### 2.1 Ultrafast solid-state lasers

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### 2.1.1 Introduction

Since 1990 we have observed a tremendous progress in ultrashort pulse generation using solid-state lasers (Fig. 2.1.1). Until the end of the 1980's, ultrashort pulse generation was dominated by dye lasers which produced pulses as short as 27 fs with a typical average output power of about 20 mW [85Val]. Shorter pulse durations, down to 6 fs, were only achieved through additional amplification and fiber-grating pulse compression at much lower repetition rates [87For]. The tremendous success of ultrashort dye lasers in the 1970's and 1980's diverted the research interest away from solid-state lasers. In 1974 the first sub-picosecond passively mode-locked dye lasers [74Sha, 76Rud, 78Die] and in 1981 the first sub-100-femtosecond Colliding Pulse Mode-locked (CPM) dye lasers [81For] have been demonstrated. The CPM dye laser was the "work horse" all through the 1980's for ultrafast laser spectroscopy in physics and chemistry.

The development of higher average-power diode lasers in the 1980's stimulated again a strong interest in solid-state lasers. Diode laser pumping provides dramatic improvements in efficiency, lifetime, size and other important laser characteristics. For example, actively mode-locked diodepumped Nd:YAG [89Mak1] and Nd:YLF [89Mak2, 90Kel1, 90Wei, 90Juh] lasers generated 7-12 ps pulse durations for the first time. In comparison, flashlamp-pumped Nd:YAG and Nd:YLF lasers typically produced pulse durations of $\approx 100 \mathrm{ps}$ and $\approx 30 \mathrm{ps}$, respectively. Before 1990 , all attempts to passively mode-lock solid-state lasers with long upper-state lifetimes (i.e. $>100 \mu \mathrm{~s}$ ) resulted however in $Q$-switching instabilities which at best produced stable mode-locked pulses within longer $Q$-switched macropulses (i.e. $Q$-switched mode-locking) (Fig. 2.1.2). In $Q$-switched mode-locking, the mode-locked pico- or femtosecond pulses are inside much longer $Q$-switched pulse envelopes


Fig. 2.1.1. Development of shortest reported pulse duration over the last three decades. Circles refer to dye-laser technology, triangles refer to Ti:sapphire laser systems. Filled symbols indicate results directly obtained from an oscillator, open symbols indicate results achieved with additional external pulse compression.


Fig. 2.1.2. Different modes of operation of a laser. cw: continuous-wave; single- and multi-mode refers to longitudinal modes.
(typically in the $\mu$ s-regime) at much lower repetition rates (typically in the kHz-regime). The strong interest in an all-solid-state ultrafast laser technology was the driving force and formed the basis for many new inventions and discoveries.

Today, reliable self-starting passive mode-locking for all types of solid-state lasers is obtained with semiconductor saturable absorbers, first demonstrated in 1992 [92Kel2]. Since then, more than a decade later, the performance of compact ultrafast solid-state lasers has been improved by several orders of magnitude in pulse durations, average powers, pulse energies and pulse repetition rates, based on semiconductor saturable absorbers that are integrated into a cavity laser mirror (i.e. generally referred to as SEmiconductor Saturable Absorber Mirrors - SESAMs) [96Kel, 99Kel, 03Kel]. Diode-pumped SESAM-mode-locked solid-state lasers offer very reliable and compact ultrafast lasers with unsurpassed performance [03Pas, 04 Kel$]$. Currently, pulse duration can range from nanosecond to a few femtoseconds depending on the different laser materials and saturable absorber parameters (Table 2.1.1 to Table 2.1.3). The average power has been increased to 60 W and 80 W directly from a mode-locked diode-pumped laser with pulse energies larger than $1 \mu \mathrm{~J}$ [03Inn, 06Inn] and most recently even more than $10 \mu \mathrm{~J}$ [07Maa]. The pulse repetition rate has been increased to more than 100 GHz [02Kra2].

The breakthrough of femtosecond solid-state lasers happened with the discovery of the Ti:sapphire laser [ 86 Mou ], which was the first laser that was able to support sub-10-femtosecond pulses. The existing passive mode-locking techniques, primarily developed for dye lasers, were inadequate because of the much smaller gain cross-section (i.e. in the $10^{-19} \mathrm{~cm}^{2}$ regime) of Ti:sapphire compared to dyes (i.e. in the ns and $10^{-16} \mathrm{~cm}^{2}$ regime). Therefore, passive pulse generation techniques had to be re-evaluated with new laser material properties in mind.

Kerr-Lens Mode-locking (KLM) [91Spe] of Ti:sapphire lasers was discovered in 1991 and is still the only successful technique to push the frontier in ultrashort pulse duration into the fewfemtosecond regime with a pulse duration that only contains 1 to 2 optical cycles. For the first time in 1999 the long-lasting world record with pulse-compressed dye lasers resulting in 6 -fs pulses in 1987 [87For] was passed by with KLM mode-locked Ti:sapphire lasers without any external pulse compression [99Sut, 99Mor1, 99Mor2, 00Mat]. Novel dispersion compensation methods based on chirped [94Szi] and double-chirped mirrors [97Kae] had to be developed for this result. Today, only slightly shorter pulses close to 5 fs has been obtained [01Ell]. However, the measurement of such pulses has become rather challenging and new complete pulse characterization methods (e.g. FROG [93Kan] and SPIDER [98Iac]) have been developed. KLM however has serious limitations because the mode-locking process is generally not self-starting and critical cavity alignment is required to obtain stable pulse generation. Thus, the laser cavity has to be optimized for best KLM and not necessarily for best efficiency and output power - this sets serious constraints on the cavity design, which becomes even more severe at higher average output powers and more compact monolithic cavities. Thus, passively mode-locked solid-state lasers using intracavity SESAMs have become a very attractive alternative to KLM and are more widely used today (Table 2.1.2).

Shorter pulses are only obtained with external pulse compression. Sub-4-femtosecond pulses have been demonstrated with external pulse compression [03Sch] for the first time using cascaded hollow fiber pulse compression. External pulse compression into the few optical cycle regime [99Ste] is either based on optical parametric amplification [99Shi], compression of cavity-dumped pulses in a silica fiber [97Bal], hollow fiber pulse compression [97Nis] or more recently through filamentation [04Hau1, 05 Hau ]. Especially the latter two allow for pulse energies of more than $100 \mu \mathrm{~J}$ with only a few optical cycles which fulfill a central task in the generation of attosecond eXtreme UltraViolet (XUV) pulses [01Dre]. For such applications using intense few-cycle pulses in the near infrared driving extreme nonlinear processes the electric field amplitude rather than the intensity envelope becomes the important factor.

Femtosecond pulses in the near infrared reached a bandwidth large enough to only support one to two optical cycles underneath the pulse envelope. Therefore, the position of the electric field underneath the pulse envelope becomes important. This Carrier-Envelope Offset (CEO) [99Tel] can be stabilized in laser oscillators with attosecond accuracy [03Hel]. At the beginning this was a challenging task as it was not obvious how to obtain this because normally only the pulse intensity and not the electric field is detected. Also mode-locking theory fully confirms that the position of the peak electric field underneath the pulse envelope can have very large fluctuations by much more than one optical cycle. The stabilization is done in the frequency domain using the extremely stable and broadband frequency comb generated with femtosecond solid-state lasers [99Tel]. The simplest approach is based on a $f$-to- $2 f$-interferometer [ 99 Tel ] which was first realized with a spectrally broadened Ti:sapphire laser pulse using photonic crystal fibers [00Jon, 00Apo].

The emphasis of this chapter is to give an updated review of the progress in ultrafast solid-state lasers since 1990 when mode-locking became a hot topic again and the era of ultrafast dye lasers has come to its end. The topics mentioned above will be discussed in more details. The goal is to give also to the non-expert an efficient starting position to enter into this field without providing all the detailed derivations. Relevant and useful references for further information are provided and a brief historic perspective is given throughout this chapter. A basic knowledge in lasers is required. The emphasis is on solid-state lasers because they will dominate the field in the future. More extended reviews and books have summarized the dye laser era [88Sha, 90Die]. Here, no emphasis is put on fiber and semiconductor lasers, but some useful references to recent review articles and book chapters will be provided.

### 2.1.2 Definition of $Q$-switching and mode-locking

### 2.1.2.1 $Q$-switching

The history of $Q$-switching goes back to 1961 , when Hellwarth [61Hel] predicted that a laser could emit short pulses if the loss of an optical resonator was rapidly switched from a high to a low value. The experimental proof was produced a year later [ $62 \mathrm{McC}, 62 \mathrm{Col}$ ]. The technique of $Q$-switching allows the generation of laser pulses of short duration (from the nanosecond to the picosecond range) and high peak power. The principle of the technique is as follows: Suppose a shutter is introduced into the laser cavity. If the shutter is closed, laser action cannot occur and the population inversion can reach a value far in excess of the threshold population that would have occurred if the shutter were not present. If the shutter is now opened suddenly, the laser will have a gain that greatly exceeds the losses, and the stored energy will be released in the form of a short and intense light pulse. Since this technique involves switching the cavity $Q$-factor from a low to a high value, it is known as $Q$-switching. Ideally $Q$-switched lasers operate with only one axial mode because strong intensity noise is observed in a multi-mode $Q$-switched laser.

In passive $Q$-switching the shutter is replaced by an intracavity saturable absorber. The saturable absorber starts to bleach as the intensity inside the laser continues to grow from noise due to spontaneous emission. Thus the laser intensity continues to increase which in turn results in stronger bleaching of the absorber, and so on. If the saturation intensity is comparatively small, the inversion still left in the laser medium after the absorber is bleached is essentially the same as the initial inversion. Therefore, after bleaching of the saturable absorber the laser will have a gain well in excess of the losses and if the gain cannot saturate fast enough, the intensity will continue to grow and stable $Q$-switching can occur. A large modulation depth of the saturable absorber then results in a high $Q$-switched pulse energy.

Typically the pulse repetition rate in $Q$-switched solid-state lasers is in the hertz to few megahertz regime, always much lower than the cavity round-trip frequency. Picosecond pulse durations can be obtained with $Q$-switched diode-pumped microchip lasers [89Zay, 97Zay] with pulses as short as 115 ps for active $Q$-switching using electro-optic light modulators [95Zay] and 37 ps for passive $Q$-switching using SESAMs [99Spu1, 01Spu3]. For LIDAR applications passively $Q$-switched Er: Yb :glass microchip lasers around $1.5 \mu \mathrm{~m}$ are particularly interesting [98Flu, 01Hae1]. The performance of $Q$-switched microchip lasers bridge the gap between $Q$-switching and mode-locking both in terms of pulse duration (nanoseconds to a few tens of picoseconds) and pulse repetition rates (kilohertz to a few tens of megahertz) (Table 2.1.3).

