of 45°, effectively creating a trapping potential.

This report focuses on a simulation-based study aimed at determining the optimal parameters for a grating in a magneto-optical trap (MOT) for trapped ion quantum computers. Our objective is to gain deeper insights into how different grating parameters impact the performance of the MOT.

In the forthcoming sections, we will discuss the principles of Fraunhofer diffraction, light polarization, and grating MOTs. Subsequently, we will introduce the simulation methods and the implemented code. Finally, we will present and analyze the outcomes of the simulations,

1.1 Fraunhofer diffraction

Diffraction occurs when waves encounter obstacles, pass through apertures or scatter from surfaces with periodic structures.

In general, we distinguish between two major regimes: the near field and the far field.

In the near field, which is also known as the Fresnel regime, the observation point is relatively close to the diffracting elements compared to their overall dimensions. As a result, the diffracted wave fronts remain curved, and the individual diffracted waves interfere with each other.

On the other hand, the far field, also referred to as the Fraunhofer regime, corresponds to observation points that are sufficiently far away from the diffracting element - this is described by the Fraunhofer condition:

$$N_F' = b^2 / \lambda d \ll 1,\tag{1}$$

where N'_F is the Fresnel number, d is the distance between the diffracting element and the observer, λ is the wavelength and b is the size of the diffracting element (e.g. the size of the aperture) [14]. In this regime, the wave fronts can be considered nearly planar, and the individual diffracted waves are approximately parallel (see figure 1). As a consequence, the interference patterns formed are simpler and can be described using the principles of Fourier optics. In Fourier optics, the propagation of light is described using the Fourier transform. By decomposing complex light patterns into simpler sinusoidal components through Fourier transforms, spatial frequencies are used to analyze how light propagates through optical systems, such as lenses or apertures [14]. [14].



Figure 1: Huygen's principle illustrates the formation of wavelets. In the far field, the wavefronts can be considered parallel. Figure taken from [17].

To do so, let us assume the simple case of a transmission grating at z = 0 with the aperture function

$$p(x,y) = \begin{cases} 1, & \text{inside the aperture} \\ 0, & \text{outside the aperture} \end{cases}$$
(2)

and the intensity of the incoming light is I_i . In the Fraunhofer approximation, the complex amplitude at z = d, where d is the distance from the grating, is then given by

$$g(x,y) \approx \sqrt{I_i} h_0 P(\frac{x}{\lambda d}, \frac{y}{\lambda d}),$$
(3)

where $P(\nu_x, \nu_y)$ is the Fourier transform of p(x, y) and $h_0 = \frac{i}{\lambda d} \exp(-ikd)$.

The intensity at (x, y, d) is therefore given by

$$I(x,y) = \frac{I_i}{(\lambda d)^2} \left| P(\frac{x}{\lambda d}, \frac{y}{\lambda d}) \right|^2.$$
(4)

Often, the geometry is more complex and the usage of different materials, each with unique optical properties, lead to a non-trivial transmission and therefore to a non-trivial aperture function. Hence, solving the problem analytically becomes unfeasible, and a numerical simulation is needed to determine the diffraction pattern.

We can already estimate the period of the grating by applying the grating equation, which reads [5]:

$$\sin(\theta_n) = \frac{n\lambda}{d} \tag{5}$$

that relates the emission angle θ_n of the n-th order at wavelength λ and normal incidence of light to the periodicity d of the grating (see figure 2).

We see that the range of emission angles of the first order between 40° and 50° corresponds to a period range between 550 nm and 660 nm.

1.2 Polarization

The polarization of light $\xi(\mathbf{r}, t)$ is defined as the space- and time dependent direction of the electric field [14]. For a plane wave at a fixed position \mathbf{r} , the endpoint of the polarization vector moves along an ellipse which lies in the plane that is orthogonal to the propagation direction of the electromagnetic field. The polarization ellipse - among other descriptions, such as the Poincaré sphere, can be used to characterize the polarization. In the following chapters, we will use two parameters that fully characterize the normalized polarization axis: The ratio of the major to the minor axis and the angle of the major axis relative to the axis of P-polarization. Note that we impose the condition $(a^2 + b^2) = 1$,



Figure 2: A reflective grating with incoming and outgoing rays. The path difference between two reflected rays is $d(\sin\beta + \sin\alpha)$. For constructive interference, we require this difference to be a multiple of the wavelength, such that $n\lambda = d(\sin\beta + \sin\alpha)$, where $n \in \mathbb{Z}$ is referred to as the diffraction order. For normal incidence ($\alpha = 0$) and by defining $\theta_n = \beta$, we obtain the grating equation 5. Figure taken from [13]



Figure 3: The ratio of the major axis a to the minor axis b and the angle φ of the major axis determine the shape of the ellipse.

where a and b are the lengths of the major and the minor axes, respectively. In general, the reflection off a medium is polarization-dependent, and so is also the diffraction off a reflection-grating. This needs to be considered when choosing the geometry of the grating. Circularly polarized light is defined by a ratio r = 1 of the major to the minor axis. In the following sections, this ratio will be simply referred to as "ratio".

1.3 Grating MOT

Charged ions can be confined using magnetic and electric fields [2]. This technique, however, does not work for neutral atoms. A commonly used method of confining neutral atoms is magneto-optical trapping. Here, a combination of magnetic fields and optical



Figure 4: The energy levels of the atom in a magnetic field. Figure taken from [6] with permission from Springer Nature.

forces is used to cool and confine atoms. This can be done in all three spatial dimensions. To illustrate the fundamental concept, we will focus solely on the trapping mechanism in one direction. However, the trapping in the other two dimensions functions similarly. To create a confining potential in z-direction, the magnetic field is chosen to be linearly inhomogeneous: $B(z) = B_0 z$ [6]. We now focus on an atom with a ground and an excited state. The ground state has a total angular momentum of J = 0, while the excited state has a total angular momentum of J = 1. The magnetic field introduces a location-dependent Zeeman shift of the exited state levels with $m_J = \pm 1$ and therefore lifts the degeneracy of the excited state. Additionally, two counter-propagating beams with opposite circular polarization σ_+ and σ_- are focused on the center of the trap. The beams are red-detuned by δ , such that $\omega_l + \delta = \delta_U$, where δ_U is the energy difference between the $\langle J = 0, m_J = 0 \rangle$ ground state and the $\langle J = 1, m_J = 0 \rangle$ excited state.

If an atom is located in the center of the trap, it will not experience a Zeeman shift due to the vanishing magnetic field and therefore the interaction probability between the photon and the atom remain low. If the atom is moving in $\pm z$ direction, the energy difference between the $\langle J = 1, m_J = \pm 1 |$ and the $\langle J = 1, m_J = 0 |$ state increases until it is equal to δ . It will then absorb a σ_{\mp} polarized photon that is incident from the $\mp z$ direction which results in a restoring force the center of the trap [6].

In a grating MOT, a grating is illuminated by a laser and due to diffraction, intensity peaks of higher order can be observed. In our case, we are determining an optimal grating design for which the first-order beams are high in intensity and approximately at a 45° angle to the surface normal of the grating.



Figure 5: General design of a grating MOT. The left figure depicts a linear grating and the right figure depicts a circular grating geometry. Both gratings produce a diffraction pattern that is suitable to trap ions. The red arrows show the propagation vectors of the first-order peaks. Figure taken from [7].

In 2013, Nshii et al. found that a grating of cylindrical elements (see figure 5 on the right side) achieves the highest number of trapped atoms. [7]. Based on this observation, we will simulate a grating MOT with a cylindrical grating, as depicted in figure 5. Additionally, we will simulate a cylindrical grating with a sidewall angle as well as a linear blazed grating and determine the optimal parameters for a maximal trapping efficiencies.

Lastly, the source produces circularly polarized light. The ideal gratingMOT conserves polarization and therefore, we aim to find a geometry that leaves the polarization of the first order as little affected as possible. As a figure of merit, we use the ratio of the major to the minor axis (see section 1.2), that is r = 1 for circularly polarized light, and r > 1for non-circularly polarized light.

1.4 Finite Difference Time Domain method

For the simulation, the software Lumerical was used. Specifically, the Finite Difference Time Domain (FDTD) method was used for all simulations.

The Finite-Difference Time-Domain (FDTD) method is a numerical technique used for solving Maxwell's equations in both time and space domains. It provides a powerful computational approach for simulating and analyzing a wide range of electromagnetic phenomena, such as wave propagation, scattering, and interaction with various structures [9].

The method is based on Yee's algorithm that Kane Yee introduced in 1966 [18] and that

gained popularity with increasing computing power.

In the FDTD (or Yee) method, the space volume is discretized by dividing it into a rectangular and structured mesh. For each mesh point, the time-dependent solution of Maxwell's equation, i.e. the electric and magnetic field components, are calculated [3]. By discretizing the space and time, the method approximates the continuous Maxwell's equations.

The FDTD method operates in a time-stepping manner, advancing the fields through time in small increments. At each time step, the electric and magnetic fields are updated based on their previous values and the interactions with the surrounding environment, including sources and boundaries. This iterative process allows the simulation to capture the temporal and spatial behavior of electromagnetic fields accurately. The derivatives in the equations are expressed as finite differences between neighboring mesh points [18]

One of the notable advantages of the FDTD method is its ability to handle complex geometries and material properties. It can simulate the interaction of electromagnetic fields with various objects, including metallic structures, dielectric materials, and dispersive media. This makes it a versatile tool in photonics. [9].

There are several mesh termination techniques, out of which the ABC (Absorbing Boundary Condition) and the PML (Perfectly Matched Layer) are the most common [3]. Both techniques absorb the light at the boundary, however, the PML method is generally considered the state-of-the-art [15]. A more elaborate description of these two methods and the different variations within these methods can be found in [3] and [15].

The periodic boundary is another frequently utilized mesh termination. It allows simulating a single unit cell in a periodic structure, such as a grating. The fields leaving trough one side of the cell are simply injected at the opposite side.[11]

1.5 Particle Swarm Optimization

Originally developed by James Kennedy, Russell C. Eberhart and Yuhui Shi [4] [16], the particle swarm optimization (PSO) is an optimization method that does not use the gradient of the function that is optimized. The general idea is that a swarm of particles is used to search the search space for the global maximum or minimum. An analogy in nature can be found in a bee swarm searching for the best nectar sources, where the bees communicate with each other. A particle is a point in the search space and the properties are its function value, location and velocity. At the beginning of each iteration, the particle moves one step in the search space along the velocity vector. The particle then receives information from its informants and based on this, the velocity is updated. The informants are other particles - the choice of how many particles serve as informants varies between different implementations of the PSO [1]. Specifically, it is necessary to find a balance here between the propagation speed and the diversity. A small number of informants leads to a large diversity, as the single particles are less dependent on each other. However, as less information is exchanged, the particles take more iterations to find maxima. On the other hand, a large number of informants leads to less diversity, as many particles are moving uniformly since they have the same information. However, as more information is exchanged, the particles need less iterations to find maxima. [1].

1.6 First order efficiency

The grating efficiency, or, as we will call in the following sections, first order efficiency η is defined here as $\eta = \frac{P_1}{P_{source}}$, where P_1 is the integrated intensity in the far field of the first order intensity peak with the highest intensity ¹ and P_{source} is the power of the source. In a grating where the unit cell is radially symmetric, all first order intensity peaks have the same intensity. However, in the opposite case, such as in a blazed grating, the first order peaks do not have the same intensity in general. In this case, the peak with higher intensity is determined and used for calculating the efficiency. A more elaborate discussion can be found further below. The integrated intensity is determined using the built-in grating projection functions provided by Lumerical. Specifically, the function *grating* returns the fraction of transmitted power into each grating order as a fraction of the source power. In the following sections, we use the terms "grating efficiency" and "first order efficiency" interchangeably. This choice stems from the parameter regime under consideration, where higher orders beyond the first order are significantly suppressed. As a result, the overall efficiency of the grating is primarily determined by the first order efficiency.

 $^{^{1}}$ To avoid confusion, it is important to note that the far field functions were not used in any calculation. Only the grating functions were used, which calculate the far field for a grating. More information on the differences between these two cases can be found in section 1.7

1.7 Far field

The far field is defined as the field at a distance from the grating much larger than the size of the grating. In Lumerical, there exist built-in functions to gain information on the far field - here, the distance to the grating is 1 m [8]. However, it is important to mention that when using the far field functions in Lumerical, only the reflection off a single unit cell is considered. One can choose to simulate a number of periods that are considered, however, the developers are advising to use the built-in grating projections functions [10]. For this project, only grating projection functions were used for calculations. Far field projection functions were found to give slightly different results compared to the grating projection functions, if no periodicity was chosen. With increasing number of periods in the far field projection, the peaks become sharper and equal to the grating projection.

2 Methods

The goal of the simulation is to find the optimal design of a grating MOT. This problem was approached by choosing different geometries and varying their parameters. The parameters that can be adjusted in this setting are: the period, the radius of the hole (cylindrical grating) or the width of the hole (linear grating), ² the depth of the hole, the thickness of the coating and the material of the coating. Figure 6 shows the different geometries that were used for the grating. There is a large space of possible combinations of the parameters, and it is important to understand how varying each parameter affects the diffraction pattern of the grating. Therefore, several simulations were performed, for which the results will be shown in the following chapters. To make the code easily adaptable for different geometries and future adaptations, it is built in a modular way. This means that the different parts of the simulation are written in separate scripts, which are then executed one after another by a meta-script. The separation is as follows:

- 1. Set up the model: define all physical components of the grating
- 2. Set up light sources and monitors
- 3. Set up analysis of monitor results

 $^{^{2}}$ A distinction between the hole width and the hole radius is only relevant (and only makes sense) in 3d simulations. In 2d simulations, both terms can be used interchangeably

4. Define the parameter sweep or parameter optimization

Therefore, different geometries can be simulated in the exact same way while minimizing the risk of errors caused by transferring code between different scripts.

2.1 Code implementation details

In the following, a detailed overview over each code section is given. More details can be found in the code (see appendix).