### 2.1.2.2 Mode-locking

Mode-locking is a technique to generate ultrashort pulses from lasers. In cw mode-locking the pulses are typically much shorter than the cavity round trip and the pulse repetition rate (from few tens of megahertz to a few hundreds of gigahertz) is determined by the cavity round-trip time. Typically an intracavity loss modulator (i.e. a loss modulator inside a laser cavity) is used to collect the laser light in short pulses around the minimum of the loss modulation with a period given by the cavity round-trip time $T_{\mathrm{R}}=2 L / v_{\mathrm{g}}$, where $L$ is the laser cavity length and $v_{\mathrm{g}}$ the group velocity (i.e. the propagation velocity of the peak of the pulse intensity). Under certain conditions, the pulse repetition rate can be some integer multiple of the fundamental repetition rate (i.e. harmonic mode-locking) [72Bec]. We distinguish between active and passive mode-locking.

For active mode-locking (Fig. 2.1.3), an external signal is applied to an optical loss modulator typically using the acousto-optic or electro-optic effect. Such an electronically driven loss modulation produces a sinusoidal loss modulation with a period given by the cavity round-trip time $T_{\mathrm{R}}$. The saturated gain at steady state then only supports net gain around the minimum of the loss modulation and therefore only supports pulses that are significantly shorter than the cavity round-trip time.

For passive mode-locking (Fig. 2.1.3), a saturable absorber is used to obtain a Self-Amplitude Modulation (SAM) of the light inside the laser cavity. Such an absorber introduces some loss to the intracavity laser radiation, which is relatively large for low intensities but significantly smaller for a short pulse with high intensity. Thus, a short pulse then produces a loss modulation because the high intensity at the peak of the pulse saturates the absorber more strongly than its low intensity wings. This results in a loss modulation with a fast initial loss saturation (i.e. reduction of the loss) determined by the pulse duration and typically a somewhat slower recovery which depends on the detailed mechanism of the absorption process in the saturable absorber. In effect, the circulating pulse saturates the laser gain to a level which is just sufficient to compensate the losses for the pulse itself, while any other circulating low-intensity light experiences more loss than gain, and thus dies out during the following cavity round trips. The obvious remaining question is - how does passive mode-locking start? Ideally from normal noise fluctuations in the laser. One noise spike is strong enough to significantly reduce its loss in the saturable absorber and thus will be more strongly amplified during the following cavity round trips, so that the stronger noise spike


Fig. 2.1.3. Schematic laser cavity setup for active and passive mode-locking.
continues to further reduce its loss and continues its growth until reaching steady state where a stable pulse train has been formed.

Generally, we can obtain much shorter pulses with passive mode-locking using a saturable absorber, because the recovery time of the saturable absorber can be very fast, resulting in a fast loss modulation. Mode-locked pulses are much shorter than the cavity round-trip time and therefore can produce an ideal fast loss modulation inversely proportional to the pulse envelope. In comparison, any electronically driven loss modulation is significantly slower due to its sinusoidal loss modulation.

In the time domain (Fig. 2.1.4), this means that a mode-locked laser produces an equidistant pulse train, with a period defined by the round-trip time of a pulse inside the laser cavity $T_{\mathrm{R}}$ and a pulse duration $\tau_{\mathrm{p}}$. In the frequency domain (Fig. 2.1.4), this results in a phase-locked frequency comb with a constant mode spacing that is equal to the pulse repetition rate $\nu_{\mathrm{R}}=1 / T_{\mathrm{R}}$. The spectral width of the envelope of this frequency comb is inversely proportional to the pulse duration. Mode-locking in the frequency domain can be easily understood by the fact that a homogeneously broadened laser normally lases at one axial mode at the peak of the gain. However, the periodic loss modulation transfers additional energy phase-locked to adjacent modes separated by the modulation frequency. This modulation frequency is normally adapted to the cavity round-trip frequency. The resulting frequency comb with equidistant axial modes locked together in phase forms a short pulse in the time domain.

Mode-locking was first demonstrated in the mid-1960s using a HeNe-laser [64Har], ruby laser [65Moc] and Nd:glass laser [66DeM]. The passively mode-locked lasers were also $Q$-switched, which means that the mode-locked pulse train was strongly modulated (Fig. 2.1.2). This continued to be a problem for passively mode-locked solid-state lasers until the first intracavity saturable absorber was designed correctly to prevent self- $Q$-switching instabilities in solid-state lasers with microsecond or even millisecond upper-state lifetimes [92Kel2].


Fig. 2.1.4. Mode-locked pulses in the time and frequency domain.

a

b

c

Fig. 2.1.5. Passive mode-locking mechanisms explained by three fundamental models: (a) slow saturable absorber mode-locking with dynamic gain saturation, (b) fast saturable absorber mode-locking and (c) slow saturable absorber mode-locking without dynamic gain saturation, which in the femtosecond regime is described by soliton mode-locking.
$Q$-switching instabilities are a serious issue with passively mode-locked solid-state lasers. The parameters of the saturable absorber have to be chosen such that the mode-locking is self-starting (i.e. starting from normal intensity noise of the laser) and stable, i.e. without any $Q$-switching instabilities (Sect. 2.1.6.8). For example, if the loss modulation becomes too large it can drive the laser unstable: The loss saturation increases the intensity inside the laser cavity. The gain then needs to saturate more strongly to compensate for the reduced loss and to keep the intensity inside the laser cavity constant. If the gain cannot respond fast enough, the intensity continues to increase as the absorber is bleached which leads to self- $Q$-switching instabilities or in the best case to stable $Q$-switched mode-locking. In the latter case, the mode-locked pulse train is strongly modulated at close to the relaxation oscillation frequency of the laser (typically in the kHz rate) (Fig. 2.1.2). A large modulation depth of the saturable absorber results in shorter pulses but an upper limit is set by the onset of $Q$-switching instabilities.

Passive mode-locking mechanisms are well-explained by three fundamental models: slow saturable absorber mode-locking with dynamic gain saturation [72New, 74New] (Fig. 2.1.5a), fast saturable absorber mode-locking [75Hau1, 92Hau] (Fig. 2.1.5b) and slow saturable absorber modelocking without dynamic gain saturation in the picosecond [01Pas1] and femtosecond domain described by soliton mode-locking [95Kae1, 96Kae] (Fig. 2.1.5c). In the first two cases, a short net-gain window forms and stabilizes an ultrashort pulse. In Fig. 2.1.5a, an ultrashort net-gain window can be formed by the combined saturation of absorber and gain for which the absorber has to saturate
and recover faster than the gain, while the recovery time of the saturable absorber can be much longer than the pulse duration. Dynamic gain saturation means that the gain experiences a fast, pulse-induced saturation that then recovers again between consecutive pulses (Fig. 2.1.5a).

For solid-state lasers we cannot apply slow saturable absorber mode-locking as shown in Fig. 2.1.5a, because no significant dynamic gain saturation is taking place due to the small gain cross-section of the laser. The upper state lifetime of solid-state lasers is typically in the $\mu \mathrm{s}$ to ms regime, much longer than the pulse repetition period, which is typically in the nanosecond regime. In addition, the gain cross-section is 1000 or even more times smaller than for dye lasers. We therefore do not observe any significant dynamic gain saturation and the gain is only saturated to a constant level by the average intracavity intensity. This is not the case for dye, semiconductor and color-center lasers for which Fig. 2.1.5a describes most mode-locking processes. Therefore it was assumed that without other pulse-forming mechanisms (such as soliton pulse shaping) a fast saturable absorber is required for solid-state lasers. Kerr-lens mode-locking is nearly an ideal example for fast saturable absorber mode-locking. However, SESAM mode-locking results revealed that even a slow saturable absorber can support significantly shorter pulses even though a net gain window remains open after the short pulse (Fig. 2.1.5c). At first this seems surprising, because on the trailing edge of the pulse there is no shaping action of the absorber and even worse one would expect that the net gain after the pulse would destabilize the pulse. However, we have shown that in the picosecond regime without soliton formation, a more strongly saturated slow saturable absorber can stabilize a shorter pulse because the pulse is constantly delayed by the absorber and therefore swallows any noise growing behind himself [01Pas1]. This means that even with solid-state lasers we can work with relatively slow saturable absorbers that have approximately a recovery time in the range of 10 to 30 times the absorber recovery time. In the femtosecond regime soliton formation is actually the dominant pulse-forming mechanism and the slow saturable absorber needs only to be fast enough to stabilize this soliton - which is referred to as soliton mode-locking [95Kae1, 95Jun2, 96Kae].

### 2.1.3 Overview of ultrafast solid-state lasers

### 2.1.3.1 Overview for different solid-state laser materials

Table 2.1.1 to Table 2.1.3 give a full overview of the different results that have been achieved using different solid-state lasers. The long list as shown in Table 2.1.2 demonstrates how active the field of cw mode-locked lasers has been. The shortest pulses in the two optical cycle regime are being generated by the Ti:sapphire laser using Kerr-Lens Mode-locking (KLM). Otherwise, more recent results clearly demonstrate that the emphasis has shifted towards SESAM mode-locking because more stable and self-starting mode-locking can be achieved and the saturable absorber can be optimized independently from the cavity design. This allowed us to push the frontier in terms of pulse repetition rate and pulse energy by several orders of magnitude. Today, we can obtain a pulse repetition rate of about 160 GHz as compared to around 1 GHz in 1990. In addition, we have increased the pulse energy from the nJ-regime to more than $10 \mu \mathrm{~J}$ from a passively mode-locked diode-pumped solid-state laser at $10-50 \mathrm{MHz}$ pulse repetition rates during the last decade which is an increase of more than four orders of magnitude. More results are summarized in Table 2.1.2 and discussed below in Sect. 2.1.3.1.1 to Sect. 2.1.3.1.3. $Q$-switching results are restricted to microchip lasers because the pulse duration scales with the photon cavity lifetime. Thus, the shorter the laser cavity, the shorter the pulses that can be generated as discussed in Sect. 2.1.3.1.4.

In the past few years, a novel type of laser has bridged the gap between semiconductor lasers and solid-state lasers. The Vertical-External-Cavity Surface-Emitting Laser (VECSEL) [99Kuz]
combines the best of both worlds: the semiconductor gain medium allows for flexible choice of emission wavelength via bandgap engineering and offers a wealth of possibilities from the semiconductor processing world. SESAM mode-locked optically pumped VECSELs have already pulled even with solid-state lasers in the GHz pulse repetition rate regime and will be briefly reviewed in Sect. 2.1.3.1.5. For a more detailed recent review we refer to [06Kel]. Semiconductor lasers have the advantage that the SESAM can be integrated into the gain structure. This holds promise for high-volume wafer-scale fabrication of compact, ultrafast lasers. Recently, this vertical integration of ultrafast semiconductor lasers has been demonstrated for the first time and is referred to as a Mode-locked Integrated External-cavity Surface Emitting Laser (MIXSEL) [07Bel].

Ultrafast fiber lasers also demonstrate very good performances and are being briefly reviewed in Sect. 2.1.3.1.6.

### 2.1.3.1.1 Solid-state laser materials

Solid-state lasers can be grouped in two types: transition-metal-doped $\left(\mathrm{Cr}^{2+}, \mathrm{Cr}^{3+}, \mathrm{Cr}^{4+}, \mathrm{Ti}^{3+}\right.$, $\mathrm{Ni}^{2+}, \mathrm{Co}^{2+}$ ) and rare-earth-doped $\left(\mathrm{Nd}^{3+}, \mathrm{Tm}^{3+}, \mathrm{Ho}^{3+}, \mathrm{Er}^{3+}, \mathrm{Yb}^{3+}\right)$ solid-state lasers (Table 2.1.1). Color-center lasers have also supported ultrashort pulse durations, but they require cryogenic cooling [87Mit, 89Isl]. A similar wavelength range can be covered with Cr:YAG lasers, for example. Table 2.1.1 to Table 2.1.3 summarize the laser parameters of these solid-state lasers and the performance that has been demonstrated with these lasers up to date with mode-locking (Table 2.1.2) and $Q$-switching (Table 2.1.3). $Q$-switching in Table 2.1.3 is restricted to microchip lasers because of the very short laser cavity that can support even picosecond pulses with $Q$ switching.

Several factors are important to achieve a good power efficiency: a small quantum defect, the absence of parasitic losses, and a high gain ( $\sigma_{\mathrm{L}} \tau_{\mathrm{L}}$ product, where $\sigma_{\mathrm{L}}$ is the gain cross section and $\tau_{\mathrm{L}}$ the upper-state lifetime of the gain medium) are desirable. The latter allows for the use of an output coupler with relatively high transmission, which makes the laser less sensitive to intracavity losses. For high-power operation, we prefer media with good thermal conductivity, a weak (or even negative) temperature dependence of the refractive index (to reduce thermal lensing), and a weak tendency for thermally induced stress fracture.

For ultrafast lasers, in addition we require a broad emission bandwidth because of large bandwidths of ultrashort pulses. More precisely, we need a large range of wavelengths in which a smoothly shaped gain spectrum is obtained for a fixed inversion level. The latter restrictions explain why the achievable mode-locked bandwidth is in some cases (e.g., some $\mathrm{Yb}^{3+}$-doped media [99Hoe2]) considerably smaller than the tuning range achieved with tunable cw lasers, particularly for quasi-three-level gain media. A less obvious requirement is that the laser cross sections should be high enough. While the requirement of a reasonably small pump threshold can be satisfied even with low laser cross sections if the fluorescence lifetime is large enough, it can be very difficult to overcome $Q$-switching instabilities (see Sect. 2.1.6.8) in a passively mode-locked laser based on a gain material with low laser cross sections. Unfortunately, many broad-band gain media tend to have low laser cross sections, which can significantly limit their usefulness for passive mode-locking, particularly at high pulse repetition rates and in cases where a poor pump beam quality or poor thermal properties necessitate a large mode area in the gain medium.

Finally, a short pump absorption length is desirable because it permits the use of a small path length in the medium, which allows for operation with a small mode area in the gain medium and also limits the effects of dispersion and Kerr nonlinearity. The latter is particularly important for very short pulses. In addition, short pump absorption length is required for the thin-disk laser concept [94Gie] which so far supports the highest pulse energies in the $10 \mu \mathrm{~J}$-regime directly generated from a passively mode-locked laser [06Mar, 07Mar].
Table 2.1.1. Relevant laser materials for short and ultrashort pulse generation. $\lambda_{0}$ : center lasing wavelength. $\sigma_{\mathrm{L}}$ : gain cross-section. $\tau_{\mathrm{L}}$ : upper-state lifetime. $\Delta \lambda_{\mathrm{g}}$ : FWHM gain bandwidth. $\tau_{\mathrm{p}, \text { min }}$ : minimal pulse duration that has been demonstrated so far (coupled-cavity mode-locking schemes are not considered because of their complexity, for further information with regards to coupled-cavity mode-locking results see Table 2.1.2).

| Laser material | Ref. | $\lambda_{0}[\mathrm{~nm}]$ | $\sigma_{\mathrm{L}}\left[10^{-20} \mathrm{~cm}^{2}\right]$ | $\tau_{\mathrm{L}}[\mu \mathrm{S}]$ | $\Delta \lambda_{\mathrm{g}}[\mathrm{nm}]$ | $\tau_{\mathrm{p}, \text { min }}$ | $\tau_{\mathrm{p}, \text { min }}$ Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Transition-metal-doped solid-state lasers ( $\mathrm{Cr}^{2+}, \mathrm{Cr}^{3+}, \mathrm{Cr}^{4+}, \mathrm{Ti}^{3+}$ ) |  |  |  |  |  |  |  |
| $\mathrm{Ti}^{3+}$ :sapphire | [86Mou, 96Koe] | 790 | 41 | 3.2 | $\approx 230$ | 5-6 fs | [99Sut, 01Ell] |
| $\mathrm{Cr}^{3+}$ :LiSAF | [89Pay, 91Sch1, 96Koe] | 850 | 5 | 67 | 180 | 9.9 fs | [03Uem] |
| $\mathrm{Cr}^{3+}: \mathrm{LiCAF}$ | [88Pay] | 758 | 1.23 | 175 | 115 | 9 fs | [02Wag] |
| $\mathrm{Cr}^{3+}$ :LiSGAF | [92Smi] | 835 | 3.3 | 88 | 190 | 14 fs | [97Sor] |
| $\mathrm{Cr}^{3+}$ :LiSCAF | [92Cha] | $\approx 800$ |  | 80 | $\approx 155$ | 90 fs | [94Wan] |
| $\mathrm{Cr}^{3+}$ :alexandrite | [79Wal, 89Sam, 96Koe] | 750 | 0.76 | 260 | $\approx 100$ | 3 ps | [84Pes] |
| $\mathrm{Cr}^{4+}$ :forsterite | [88Pet, 93Car, 96Koe] | 1240 | 14.4 | 2.7 | 170 | 14 fs | [01Chu] |
| $\mathrm{Cr}^{4+}$ :YAG | [88Ang, 95Kue] | 1378 | 33 | 4.1 | $\approx 250$ | 20 fs | [02Rip1] |
| $\mathrm{Cr}^{2+}: \mathrm{ZnSe}$ | [97Pag, 03Dru] | 2500 | 90 | 7 | 600 ( $\approx 11 \mathrm{fs}$ ) | 83 fs | [07Sor] |
| $\mathrm{Cr}^{2+}: \mathrm{ZnS}$ | [97Pag, 03Dru] | 2350 | 140 | 4.5 | 500 |  |  |
| Rare-earth-doped solid-state lasers ( $\left.\mathbf{N d}^{3+}, \mathrm{Yb}^{3+}, \mathrm{Er}^{3+}\right)$ |  |  |  |  |  |  |  |
| Nd:YAG | [64Geu, 97Zay] | 1064 | 33 | 230 | 0.6 | 4.5 ps | [00Lar] |
| Nd:YLF | [69Har, 97Zay, 96Koe] | 1047 | 18 | 480 | 1.2 | 1.5 ps | [90Mal] |
|  |  | 1314 |  | 480 |  | 5.7 ps | [96Flu2] |
| $\mathrm{Nd}: \mathrm{YVO}_{4}$ | [87Fan, 88Ris, 98For] | 914 | 4 |  |  | 3 ps | [05Sch1] |
|  | [97Zay] | 1064 | 300 | 100 | 0.8 | 2.7 ps | [00Kra2, 05Lec1] |
|  |  | 1342 | 60 | 100 |  | 4.6 ps | [96Flu2] |
| $\mathrm{Nd}: \mathrm{YAlO}_{3}$ |  | 930 | 4.1 | 160 | 2.5 | 1.9 ps | [98Kel] |
| Nd:LSB (10 at.\%) | [91Kut, 94Mey] | 1064 | 13 | 118 | 4 | 1.6 ps | [96Bra2] |
| Nd:GdVO ${ }_{4}$ | [94Jen] | 1064 | 76 | 90 |  | 4.4 ps | [05Agn] |
| $\mathrm{Nd}:(\mathrm{Gd}, \mathrm{Y}) \mathrm{VO}_{4}$ | [03Qin] | 1064 |  |  |  | 2.6 ps | [05Wan] |
| Nd:phosphate glass (LG-760) | [99Sch] | 1054 | 4.5 | 323 | 24.3 | 150 fs | [95Kop1] |

Table 2.1.1 continued.