2.1.1 Metascript

The metascript calls every code block that is needed for the specific simulation. The variables for determining the specific geometry of the grating are stored in the model as user properties. This makes sure that a parameter sweep or an optimization sweep can change these properties. All code blocks are called in the setup script of the model which itself is executed in the metascript - except for the parameter sweep or optimize sweep, which are called directly in the metascript. Therefore, while performing a sweep, the user properties can be updated and since the setup script of the model is executed in every step of the sweep, the geometry is updated as well. At the end of the script, a file name and storage location is specified.

2.1.2 Set up the grating geometry

The implementation of the grating geometry is straightforward: The rectangular silicon base and the other elements of the grating are implemented as components in a structure group. The entire structure is implemented in 3d and rotated so that a 2d simulation is performed in the x-y plane and a 3d simulation is possible by extending the simulation region along the z-axis. This is necessary due to the way the simulation region is configured in Lumerical.

2.1.3 Set up light sources and monitors

All light sources and monitors are implemented in 3d and extend over a range wider than the simulation region. Two light sources are implemented as plane waves with a relative polarisation angle of 90° and a relative phase of 90° . The resulting light wave is a circularly polarised plane wave. The monitors record the field at the top end of the simulation region.

2.1.4 Analysis of monitor results

The goal of the analysis is to determine the intensity peaks in the far field and to check whether the first order intensity peak is emitted close to an angle of 45°. The code uses built-in grating functions and polarization analysis provided by Lumerical and determines all necessary information, such as the transmission of the source power into the far field, the emission angle and transmission of the first order intensity peaks as well as the polarization ellipses of all grating orders.

2.1.5 Define the parameter sweep or parameter optimization

As a final step, the parameter sweep or parameter optimization is defined. For each case, there exists a separate script where the sweep parameters and the parameter ranges are defined. A more elaborate discussion of the parameter sweeps and optimization can be found further below.

2.2 Grating geometries

2.2.1 Linear (blazed) grating

A common type of grating is the blazed grating, which resembles the shape of a sawtooth. In this context, we will not restrict ourselves to the conventional blazed grating. Instead, we will adopt a geometry similar to the one illustrated in figure 6e. It is important to note that by choosing the period to be equal to the hole width, a sawtooth geometry can be implemented. Therefore, the set of sawtooth geometries is contained within the set that we examine. The blazed grating is not radially symmetric, from which follows that the diffraction pattern is not symmetric either. The ideal diffraction pattern consists of a suppressed zeroth order peak as well as three suppressed first order peaks, while one first order peak (in our case (n, m) = (1, 0)) is maximal in intensity. An example of such a diffraction spectrum can be found in section 3. The grating needs then to be assembled similarly to the linear grating in figure 5 so that the high intensity first order peaks are directed towards the center of the trap. Simulating the grating in a 2d FDTD simulation



(e)

Figure 6: **a** - **e** show several unit cells of the grating for different grating geometries. **a** and **b** depict the circular grating that was used in the simulations. **a** shows the grating from the top-view, **b** shows a cross-section. **c** and **d** show the cylindrical grating with a sidewall angle. **e** shows the blazed grating, θ is the blaze angle. Here it can be seen that for a blaze angle of 90°, the grating is simply linear, without a blazing. Note that the sidewall angle in **c** is defined analogously to the blaze angle in **e**. The wafer consists of silicon, while the top layer is composed of a coating material.

proved to be equivalent to simulating it in a 3d FDTD simulation. This can be explained by the fact that the structure in 3d is an infinite extension of the 2d structure along the third axis. It is important to note that the 2d simulation accurately models both s- and ppolarized light, and thus also circularly polarized light. However, the built-in polarization analysis functions provided by Lumerical can only be applied in a 3d simulation.

2.2.2 Cylindrical grating (with sidewall angle)

Nshii et al. have found that the highest grating efficiency in a grating MOT is achieved with a cylindrical grating [7], as depicted on the right side of figure 5. Four unit cells of the grating and a cross-section are shown in figure 6. The cylindrical grating can be adjusted by adding a sidewall angle, analogously to the linear blazed grating. An example is depicted in figure 6d. The sidewall angle Θ is defined analogously to the blaze angle in the linear blazed grating. No 2d FDTD simulation was found to be equivalent to a 3d simulation of the structure. Therefore, it is necessary to use the 3d FDTD simulation. In the case of a grating with no sidewall angle, the optimal hole depth is $\lambda/4$ [12], where λ is the wavelength. This can be explained by the fact that a wave that is reflected at the bottom of the hole, has a phase shifted by $\lambda/2$ compared to a wave that is reflected outside the hole - leading to destructive interference.

2.3 Simulations

2.3.1 Parameter sweeps

In Lumerical, parameter sweeps can be performed, where one chooses the range of a parameter and the number of steps k. Lumerical allows for a parameter sweep of any number of parameters. It needs to be noted, however, that the number of simulations per n-parameter sweep is k^n , where k is the number of steps per sweep (the same number of steps per sweep is chosen for all simulations). Therefore, we limit ourselves to varying one or two parameters. For the 2d FDTD method, a 3-parameter sweep is feasible, however, for the 3d FDTD method, this would take too long. There exists a set of parameters where the diameter of the hole is greater than the grating period. In this regime, the structure is simply a flat surface of silicon that is coated. There are two ways for setting the period of the grating. First, the period can be set as an absolute number. Second,

it can be set as a multiple of the radius - by choosing the factor to be greater than 2, the regime can be avoided in which the diameter is greater than the period. Both ways are implemented in the code, and they can be chosen depending on whether a sweep or an optimization sweep is performed. When performing a sweep, the period is set as an absolute number for visual reasons (this makes the figures easier to read). When performing an optimization sweep, the period is set as a multiple of the diameter, since here no visualization of the optimization process is made. ³

To find optimal parameters, first the hole depth is set to 105.75 nm and the coating thickness is set to 150 nm. The selection of the coating thickness is based on the suitability for fabrication, ensuring the resulting gratings meet the necessary fabrication criteria. The hole depth is chosen to be $\lambda/4$, as it is described above, where λ is the wavelength. These values are flexible and can be adjusted as needed based on specific fabrication requirements. For the cylindrical grating, a parameter sweep over the radius of the hole and the period of the grating is performed. From this sweep, the optimal radius and period are determined. These are then used in a parameter sweep over the hole depth and the coating thickness. Finally, a sweep over the sidewall angle is performed. This determines all necessary parameters.

2.3.2 Parameter optimization

A particle swarm optimization method is provided by Lumerical. Since the coating thickness is irrelevant, as discussed in section 3, this parameter will not be included as an optimization parameter - instead a common thickness of 150 nm is chosen. The hole depth ⁴, hole width/radius and period are set as optimization parameters, i.e. the parameters that are variable throughout the search. Additionally, for the linear and cylindrical blazed grating, the blaze or sidewall angle is set as an optimization parameter. For the PSO, it is necessary to choose a particle number as well as a maximum step number. The particle number corresponds to the number of simulations that are performed in each iteration

³Alternatively, one can create a list of all possible combinations of the period and the radius, which lie outside the regime where the hole diameter is larger than the period. This list is then used for setting up the sweep over the period and the radius. This method was implemented together with a separate analysis script to post-process the results and create figures. Details as well as the code are available upon request.

⁴Below we discuss that for the silver and aluminum coating, the hole depth does not need to be included as a variational parameter. However, we are still including it. The PSO was found to converge to an optimal solution, no matter if the hole depth is included as variational parameter or not

step, while the maximum step number corresponds to the maximum number of iterations. As recommended by M. Clerc [1], a particle number of 20 is chosen for all optimizations. The maximum step number is set to 100. The value to be maximized by the PSO is the efficiency of the first order. There exists an additional condition that the emission angle of the first order intensity maximum ϕ is within the range $42^{\circ} < \phi < 48^{\circ}$. To include this constraint, the grating efficiency is set to zero for a solution that does not fulfill this condition. We have not found a way to perform the PSO on the Euler cluster of ETH and due to the high computational complexity of the 3d simulation, the PSO could be only performed for 2d simulation. The parameter ranges are shown in table 1.

Parameter	Range
Hole width	$50\mathrm{nm}-400\mathrm{nm}$
P_H	2 - 5
Hole depth	$10\mathrm{nm}-1\mathrm{\mu m}$
$ heta_f$	0 - 1

Table 1: The parameter ranges for the PSO sweep. The period P is given by $P = P_H \cdot R$, where R is the radius and the blaze angle θ is given by $\theta = \theta_F * \theta_{max}$, where θ_{max} is the angle for which the blazing forms a sawtooth shape.

3 Results

The observations mentioned here were found to be valid for all grating geometries. Details are discussed in the respective subsections. While the diffraction off the grating is dependent on the hole depth, the hole width (or radius), the period and the blaze (or sidewall) angle, it does not depend on the coating thickness. This was found by performing parameter sweeps over all mentioned parameters. Parameter sweeps over the hole depth and the coating thickness for three different coating materials can be found in figure 9. Here, the sweep is for the cylindrical geometry, however, this behavior was found for all gratings and coatings. This reduces the parameter space significantly, and the coating thickness was set to 150 nm, which is a common thickness in fabrication. An exception is the gold coating, where the first order efficiency is highest for a small coating thickness. This could be due to a reflection off the silicon for a small gold coating thickness. A further analysis was not performed, since the gold coating performs poorly at the wavelength of our setup. For all coating materials, a periodicity of the first order efficiency with respect to the hole depth was found. However, the following observation arose: by initially optimizing hole width and period with arbitrary hole depth, followed by subsequent variations in hole depth, the peak first-order efficiency consistently coincided with the originally chosen hole depth. From this, we can conclude that the hole depth can be chosen arbitrarily. By varying the hole depth, the transmission of source power into the far field is periodic, too. However, the maxima of the first order efficiency and of the transmission generally do not overlap, which is why the values of the maxima of first order efficiency vary at each period.

3.1 Linear (blazed) grating

To find optimal parameters for the linear grating, a particle swarm optimization sweep (PSO) is performed with the parameter ranges, as shown in table 1.

Coating material	Hole width	Period	Hole depth	Coat. Thick.	θ_{f}	fom
Gold	$315.49\mathrm{nm}$	632.16 nm	$186.18\mathrm{nm}$	$150\mathrm{nm}$	0.94	0.31
Silver	$281.17\mathrm{nm}$	$632.04\mathrm{nm}$	$166.58\mathrm{nm}$	$150\mathrm{nm}$	0.94	0.66
Aluminum	$178.383\mathrm{nm}$	$616.67\mathrm{nm}$	$298.75\mathrm{nm}$	$150\mathrm{nm}$	0.62	0.74

Table 2: The optimal parameters for the linear grating found with the PSO sweep for different coating materials. Coat. Thick. stands for coating thickness. θ_f denotes the fraction $\theta_f = \frac{\theta}{\theta_{max}}$, where θ denotes the blaze angle and θ_{max} is the angle for which the grating is given by a sawtooth shape. The coating thickness was fixed to 150 nm, since the diffraction is independent of the coating thickness. The figure of merit (fom) is the transmission of source power to the (n,m)=(1,0) mode. Since for the linear geometry, the maximum transmission is through this mode, this value is chosen as the figure of merit for the optimization algorithm.

The diffraction and the polarization ellipses of the first order of the best solutions that were found are shown in figure 7. We see here that aluminum gives the highest first order efficiency and that any order than (n, m) = (1, 0) is strongly suppressed. Also, a ratio of the major to the minor axis of the polarization ellipse of 1.33 is acceptable. We have therefore found a good solution to our problem.

The source light is circularly polarized. In figure 7 we see that the diffracted light is not circularly polarized anymore, which is expected and can not be avoided entirely. However, as we will show further below, the effect on the polarization is slightly larger compared to the cylindrical grating.

In the simulations, it was found that the regions of highest grating efficiency are located in a regime where the ratio is < 2. To reduce the ratio and therefore get closer to a circular polarization of the diffracted light, we would need to find a balance between the



(e) First order efficiency, aluminum coating

(f) Polarization ellipse, aluminum coating

_____Gs

_____G3

30.9592

Gs

Figure 7: The efficiencies of the diffraction orders of the best solutions that were found with the PSO algorithm for different coating materials, as well as the corresponding polarization ellipses. We find that the ratio for the gold coating is the smallest, therefore the gold coating affects the polarization the least. In the case of the aluminum coating, we find a ratio of r = 1.33, which is acceptable.

ratio and the grating efficiency. Since we have set the priority to the grating efficiency, we will not do this. However, all the tools are given in the code and one could for example do an optimization sweep with the figure of merit ⁵ set to $\frac{\eta}{r}$, where η is the grating efficiency and r is the ratio of the major to the minor axis in the polarization ellipse. Since the polarization ratio makes only sense in a 3d simulation, it is necessary to perform the PSO with 3d FDTD simulations, which was not feasible given our computational resources.

3.2 Cylindrical grating (with sidewall angle)

Since the PSO sweep could not be implemented for the ETH High-Performance-Cluster Euler, no PSO was performed for this geometry. Instead, at first, a parameter sweep over the period and the hole radius was performed (see figure 8), followed by a sweep over the coating thickness and the hole depth (see figure 9), using the optimal solution from the previous sweep. From these two sweeps, the aluminum coating proved to be performing the best. For the grating with aluminum coating, a sweep over the sidewall angle was performed, again using the optimal solution of the previous sweep. Here, an optimal solution was found, maximizing the efficiency of the first order and minimizing the ratio of the polarization ellipse. When examining figure 8, two striking observations emerge. Firstly, there exist two discontinuities at a period of ca. 400 nm and at 600 nm. This could be due to plasmonic effects or due to simulation effects. The specific reason for these two discontinuities was not found. Our optimal solutions are located close to but not directly at the discontinuities. Secondly, there are areas of maxima and minima in the first order efficiency 6 . It is important to mention that the azimuthal emission angle of the first order only depends on the period. It is independent of the hole radius (see fig. 10), hole depth and the coating thickness.