| Laser material | Ref. | $\lambda_{0}[\mathrm{~nm}]$ | $\sigma_{\mathrm{L}}\left[10^{-20} \mathrm{~cm}^{2}\right]$ | $\tau_{\mathrm{L}}[\mu \mathrm{S}]$ | $\Delta \lambda_{\mathrm{g}}[\mathrm{nm}]$ | $\tau_{\mathrm{p}, \text { min }}$ | $\tau_{\mathrm{p}, \text { min }}$ Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nd:silicate glass (LG-680) | [99Sch] | 1059.7 | 2.54 | 361 | 35.9 | 68 fs | [97Aus] |
| Nd:fluorophosphate <br> glass (LG-812) | [78Sch] | 1054 | 2.6 | 495 | 26.1 | 60 fs | [97Aus] |
| Dual glass gain laser | Nd:fluorophosphate \& silicate | 1064 |  |  |  | 38 fs | [02Han] |
| Yb:YAG | [93Fan] | 1030 1050 | 2.0 | 950 | 6.3 | 340 fs 136 fs | [96Kel, 99Hoe2] [05Uem] |
| $\mathrm{Yb}: \mathrm{YVO}_{4}$ | [04Kis, $04 \mathrm{Kra1}$ ] | 1037 | 1.25 | 250 |  | 120 fs | [05Kis] |
| $\mathrm{Yb}: \mathrm{LuVO}_{4}$ | [05Liu, 06Riv] | 1020-1055 | 0.2-1.0 | 256 |  | 58 fs | [06Riv] |
| Yb:CAlGO | [05Pet] | 1016-1050 | 0.75 |  |  | $110 \mathrm{fs}(47 \mathrm{fs})$ | [06Zao] |
| Yb:KGW | [97Kul1, 97Kul2, 03Kul] | 1026 | 2.8 | $\approx 250$ | $\approx 25$ | 100 fs | [04Pau] |
| Yb:KYW | [97Kul1, 97Kul2, 02Puj, 00Dem] | 1025 | 3.0 | $\approx 250$ | $\approx 25$ | 71 fs | [01Liu] |
| Yb:KLuW |  |  |  |  |  | 114 fs | [05Riv] |
| Yb:NGW | [06Cas] | 1014-1079 | $\approx 2.0$ | 380 |  | 120 fs | [06Cas] |
| Yb:NaYW | [07Gar] | $\approx 1030$ | 3 | 309 |  | 67 fs ( 53 fs ) | [07Gar] |
| Yb:NLM | [05Man] | 1000 | 3.5 | 285 |  |  |  |
| Yb:GdCOB | [99Mou] | 1045 | 0.36 | 2600 | 44 | 90 fs | [00Dru] |
| Yb:BOYS | [02Dru1] | 1062 | 0.2 | 1100 | 60 | 69 fs | [02Dru1] |
| Yb:SIS | [03Dru] | 1040 | 0.44 | 820 | 73 | 70 fs | [04Dru] |
| $\mathrm{Yb}: \mathrm{CaF}_{2}$ | [04Pet] |  |  |  |  | 150 fs | [04Luc] |
| Yb:YSO | [04Jac, 95Jac] | 1000-1010 |  |  |  | 122 fs | [06Thi] |
| Yb:LSO | [95Jac] |  |  |  |  | 198 fs | [06Thi] |
| Yb:GSO | [06Xue] | 1088 | 0.42 | 1110 | 70 | 343 fs | [07Li] |
| $\mathrm{Yb}: \mathrm{Lu}_{2} \mathrm{O}_{3}$ | [04Gri] | 1030 | 1.0 | 820 |  | 220 fs | [04Gri] |
| Yb :BCBF | [96Sch] | 1034 | 1.3 | 1170 | 24 |  |  |
| Yb:LSB | [05Rom] | 1041 | 0.28 | 600-1200 |  | 72 fs ( 58 fs ) | [07Riv] |
| Yb:YAB | [00Wan] | 1040 | 0.8 | 680 | 25 | 198 fs | [02Led] |
| Yb:S-FAP | [94DeL] | 1047 | 7.3 | 1260 | 4 |  |  |
| Yb:FAB | [94DeL] | 1043 | 5.9 | 1100 | 4.1 |  |  |
| Yb:phosphate glass |  | 1025-1060 | 0.049 | 1300 | 62 | 58 fs | [98Hoe, 99Hoe2] |
| Yb :silicate glass |  | 1025-1060 | 0.093 | 1100 | 77 | 61 fs | [98Hoe, 99Hoe2] |
| Yb:fluoride phosphate |  | 1025-1060 | 0.158 | 1300 | 81 | 60 fs | [98Hoe] |
| Er,Yb:glass | [91Lap, 96Kig, 99Lap] | 1535 | 0.8 | 7900 | 55 | 255 fs | [05Spu1] |

Table 2.1.2. CW mode-locked solid-state lasers using different mode-locking techniques. "Best" means in terms of pulse duration, highest average output power, highest pulse repetition rate etc. - the result for which "best" applies is in bold letters. The lasers are assumed to be diode-pumped, if not stated otherwise (except Ti:sapphire laser). ML: Mode-Locking. CCM: Coupled-Cavity Mode-locking. APM: Additive Pulse Mode-locking. RPM: Resonant Passive Mode-locking. KLM: Kerr-Lens Mode-locking. SESAM: passive mode-locking using SEmiconductor Saturable Absorber Mirrors (SESAMs). Soliton-SESAM: Soliton mode-locking with a SESAM. AOM: Acousto-Optic Modulator. EOM: Electro-Optic phase Modulator. $\lambda_{0}$ : center lasing wavelength. $\tau_{\mathrm{p}}$ : measured pulse duration. $P_{\mathrm{av}, \text { out }}$ : average output power. $f_{\text {rep }}$ : pulse repetition rate.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ti:sapphire |  |  |  |  |  |  |  |
| $\mathrm{Ti}^{3+}: \mathrm{Al}_{2} \mathrm{O}_{3}$ | active-AOM | 814 nm | 150 fs | 600 mW | 80.5 MHz |  | [91Cur] |
|  |  | 780 nm | 1.3 ps | 2 W | 82 MHz |  | [92Kaf] |
|  | CCM-APM |  | 1.4 ps | 300 mW |  | highly chirped 1.4 ps output pulses externally compressed down to 200 fs | [89Goo] |
|  | CCM-RPM | 860 nm | 2 ps | 90 mW | 250 MHz |  | [90Kel2] |
|  | dye sat. absorber | 750 nm | 140 fs |  |  | KLM started with dye saturable absorber (not understood - assumed to have a CPM Ti:sapphire laser) | [91Sar] |
|  | KLM | 880 nm | 60 fs | 300 mW |  | first demonstration of KLM (but KLM not understood) | [91Spe] |
|  |  | 852 nm | 73 fs | 240 mW | 134 MHz | first experimental evidence for KLM, self-starting due to RPM | [91Kel] |
|  |  |  |  |  |  | KLM, a Gaussian approximation | [91Sal1] |
|  |  |  | 47 fs | 110 mW |  |  | [92Riz1] |
|  |  | 820 nm | 39 fs | 1.5 W | 82 MHz |  | [92Kaf] |
|  |  | 813 nm | 32 fs | 320 mW | $\approx 100 \mathrm{MHz}$ | LaFN28-glass prisms, 2 cm Ti:sapphire crystal thickness | [92Hual] |
|  |  |  | 33 fs |  |  | Schott F2 prisms, 8 mm Ti:sapphire crystal thickness | [92Kra1] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 804 nm | 22 fs | 950 mW | 100 MHz | Schott LaK31 prisms, 2 cm Ti:sapphire crystal thickness | [92Lem] |
|  |  | 817 nm | 17 fs | 500 mW | 80 MHz | Schott LaKL21 prisms, 9 mm Ti:sapphire crystal thickness | [92Hua2] |
|  |  | 775 nm | 12.3 fs |  |  | fused silica prisms, 4 mm Ti:sapphire crystal thickness | [93Cur] |
|  |  | 780 nm | 11 fs | 500 mW |  | fused silica prisms, 4.5 mm Ti:sapphire crystal thickness | [93Asa] |
|  |  |  | 11 fs | 300 mW | 100 MHz | chirped mirrors, no prisms | [94Sti] |
|  |  | 850 nm | 8.5 fs | $\approx 1 \mathrm{~mW}$ |  | metal mirrors and fused silica prisms | [94Zho] |
|  |  | 800 nm | 8.2 fs | 100 mW | 80 MHz | chirped mirrors only | [95Sti] |
|  |  | 800 nm | 7.5 fs | 150 mW |  | chirped mirrors, ring cavity | [96Xu2] |
|  |  | 800 nm | 6.5 fs | 200 mW | 86 MHz | fused silica prisms and double-chirped mirrors, KLM is self-starting with SESAM | [97Jun3] |
|  |  | $\approx 800 \mathrm{~nm}$ | 5.8 fs | 300 mW | 85 MHz | fused silica prisms and double-chirped mirrors, KLM is self-starting with SESAM, pulse duration measured with SPIDER [00Mat] | [99Sut, 00Mat] |
|  |  | $\approx 800 \mathrm{~nm}$ | $\approx 5 \mathrm{fs}$ | 200 mW | 90 MHz | $\mathrm{CaF}_{2}$ prisms, double-chirped mirrors, pulse duration measured with fit to IAC (not very accurate) | $\begin{aligned} & \text { [99Mor 1, } \\ & \text { 99Mor2] } \end{aligned}$ |
|  |  | $\approx 800 \mathrm{~nm}$ | $\approx 5 \mathrm{fs}$ | 120 mW | 65 MHz | similar to [99Mor1] but with double-Z cavity with second focus in a glass plate for additional SPM | [01Ell] |
|  |  | $\approx 800 \mathrm{~nm}$ | 9.5 fs | 180 mW | 85 MHz | KLM self-starting with novel broadband fluoride SESAM | [02Sch2] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | soliton-SESAM | 780 nm | 8.5 fs | 1 W | 75 MHz | 1.5 MW peak, focused intensity $5 \times 10^{13} \mathrm{~W} / \mathrm{cm}^{2}$ | [98Xu] |
|  |  | 850 nm | 13 fs | 1.5 W | 110 MHz | 1 MW peak, 13 nJ out | [99Bed] |
|  |  | 800 nm | 16.5 fs | 170 mW | 15 MHz | 0.7 MW peak, $0.011 \mu \mathrm{~J}$ | [99Cho] |
|  |  | 788 nm | 43 fs |  | 5.85 MHz | $150 \mathrm{~nJ}, 3.5 \mathrm{MW}$ peak | [03Kow] |
|  |  | $\approx 800 \mathrm{~nm}$ | $\begin{aligned} & 26 \mathrm{fs} \\ & 30 \mathrm{fs} \end{aligned}$ | $\begin{aligned} & \approx 1.5 \mathrm{~W} \\ & \approx 2 \mathrm{~W} \end{aligned}$ | $\begin{aligned} & 11 \mathrm{MHz} \\ & 11 \mathrm{MHz} \end{aligned}$ | 130 nJ par $280 \mathrm{~nJ},>5 \mathrm{MW}$ peak | [04Fer] |
|  |  | $\approx 800 \mathrm{~nm}$ | 50 fs | $\begin{aligned} & 1 \mathrm{~W} \\ & 2.5 \mathrm{~W} \end{aligned}$ | $\begin{aligned} & 2 \mathrm{MHz} \\ & 50 \mathrm{MHz} \end{aligned}$ | $\begin{aligned} & \mathbf{0 . 5} \mu \mathbf{J} \\ & 50 \mathrm{~nJ} \end{aligned}$ | [05Nau] |
|  |  | 782 nm | 23 fs | 300 mW | 2 GHz | ring laser, ML is self-starting due to feedback from external mirror | [99Bar] |
|  |  | $\begin{aligned} & 560-1150 \mathrm{~nm} \\ & @-50 \mathrm{dBc} \end{aligned}$ |  |  | 1 GHz | five-element ring laser | [02Bar] |
|  |  | 840 nm | 34 fs | 140 mW | 98.9 MHz | first SESAM design with a single quantum-well absorber in a Bragg reflector | [95Bro2] |
|  |  |  | 90 fs |  |  | new acronym for special SESAM design: SBR | [95Tsu] |
|  |  | 810 nm | 13 fs | 80 mW | 85 MHz | shortest pulse with soliton mode-locking and no KLM | [96Kae] |
|  | KLM and dumped | 840 nm | 240 fs | 10 mW | 2.3 GHz |  | [03Sto] |
|  |  | 800 nm | 54 fs | 3.5 W | 6.23 MHz | $0.56 \mu$ s pulse energy | [06Dew] |
|  |  | cavity-835 nm | 50 fs |  | $\leq 950 \mathrm{kHz}$ | 100 nJ pulse energy | [93Ram2] |
|  |  | 800 nm | 13 fs |  | 80 kHz | $62 \mathrm{~nJ}, 5 \mathrm{MW}$ peak power | [94Psh] |
|  |  |  | 17 fs |  | 1 kHz | 212 nJ pulse energy | [96Gib] |
|  |  |  | 4.6 fs |  | $\leq 1 \mathrm{MHz}$ | 2 MW peak power | [97Bal] |
|  |  | 780 nm | 60 fs | 0.36 W | 0.8 MHz | $\mathbf{0 . 4 5} \mu \mathbf{J}$ pulse energy | [06Zho] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cr:LiSAF |  |  |  |  |  |  |  |
| $\mathrm{Cr}^{3+}: \mathrm{LiSrAlF}_{6}$ | KLM | 800-880 nm | 150 fs | 50 mW | 82 MHz | first mode-locked femtosecond Cr:LiSAF laser, Kr-pumped | [92Mil] |
|  |  | $\approx 840 \mathrm{~nm}$ | 50 fs | 135 mW |  | Ar-ion pumped, intracavity dye absorber for starting KLM | [92Riz2] |
|  |  | 880-920 nm | 50 fs | 150 mW | 85 MHz | Ar-ion pumped, regenerative AOM for starting KLM | [92Eva] |
|  |  |  | 33 fs | 25 mW |  | Ar-ion pumped, intracavity dye absorber for starting KLM | [92Riz3] |
|  |  |  | 93 fs | 5 mW |  | Ar-ion pumped, KLM started with intracavity SESAM | [93Riz] |
|  |  |  | 300 ps | $\approx 1 \mathrm{~mW}$ |  | first diode-pumped modelocked Cr:LiSAF laser, AOM or RPM for starting KLM | [93Fre] |
|  |  |  | 220 fs | $\approx 10 \mathrm{~mW}$ |  | KLM started by SESAM | [94Mel] |
|  |  | 870 nm | 90 fs | $<20 \mathrm{~mW}$ | 90 MHz | pumped by a SHG diodepumped actively mode-locked Nd:YLF laser, prism modelocker to start KLM | [94Lin1] |
|  |  | 860 nm | 97 fs | 2.7 mW | 80 MHz | KLM started by regen. AOM | [94Dym] |
|  |  | 880 nm | 34 fs | 42 mW | 80 MHz | KLM started by regen. AOM | [95Dym] |
|  |  | 850 nm | 55 fs | 10 mW |  | KLM self-starting | [95Fal] |
|  |  |  | 40 fs (24 fs) | $\begin{aligned} & 70 \mathrm{~mW} \\ & (\approx 1 \mathrm{~mW}) \end{aligned}$ |  |  | [ 95 Mel ] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| soliton-SESAM |  | 875 nm | 18 fs | $\approx 1 \mathrm{~mW}$ |  |  | [97Dym] |
|  |  | 880 nm | 14.8 fs | 70 mW | 70 MHz | Kr-ion-laser pumped | [97Sor] |
|  |  | 850 nm | 12 fs | 23 mW | 200 MHz | ML not self-starting | [99Uem] |
|  |  | $\approx 850 \mathrm{~nm}$ | 9.9 fs |  |  | strong wings in IAC | [03Uem] |
|  |  | 840 nm | 98 fs | 50 mW | 120 MHz | first soliton mode-locking, no KLM required | [94Kop1] |
|  |  | 850 nm | 45 fs | 105 mW | 176 MHz |  | [95Kop2, <br> 97Kop2] |
|  |  | 865 nm | 100 fs | 11 mW | 178 MHz |  | [95Tsu] |
|  |  | 842 nm | 160 fs | 25 mW |  | compact cavity design with no prisms for dispersion compensation (dispersive SESAM) | [96Kop2] |
|  |  | 868 nm | 70 fs | 100 mW |  | 0.5 W diffraction-limited MOPA pump | [96Tsu] |
|  |  | 860 nm | 60 fs | 125 mW | 176 MHz |  | [97Kop2] |
|  |  | 875 nm | 50 fs | 340 mW | 150 MHz | low-brightness 0.9 cm wide, 15 W diode laser array | [97Kop3] |
|  |  | 875 nm | 110 fs | 500 mW | 150 MHz | low-brightness 0.9 cm wide, 15 W diode laser array | [97Kop3] |
|  |  | 855 nm | 57 fs | 6.5 mW | 150 MHz | only 72 mW pump power with 1.5 V AA batteries | [98Hop] |
|  |  | 848 nm | 94 fs | 110 mW | 130 MHz | only one GTI mirror | [99Rob] |
|  |  |  | 80 fs |  | 100 MHz | $20 \mathrm{fs}(25 \mathrm{mHz} \ldots 10 \mathrm{kHz})$ rms timing jitter | [99Tsu] |
|  |  | 857 nm | 146 fs | 3 mW | 1 GHz |  | [01Kem] |
|  |  | 844 nm | 113 fs | 20 mW | 407 MHz | less than 110 mW pump | [02Hop] |
|  |  | 867 nm | 39 fs | 6.5 mW | 8.6 MHz | $0.75 \mathrm{~nJ}, \mathrm{DCM}$ without prisms | [03Pra] |
|  |  | 856 nm | 43 fs | 5.5 mW | 8.4 MHz | 0.66 nJ, DCM with prisms | [03Pra] |

[^0]Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cr:LiCAF |  |  |  |  |  |  |  |
| $\mathrm{Cr}^{3+}$ :LiCaAlF $_{6}$ | KLM | 800 nm | 170 fs | 100 mW | 90 MHz | Kr-pumped | [92LiK] |
|  |  | 793 nm | 52 fs | 75 mW | 95 MHz |  | [98Gab] |
|  |  | 820 nm | 20 fs | 13 mW | 95 MHz |  | [98Gab] |
|  |  | $\approx 850 \mathrm{~nm}$ | 9 fs | 220 mW | 97 MHz | Ti:sapphire laser pumped, only fit to IAC measurement | [02Wag] |
|  |  | $\approx 850 \mathrm{~nm}$ | 10 fs | 40 mW | 110 MHz | DCM and prisms, SPIDER | [03Wag] |
| Cr:LiSGaF |  |  |  |  |  |  |  |
| $\mathrm{Cr}^{3+}: \mathrm{LiSrGaIF}_{6}$ | KLM | 830 nm | $100 \mathrm{fs}(50 \mathrm{fs})$ | 35 mW | 71 MHz |  | [95Yan] |
|  |  | 835 nm | 64 fs |  |  | Kr-ion-laser pumped | [96Sor1] |
|  |  | 842 nm | 44 fs | 200 mW | 80 MHz | Kr-ion-laser pumped, GTI | [96Sor2] |
|  |  | 895 nm | 14 fs | 100 mW | 70 MHz | Kr -ion-laser pumped, chirped mirror | $\begin{aligned} & \text { [97Sor, } \\ & \text { 98Sor] } \end{aligned}$ |
|  | soliton-SESAM | 839 nm | 61 fs | 78 mW | 119 MHz |  | [97Loe] |
|  |  |  | 38 fs | 20 mW | 90 MHz |  | [01Dai] |
| Cr:LiSCAF |  |  |  |  |  |  |  |
| $\mathrm{Cr}^{3+}: \mathrm{LiSr}_{0.8} \mathrm{Ca}_{0.2} \mathrm{AlF}_{6}$ | KLM | 860 nm | 90 fs | 100 mW | 140 MHz | Kr-ion-laser pumped | [94Wan] |
| Cr:forsterite |  |  |  |  |  |  |  |
| $\mathrm{Cr}^{4+}: \mathrm{Mg}_{2} \mathrm{SiO}_{4}$ | KLM | $\begin{aligned} & 1.23 \mu \mathrm{~m} \\ & (1.21-1.27 \mu \mathrm{~m}) \end{aligned}$ | 48 fs | 380 mW | 81 MHz | Nd:YAG laser pumped, KLM self-starting with AOM | [93Sen] |
|  |  | $1.24-1.27 \mu \mathrm{~m}$ | 50 fs | 45 mW | 82 MHz | Nd:YAG laser pumped | [93Sea] |
|  |  | $1.27 \mu \mathrm{~m}$ | 25 fs | 300 mW | 80 MHz | Nd:YAG laser pumped | [93Yan] |
|  |  | $1.28 \mu \mathrm{~m}$ | 20 fs |  |  | $\mathrm{Nd}: \mathrm{YVO}_{4}$ laser pumped, not self-starting | [97Zha2] |

Table 2.1.2 continued.