In figures 11a and 11b it is visible that there are regions of higher and lower ratio of the polarization ellipse. These figures would provide important information if we optimized for the ratio. However, since we are optimizing for a high first order efficiency, we do

⁵The figure of merit is the value that the PSO algorithm will maximize

⁶Interestingly, in all three coating materials there exists the (more or less) same parameter regime for the hole radius and the period where the first order efficiency is globally maximal. In the case of the aluminum coating, there exists one further regime with slightly smaller radius and equal peak first order intensity, which is discontinuous. For a solution in the latter regime, however, the ratio of the polarization ellipse is 1.6 and therefore higher than the ratio for a solution in the former regime, where the ratio is r = 1.1

not analyze these figures further. More important for our purpose is figure 11c, where in a final step we see that by varying the sidewall angle in order to optimize the first order efficiency, we also minimize the ratio of the polarization ellipse. This results in a solution with high first order efficiency and low ratio of the polarization ellipse of 1.10. The diffraction and the polarization ellipse of this grating are shown in figure 12.

	Hole radius	Period	Hole depth	Coating thickness
Gold coating	242.86 nm	$574.50\mathrm{nm}$	$105.75\mathrm{nm}$	10 nm
Silver coating	$250.00\mathrm{nm}$	$587.76\mathrm{nm}$	$105.75\mathrm{nm}$	$150\mathrm{nm}$
Aluminum coating	242.86 nm	$614.28\mathrm{nm}$	$105.75\mathrm{nm}$	$150\mathrm{nm}$

Table 3: The optimal parameters for the cylindrical grating for different coating materials. The coating thickness was chosen to be 150 nm, since the diffraction is independent of the coating thickness, except in the case of the gold coating. The reasons for this are not known and were not further investigated, since the gold coating performs poorly due to the low reflectivity at a wavelength of 423 nm. It is striking that the values are very similar for all coating material. From this follows that the coating material has an influence on the grating, yet the influence is limited. Furthermore, the hole depth is the same for all coating materials. This value was chosen randomly for the period-radius sweep and by optimizing the first order efficiency by varying the hole radius and the period, we already found an optimal solution. The azimuthal angles of the first order are 42.6°, 44° and 42.6° for the gold, silver and aluminum coating, respectively.

The source light is, as mentioned above, circularly polarized, and we see that the grating affects the ratio of the polarization ellipse. In figure 11a and 11b, one can see that there exist regions of higher and lower ratio. This was the case for all coatings. However, except for the sidewall angle, all parameters were chosen to maximize the first grating order efficiency, ignoring the ratio. As it is visible in figure 11c, the sidewall angle can be chosen such that the first order is still maximal, and the ratio is low. This leads to an optimal solution, with a polarization ellipse and the efficiencies of the grating as shown in figure 12. Note that the emission angle of the first order was observed to be independent of the sidewall angle.





(f) Far field transmission, aluminum coating

Figure 8: The first order efficiencies and the transmission into the far field for different coating materials. The varied parameters are the period and the radius, and the grating is cylindrical without a sidewall angle.



(e) First order efficiency, aluminum coating

(f) Far field transmission, aluminum coating

Figure 9: The first order efficiencies and the transmission into the far field for different coating materials. The varied parameters are the coating thickness and the hole depth, and the grating is cylindrical without a sidewall angle. The radius and period of the grating that resulted in maxima at the radius-period parameter sweep were utilized.



Figure 10: The azimuthal emission angle of the (n,m) = (1,0) order as a function of the hole radius and the grating period. The grating is cylindrical, and the coating is made of aluminum. It can be observed that the azimuthal emission angle only depends on the period and not on the radius.

4 Conclusion

Aluminum proved to be the most suitable coating material. We found optimal parameters for both grating geometries that we considered: one linear blazed grating and one cylindrical grating with a sidewall angle. The ratio of the major to the minor axis of the polarization ellipse in the cylindrical grating (r = 1.10) was slightly lower than in the linear grating (r = 1.3). However, one could find a solution of lower grating efficiency and lower ratio of the polarization ellipse. The tools for this are provided by the code in the appendix. This could for example be done by using as figure of merit $\frac{\eta}{r}$, where η is the first order efficiency and r is the ratio. Using several parameter sweeps, we got an understanding of how each parameter affects the diffraction, and we found the optimal parameters, which are given in table 3 and 2. The code that was developed for the simulations is provided in the appendix and may be freely used and adapted.



Figure 11: The ratio of the major to the minor axis of the polarization ellipse in the **a** radiusperiod sweep, **b** groove depth - coating thickness sweep and the **c** blaze angle fraction sweep. All three results are with the aluminum coating and cylindrical grating. In **c**, the left axis denotes the efficiency of the first order and the right axis denotes the ratio. The blazing here is in the form of a sidewall and the sidewall angle corresponds to the blazing angle in a blazed grating. A sidewall angle ratio of 1 corresponds to a geometry where the sidewall angle is such that the sidewall extends to the center point of the cylinder. In **a-b**, the color scale is logarithmic.



Figure 12: The polarization ellipse and the grating efficiency for different orders for the optimal solution of the cylindrical aluminum grating with sidewall angle.

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References

- [1] Maurice Clerc. Particle swarm optimization. ISTE, 2010.
- [2] Hans Dehmelt. A single atomic particle forever floating at rest in free space: New value for electron radius. *Physica Scripta*, 1988.
- [3] Stephen D. Gedney. Introduction to the Finite-Difference Time-Domain (FDTD) Method for Electromagnetics. Morgan & Claypool, San Rafael, California, 2011.
- [4] J. Kennedy and R. Eberhart. Particle swarm optimization. In Proceedings of ICNN'95 - International Conference on Neural Networks, volume 4, pages 1942– 1948 vol.4, 1995.
- [5] R. S. Longhurst. Geometrical and Physical Optics 2nd edition. Longman, 1967.
- [6] Harold J Metcalf and Peter Van Der Straten. Laser Cooling and Trapping. Springer, New York, NY, 1999.
- [7] C. C. Nshii, M. Vangeleyn, J. Cotter, et al. A surface-patterned chip as a strong source of ultracold atoms for quantum technologies. *Nature Nanotech 8*, page 321–324, 2013.
- [8] ANSYS Optics. Far field projections in fdtd overview. https://optics.ansys.com/hc/en-us/articles/ 360034914713-Far-field-projections-in-FDTD-overview, Accessed 2023.
- [9] ANSYS Optics. Finite difference time domain (fdtd) solver introduction. https://optics.ansys.com/hc/en-us/articles/ 360034914633-Finite-Difference-Time-Domain-FDTD-solver-introduction, Accessed 2023.
- [10] ANSYS Optics. Grating projections in fdtd overview. https://optics.ansys.com/ hc/en-us/articles/360034394354, Accessed 2023.
- [11] ANSYS Optics. Periodic boundary conditions in fdtd and mode. https://optics.ansys.com/hc/en-us/articles/ 360034382734-Periodic-boundary-conditions-in-FDTD-and-MODE, Accessed 2023.

- [12] O'Shea, Donald and Suleski, Thomas and Kathman, Alan and Prather, Dennis. Diffractive Optics: Design, Fabrication, and Test. SPIE Press, 2003.
- [13] Christopher Palmer. Diffraction Grating Handbook, 8th edition. MKS Instruments, Inc., 2020.
- [14] B.E.A. Saleh and M.C. Teich. Fundamentals of photonics, 2nd edition. John Wiley & Sons, Hoboken, New Jersey, 2007.
- [15] John B. Schneider. Understanding the finite-difference time-domain method. www. eecs.wsu.edu/~schneidj/ufdtd, 2010.
- [16] Y. Shi and R. Eberhart. A modified particle swarm optimizer. In 1998 IEEE International Conference on Evolutionary Computation Proceedings. IEEE World Congress on Computational Intelligence (Cat. No.98TH8360), pages 69–73, 1998.
- [17] Oregon State University. Single slit diffraction. https://sites.science. oregonstate.edu/~hadlekat/COURSES/ph212/waveOptics/single-slit.html, Accessed 2023.
- [18] Kane Yee. Numerical solution of initial boundary value problems involving maxwell's equations in isotropic media. *IEEE Transactions on Antennas and Propagation*, 14(3):302–307, 1966.

Appendix: Code

Meta script

```
1 newproject;
2 deleteall;
3 clear;
4 switchtolayout;
5
6 # The gold and the aluminium coating material is taken from the following
      material database. The database is available upon request.
  importmaterialdb ("/scratch/Gillen_ChipDesign/MaterialData/
7
      LumericalMaterialData.mdf");
8
10 # Input properties:
11 # grating_geometry: This defines the geometry.
12 #
         The options are: linear_one (linear blazed grating), linear_two (
      linear grating with symmetrical blazed grating)
              cylindrical_zero (cylindrical grating), cylindrical_two (
13 #
      cylindrical grating with side wall angle)
14 #
15 \# simulationdim:
                     The dimension of the simulation -2 for 2d and 3 for 3d
                          "True", if in a sweep the period itself is a
16 #
       true_period:
      parameter,
17 #
                          "False", if in a sweep the period_radiusfraction is
       a parameter
18 \# \text{ coating_material}:
                       The material of the coating
       folder_path: The absolute path of the folder in which all scripts are
19
  #
      located
  #
20
21
  22
   folder_path = "/scratch/SemesterProjects/gratingMOT/SimulationsJohannes/
23
      scripts/modular scripts V2"
   grating_geometry = "linear_one";
24
   simulationdim = 2;
25
   true_period = "False";
26
   coating_material = "Ag (Silver) - Palik (0-2um)";
27
  \#coating_material = "Au (Gold) - Palik";
28
```

```
\#coating_material = "Al (Aluminium) - Palik";
29
  sweep = "two_d_sweep";
30
   sweep = "optimize_sweep";
31
32
   adduserprop("folder_path", 1, folder_path);
33
34
   adduserprop("coating_material", 1, coating_material);
   adduserprop ("lambda_um", 2, 0.423e-6); # the wavelength of the source
35
   adduserprop ("coating_thickness", 2, 0.15e-6); # the coating thickness
36
37
   adduserprop("groove_depth", 2, 98.55e-9);
   adduserprop("hole_radius", 2, 206.54e-9);
38
   adduserprop("period_radius_fraction", 0, 656.11/206.54);
39
   adduserprop("blaze_angle_fraction", 0, 0.77);
40
   adduserprop("grating_geometry", 1, grating_geometry);
41
42
   adduserprop("simulationdim", 0, simulationdim);
   adduserprop("true_period", 1, true_period);
43
44
  45
46
47
   clearpath;
   addpath(folder_path);
48
   geometry_universal; # inserts the code of the script geometry_universal
49
      which cotains the function geometry (...)
50
   sources_and_monitors_universal; # inserts the code of the script
      sources_and_monitors_universal which contains the function
      sources_monitors (...)
   geometry ("True", grating_geometry, coating_material); # build the grating
51
   sources_monitors("True", simulationdim, true_period); #set up all sources
52
      and monitors
53
   select ("::model");
54
  # This script will be called every time the model is set up - for example
55
      in a parameter or optimization sweep
   set("Setup script", '
56
       addpath(folder_path);
57
       geometry_universal;
58
59
       sources_and_monitors_universal;
60
61
       geometry("False", grating_geometry, coating_material);
       sources_monitors("False", simulationdim, true_period);
62
```

```
31
```

```
63
   ');
   runsetup;
64
65
66
   analysis_grating;
67
   if(sweep == "two_d_sweep") {
68
69
    two_d_sweep;
70
   }
71
   else if (sweep == "optimize_sweep") {
72
    optimize_sweep;
73
   }
74
   \# save the simulation file
75
   basename = "test";
76
   f_{save_name} = folder_{path} + "/" + basename;
77
   save(f_save_name);
78
```

Geometry setup

```
1
  function geometry(firstsetup, grating_geometry, coating_material) {
2
      # input:
3
      # firstsetup: boolean
4
5
      #
                - true if this function is used to set up the geometry in a
                  new simulation
6
      #
                - false if this function is called to update parameters
7
      #
      \# grating_geometry: char string-determines the geometry of the grating;
8
         The options are: linear_one (linear blazed grating),
9
      #
10
      #
                         linear_two (linear with symmetrical blazing)
                         cylindrical_zero (cylindrical grating),
11
      #
                         cylindrical_two (cylindrical with side wall angle)
12
      #
13
      # This function can easily be extended by other geometries!
14
      #
15
      \# coating_material: char string - specifies the material of the coating
16
      #
      # output: nothing - this function builds the grating or updates all
17
18
                necessary parameters
      #
19
      20
21
      select ("::model");
```

```
32
```

```
22
        hole_radius = get("hole_radius");
        coating_thickness = get("coating_thickness");
23
24
        groove_depth = get("groove_depth");
        blaze_angle_fraction = get(" blaze_angle_fraction");
25
26
27
       # Substrate and coating layer are the same in every geometry
28
29
       if(firstsetup == "True") {
30
31
32
            addstructuregroup;
            adduserprop("coating_material", 1, coating_material);
33
            adduserprop(" hole_radius",2, hole_radius);
34
            adduserprop("coating_thickness",2, coating_thickness);
35
            adduserprop("groove_depth",2, groove_depth);
36
            adduserprop("blaze_angle_fraction",0, blaze_angle_fraction);
37
            adduserprop("firstsetup",1, firstsetup);
38
39
            set("name", "structure group");
            set("x", 0);
40
            set("y", 0);
41
            set("z", 0);
42
43
       }
       else {
44
            select ("::model::structure group");
45
            set(" hole_radius", hole_radius);
46
            set("coating_thickness", coating_thickness);
47
            set("groove_depth", groove_depth);
48
            set(" blaze_angle_fraction", blaze_angle_fraction );
49
       }
50
51
        script = '
52
            deleteall;
53
54
            if (firstsetup == "True") {
55
                addrect;
56
             set("name", "Substrate");
57
             set("material", "Si (Silicon) - Palik");
58
                set("x", 0);
59
                set("x span", 100e-6);
60
```

```
61
                 set("y", 0);
                 set("y span", 100e-6);
62
                 set("z min", -20e-6);
63
64
                 \operatorname{set}(\operatorname{"z} \max", 0);
                 set("render type", 1);
65
                 set(" detail", 0.3);
66
                 set("alpha", 0.3);
67
                 set ("override mesh order from material database", 1);
68
                 set("mesh order", 4);
69
70
71
                 addrect;
                 set("name", "coating layer");
72
                 set("material", coating_material);
73
                 set("x", 0);
74
                 set("x span", 100e-6);
75
                 set("y", 0);
76
                 set ("y span", 100e-6);
77
                 set ("z min", 0);
78
                 set("z max", coating_thickness);
79
                 set("render type", 1);
80
                 set(" detail", 0.3);
81
82
                 set ("alpha", 0.3);
                 set ("override mesh order from material database", 1);
83
                 set("mesh order", 3);
84
85
            }
            else {
86
87
                 select("structure group::coating layer");
                 set("z min", 0);
88
                 set("z max", coating_thickness);
89
90
            }
        ':
91
        \# End of first part of script, Now, the script is extended, depending
92
           on the geometry
93
        if (grating_geometry == "cylindrical_zero") {
94
             script = script + '
95
                 if (firstsetup == "True") {
96
97
                     addcircle;
                     set("name", "coating circle");
98
```

```
99
                     set("material", coating_material);
                     set("render type", 1);
100
                     set(" detail", 0.3);
101
102
                     set ("alpha", 0.3);
                     set ("override mesh order from material database", 1);
103
                     set("mesh order", 3);
104
                     set("radius", hole_radius + coating_thickness);
105
106
                     set (" z \max", 0);
                     set("z min", -1*groove_depth);
107
108
                     addcircle;
109
                     set ("name", "Vacuum circle");
110
                     set("material", "etch");
111
                     set("render type", 1);
112
                     set(" detail", 0.3);
113
                     set ("alpha", 0.3);
114
                     set ("override mesh order from material database", 1);
115
                     set("mesh order", 1);
116
                     set("radius", hole_radius);
117
                     set("z max", coating_thickness);
118
                     set("z min", coating_thickness - groove_depth); # -(
119
                         groove_depth - coating_thickness)
120
                 }
                 else {
121
                     select("structure group::coating circle");
122
123
                     set("radius", hole_radius + coating_thickness);
124
                     set("z min", -1*groove_depth);
125
                     select("structure group::Vacuum circle");
126
                     set("radius", hole_radius);
127
                     set("z max", coating_thickness);
128
129
                     set("z min", coating_thickness - groove_depth); # -(
                         groove_depth - coating_thickness);
                 }
130
         ';
131
132
        }
133
        else if(grating_geometry == "linear_one") {
134
             script = script + '
135
```
```
136
                  if (firstsetup == "True") {
137
                      addpoly;
                      set("name", "coating poly");
138
                   set("material", coating_material);
139
                   set("render type", 1);
140
                   set(" detail", 0.3);
141
                   set ("alpha", 0.3);
142
143
                   set ("override mesh order from material database", 1);
144
                   set("mesh order", 3);
145
                  x = hole_radius + coating_thickness;
                   set ("vertices", [x, 2e-6; -x, 2e-6; -x, -2e-6; x, -2e-6]);
146
                   \operatorname{set}(\operatorname{"z} \max", 0);
147
                   set("z min", -1*groove_depth);
148
149
150
                      addpoly;
                      set("name", "Vacuum poly");
151
                      set("material", "etch");
152
                      set("render type", 1);
153
                      set(" detail", 0.3);
154
                      set ("alpha", 0.3);
155
                      set ("override mesh order from material database", 1);
156
157
                      set("mesh order", 2);
                      x = hole_radius;
158
                      set ("vertices", [x,2e-6;-x,2e-6;-x,-2e-6;x,-2e-6]);
159
                      set("z max", coating_thickness);
160
                      set("z min", coating_thickness - groove_depth); # -(
161
                          groove_depth - coating_thickness)
162
163
                      # add a blaze structure
                      min_angle = atan(groove_depth / (2*hole_radius));
164
                      blaze_angle = 0.5*pi - blaze_angle_fraction * (0.5*pi - 
165
                          min_angle);
166
                      x = groove_depth/tan(blaze_angle);
167
                      addtriangle;
168
169
                      set("name", "blaze");
170
                      set("material", coating_material);
171
                      set("render type", 1);
                      set(" detail", 0.3);
172
```

```
173
                      set ("alpha", 0.3);
                      set ("override mesh order from material database", 1);
174
                      set("mesh order", 1);
175
                      set("first axis",2);
176
                      set("rotation 1",90);
177
                      set("vertices", [0,0;x,0;0,groove_depth]);
178
                      set("z max", hole_radius);
179
180
                      set("z min", -hole_radius); # -(groove_depth -
                          coating_thickness)
181
                      set("z", 0);
182
                      \operatorname{set}(\operatorname{"z span"}, 4e-6);
                      set("z",coating_thickness_groove_depth);
183
                      set("x",-hole_radius);
184
                      set("y",0);
185
                 }
186
                  else{
187
                      select("structure group::coating poly");
188
                  x = hole_radius + coating_thickness;
189
                   set ("vertices", [x, 2e-6; -x, 2e-6; -x, -2e-6; x, -2e-6]);
190
                     set("z min", -1*groove_depth);
191
192
193
                     select("structure group::Vacuum poly");
                     x = hole_radius;
194
                     set ("vertices", [x,2e-6;-x,2e-6;-x,-2e-6;x,-2e-6]);
195
                     set("z max", coating_thickness);
196
                     set("z min", coating_thickness - groove_depth); # -(
197
                        groove_depth - coating_thickness)
198
199
                     select("structure group::blaze");
                     set("vertices", [0,0;x,0;0,groove_depth]);
200
                     set("z max", hole_radius);
201
202
                     set ("z min", -hole_radius); # -(groove_depth -
                         coating_thickness);
203
                     set("z", coating_thickness-groove_depth);
204
                     set("x",-hole_radius);
             }
205
             ';
206
207
         }
208
```

```
209
         else if(grating_geometry == "linear_two") {
210
              script = script + '
211
                  if(firstsetup == "True"){
212
213
                       addpoly;
                       set("name", "coating poly");
214
                       set("material", coating_material);
215
216
                       x = hole_radius + coating_thickness;
                       set ("vertices", [x, x; -x, x; -x, -x; x, -x]);
217
218
                       \operatorname{set}(\operatorname{"z} \max \operatorname{"}, 0);
                       set("z min", -1*groove_depth);
219
                       set("render type", 1);
220
221
                       set(" detail", 0.3);
222
                       set ("alpha", 0.3);
223
                       set ("override mesh order from material database", 1);
224
                       set("mesh order", 3);
225
226
                       addpoly;
                       set("name", "Vacuum poly");
227
                       set("material", "etch");
228
                       x = hole_radius;
229
                       set("vertices", [x,x;-x,x;-x,-x;x,-x]);
230
                       set("z max", coating_thickness);
231
                       set("z min", coating_thickness - groove_depth); # -(
232
                           groove_depth - coating_thickness);
233
                       set("render type", 1);
234
                       set(" detail", 0.3);
                       set ("alpha", 0.3);
235
236
                       set ("override mesh order from material database", 1);
                       \operatorname{set}(\operatorname{"mesh} \operatorname{order"}, 2);
237
238
239
                       # add a blaze structure
                       min_angle = atan(groove_depth / hole_radius);
240
                       blaze_angle = 0.5*pi - blaze_angle_fraction * (0.5*pi - 
241
                           min_angle);
242
                       x = groove_depth/tan(blaze_angle);
243
244
                       addtriangle;
                       set("name", "blaze");
245
```

```
246
                      set("material", coating_material);
                      set("vertices", [0,0;x,0;0,groove_depth]);
247
                      set("z max", hole_radius);
248
                      set("z min", -hole_radius); # -(groove_depth -
249
                         coating_thickness)
                      set("z", coating_thickness-groove_depth);
250
                      set ("x",-hole_radius);
251
252
                      set("y",0);
253
                      set("render type", 1);
254
                      set(" detail", 0.3);
                      set ("alpha", 0.3);
255
                      set ("override mesh order from material database", 1);
256
                      set("mesh order", 1);
257
                      set("first axis",2);
258
259
                      set ("rotation 1", 90);
260
                     # add a second blaze structure
261
262
                      addtriangle;
                      set("name", "second blaze");
263
264
                      set("material", coating_material);
                      set ("vertices", [-x,0;0,0;0,\text{groove_depth}]);
265
266
                      set("z max", hole_radius);
                      set("z min", -hole_radius); # -(groove_depth -
267
                         coating_thickness)
268
                      set("z", coating_thickness-groove_depth);
                      set("x", hole_radius);
269
270
                      set("y",0);
                      set("render type", 1);
271
272
                      set(" detail", 0.3);
                      set ("alpha", 0.3);
273
                      set ("override mesh order from material database", 1);
274
275
                      set("mesh order", 1);
                      set("first axis",2);
276
277
                      set ("rotation 1", 90);
                 }
278
                 else {
279
280
                      select("structure group::coating poly");
281
                     x = hole_radius + coating_thickness;
                      set ("vertices", [x, x; -x, x; -x, -x; x, -x]);
282
```

```
283
                     set("z min", -1*groove_depth);
284
                     select("structure group::Vacuum poly");
285
                     x = hole_radius;
286
                     set("vertices", [x,x;-x,x;-x,-x;x,-x]);
287
                     set("z max", coating_thickness);
288
                     set("z min", coating_thickness - groove_depth); # -(
289
                         groove_depth - coating_thickness);
290
291
                     min_angle = atan(groove_depth / hole_radius);
                     blaze_angle = 0.5*pi - blaze_angle_fraction * (0.5*pi - 
292
                         min_angle);
293
                     x = groove_depth/tan(blaze_angle);
294
295
                     select("structure group::blaze");
                     set ("vertices", [0,0;x,0;0,groove_depth]);
296
                     set("z max", hole_radius);
297
                     set("z min", -hole_radius); # -(groove_depth -
298
                         coating_thickness)
299
                     set("z", coating_thickness_groove_depth);
                     set("x",-hole_radius);
300
301
                     select("structure group::second blaze");
302
                     set ("vertices", [-x,0;0,0;0,\text{groove_depth}]);
303
304
                     set("z max", hole_radius);
                     set("z min", -hole_radius); # -(groove_depth -
305
                         coating_thickness)
306
                     set("z", coating_thickness_groove_depth);
307
                     set("x", hole_radius);
308
                 }
             ';
309
310
311
        }
        else if(grating_geometry == "cylindrical_two") {
312
             script = script + '
313
                 if (firstsetup == "True") {
314
315
                     addcircle;
                     set("name", "coating circle");
316
                     set("material", coating_material);
317
```

```
318
                     set("radius", hole_radius + coating_thickness);
                     \operatorname{set}(\operatorname{"z} \max", 0);
319
320
                     set("z min", -1*groove_depth);
321
                     set("render type", 1);
322
                     set(" detail", 0.3);
                     set ("alpha", 0.3);
323
                     set ("override mesh order from material database", 1);
324
325
                     set("mesh order", 3);
326
327
                     addcircle;
                     set("name", "Vacuum circle");
328
                     set("material", "etch");
329
330
                     set("radius", hole_radius);
                     set("z max", coating_thickness);
331
332
                     set("z min", coating_thickness - groove_depth); # -(
                        groove_depth - coating_thickness);
333
                     set("render type", 1);
334
                     set(" detail", 0.3);
                     set ("alpha", 0.3);
335
336
                     set ("override mesh order from material database", 1);
                     set("mesh order", 2);
337
338
                    # add polygon toroid
339
                     theta_start = 0;
340
                     theta_stop = 360;
341
342
                     material = coating_material;
343
                     resolution = 1000;
344
                     radius = hole_radius;
345
346
                    347
                    # General polygon toroid
348
                    # This object created a 3D structure by revolving an
                        arbitrary outline,
349
                    \# as defined by a set of polygon vertices, around the Z
                        axis with a radius R.
350
                    # The vertices of the polygon shape can be defined
                        following the
351
                    # instructions at http://docs.lumerical.com/en/fdtd/
                        user_guide_set_polygon_vertices.html
```

352	#
353	# Input properties
354	# theta start: starting angle of toroid
355	# theta stop: stopping angle of toroid
356	# radius: distance from the center of the toroid to
	the center of
357	# the each slice that makes up the toroid
358	# material: material of object
359	# resolution: number of slices that make up overall shape
360	#
361	# Tags: toroid ring general custom polygon
362	#
363	# Copyright 2010 Lumerical Solutions Inc
364	#####################################
365	
366	# USER specifies polygon vertices here. The 3D structure will be created by revolving this shape around Z axis,
	with a radius R.
367	# Note: It is OK, but not necessary to close the polygon
368	<pre>min_angle = atan(groove_depth / hole_radius);</pre>
369	<pre>blaze_angle = 0.5*pi - blaze_angle_fraction * (0.5*pi - min_angle);</pre>
370	$x = groove_depth/tan(blaze_angle);$
371	
372	V=matrix(4,2);
373	V(1,1:2) = [-x,0];
374	$V(2,1:2) = [0, groove_depth];$
375	V(3,1:2) = [0, 0];
376	V(4,1:2) = [-x,0];
377	
378	
379	<pre>#plot(pinch(V,2,1)*1e6,pinch(V,2,2)*1e6,"x (um)","y (um)"," Polygon outline"); # plot vertices (for debugging)</pre>
380	
381	
382	# calculate slice thickness
383	<pre>th = 4*pi*radius/resolution; # divide circumference by resolution</pre>
384	th = th * 1.1; # scale up thickess slightly. Required

```
when polygon vertices extend beyond zero, which
                          increases the maximum radius.
385
386
                     \# if partial revolution, use only a fraction of slices
                      resolution=round(resolution*abs(theta_start-theta_stop)
387
                          (360):
388
389
                     # Calculate revolution angle vector
390
                      theta = linspace(theta_start*pi/180,theta_stop*pi/180,
                          resolution);
391
                      for (i=1:resolution) {
392
393
                          addpoly;
394
                          set("name", "coating blazing");
395
                          set("vertices",V);
                          set("first axis","x");
396
397
                          set("rotation 1", 90);
398
                          set("second axis","z");
                          set ("rotation 2", theta(i) *180/pi);
399
400
                          set("x", radius * cos(theta(i)));
                          set("y", radius*sin(theta(i)));
401
402
                          set("z min", -th/2 + coating_thickness - groove_depth);
403
                          set("z max",th/2 + coating_thickness - groove_depth);
404
405
                          set(" material", material);
                          set ("override mesh order from material database", 1);
406
407
                          set("mesh order", 1);
                  }
408
                 }
409
410
                 else {
                      select("structure group::coating circle");
411
412
                      set("radius", hole_radius + coating_thickness);
413
                      \operatorname{set}(\operatorname{"z} \max", 0);
                      set("z min", -1*groove_depth);
414
415
                      select("structure group::Vacuum circle");
416
                      set("radius", hole_radius);
417
                      set("z max", coating_thickness);
418
419
                      set("z min", coating_thickness - groove_depth); # -(
```