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | soliton-SESAM | $1.541 \mu \mathrm{~m}$ | 110 fs | 70 mW |  | Nd: $\mathrm{YVO}_{4}$ laser pumped | [96Col] |
|  |  | $1.5 \mu \mathrm{~m}$ | 114 fs | 94 mW | 185 MHz | $\mathrm{Nd}: \mathrm{YVO}_{4}$ laser pumped | [97Spa] |
|  |  | $1.52 \mu \mathrm{~m}$ | 200 fs | 82 mW | $\begin{aligned} & 0.9, \\ & 2.7 \mathrm{GHz} \end{aligned}$ | 1.8,Nd: $\mathrm{YVO}_{4}$ laser pumped, 0.9 GHz fundamental, then double and triple harmonics | [97Col] |
|  |  | $1.52 \mu \mathrm{~m}$ | 75 fs | 280 mW | 1 GHz | Nd: $\mathrm{YVO}_{4}$ laser pumped | [98Mel] |
|  |  | $1.46 \mu \mathrm{~m}$ | 400 fs | 230 mW | 152 MHz | Nd:YAG laser pumped, single prism for dispersion comp. | [98Cha] |
|  |  | $1.52 \mu \mathrm{~m}$ | 44 fs | 65 mW |  | Nd: $\mathrm{YVO}_{4}$ laser pumped | [99Zha] |
|  |  | $1.5 \mu \mathrm{~m}$ | 36 fs | 300 mW |  | oxidized GaAs/AlAs SESAM | [02Rip2] |
|  |  | $1.528 \mu \mathrm{~m}$ | 120 fs | 95 mW | 205 MHz | Yb:fiber laser pumped | [03Lag2] |
|  |  | $\approx 1.5 \mu \mathrm{~m}$ | 57 fs | 200 mW |  | Yb:fiber laser pumped | [03Nau] |
|  | semiconductor-doped glass | 1.510 nm | 10 ps | 35 mW | 235 MHz | PbS -doped glass as sat. abs. | [04Lag2] |
| $\mathrm{Cr}^{2+}$ :ZnSe |  |  |  |  |  |  |  |
|  | active AOM | $2.5 \mu \mathrm{~m}$ | 4.4 ps | 82 mW | 81 MHz |  | [00Car] |
|  | soliton-SESAM | $2.4 \mu \mathrm{~m}$ | 83 fs | 80 mW | 180 MHz | 10 optical cycles | [07Sor] |
| Nd:YAG |  |  |  |  |  |  |  |
| $\mathrm{Nd}^{3+}: \mathrm{Y}_{3} \mathrm{Al}_{5} \mathrm{O}_{12}$ | active AOM | $1.064 \mu \mathrm{~m}$ | 25 ps |  |  | lamp-pumped: pulse shortening due to intracavity etalon | [86Ros] |
|  | active FM | $1.064 \mu \mathrm{~m}$ | 12 ps | 65 mW | 350 MHz |  | [89Mak1] |
|  | active EOM | $1.32 \mu \mathrm{~m}$ | 8 ps | 240 mW | 1 GHz |  | [91Zho] |
|  | active AOM | $1.32 \mu \mathrm{~m}$ | 53 ps | 1.5 W | 200 MHz | lamp-pumped and harmonic mode-locked | [88Kel] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | CCM-APM | $1.064 \mu \mathrm{~m}$ | 1.7 ps | 25 mW | 136 MHz |  | [90Goo] |
|  |  |  | 2 ps | 110 mW | 125 MHz |  | [91McC] |
|  |  |  | 6 ps | 2.4 W | 100 MHz | lamp-pumped | [90Liu1] |
|  |  | $1.32 \mu \mathrm{~m}$ | 10 ps | 700 mW | 100 MHz | lamp-pumped | [90Liu1] |
|  | KLM | $1.064 \mu \mathrm{~m}$ | 8.5 ps | 1 W | 100 MHz |  | [92Liu] |
|  |  |  |  |  |  | lamp-pumped, severe instabilities | [95Chu1] |
|  |  |  | 6.7 ps | 675 mW | 106 MHz | Ti:sapphire laser pumped | [97Hen] |
|  |  |  | 4.5 ps | 800 mW | 101.5 MHz |  | [00Lar] |
|  | SESAM | $1.064 \mu \mathrm{~m}$ | 8.7 ps | 100 mW | 100 MHz |  | [93Wei] |
|  |  |  | 6.8 ps | 400 mW | 217 MHz |  | [94Kel] |
|  |  |  | 16 ps | 10.7 W | 88 MHz |  | [99Spu3] |
|  |  |  | 19 ps | 27 W | 55 MHz | multiple laser heads | [00Spu] |
|  |  |  | 8.3 ps | 1.59 W | 130 MHz | ceramic Nd:YAG | [05Guo] |
|  | polarization switching in nonlinear crystal | $1.064 \mu \mathrm{~m}$ | 23 ps | 4 W | 150 MHz | lamp-pumped, KTP crystal | [99Kub] |
| Nd:YLF |  |  |  |  |  |  |  |
| $\mathrm{Nd}^{3+}: \mathrm{LiYF}_{4}$ | active AOM | $1.053 \mu \mathrm{~m}$ | 37 ps | 6.5 W | 100 MHz | lamp-pumped | [87Bad] |
|  |  |  | 18 ps | 12 mW | 230 MHz |  | [89Mak2] |
|  |  | $1.047 \mu \mathrm{~m}$ | 9 ps | 150 mW | 500 MHz |  | [90Kel1] |
|  |  |  | 7 ps | 135 mW | 2 GHz |  | [90Wei] |
|  |  |  | 6.2 ps | 20 mW | 1 GHz | Ti:sapphire laser pumped | [90Wal] |
|  | active EOM | $1.053 \mu \mathrm{~m}$ | 13 ps | 350 mW | 5.4 GHz | Ti:sapphire laser pumped | [91Sch2] |
|  |  |  | 4 ps | 400 mW | 237.5 MHz |  | [92Wei] |
|  |  |  | 4.5 ps | 400 mW | 2.85 GHz |  | [92Wei] |
|  |  | $1.3 \mu \mathrm{~m}$ | 8 ps | 240 mW | 1 GHz |  | [91Zho] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | active MQW | $1.047 \mu \mathrm{~m}$ | 200 ps | 27 mW | 100 MHz | semiconductor Multiple-Quantum-Well (MQW) modulator | [95Bro3] |
|  | active piezoelectric diffraction modulator | $1.047 \mu \mathrm{~m}$ | 7 ps | 160 mW | 160 MHz |  | [90Juh] |
|  | KLM | $1.047 \mu \mathrm{~m}$ | 3 ps | 250 mW |  |  | [94Lin2] |
|  |  |  | 2.3 ps | 800 mW | 82 MHz | lamp-pumped, microdot mirror | [93Ram1] |
|  | SESAM | $1.047 \mu \mathrm{~m}$ | 3.3 ps | 700 mW | 220 MHz | Ti:sapphire laser pumped | [92Kel2] |
|  |  |  | 5.1 ps | 225 mW | 100 MHz |  | [93Wei] |
|  |  |  | 2.8 ps | 460 mW | 220 MHz |  | [94Kel] |
|  |  | $1.3 \mu \mathrm{~m}$ | 5.7 ps | 130 mW | 98 MHz |  | [96Flu2] |
|  |  |  | $>22 \mathrm{ps}$ | $\begin{aligned} & <20 \mathrm{~W} \\ & \text { on-time } \end{aligned}$ |  | GaInNAs-SESAM but only quasi-cw mode-locking demonstrated | [02Sun] |
|  |  |  | 6.7 ps | 580 mW | 117 MHz | GaInNAs-SESAM | [04Liv] |
|  |  |  | 48 ps | 630 mW | 119 MHz | detailed studies about ML stability above the $Q$-switched mode-locking threshold | [04Sch1] |
|  | CCM-APM |  | 21 ps | 127 mW | 1.4 GHz | low-loss buried resonant GaInNAs SESAM | [06Zel] |
|  |  | $1.053 \mu \mathrm{~m}$ | $70 \mathrm{ps} \ldots 4 \mathrm{~ns}$ | < 680 mW |  |  | [02Rot] |
|  |  | $1.053 \mu \mathrm{~m}$ | 3.7 ps | 7 W | 76 MHz | lamp-pumped | [90Liu2] |
|  |  | $1.047 \mu \mathrm{~m}$ | 1.7 ps |  | 103 MHz |  | [99Jeo] |
|  |  |  | 1.5 ps | 20 mW | 123 MHz |  | [90Mal] |
|  |  |  | 4 ps | 1 W | 120 MHz | pump laser for PPLN OPO | [99Lef] |
|  | CCM-RPM | $1.047 \mu \mathrm{~m}$ | 3.7 ps | 550 mW | 250 MHz | Ti:sapphire laser pumped | [92Kel1] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Nd}: \mathrm{YVO}_{4}$ |  |  |  |  |  |  |  |
|  | SESAM | $1.064 \mu \mathrm{~m}$ | 7 ps | 4.5 W | 84 MHz |  | [97Ruf] |
|  |  |  | 8.3 ps | 198 mW | 13 GHz |  | [99Kra1] |
|  |  |  | 6.8 ps | 81 mW | 29 GHz | Ti:sapphire laser pumped | [99Kra2] |
|  |  |  | 33 ps | 4.4 W | 235 \& 440 MHz |  | [99Gra] |
|  |  |  | 21 ps | 20 W | 90 MHz |  | [00Bur] |
|  |  |  | 21.5 ps | 23.5 W | 147 MHz |  | [01Che1] |
|  |  |  | 4.8 ps | 80 mW | $39,49,59 \mathrm{GHz}$ | Ti:sapphire laser pumped | [00Kra1] |
|  |  |  | 2.7 ps | 288 mW | 40 GHz |  | [05Lec1] |
|  |  |  | 2.7 ps | 65 mW | 77 GHz | Ti:sapphire laser pumped | [00Kra2] |
|  |  |  | 2.7 ps | 45 mW | 157 GHz | Ti:sapphire laser pumped | [02Kra2] |
|  |  |  | 13.7 ps | 2.1 W | 10 GHz |  | [04Lec] |
|  |  |  | 9-23 ps | $<220 \mathrm{~mW}$ |  | ion-implanted InGaAs <br> SESAM, <br> also see [99Led] for SESAM details | [01Led] |
|  |  |  | 31 ps | 1.5 W | 154 MHz | coated GaAs wafer for ML | [02She] |
|  |  |  | 6 ps |  |  | all-optical synchronization | [03Sei] |
|  |  |  | 10.6 ps | 400 mW | 100 MHz | detailed studies about ML stability above the $Q$-switched mode-locking threshold | [04Sch1] |
|  |  |  | 2.1 ps | 1.28 W | 96.5 MHz | output coupling (OC) <br> SESAM, <br> more OC-SESAM [01Spu1] and [96Sha] | [05Fan] |
|  |  |  | 13 ps | $\begin{aligned} & 4.1 \mathrm{~W} \\ & 3.9 \mathrm{~W} \\ & 3.5 \mathrm{~W} \end{aligned}$ | $\begin{aligned} & \text { 4.1 MHz } \\ & 2.6 \mathrm{MHz} \\ & 1.5 \mathrm{MHz} \end{aligned}$ |  | [03Kol] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 16.3 ps | 470 mW | 1.2 MHz | 24 kW peak | [03Pap] |
|  |  |  | 13 ps | 3.5, 3.9, 4.1 W | $\begin{aligned} & 1.5, \\ & 4.1 \mathrm{MHz} \end{aligned}$ | 2.6 ,with additional amplifier 50 W | [04Lut] |
|  |  | $1.34 \mu \mathrm{~m}$ | 4.6 ps | 50 mW | 93 MHz |  | [96Flu2] |
|  |  |  | 7 ps | 45 mW | 5 GHz | GaInNAs SESAM | [05Spu2] |
|  |  |  | 7.3 ps | 40 mW | 10 GHz | $4 \mathrm{pJ} @ 10 \mathrm{GHz}$ | [05Spu2] |
|  |  |  | 26 ps | 850 mW | 152 MHz | InAs/GaAs quantum dot SESAM | [05Su] |
|  |  | 914 nm | 3 ps | 42 mW | 234 MHz | Ti:sapphire laser pumped | [05Sch1] |
|  | nonlinear mirror ML | $1.064 \mu \mathrm{~m}$ | 7.9 ps | 1.35 W | 150 MHz |  | [97Agn] |
|  |  | $1.064 \mu \mathrm{~m}$ | 29 ps | 3.25 W | 170 MHz | two LBO crystals used | [05Dat] |
|  | intensity-dependent polarization rotation | $1.064 \mu \mathrm{~m}$ | 2.8 ps | 670 mW | 130 MHz |  | [99Cou] |
| Nd:LSB |  |  |  |  |  |  |  |
| $\mathrm{Nd}: \mathrm{LnM}_{3}\left(\mathrm{BO}_{3}\right)_{4}$ | SESAM | $1.062 \mu \mathrm{~m}$ | 1.6 ps | 210 mW | 240 MHz | Ti:sapphire laser pumped | [96Bra2] |
|  |  |  | 2.8 ps | 400 mW | 177 MHz |  | [96Bra2] |
| Nd:BEL |  |  |  |  |  |  |  |
| $\mathrm{Nd}: \mathrm{La}_{2} \mathrm{Be}_{2} \mathrm{O}_{5}$ | active-AOM | $1.070 \mu \mathrm{~m}$ | 7.5 ps | 230 mW | 250 MHz |  | [91Li] |
|  | active-FM | $1.070 \mu \mathrm{~m}$ | 2.9 ps | 30 mW | 238 MHz | harmonic mode-locking | [91God] |
|  |  |  | 3.9 ps | 30 mW | 20 GHz | harmonic mode-locking | [91God] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nd:YAP |  |  |  |  |  |  |  |
| $\mathrm{Nd}: \mathrm{YAlO}_{3}$ | active AOM | $1.08 \mu \mathrm{~m}$ | 10 ps | 220 mW |  |  | [96Guy] |
|  | SESAM | 930 nm | 1.9 ps | 410 mW | 178 MHz |  | [98Kel] |
|  |  | $1.34 \mu \mathrm{~m}$ | 24 ps | 7 W on-time |  | GaInNAs-SESAM but only quasi-cw mode-locking demonstrated | [02Sun] |
|  | nonlinear mirror ML | $\begin{aligned} & 1.08 \mu \mathrm{~m} \\ & 1.34 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 50 \mathrm{ps} \\ & 15 \mathrm{ps} \end{aligned}$ |  |  | $\mathrm{LiIO}_{3}$ frequency doubler | [91Sta] |
|  |  | $1.08 \mu \mathrm{~m}$ | 31 ps |  |  | pure passive ML unstable, thus used additionally AOM | [99Agn] |
| Nd:KGW |  |  |  |  |  |  |  |
| $\mathrm{Nd}^{3+}: \operatorname{KGd}\left(\mathrm{WO}_{4}\right)_{2}$ | active-FM | $1.067 \mu \mathrm{~m}$ | 12 ps |  | 200 MHz |  | [95Flo] |
|  | KLM | $1.067 \mu \mathrm{~m}$ | 1.7 ps |  |  |  | [96Let] |
|  | CCM-APM | $1.067 \mu \mathrm{~m}$ | 2.3 ps | 850 mW | 76.5 MHz |  | [02Maj1] |
|  | SESAM | $1.067 \mu \mathrm{~m}$ | 6.3 ps | 1 W | 64.5 MHz |  | [02Maj2] |
| $\mathrm{Nd}: \mathrm{GdVO}_{4}$ |  |  |  |  |  |  |  |
|  | SESAM | $1.064 \mu \mathrm{~m}$ | 9.2 ps | 5.4 W | 119 MHz |  | [03He] |
|  |  |  | 8 ps | 600 mW | 154 MHz |  | [03Zha] |
|  |  |  | 11.5 ps | 4.9 W | 140 MHz |  | [04Zha1] |
|  |  |  | 18.9 ps | 3.46 W | 0.37-3.4 GHz | GaAs wafer SESAM | [04Kon] |
|  |  |  | 12 ps | 500 mW | 9.66 GHz |  | [04Kra2] |