		$groove_depth - coating_thickness);$
420		
421		<pre>select("structure group::coating blazing");</pre>
422		#perform same calculations as above
423		<pre>min_angle = atan(groove_depth / hole_radius);</pre>
424		$blaze_angle = 0.5*pi - blaze_angle_fraction * (0.5*pi - $
		<pre>min_angle);</pre>
425		$x = groove_depth/tan(blaze_angle);$
426		V=matrix(4,2);
427		V(1, 1:2) = [-x, 0];
428		$V(2,1:2) = [0, groove_depth];$
429		V(3,1:2) = [0, 0];
430		V(4, 1:2) = [-x, 0];
431		th = 4*pi*radius/resolution; # divide circumference by
		resolution
432		th = th * 1.1; # scale up thickess slightly. Required
		when polygon vertices extend beyond zero, which
		increases the maximum radius.
433		$resolution = round(resolution*abs(theta_start-theta_stop)$
		/360);
434		theta = linspace(theta_start*pi/180,theta_stop*pi/180,
		resolution);
435		set("vertices",V);
436		set ("rotation 2", theta(i) *180/pi);
437		set ("x", radius * cos (theta (i)));
438		set ("y", radius * sin (theta(i)));
439		$set("z min", -th/2 + coating_thickness - groove_depth);$
440		$set("z max", th/2 + coating_thickness - groove_depth);$
441		}
442		';
443	}	
444		
445	5	<pre>select ("::model::structure group");</pre>
446	5	<pre>set("first axis", 2); # first axis is x axis</pre>
447	5	set("rotation 1", 270);
448	5	<pre>set("script", script);</pre>
449	}	

Sources and monitors setup

1 function sources_monitors(firstsetup, dimension, trueperiod) { 23 # input: 4 # firstsetup: boolean - true if this function is used to set up the geometry in a new simulation 5# - false if this function is called to 6 # 7 # update parameters 8 # dimension: integer - the dimension of the FDTD simulation region The options are: 2(2D) or 3(3D)9 # trueperiod: char string - specifies whether the 10 # 11 period_radius_fraction is used for # 12# determining the period or whether the 13period is set as an absolute number. # This information is necessary for 14# 15updating the FDTD simulation region # in parameter sweeps 16# 17# - "true" if the period is set an an absolute number - "false" if set by the period_radius_fraction 18 # 19# # output: nothing – this **function** sets up the monitors or updates 2021all necessary parameters # 22# This function can easily be extended by other monitors! 232425select ("::model"); 26 $lambda_um = get("lambda_um");$ 27coating_thickness = get("coating_thickness"); $groove_depth = get("groove_depth");$ 28hole_radius = get("hole_radius"); 29period_radius_fraction = get("period_radius_fraction"); 30 31 blaze_angle_fraction = get(" blaze_angle_fraction"); 32 $lambda_um = get("lambda_um");$ 33 34period = period_radius_fraction * hole_radius; 35if(firstsetup == "True") { 36 #add a plane wave source 37 addplane; 38

```
set("injection axis", "y");
39
            set("direction", "backward");
40
            set("x", 0);
41
            set ("x span", 100e-6);
42
            set("z", 0);
43
            set("z", 0);
44
            set("z span", 100e-6);
45
            set("wavelength start", lambda_um);
46
            set("wavelength stop", lambda_um);
47
            set(" polarization angle", 90);
48
            set ("phase", 90);
49
            set("y", coating_thickness + 1e-6);
50
51
52
            #add a second plane wave source
53
            addplane;
54
            set("injection axis", "y");
55
            set(" direction", "backward");
56
            set("x", 0);
57
            set("x span", 100e-6);
58
            set("z", 0);
59
60
            set("z span", 100e-6);
            set("wavelength start", lambda_um);
61
            set("wavelength stop", lambda_um);
62
            set("y", coating_thickness + 1e-6);
63
64
65
66
67
            #add a power monitor
68
69
            addpower;
70
            set("name", "3dpowermonitor");
            if (dimension==3){
71
                set ("monitor type", 8); # 3d
72
                set ("y span", 0);
73
74
            }
            else{
75
76
                set ("monitor type", 6); # 2d y normal
            }
77
```

```
78
             set("x", 0);
 79
             set("x span", 100e-6);
             set("y", coating_thickness + 1.2e-6);
 80
 81
             set("z", 0);
             set("z span", 100e-6);
 82
             set("override global monitor settings", 1);
 83
             set("use source limits", 0);
 84
             set("frequency points", 1);
 85
             set("wavelength center", lambda_um);
 86
             set("wavelength span", 0);
87
 88
 89
 90
 91
             #add a side view power monitor
 92
             addpower;
             set("name", "sideview");
 93
 94
             set("monitor type", 7); # 2d z normal
             set("x", 0);
 95
             set("x span", 10e-6);
 96
97
             set("y", 0);
             set ("y span", 10e-6);
98
99
             set("z", 0);
             set("override global monitor settings", 1);
100
             set("use source limits", 0);
101
102
             set("frequency points", 1);
             set("wavelength center", lambda_um);
103
104
             set("wavelength span", 0);
105
106
107
108
109
             \# add the simulation region
             addfdtd;
110
             set ("dimension", dimension -1); # 1 = 2D, 2 = 3D
111
             set("x", 0);
112
113
             set("z", 0);
             set("x min bc", "Periodic");
114
             set("y min bc", "PML");
115
             set("y max bc", "PML");
116
```

```
117
             if(dimension == 3) {
                 set("z max bc", "Periodic");
118
                 set("z min bc", "Periodic");
119
120
             }
             set("x span", period);
121
             set("y min", -1.0 * (groove_depth + 0.5e-6));
122
             set("y max", coating_thickness + 1.3e-6);
123
             set("z span", period);
124
             set("mesh accuracy", 4);
125
126
        }
        else {
127
             select("3dpowermonitor");
128
129
             set("y", coating_thickness + 1.2e-6);
130
             select("FDTD");
131
             if(trueperiod == "False") {
132
133
                 set("x span", period);
                 set("z span", period);
134
             }
135
             set("y min", -1.0 * (groove_depth + 0.5e-6));
136
             set("y max", coating_thickness + 1.3e-6);
137
138
139
             select("source");
             set("y", coating_thickness + 1e-6);
140
141
             select("source_1");
142
             set("y", coating_thickness + 1e-6);
143
        }
144
145 }
```

Analysis scripts

```
1
  mname = "::model::3 dpowermonitor";
   select ("::model::FDTD");
2
   dimension = get("dimension");
3
4
   select ("::model");
   lambda_um = get("lambda_um");
5
6
7
8
  9
  # all analysis scripts are set up in this script:
       1. Grating Transmission (Lumerical built-in plus own code)
10
  #
      2. Polarization Ellipse (Lumerical built-in)
11
   #
12
  #
  # Results:
13
14
   #
       Grating Transmission:
           T:
               total transmitted power vs frequency. Will be negative for
  #
15
               power flowing in negative direction
16
  #
           T_grating:
                      (3D) fraction of source power transmitted to each
17
  #
18
  #
                       grating order, S & P polarization components, direction
                       cosine vectors, and theta, phi angles
19
  #
           T_grating: (2D) fraction of source power transmitted to each
20
  #
                       grating order, S & P polarization components,
21
   #
22
   #
                       and theta angle
           num_orders: the number or orders that were detected
23
   #
      first_order_efficiency: fraction of far field power transmitted to
24
   #
                                   the (n,m) = (1,0) mode
25
   #
                        for 2D: Can be set to 0 outside a range of
26
  #
                                   angles that are desired; The code for this
27
  #
                                   can be commented/uncommented further below!
28
   #
29
   #
      first_order_theta: emission angle of the (n,m) = (1,0) mode
      first_order_efficiency_normalized: fraction of source power
30
  #
                                              transmitted to the
31
  #
  #
                                              (n,m) = (1,0) \mod 1
32
33
  #
       Polarization ellipse:
34
  #
           Gs_plot, Gp_plot: returns polarization in S and P direction for all
35
  #
                             orders as a function of lambda
36
  #
      num_orders: returns the number of valid grating order vs lambda
37
  #
                        (may also include orders due to numberical error, e.g.
38
  #
```

```
G=10^{-30}
39
  #
           pol: contains the fraction transmitted power (G), phase differece
40
  #
                in s and p polarization (phase_diff), polarization handedness
41
  #
  #
                (pol_handed), angle of major axis (major_angle) and ratio of
42
                major/minor axis (ratio) for all grating orders and
43
  #
                wavelengths.
44
  #
           ratio_1_0: returns the ratio of the major to the minor axis for
45
  #
46
  #
                      the (n,m) = (1,0) mode
  47
48
49
   addanalysisgroup;
50
51
   set("name", "Grating Transmission");
52
   set ("x", 0);
  set("y", 0);
53
  set ("z", 0);
54
   adduserprop("normal", 1, "y");
55
   adduserprop("x span", 2, 5e-6);
56
   adduserprop("y span",2,0);
57
   adduserprop ("z span", 2, 5e-6);
58
   addanalysisprop("make plots", 0, 0);
59
60
   addanalysisprop("n target", 0, 1);
   addanalysisprop("m target", 0, 0);
61
   addanalysisprop("lambda target", 2, lambda_um);
62
   addanalysisresult ("T");
63
   addanalysisresult ("T_grating");
64
   addanalysisresult ("num_orders");
65
66
   addanalysisresult (" first_order_efficiency ");
   addanalysisresult ("first_order_theta");
67
   addanalysisresult ("first_order_efficiency_normalized");
68
69
70
71
   analysis_script = '
72
      mname = "::model::3 dpowermonitor";
73
74
75
      76
      # Grating transmission
```

. ,

77 # This object calculates the fraction of source power transmitted to 78# each grating order (total, S and P polarization) at all frequency # points recorded by the monitor. It also calculates the number of 79 # propagating grating orders 80 81 # 82 # Input properties make plots: 1 to make plots, 0 otherwise 83 # n,m target: grating order to plot. These parameters only affect 84 # 85 the plots. They do not affect the output results. # lambda target: wavelength to plot. These parameters only affect 86 # the plots. They do not affect the output results. 87 # # Output properties 88 T(f): total transmitted power vs frequency. Will be negative for 89 # 90 power flowing in negative direction # 91 # T_grating(n,m,f): (3D) fraction of source power transmitted to each grating order, S&P polarization components, 92# direction cosine vectors, and theta, phi angles 93 # T_{-} grating (n, f): (2D) fraction of source power transmitted to each 94# 95 # grating order, S & P polarization components, and theta angle # 96 num_orders(f): number of supported grating orders 97# 98 # # Notes 99 - grating_S, grating_P are normalized so that $|grating_S|^2$ gives 100# 101 the fraction of the source power to each grating order that is # S polarized. $|\text{grating}_S|^2 + |\text{grating}_P|^2 = T_{\text{grating}}$. 102# 103- Interpretation of results for various monitor orientations for # 3D simulations: 104 # 105XY plane: n, U1 correspond to X axis. m, U2 correspond to Y axis # XZ plane: n, U1 correspond to X axis. m, U2 correspond to Z axis 106 # YZ plane: n, U1 correspond to Y axis. m, U2 correspond to Z axis 107 # 108 # 109# Tags: far field grating order transmission # Copyright 2016 Lumerical Solutions Inc 110 111 112 113114 # simplify input variable names by removing spaces 115

51

```
116
         make_plots = \%make_plots\%;
         n_target = \% n_target\%;
117
         m_{target} = \% m target\%;
118
         lambda_target = %lambda target%;
119
120
        # specify monitor name
121
        mname="::model::3 dpowermonitor";
122
123
124
        # get frequency vector
125
         f=getdata(mname, "f");
         size_f = length(f);
126
127
        # get total net power transmitted through monitor
128
129
        T=transmission(mname);
130
         if (getdata(mname," dimension") == 3) { # 3D simulation
131
132
133
             # find the maximum possible number of grating orders
134
             # this occurs at the maximum frequency
135
             n = gratingn(mname, size_f);
136
137
            m=gratingm(mname, size_f);
138
             size_n = length(n);
139
             size_m = length(m);
140
             # initialize matrices
141
142
             T_grating
                         = matrix(size_n, size_m, size_f); # grating order
                strength vs f
143
             grating_S
                         = matrix(size_n, size_m, size_f); # |grating_S|^2 gives
                the fraction of the source power to each grating order that is S
                 polarized
144
             grating_P
                        = matrix(size_n, size_m, size_f); # |grating_P|^2 gives
                the fraction of the source power to each grating order that is P
                  polarized
                         = matrix(size_n, size_m, size_f); # first direction
145
             U1
                         (if monitor is in XY plane, this corresponds to Ux)
                cosine
146
             U2
                          = matrix(size_n, size_m, size_f); # second direction
                         (if monitor is in XY plane, this corresponds to Uy)
                cosine
147
```

52

```
148
             # loop over each frequency point
149
              for (i=1:size_f) {
150
151
                  # get the grating numbers at this frequency
152
153
                  n_{tmp} = gratingn(mname, i);
154
                  m_{tmp} = gratingm(mname, i);
155
156
                  # calculate indices for inserting these results into final
                      matrix
                         = find (n, n<sub>t</sub>mp(1));
157
                  n1
                         = find (n, n_tmp(length(n_tmp)));
158
                  n2
                         = find (m, m<sub>-</sub>tmp(1));
159
                  m1
160
                  m^2
                         = find (m, m_tmp(length(m_tmp)));
161
                  # calculate grating order angles (direction cosine units)
162
                  \# and save into U1, U2 matrix.
163
                  \# set unused orders to -1 or +1
164
165
                  \mathbf{u1}
                                  = matrix (size_n);
                                  = matrix(size_m);
166
                  u2
167
                  u1(1:n1)
                                  =-1;
                  u2(1:m1)
168
                                  =-1;
169
                  u1(n2:size_n) = 1;
170
                  u2(m2:size_m) = 1;
171
                  u1(n1:n2)
                                = gratingu1(mname, i);
                  gratingu2(mname, i);
172
173
                  u2(m1:m2)
                                  = gratingu2 (mname, i);
                  U1(1:size_n, 1:size_m, i) = meshgridx(u1, u2);
174
175
                  U2(1:size_n, 1:size_m, i) = meshgridy(u1, u2);
176
177
                  # calculate grating orders and save into T_grating matrix
178
                  grating_temp
                                                = gratingpolar(mname, i);
179
                                               = grating_temp * sqrt(abs(T(i))); #
180
                  grating_temp
                      normalize result such that sum of all grating orders of |
                      Etheta|^2 + |Ephi|^2 equals
181
                                   \# the fraction of source power transmitted
                                       through the monitor.
182
                  \operatorname{grating}_{S}(n1:n2,m1:m2,i) = \operatorname{pinch}(\operatorname{grating}_{temp},3,3);
                                                                                      # |
```

	$\operatorname{grating}_S ^2$ gives the fraction of the source power to each
	grating order that is S polarized
183	$grating_P(n1:n2,m1:m2,i) = pinch(grating_temp,3,2); \# $
	grating_ $P \mid 2$ gives the fraction of the source power to each
	grating order that is P polarized
184	$T_{grating}(n1:n2,m1:m2,i) = abs(pinch(grating_temp,3,2))^2 +$
	$abs(pinch(grating_temp, 3, 3))^2; \# fraction of source power$
	to each grating order
185	
186	}
187	
188	# calculate U3 and convert grating directions to theta, phi. If
	monitor is in XY plane, U3=Uz
189	$U3 = sqrt (1-U1^2-U2^2);$
190	theta = real ($a\cos(U3)$) * $180/pi$;
191	phi = atan2(U2,U1) * 180/pi;
192	
193	
194	# Calculate the number of grating orders (theta < 90)
195	# NOTE: this script for counting grating orders assumes a
	rectangular
196	# unit cell. The count will not be correct for triangular lattices.
197	$num_orders_matrix = sum(sum((real(theta) < 89.9) , 2), 1);$
198	
199	$T_matrix=T;$
200	$T_{grating_matrix} = T_{grating};$
201	
202	T = matrixdataset("T");
203	T. addparameter ("lambda", c/f , "f", f);
204	T. addattribute ("T", T_matrix);
205	
206	<pre>num_orders = matrixdataset("num_orders");</pre>
207	$num_orders.addparameter("lambda", c/f,"f", f);$
208	<pre>num_orders.addattribute("num_orders", num_orders_matrix);</pre>
209	
210	$T_{-}grating = matrixdataset("T_{-}grating");$
211	$T_{grating}$. addparameter ("n", n);
212	$T_{-}grating.addparameter("m",m);$
213	$T_{grating}$. addparameter ("lambda", c/f, "f", f);

214	$T_{grating}$. addattribute (" $T_{grating}$ ", $T_{grating}$ matrix);
215	T_grating.addattribute("grating_S",grating_S);
216	T_grating.addattribute("grating_P",grating_P);
217	T_grating.addattribute("U1",U1);
218	T_grating.addattribute("U2",U2);
219	T_grating.addattribute("U3",U3);
220	T_grating.addattribute("theta",theta);
221	T_grating.addattribute("phi",phi);
222	
223	
224	if (make_plots) {
225	
226	# plot number of orders
227	plot(c/f*1e6, num_orders_matrix,
228	"wavelength (um)",""," Number of grating orders");
229	
230	
231	# plot data for a particular grating order
232	$T_grating_plot = pinch(pinch(T_grating_matrix, 2, find(m, m_target))$
)) ,1, find(n, n_target));
233	theta_plot = pinch(pinch(theta, 2, find(m, m_target)) , 1,
	$find(n, n_target));$
234	$phi_plot = pinch(pinch(phi, 2, find(m, m_target))), 1,$
	$find(n, n_target));$
235	
236	$plot(c/f*1e6, abs(T_matrix), T_grating_plot,$
237	"wavelength (um)", "Transmission", "Transmission");
238	legend ("Total", "To order ("+num2str(n_target)+", "+num2str(
	m_target)+")");
239	$plot(c/f*1e6, theta_plot, phi_plot,$
240	"wavelength (um)", "angle (deg)", "Propagation direction for
	order ("+num2str(n_target)+","+num2str(m_target)+")");
241	legend ("Theta", "Phi");
242	
243	
244	/////////////////////////////////////
245	# plot results at one frequency point
246	fi $=$ find (c/f, lambda_target);
247	$u1_plot = pinch(pinch(U1,3,fi),2,1);$

248u2_plot = pinch (pinch (U2,3,fi),1,1); 249 $T_{grating_plot} = pinch(T_{grating_matrix}, 3, fi);$ image(u1_plot, u2_plot, T_grating_plot, 250251"u1","u2","Transmission at "+num2str(c/f(fi)*1e6)+"um"," polar plot"); 252253# re-plot at higher resolution for a nicer plot 254= 35;pts = linspace (-1,1,pts); 255u1_plot2 = linspace (-1,1,pts); 256u2_plot2 $T_{grating_plot2} = matrix(pts, pts);$ 257258for $(i=1:size_n)$ { 259260for $(j=1:size_m)$ { 261 $u1i = find(u1_plot2, u1_plot(i));$ 262 $u2j = find(u2_plot2, u2_plot(j));$ 263264 $T_{grating_plot2}(u1i, u2j) = T_{grating_plot}(i, j);$ } 265} 266267268image(u1_plot2, u2_plot2, T_grating_plot2, "u1","u2","Transmission at "+num2str(c/f(fi)*1e6)+"um","polar 269plot"); 270 $image(u1_plot2, u2_plot2, log10(abs(T_grating_plot2)+1e-5))$ "u1","u2","Log10(|Transmission|) at "+num2str(c/f(fi)*1e6)+"um 271"," polar plot"); 272} 273} else { # 2D simulation 274275276277 # find the maximum possible number of grating orders 278# this occurs at the maximum frequency 279 $n = gratingn (mname, size_f);$ 280 $size_n = length(n);$ 281282# initialize matrices T_grating = matrix(size_n, size_f); # grating order strength vs f 283

284	theta = $matrix(size_n, size_f); # angle matrix$
285	$grating_S = matrix(size_n, size_f); # grating_S ^2$ gives the
	fraction of the source power to each grating order that is S
	polarized
286	$grating_P = matrix(size_n, size_f); # grating_P ^2$ gives the
	fraction of the source power to each grating order that is P
	polarized
287	
288	
289	# loop over each frequency point
290	for $(i=1:size_f)$ {
291	
292	# get the grating numbers at this frequency
293	$n_{tmp} = gratingn(mname, i);$
294	
295	# calculate indices for inserting these results into final
	matrix
296	$n1 = find(n, n_tmp(1));$
297	$n2 = find(n, n_tmp(length(n_tmp)));$
298	
299	# calculate grating order angles
300	# set unused orders to -90 or $+90$
301	theta(1:n1,i) = -90;
302	$theta(n2:size_n, i) = 90;$
303	theta $(n1:n2,i) = gratingangle(mname,i);$
304	
305	$\#$ calculate grating orders and save into ${\rm T}_{\rm grating}$ matrix
306	$grating_temp = gratingpolar(mname, i);$
307	grating_temp = grating_temp * $sqrt(abs(T(i))); #$
	normalize result such that sum of all grating orders of \mid
	$\operatorname{Etheta} ^2 + \operatorname{Ephi} ^2$
308	# equals the fraction of source power
	transmitted through the monitor.
309	$grating_S(n1:n2,i) = pinch(grating_temp,2,3); \# $
	$\operatorname{grating}_S \mid \ 2$ gives the fraction of the source power to each
	grating order that is S polarized
310	$grating_P(n1:n2,i) = pinch(grating_temp,2,2); \# $
	grating_ $P \mid 2$ gives the fraction of the source power to each
	grating order that is P polarized

311	$T_{grating}(n1:n2,i) = abs(pinch(grating_temp,2,2))^2 + abs(pinc$
	pinch(grating_temp,2,3))^2; $\#$ fraction of source power to
	each grating order
312	}
313	
314	
315	# Calculate the number of grating orders (theta < 90)
316	$num_orders_matrix = sum((abs(theta) < 89.9) , 1);$
317	
318	
319	T_matrix=T;
320	$T_grating_matrix = T_grating;$
321	
322	T = matrixdataset("T");
323	T. addparameter ("lambda", c/f , "f", f);
324	T. addattribute ("T", T_matrix);
325	
326	<pre>num_orders = matrixdataset("num_orders");</pre>
327	$num_orders.addparameter("lambda", c/f,"f", f);$
328	num_orders.addattribute("num_orders", num_orders_matrix);
329	
330	$T_{grating} = matrixdataset("T_{grating"});$
331	$T_{grating}$. addparameter ("n", n);
332	$T_{-}grating.addparameter("lambda", c/f,"f",f);$
333	$T_{grating.addattribute}$ (" $T_{grating}$ ", $T_{grating_matrix}$);
334	$T_{grating.addattribute}$ ("grating_S", grating_S);
335	$T_grating.addattribute("grating_P", grating_P);$
336	T_grating.addattribute("theta",theta);
337	
338	
339	
340	if (make_plots) {
341	
342	# plot number of orders
343	$plot(c/f*1e9, num_orders_matrix,$
344	"wavelength (nm)","","Number of grating orders");
345	
346	# plot data for a particular grating order
347	$T_grating_plot = pinch(T_grating_matrix, 1, find(n, n_target))$

;

```
348
                 theta_plot
                              = pinch ( theta , 1, find (n, n_target ) );
349
350
                plot(c/f*1e9, abs(T_matrix), T_grating_plot,
351
                "wavelength (nm)", "Transmission", "Transmission");
                legend("Total","To order ("+num2str(n_target)+")");
352
                plot(c/f*1e9, theta_plot,
353
                "wavelength (nm)", "angle (deg)", "Propagation angle for order
354
                    ("+num2str(n_target)+")");
355
356
                # plot results at one frequency point
357
                fi
                               = find (c/f, lambda_target);
358
                               = pinch (theta, 2, fi);
359
                theta_plot
360
                T_{-}grating_{-}plot = pinch(T_{-}grating_{-}matrix, 2, fi);
361
                plot(theta_plot, T_grating_plot,
                "theta (deg)"," Transmission"," Transmission at "+num2str(round(c
362
                    /f(fi)*1e9))+"nm"," plot points");
363
            }
364
365
        }
366
    ';
    367
368
369
    if (dimension == "3D") { # 3D simulation
370
371
        analysis_script = analysis_script + '
372
            orders = gratingordercount(mname);
373
            u1 = gratingu1 (mname);
374
            u2 = gratingu2 (mname);
            uz = sqrt(1 - u1*u1 - u2*u2);
375
            theta = a\cos(u2) * 180 / pi; # azimuth angle
376
377
            phi = atan(u2/u1) * 180 / pi; \# polar angle
378
            T = transmission (mname);
379
380
            grating_efficiencies = grating(mname);
381
382
            grating_n = gratingn(mname);
383
            grating_m = gratingm(mname);
384
```