Table 2.1.2 continued.

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nd:fluorophosphate | soliton-SESAM | $1.065 \mu \mathrm{~m}$ | 60 fs | 84 mW | 114 MHz |  | [97Aus] |
| Nd:silicate | soliton-SESAM | $1.064 \mu \mathrm{~m}$ | 130 fs | 80 mW | 180 MHz |  | [95Kop1] |
|  | KLM | $\approx 1.07 \mu \mathrm{~m}$ | 64 fs | 30 mW |  | spectral shaping required | [01Lu] |
| Nd: fluorophosphate and Nd:silicate | soliton-SESAM | $1.064 \mu \mathrm{~m}$ | 38 fs | 40 mW |  | dual gain medium both at Brewster's angle | [02Han] |
| Yb:YAG |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{Y}_{3} \mathrm{Al}_{5} \mathrm{O}_{12}$ | soliton-SESAM | $1.03 \mu \mathrm{~m}$ | 540 fs | 100 mW | 81 MHz | first passively mode-locked Yb:YAG laser | [95Hoe] |
|  |  |  | 340 fs | 170 mW |  |  | [99Hoe2] |
|  |  |  | 2.2 ps | 8.1 W | 63 MHz |  | [99Aus] |
|  |  |  | 730 fs | 16.2 W | 35 MHz | first passively mode-locked thin-disk laser, $0.47 \mu \mathrm{~J}$ pulse energy | [00Aus] |
|  |  |  | $\begin{aligned} & 3.3-89 \mathrm{ps} \\ & 0.83-1.57 \mathrm{ps} \end{aligned}$ | 12 W | 28 MHz | tunable pulse duration | [01Bru] |
|  |  |  | 810 fs | 60 W | 34.3 MHz | thin-disk laser, $1.75 \mu \mathrm{~J}$ pulse energy, 1.9 MW peak power | [03Inn] |
|  |  |  | 705 fs | 80 W | 57 MHz | thin-disk laser, $1.4 \mu \mathrm{~J}$ pulse energy | [04Bru] |
|  |  |  | 796 fs | 63 W | 12.3 MHz | thin-disk laser, $5.1 \mu \mathrm{~J}$ pulse energy, 5.6 MW peak power | [06Mar] |
|  |  |  | 791 fs | 45 W | 4 MHz | thin-disk laser with multipass cavity $[64 \mathrm{Her}], \mathbf{1 1} \mu \mathbf{J}$ pulse energy | [07Mar] |
|  |  | $\approx 1.05 \mu \mathrm{~m}$ | 136 fs | 3.1 mW |  | shorter pulses only with extra spectral filtering | [05Uem] |
|  | CCM-APM | $1.03 \mu \mathrm{~m}$ | $1.9 \mathrm{ps}(4.7 \mathrm{ps})$ | 2.5 W (2.7 W) | 115 MHz |  | [03Maj] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y b}: \mathrm{YVO}_{4}$ |  |  |  |  |  |  |  |
|  | soliton-SESAM | $1.021 \mu \mathrm{~m}$ | 120 fs | 300 mW | 150 MHz |  | [05Kis] |
| $\mathrm{Yb}: \mathrm{LuVO}_{4}$ |  |  |  |  |  |  |  |
|  | soliton-SESAM | $1.036 \mu \mathrm{~m}$ | 58 fs | 85 mW | 94 MHz |  | [06Riv] |
| Yb:CAlGO |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{CaGdAlO}_{4}$ | soliton-SESAM | $1.050 \mu \mathrm{~m}$ | 110 fs | 48 mW | 109 MHz | strongly chirped output pulses | [06Zao] |
|  |  |  | 47 fs | 38 mW | 109 MHz | plus external prism pulse compressor | [06Zao] |
| Yb:KGW |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{KGd}\left(\mathrm{WO}_{4}\right)_{2}$ | soliton-SESAM | $1.037 \mu \mathrm{~m}$ | 176 fs | 1.1 W | 86 MHz |  | [00Bru] |
|  |  | $1.046 \mu \mathrm{~m}$ | 112 fs | 200 mW | 86 MHz |  | [00Bru] |
|  |  | $1.028 \mu \mathrm{~m}$ | 169 fs | 18 mW | 100 MHz |  | [02Maj3] |
|  |  | $1.037 \mu \mathrm{~m}$ | 100 fs | 126 mW |  | $\mathrm{Yb}: \mathrm{KGW}$ and Y:KYW tested with the same cavity and SESAM | [04Pau] |
|  |  | $1.031 \mu \mathrm{~m}$ | 296 fs | 3.7 W | 61 MHz |  | [06Maj] |
|  |  | $1.040 \mu \mathrm{~m}$ | 433 fs | 10 W | 45 MHz | $0.22 \mu \mathrm{~J}$ pulse energy | [06Hol] |
|  |  |  | 134 fs | 5.3 W | 45 MHz | $0.12 \mu \mathrm{~J}$ pulse energy | [06Hol] |