385386 # Depending on the number of orders, the first order can be found with a different index 387 # The case of 3 orders was observed in a blazed grating. In a radially symmetric grating, the number of orders is 1, 5 or 9 if (orders = 1) { 388 389 firstordern = 1;390 firstorderm = 1; $first_order_efficiency = 0;$ 391392firstorderu2 = 1; first_order_theta = acos(firstorderu2) * 180/ pi; 393394} 395396 else if (orders = 3) { 397 firstordern = 1; firstorderm = 0;398 $first_order_efficiency = grating_efficiencies(3);$ 399 firstorderu2 = u1(3); 400 401 first_order_theta = acos(firstorderu2) * 180/ pi; } 402 403404 else if (orders = 5) { firstordern = 2;405firstorderm = 3;406 407 first_order_efficiency = grating_efficiencies (firstordern, firstorderm); 408 firstorderu2 = u2(3); first_order_theta = acos(firstorderu2) * 180/ pi; 409 410} 411 else if (orders = 9) { 412 firstordern = 2;413 414 firstorderm = 3;first_order_efficiency = grating_efficiencies (firstordern, 415firstorderm); 416firstorderu2 = u2(3); first_order_theta = acos(firstorderu2) * 180/ pi; 417 418 } 419

```
420
      \# Here a more experimental algorithm that finds the first order
          automatically. It was not thoroughly tested and needs to be adapted
421
             else {
422
              print("Universal algorithm");
423
                  firstordern = find(gratingn(mname), 0);
                  firstorderm = find(gratingm(mname), 1);
424
425
                  first_order_efficiency = grating_efficiencies(firstordern,
                     firstorderm);
426
427
                 \operatorname{zerou2} = \operatorname{find}(\operatorname{u2}, 0);
                  if (zerou2 == 1) {
428
                      firstorderu2 = 1;
429
430
                  }
431
                  else {
432
                      firstorderu2 = u2(zerou2 + 1);
433
                  }
                  first_order_theta = acos(firstorderu2) * 180/ pi;
434
435
             }
436
             # grating (mname) gives only the power relative to the farfield
                 power.
437
             \# To get the power relative to the source power, we need to
                 multiply with T (farfield power / source power)
             first_order_efficiency_normalized = T * first_order_efficiency;
438
       ';
439
440
    }
    else if (dimension == "2D") { # 2D simulation
441
442
         analysis_script = analysis_script + '
             orders = gratingordercount(mname);
443
444
             theta = theta;
445
             first_order_efficiencies = T_grating. T_grating;
             T = transmission (mname);
446
447
448
             if (orders = 3) {
                  first_order_efficiency_normalized = first_order_efficiencies (3)
449
                  first_order_theta = theta(3);
450
451
             }
             else {
452
                  first_order_efficiency_normalized = 0;
453
```

```
454
                 first_order_theta = 90;
             }
455
456
             first_order_efficiency = first_order_efficiency_normalized / T;
457
458
             first_order_n = 1;
             first_order_m = 0;
459
460
461
             \# for the optimization algorithm we can set the
                 first_order_efficiency_normalized to 0 if the emission angle of
                the first order is not within the
462
             # range [42 degrees, 48 degrees]. Comment/uncomment as needed
             if ((first_order_theta <=42) or (first_order_theta >= 48)) {
463
                 first_order_efficiency = 0;
464
465
                 first_order_efficiency_normalized = 0;
466
             }
467
         ';
468
469
    }
470
    set("analysis script", analysis_script);
471
472
473
    \# add a polarization analysis
474
475
    addanalysisgroup;
    set("name", "polarization ellipse");
476
477
    set("x", 0);
478
    set ("y", 1.35e-6);
    set ("z", 0);
479
480
    adduserprop("normal", 1, "y");
    adduserprop("x span", 2, 5e-6);
481
482
    adduserprop("y span",2,0);
483
    adduserprop ("z span", 2, 5e-6);
    addanalysisprop("make plots", 0, 0);
484
    addanalysisprop("n target", 0, 1);
485
    addanalysisprop("m target", 0, 0);
486
487
    addanalysisprop("lambda target", 2, lambda_um);
488
    addanalysisprop ("ellipse res", 0, 1000);
    addanalysisresult ("Gp_plot");
489
    addanalysisresult ("Gs_plot");
490
```

```
491
    addanalysisresult ("pol");
492
    addanalysisresult ("num_orders");
    addanalysisresult ("ratio_1_0");
493
494
495
496
    analysis_script = '
           497
498
            # Polarization ellipse
499
            # This script calculates the polarization of all grating orders.
500
            \# The results of all orders (n,m) are returned to the Gs_plot and
501
            # Gp_plot datasets
            # The results of a user-specified grating order and frequency
502
            # point can be plotted in terms of the polarization ellipse
503
504
            #
505
            # Input parameters:
            # make plots: 1 to make plots, 0 otherwise
506
            # n_target, m_target: grating order of interest (n,m).
507
            # These parameters only affect the ellipse plot. They do not
508
509
            # affect the output results.
            # lambda_target: wavelength of interest. This parameter only
510
            \# affects the ellipse plot. It does not affect the output results.
511
            # ellipse_res: resolution of the polarization ellipse.
512
513
            \# This parameter affects the ellipse plot, it may also affect the
514
            \# output results.
515
            #
            # Output results:
516
            # Gs_plot, Gp_plot: returns polarization in S and P direction for
517
            # all orders as a function of lambda
518
519
            \# num_orders: returns the number of valid grating order vs lambda
            \# (may also include orders due to numberical error, e.g., G=10^-30)
520
            \# pol: contains the fraction transmitted power (G), phase differece
521
            \# in s and p polarization (phase_diff), polarization handedness
522
523
            # (pol_handed), angle of major axis (major_angle) and ratio of
            # major/minor axis (ratio) for all grating orders and wavelengths.
524
525
            #
            \# Note – Since the size of the pol dataset is a function of the
526
527
            #
                      number of grating orders
                      Therefore, a larger dataset is created and then stitch
528
            #
                      data into the whole matrix
529
            #
```

530	# The ratio of major/minor axis can be a "not a number" $\#$
531	# (NAM)
532	# For some invalid grating orders, the major and minor
533	# axis can be both zero that causes NAM
534	# The visualizer may not be able to properly display
535	# these entries
536	# Users can use the View Data function in the visualizer
537	# to see the exact numbers
538	#
539	# — The polarization handedness is defined from the point
540	# of view of the receiver
541	#
542	# Plot:
543	# ellipse: plots a polarization ellipse based on the s,
544	# p polarization components of a user-specified n,
545	# m and lambda. Numbers in the plot title are rounded
546	# to integer
547	#
548	# Tags: far field polarization ellipse grating
549	#
550	# Copyright 2014 Lumerical Solutions Inc.
551	/////////////////////////////////////
552	
553	mname = "::model::3 dpowermonitor";
554	
555	
556	# simplify input variable names by removing spaces
557	$make_plots = \%make plots\%;$
558	$n_target = \%n target\%; # target grating order for the ellipse plot$
559	$m_target = \% m target\%;$
560	$lambda_target = \% lambda target\%; # target frequency point for the$
	ellipse plot
561	ellipse_res = %ellipse res%; $\#$ pol ellipse resolution. This number
	affects the accuracy
562	
563	# specify monitor name, get frequency vector
564	f = getdata(mname, "f");
565	
566	# find the maximum possible number of grating orders, this occurs

	at the maximum frequency
567	n = gratingn(mname, length(f));
568	m = gratingm(mname, length(f));
569	
570	# initialize matrices
571	u1 = matrix(length(n));
572	u2 = matrix(length(m));
573	<pre>U1 = matrix(length(n),length(m),length(f)); # first direction cosine (if monitor is in XY plane, this corresponds to Ux)</pre>
574	U2 = matrix(length(n),length(m),length(f)); # second direction cosine (if monitor is in XY plane, this corresponds to Uy)
575	Gs_all = matrix(ellipse_res, length(n), length(m), length(f)); # s pol vs res n m f
576	<pre>Gp_all = matrix(ellipse_res,length(n),length(m),length(f)); # p pol . vs res,n,m,f</pre>
577	<pre>kappa = linspace(0,360,ellipse_res)*pi/180; # setting kappa for Gs and Gp</pre>
578	G = matrix(length(n), length(m), length(f)); # grating order strength vs n, m, f
579	<pre>major_angle_all = matrix(length(n),length(m),length(f)); # major angle vs n,m,f (this is also called the orientation or tilt angle)</pre>
580	<pre>ratio_all = matrix(length(n),length(m),length(f)); # ratio vs n,m ,f (for linear pol., ratio can be very high)</pre>
581	<pre>phase_diff_all = matrix(length(n),length(m),length(f)); # phase vs n,m,f (the phase difference between s and p polarization (p minus s))</pre>
582	$pol_handed_all = matrix(length(n), length(m), length(f));$
583	# left or right handed polarization. 1 is right-handed, -1 is left-handed, 0 means no entry/linear.
584	$\#$ In other words, from <code>phase_diff</code> , <code>-180<p-s<0< code=""> is left , <code>0<p-s<180< code=""> is right .</p-s<180<></code></p-s<0<></code>
585	<pre># This is defined from the point of view of the receiver (against the progation direction).</pre>
586	# User can multiply -1 to this matrix if from the point of view of the source.
587	
588	# loop over each frequency point
589	for $(fi=1:length(f))$ {

590	
591	# get the grating numbers at this frequency point
592	$n_tmp = gratingn(mname, fi);$
593	$m_tmp = gratingm(mname, fi);$
594	
595	# calculate indices for inserting these results into the final matrix
596	# that the final matrix is filled from n1 to n2, and m1 to m2
597	$n1 = find(n, n_tmp(1));$
598	$n2 = find(n, n_tmp(length(n_tmp)));$
599	$m1 = find(m,m_tmp(1));$
600	$m2 = find(m, m_tmp(length(m_tmp)));$
601	
602	# calculate grating order angles (direction cosine units)
603	# and save into U1, U2 matrix. Set unused orders to -1 or $+1$
604	u1(1:n1) = -1;
605	u2(1:m1) = -1;
606	u1(n2:length(n)) = 1;
607	u2(m2: length(m)) = 1;
608	u1(n1:n2) = gratingu1(mname, fi);
609	u2(m1:m2) = gratingu2(mname, fi);
610	U1(1: length(n), 1: length(m), fi) = meshgridx(u1, u2);
611	U2(1: length(n), 1: length(m), fi) = meshgridy(u1, u2);
612	
613	# calculate grating orders and save into G matrix
614	$G_{-vec} = gratingpolar(mname, fi);$
615	$Gtheta = pinch(G_vec, 3, 2);$
616	$Gphi = pinch(G_vec, 3, 3);$
617	
618	# grating order strength (fraction of transmitted power)
619	# stitch data into the central columns of the final result matrices
620	# to have all data from different grating orders packaged in a
	single matrix dataset
621	$G(n1:n2,m1:m2, fi) = abs(Gtheta)^2+abs(Gphi)^2;$
622	
623	#loop over all grating numbers
624	for $(ni=1:length(n_tmp))$ {
625	for ($mi=1:length(m_tmp)$) {
626	

627	<pre># convert spherical coordinates polarization into s,p polarization and select the grating order</pre>
628	# calculate the polarization ellipse. kappa is the resolution
629	Gs = Gphi(ni, mi);
630	Gp = Gtheta(ni, mi);
631	Gs = real(Gs*exp(1i*kappa));
632	Gp = real(Gp*exp(1i*kappa));
633	
634	$\#$ measure parameters(ratio, major_angle) from the ellipse. normalize
	Gs and Gp
635	diameter = $\operatorname{sqrt}((\operatorname{Gs})^2+(\operatorname{Gp})^2);$
636	<pre>major_axis = max(diameter); # for some grating numbers, the major_axis can be 0</pre>
637	<pre>minor_axis = min(diameter); # for some grating numbers, the minor_axis can be 0</pre>
638	ratio = major_axis / minor_axis; # for some grating numbers, the ratio can be a NAM $(0/0)$
639	<pre>if (almostequal(ratio,1,0.0001,0.0001)){major_axis_i = find(Gp, max(Gp)); # if ratio ~ 1, then it will have no major axis</pre>
640	<pre>}else{ major_axis_i = find(diameter, max(diameter));}</pre>
641	<pre>major_angle = atan2(Gs(major_axis_i), Gp(major_axis_i))*180/ pi;</pre>
642	if $(major_angle < -90)$ { $major_angle = major_angle + 180$; }
643	if $(major_angle > 90)$ { major_angle = major_angle -180; }
644	$Gs = Gs/major_axis;$
645	$Gp = Gp/major_axis; \#$ normalization
646	
647	# measure phase difference from the s and p component
648	<pre>phase_diff = (angle(Gtheta(ni,mi))-angle(Gphi(ni,mi)))*180/pi; # phase difference of s and p pol. in degree</pre>
649	<pre>if (Gphi(ni,mi)==0+1i*0) { phase_diff = 0; } # define linearly pol light</pre>
650	<pre>if (Gtheta(ni,mi)==0+1i*0) { phase_diff = 0; } # define linearly pol light</pre>
651	if (phase_diff > 180) { phase_diff = phase_diff - 180; } # -180< phase_diff <180
652	if (phase_diff < -180) { phase_diff = phase_diff + 180; } # -180< phase_diff <180
652	

```
654
            # measure polarization handedness based on phase_diff
             pol_handed = 0; \# initiallise an entry
655
             if (phase_diff < 0) { pol_handed = -1; } # define left-handed
656
             if (phase_diff > 0) { pol_handed = 1; } # define right-handed
657
658
659
            # stitch data into the central columns of the final result matrices
             # to have all data from different grating orders packaged in a
660
                single matrix dataset (as a function of n, m, f)
661
             Gs_all(1:ellipse_res, n1+ni-1, m1+mi-1, fi) = Gs;
             Gp_all(1:ellipse_res, n1+ni-1, m1+mi-1, fi) = Gp;
662
663
             phase_diff_all(n1+ni-1,m1+mi-1,fi) = phase_diff;
664
             pol_handed_all(n1+ni-1,m1+mi-1,fi) = pol_handed;
             ratio_all(n1+ni-1,m1+mi-1,fi) = ratio;
665
666
             major_angle_all(n1+ni-1,m1+mi-1,fi) = major_angle;
667
                 }
             }
668
             }
669
670
671
            # calculate U3 and convert grating directions to theta, phi. If
                monitor is in XY plane, U3=Uz
                   = sqrt ( 1-U1^2-U2^2);
             U3
672
             theta = real ( a\cos(U3) ) * 180/pi;
673
                   = \operatorname{atan2}(U2,U1) * 180/\operatorname{pi};
674
             phi
675
            # Calculate the number of grating orders (theta < 90)
676
            # NOTE: this script for counting grating orders assumes a
677
                rectangular
            # unit cell. The count will not be correct for triangular lattices.
678
679
             \# this will count all non-zero entries, including numerical error
                roders
                                             (real(theta) < 89.9), 2),1);
680
             num_orders_matrix = sum(sum(
681
682
            # Create datasets
             num_orders = matrixdataset("num_orders");
683
             num_orders.addparameter("lambda",c/f,"f",f);
684
             num_orders.addattribute("num_orders", num_orders_matrix);
685
686
             pol = matrixdataset("polarization");
687
             pol.addparameter("n",n);
688
```

689	pol.addparameter ("m",m);
690	pol.addparameter ("lambda", c/f , "f", f);
691	pol.addattribute("G",G);
692	pol.addattribute("phase_diff", phase_diff_all);
693	<pre>pol.addattribute("pol_handed", pol_handed_all);</pre>
694	<pre>pol.addattribute("major_angle", major_angle_all);</pre>
695	<pre>pol.addattribute("ratio", ratio_all);</pre>
696	
697	Gs_plot = matrixdataset("Gs_all");
698	<pre>Gs_plot.addparameter("ellipse_point", linspace(1, ellipse_res, ellipse_res));</pre>
699	Gs_plot.addparameter("n",n);
700	Gs_plot.addparameter("m",m);
701	$Gs_plot.addparameter("lambda", c/f,"f", f);$
702	Gs_plot.addattribute("Gs_all",Gs_all);
703	
704	$Gp_plot = matrixdataset("Gp_all");$
705	<pre>Gp_plot.addparameter("ellipse_point", linspace(1, ellipse_res, ellipse_res));</pre>
706	Gp_plot.addparameter("n",n);
707	Gp_plot.addparameter("m",m);
708	$Gp_plot.addparameter("lambda", c/f,"f", f);$
709	Gp_plot.addattribute("Gp_all",Gp_all);
710	
711	<pre># make ellipse plot for the user-specified grating orders and frequency point</pre>
712	if (make_plots) {
713	
714	$ni = find(n, n_target);$
715	$mi = find(m, m_target);$
716	fi=find(f,c/lambda_target);
717	
718	# these command lines can be also used to plot Gs and Gp in
	other tools, such as excel
719	Gp_all=Gp_plot.Gp_all;
720	Gs_all=Gs_plot.Gs_all;
721	$Gp=pinch(pinch(pinch(Gp_all,2,ni),2,mi),2,fi);$
722	$Gs=pinch(pinch(pinch(Gs_all,2,ni),2,mi),2,fi);$
723	

724# plot ellipse, and ellipse parameters # numbers are rounded to integer to save title space 725726plot(Gp,Gs,"P-pol","S-pol"," pol ellipse (N,M)=(" +num2str(n(ni))+","+num2str(m(mi))+ ")" + " (theta, phi) = (" +num2str(round(727theta (ni, mi, fi)) +","+num2str(round(phi(ni,mi,fi)))+")" + " ratio = " +num2str(ratio_all(ni 728, mi, fi)) +729" major angle (deg) = " + num2str(major_angle_all(ni,mi,fi))); 730 $\operatorname{setplot}(\operatorname{"x min"}, -1);$ 731setplot("x max", 1); 732 $\operatorname{setplot}("y \min", -1);$ 733setplot("y max", 1); 734} 735 736 $ni = find(n, n_target);$ $mi = find(m, m_target);$ 737738fi=find(f,c/lambda_target); $ratio_1_0 = ratio_all(ni, mi, fi);$ 739740 '; 741set("analysis script", analysis_script); 742

Two-parameter sweep

```
# A nested sweep over one or two parameters
1
\mathbf{2}
3
  mname = "::model::3 dpowermonitor";
4
  5
  \# Here, we choose the parameters to sweep over.
6
  \# The sweeps that can be found below were implemented.
7
  # A sweep can be selected by uncommenting it.
8
9
  \# The code can be easily adapted to add other parameter sweeps.
  10
11
  \# the number of sweep parameters
12
  num_sweeppar1_sweeps=50;
13
  num_sweeppar2_sweeps=50;
14
15
16
  17
18
  sweepparl_start = 0.15e-6;
  sweepparl_stop = 0.8e-6;
19
  sweeppar2\_start = 0.05e-6;
20
  sweeppar2\_stop = 0.4e-6;
21
  sweepparl_name = "period";
22
  sweeppar2\_name = "radius";
23
24
  25
  26
  \#sweepparl_start = 0.01e-6;
27
  \#sweeppar1_stop = 0.5e-6;
28
29
  \#sweeppar2_start = 0.01e-6;
  \#sweeppar2_stop = 1e-6;
30
  #sweepparl_name = "coatingThickness";
31
  #sweeppar2_name = "grooveDepth";
32
  33
34
  35
  \#sweeppar1_start = 0;
36
  \#sweepparl_stop = 1;
37
  #sweepparl_name = "period_radius_fraction";
38
```
```
39
  \#sweeppar2_name = "none";
41
43 #sweepparl_name = "blaze_angle_fraction";
44 \#sweeppar1_start = 0:
45 \#sweeppar1\_stop = 1;
  \#sweeppar2_name = "none";
46
47
  48
  if (sweepparl_name == "coatingThickness") {
49
      select ("::model");
50
      para1 = struct;
51
52
      para1.Name = "coating thickness";
      para1.Parameter = "::model::coating_thickness";
53
      para1.Type = "Length";
54
      para1.Start = sweeppar1\_start;
55
      para1.Stop = sweeppar1_stop;
56
      para1.Units = "microns";
57
58
59
  }
  if(sweepparl_name == "period"){
60
      select ("::model::FDTD");
61
      para1 = struct;
62
      para1.Name = "period";
63
      para1.Parameter = "::model::FDTD::x span";
64
65
      para1.Type = "Length";
66
      para1.Start = sweeppar1_start;
67
      para1.Stop = sweeppar1\_stop;
      para1.Units = "microns";
68
69
70
      para1_2 = struct;
      para1_2.Name = "period";
71
72
      para1_2.Parameter = "::model::FDTD::z span";
      para1_2.Type = "Length";
73
74
      para1_2. Start = sweeppar1_start;
75
      para1_2. Stop = sweeppar1_stop;
76
      para1_2. Units = "microns";
77 }
```

```
if (sweeppar2_name == "grooveDepth") {
 78
        select ("::model");
 79
        para2 = struct;
 80
        para2.Name = "groove depth";
 81
        para2.Parameter = "::model::groove_depth";
 82
        para2.Type = "Length";
 83
        para2.Start = sweeppar2_start;
 84
        para2.Stop = sweeppar2\_stop;
 85
 86
        para2.Units = "microns";
 87
    }
    if (sweeppar2_name == "radius") {
 88
 89
        para2 = struct;
        para2.Name = "radius";
 90
 91
        para2.Parameter = "::model::hole_radius";
 92
        para2.Type = "Length";
        para2.Start = sweeppar2_start;
 93
 94
        para2.Stop = sweeppar2\_stop;
        para2.Units = "microns";
 95
 96
   }
    if (sweepparl_name == "period_radius_fraction") {
 97
        para1 = struct;
 98
        para1.Name = "period_radius_fraction";
99
        para1.Parameter = "::model::period_radius_fraction";
100
        para1.Type = "Number";
101
102
        para1.Start = sweeppar1_start;
103
        para1.Stop = sweeppar1_stop;
104
    }
    if (sweepparl_name == "blaze_angle_fraction") {
105
106
        para1 = struct;
        para1.Name = "blaze_angle_fraction";
107
        para1.Parameter = "::model::blaze_angle_fraction";
108
109
        para1.Type = "Number";
110
        para1.Start = sweeppar1_start;
        para1.Stop = sweeppar1_stop;
111
112 }
113
115
116 # child paramter sweep over width of simulation region
```

```
117 addsweep(0);
    sweepname = sweeppar1_name+" sweep";
118
    setsweep("sweep", "name", sweepname);
119
    setsweep(sweepname, "type", "Ranges");
120
121
    setsweep(sweepname, "number of points", num_sweeppar1_sweeps);
122
123
124
    addsweepparameter(sweepname, para1);
    if(sweepparl_name == "period"){
125
        addsweepparameter(sweepname, para1_2);
126
127
    }
128
129
   result = struct;
130
    result. Name = "T";
131
    result.Result = "::model::Grating Transmission::T";
    addsweepresult(sweepname, result);
132
133
134 \quad \text{result} = \text{struct};
135
    result.Name = "num_orders";
    result.Result = "::model::Grating Transmission::num_orders";
136
137
    addsweepresult (sweepname, result);
138
139
   result = struct;
140
    result.Name = "grating_efficiency";
    result.Result = "::model::Grating Transmission::grating_efficiency";
141
    addsweepresult(sweepname, result);
142
143
144 result = struct;
145
    result.Name = "first_order_efficiency";
    result . Result = "::model::Grating Transmission::first_order_efficiency";
146
147
    addsweepresult(sweepname, result);
148
149
    result = struct;
    result.Name = "first_order_theta";
150
    result.Result = "::model::Grating Transmission::first_order_theta";
151
    addsweepresult(sweepname, result);
152
153
154 result = struct;
155 result.Name = "grating_n";
```

```
156
    result . Result = "::model::Grating Transmission::grating_n";
157
    addsweepresult(sweepname, result);
158
159
    result = struct;
160
    result.Name = "grating_m";
    result.Result = "::model::Grating Transmission::grating_m";
161
162
    addsweepresult(sweepname, result);
163
164
    result = struct;
    result.Name = "first_order_efficiency_normalized";
165
    result.Result = "::model::Grating Transmission::
166
        first_order_efficiency_normalized ";
167
    addsweepresult(sweepname, result);
168
169
    result = struct;
    result.Name = "ratio_1_0";
170
    result.Result = "::model::polarization ellipse::ratio_1_0";
171
    addsweepresult(sweepname, result);
172
173
174
175 \# parent sweep
    if(sweeppar2_name != "none"){
176
177
        insertsweep(sweepname);
        sweepname2 = sweeppar2_name+" sweep";
178
        setsweep("sweep", "name", sweepname2);
179
180
        setsweep(sweepname2, "type", "Ranges");
181
        setsweep(sweepname2, "number of points", num_sweeppar2_sweeps);
182
        addsweepparameter(sweepname2, para2);
183
184
         result = struct;
         result.Name = "T":
185
186
         result. Result = "T";
187
         addsweepresult(sweepname2, result);
188
         result = struct;
189
190
         result.Name = "num_orders";
         result.Result = "num_orders";
191
192
         addsweepresult(sweepname2, result);
193
```

```
194
         result = struct;
         result.Name = "grating_efficiency";
195
196
         result. Result = "grating_efficiency";
         addsweepresult(sweepname2, result);
197
198
         result = struct;
199
         result.Name = "first_order_efficiency";
200
         result.Result = "first_order_efficiency";
201
         addsweepresult(sweepname2, result);
202
203
204
         result = struct;
         result.Name = "first_order_theta";
205
206
         result.Result = "first_order_theta";
         addsweepresult(sweepname2, result);
207
208
209
         result = struct;
210
         result.Name = "grating_n";
211
         result.Result = "grating_n";
         addsweepresult(sweepname2, result);
212
213
214
         result = struct;
215
         result.Name = "grating_m";
216
         result. Result = "grating_m";
         addsweepresult(sweepname2, result);
217
218
219
         result = struct;
220
         result.Name = "first_order_efficiency_normalized";
         result . Result = "first_order_efficiency_normalized";
221
         addsweepresult(sweepname2, result);
222
223
224
         result = struct;
225
         result.Name = "ratio_1_0";
         result. Result = "ratio_1_0";
226
        addsweepresult(sweepname2, result);
227
228 }
```

PSO optimization sweep

```
2 # This script implements a PSO optimization sweep.
3 # Optimization parameters can be added/removed.
4
  5
6
  select ("::model");
7
8
  mname = "::model::3 dpowermonitor";
  lambda_um = get("lambda_um");
9
  lambdas_SI = [lambda_um];
10
  ### Here, we choose the parameters to optimize and their allowed ranges ###
11
12
13
   radius_start = 0.05e-6;
14
   radius_stop = 0.4e-6;
15
16
17
   period_radius_fraction_start = 2;
18
   period_radius_fraction_stop = 5;
19
   groove_depth_start = 0.01e-6;
20
   groove_depth_stop = 1e-6;
21
22
23
   blaze_angle_fraction_start = 0;
   blaze_angle_fraction_stop = 1;
24
25
  \#coating_thickness_start = 30e-9;
26
  \#coating_thickness_stop = 200e-9;
27
28
29
  # set up parameters for period_radius_fraction
30
  select ("::model");
31
32
  para1 = struct;
  para1.Name = "period_radius_fraction";
33
  para1.Parameter = "::model::period_radius_fraction";
34
  para1.Type = "Number";
35
36
  para1.Min = period_radius_fraction_start;
   para1.Max = period_radius_fraction_stop;
37
38
```

```
#set up parameters for radius
39
40
  para1_2 = struct;
   para1_2.Name = "radius";
41
   para1_2.Parameter = "::model::hole_radius";
42
   para1_2. Type = "Length";
43
   para1_2. Unit = "microns":
44
   para1_2. Min = radius_start;
45
   para1_2. Max = radius_stop;
46
47
  #set up parameters for groove depth
48
   para2 = struct;
49
   para2.Name = "groove depth";
50
   para2.Parameter = "::model::groove_depth";
51
52
   para2.Type = "Length";
53
   para2.Min = groove_depth_start;
   para2.Max = groove_depth_stop;
54
   para2. Units = "microns":
55
56
57
  #set up parameters for blaze angle
   para3 = struct;
58
   para3.Name = "blaze angle fraction";
59
   para3.Parameter = "::model::blaze_angle_fraction";
60
   para3.Type = "Number";
61
   para3.Min = blaze_angle_fraction_start;
62
   para3.Max = blaze_angle_fraction_stop;
63
64
  #set up parameters for coating thickness
65
66 \# para4 = struct;
67 #para4.Name = "coating thickness";
68 #para4.Parameter = "::model::coating_thickness";
69 \# para4.Type = "Length";
70 #para4.Min = coating_thickness_start;
  #para4.Max = coating_thickness_stop;
71
  \#para4. Units = "microns";
72
73
74
75
76
  77
```

```
78
```

```
78 \# optimization over width of simulation region
79 addsweep(1);
   sweepname = "period-radius sweep";
80
    setsweep("optimization", "name", sweepname);
81
    setsweep(sweepname, "type", "Maximize");
82
    setsweep(sweepname, "Algorithm", "Particle Swarm");
83
    setsweep(sweepname, "Maximum Generations", 200);
84
    setsweep(sweepname, "Generation Size", 30);
85
86
87
88
    addsweepparameter(sweepname, paral); # period-radius fraction
89
    addsweepparameter(sweepname, para1_2); # radius
90
    addsweepparameter(sweepname, para2); # groove depth
91
92
    addsweepparameter(sweepname, para3); # blaze angle
   #addsweepparameter(sweepname, para4); #coating thickness
93
94
95
   result = struct;
    result.Name = "T";
96
    result.Result = "::model::Grating Transmission::T";
97
    result. Optimize = false;
98
    addsweepresult(sweepname, result);
99
100
101
   result = struct;
102 result.Name = "num_orders";
    result.Result = "::model::Grating Transmission::num_orders";
103
104
    result. Optimize = false;
    addsweepresult(sweepname, result);
105
106
107
    result = struct;
    result.Name = "first_order_efficiency";
108
    result . Result = "::model::Grating Transmission::first_order_efficiency";
109
    result. Optimize = false;
110
    addsweepresult(sweepname, result);
111
112
113 result = struct;
114 result.Name = "first_order_efficiency_normalized";
115 result.Result = "::model::Grating Transmission::
        first_order_efficiency_normalized ";
```

- 116 result.Optimize = true;
- 117 addsweepresult(sweepname, result);
- 118
- 119 result = struct;
- 120 result.Name = "first_order_theta";
- 121 result.Result = "::model::Grating Transmission::first_order_theta";
- 122 result.Optimize = false;
- 123 addsweepresult(sweepname, result);