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Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Yb:KYW |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{KY}\left(\mathrm{WO}_{4}\right)_{2}$ | soliton-SESAM | $1.046 \mu \mathrm{~m}$ | 101 fs | 100 mW | 95 MHz |  | [02Klo] |
|  |  | $1.028 \mu \mathrm{~m}$ | 240 fs | 22 W | 25 MHz | thin-disk laser, $0.9 \mu \mathbf{J}$ pulse energy, 3.3 MW peak power | [02Bru] |
|  |  | $1.047 \mu \mathrm{~m}$ | 123 fs | 107 mW | 114 MHz |  | [03Lag1] |
|  |  | $1.039 \mu \mathrm{~m}$ | 106.5 fs | 92 mW |  | Yb:KGW and Y:KYW tested with the same cavity and SESAM | [04Pau] |
|  |  | $1.029 \mu \mathrm{~m}$ | 6.8 ps | 90 mW | 105 MHz | quantum dot SESAM under reverse bias | [05Lag] |
|  | KLM | $1.057 \mu \mathrm{~m}$ | 71 fs | 120 mW | 110 MHz |  | [01Liu] |
|  |  | $1.056 \mu \mathrm{~m}$ | 107 fs | 126 mW | 294 MHz | tunable 1042-1075 nm | [04Lag1] |
|  | SESAM and cavity-dumping | $1.040 \mu \mathrm{~m}$ | 380 fs | 1.35 W | 1 MHz | $1.35 \mu \mathrm{~J}$ pulse energy | [05Kil1] |
|  |  | $1.024 \mu \mathrm{~m}$ | 680 fs | 3.21 W | 1.06 MHz | $3 \mu \mathbf{J}$ pulse energy | [07Pal] |
| Yb:KLuW |  |  |  |  |  |  |  |
| Yb:NGW |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{NaGd}\left(\mathrm{WO}_{4}\right)_{2}$ | soliton-SESAM | $1.038 \mu \mathrm{~m}$ | 120 fs | 360 mW | 97 MHz | potential for shorter pulses | [06Cas] |
| Yb:NaYW |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{NaY}\left(\mathrm{WO}_{4}\right)_{2}$ | soliton-SESAM | $1.030 \mu \mathrm{~m}$ | 67 fs |  | 96 MHz | Ti:sapphire laser pumped | [07Gar] |
|  |  |  | 53 fs | 91 mW | 96 MHz | plus external cavity SF10prism compressor | [07Gar] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Yb:GdCOB |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{Ca}_{4} \mathrm{GdO}\left(\mathrm{BO}_{3}\right)_{3}$ | soliton-SESAM | $1.045 \mu \mathrm{~m}$ | 90 fs | 40 mW | 100 MHz |  | [00Dru, 02Dru2] |
| Yb:BOYS |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{Sr}_{3} \mathrm{Y}\left(\mathrm{BO}_{3}\right)_{3}$ | soliton-SESAM | $1.062 \mu \mathrm{~m}$ | 69 fs | 80 mW | 113 MHz |  | [02Dru1] |
| Yb:SIS |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{SrY}_{4}\left(\mathrm{SiO}_{4}\right)_{3} \mathrm{O}$ | soliton-SESAM | $\begin{aligned} & 1.068 \mu \mathrm{~m} \\ & 1.066 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 94 \mathrm{fs} \\ & 70 \mathrm{fs} \end{aligned}$ | $\begin{aligned} & 110 \mathrm{~mW} \\ & 156 \mathrm{~mW} \end{aligned}$ | $\begin{aligned} & 108 \mathrm{MHz} \\ & 98 \mathrm{MHz} \end{aligned}$ |  | [02Dru1] <br> [04Dru] |
| $\mathrm{Yb}: \mathrm{CaF}_{2}$ |  |  |  |  |  |  |  |
|  | soliton-SESAM | $1.049 \mu \mathrm{~m}$ | $\begin{aligned} & \mathbf{1 5 0 ~ f s} \\ & 230 \mathrm{fs} \end{aligned}$ | $\begin{aligned} & 880 \mathrm{~mW} \\ & 1.74 \mathrm{~W} \end{aligned}$ |  |  | [04Luc] |
| Yb:LSB |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{LnM}_{3}\left(\mathrm{BO}_{3}\right)_{4}$ | soliton-SESAM | $1.053 \mu \mathrm{~m}$ | 72 fs | 79 mW | 90 MHz | Ti:sapphire laser pumped | [07Riv] |
|  |  |  | 58 fs | 73 mW | 90 MHz | plus external cavity SF10 prism compressor | [07Riv] |
| $\mathrm{Yb}: \mathrm{Lu}_{2} \mathrm{O}_{3}$ | soliton-SESAM | $1.034 \mu \mathrm{~m}$ | 220 fs | 266 mW | 97 MHz | Ti:sapphire laser pumped | [04Gri] |

(continued)
1:sapphire laser pumped
266 mW
220 fs

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90 MHz
90 MHz
97 MHz
79 mW
73 mW
$1.053 \mu \mathrm{~m} \quad 72 \mathrm{fs}$
Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Yb:YSO |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{Y}_{2} \mathrm{SiO}_{5}$ | soliton-SESAM | $1.041 \mu \mathrm{~m}$ | 122 fs | 410 mW | 75 MHz |  | [06Thi] |
| Yb:LSO |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{Lu}_{2} \mathrm{SiO}_{5}$ | soliton-SESAM | $\begin{aligned} & 1.044 \mu \mathrm{~m} \\ & 1.059 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 198 \mathrm{fs} \\ & 260 \mathrm{fs} \end{aligned}$ | $\begin{aligned} & 2.61 \mathrm{~W} \\ & 2.6 \mathrm{~W} \end{aligned}$ | $\begin{aligned} & 75 \mathrm{MHz} \\ & 75 \mathrm{MHz} \end{aligned}$ |  | [06Thi] |
| Yb:GSO |  |  |  |  |  |  |  |
| $\mathrm{Yb}^{3+}: \mathrm{Gd}_{2} \mathrm{SiO}_{5}$ | soliton-SESAM | $\begin{aligned} & 1.031 \mu \mathrm{~m} \\ & 1.030 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 1.3 \mathrm{ps} \\ & 343 \mathrm{fs} \end{aligned}$ | $\begin{aligned} & 586 \mathrm{~mW} \\ & 396 \mathrm{~mW} \end{aligned}$ | 101 MHz |  | [07Li] |
| Yb:glass |  |  |  |  |  |  |  |
| Yb :phosphate glass | soliton-SESAM | 1.025-1.065 $\mu \mathrm{m}$ | 58 fs | 65 mW | 112 MHz |  | [98Hoe] |
| Yb :silicate glass |  | 1.03-1.082 $\mu \mathrm{m}$ | 61 fs | 53 mW | 112 MHz |  | [98Hoe] |
|  | SESAM and cavity-dumped | $1.04 \mu \mathrm{~m}$ | $\begin{aligned} & 250 \mathrm{fs} \\ & 470 \mathrm{fs} \end{aligned}$ | $\begin{aligned} & 0.33 \mathrm{~W} \\ & 0.375 \mathrm{~W} \end{aligned}$ | $\begin{aligned} & 1.1 \mathrm{MHz} \\ & 0.5 \mathrm{MHz} \end{aligned}$ | $0.3 \mu \mathrm{~J}$ pulse energy $0.75 \mu \mathrm{~J}$ pulse energy | [05Kil2] |
| Er:Yb:glass |  |  |  |  |  |  |  |
|  | active AOM | $\approx 1.53 \mu \mathrm{~m}$ | 90 ps | 7 mW | 100 MHz |  | [94Cer] |
|  |  | $1.53 \mu \mathrm{~m}$ | 9.6 ps | 3 mW | 2.5 GHz | $3^{\text {rd }}$-order harmonic modelocking | [94Lon] |
|  |  | $\approx 1.5 \mu \mathrm{~m}$ | $9.6-30 \mathrm{ps}$ | 3 mW | 2.5 and 5 GHz | $3^{\text {rd }}$-order harmonic modelocking | [95Lap] |
|  |  | $1.533 \mu \mathrm{~m}$ | 48 ps | 1 mW | 5 GHz | dual wavelength with 165 GHz separation | [98Lon] |

Table 2.1.2 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SESAM | $1.534 \mu \mathrm{~m}$ | 2.5 ps | 68 mW | 114 MHz |  | [99Spu2] |
|  |  | $1.534 \mu \mathrm{~m}$ | 3.8 ps | 12 mW | 10 GHz | nearly quantum-noise-limited timing jitter [05Sch2] | [02Kra1] |
|  |  | $1.535 \mu \mathrm{~m}$ | 2.5 ps | 50 mW | 10 GHz |  | [02Spu] |
|  |  |  | 2.5 ps | $>5 \mathrm{dBm}$ | 40 GHz MUX | 40 GHz multiplexed (MUX) | [02Spu] |
|  |  | 1.528-1.561 $\mu \mathrm{m}$ | 1.9 ps | 25 mW | 25 GHz | gain equalized frequency comb with 36 discrete channels, tunable over C-band | [03Spu] |
|  |  | $1.534 \mu \mathrm{~m}$ | 4.3 ps | 18 mW | 40 GHz |  | [03Zel] |
|  |  | $1.534 \mu \mathrm{~m}$ | $1.7-1.9 \mathrm{ps}$ | $>20 \mathrm{~mW}$ | $8.8-13.3 \mathrm{GHz}$ | pulse repetition rate is continuously tunable | [04Ern] |
|  |  | $1.533 \mu \mathrm{~m}$ | 2 ps | 7.5 mW | 50 GHz | 10 discrete channels locked to 50 GHz ITU grid | [04Zel] |
|  |  | $1.536 \mu \mathrm{~m}$ | 3 ps | 10.7 mW | 77 GHz | optical frequency comb with $>56 \mathrm{~dB}$ OSNR (Optical Signal-to-Noise Ratio) | [07Zel] |
|  |  | $1.535 \mu \mathrm{~m}$ | 20 ps | 80 mW | 61 MHz | first AlGaAsSb-SESAM | [04Gra] |
|  |  | $1.534 \mu \mathrm{~m}$ | 5 ps | 70 mW | 61 MHz | first GaInNAs-SESAM at $1.5 \mu \mathrm{~m}$ | [05Rut] |
|  |  | $1.535 \mu \mathrm{~m}$ | 4.7 ps | 9 mW | 10 GHz | AlGaAsSb-SESAM | [06Gra] |
|  | soliton-SESAM | $1.535 \mu \mathrm{~m}$ | 380 fs | 4 mW | 100 MHz |  | [01Was] |
|  |  | $1536 \mu \mathrm{~m}$ | 255 fs | 58 mW | 50 MHz |  | [05Spu1] |
|  |  | $1.54 \mu \mathrm{~m}$ |  |  | 169 MHz | 220 fs with external pulse compression, first $\mathrm{Si} / \mathrm{Ge}-$ SESAM | [05Gra1] |

Table 2.1.2 continued.

Table 2.1.3. $Q$-switched microchip lasers using different techniques. First microchip laser introduced by Zayhowski and Mooradian [89Zay]. "Best" means in terms of pulse duration, highest average output power, highest pulse repetition rate etc. - the result for which "best" applies is in bold letters. The lasers are assumed to be diode-pumped, if not stated otherwise. SESAM: passive $Q$-switching using SEmiconductor Saturable Absorber Mirrors (SESAMs). EOM: Electro-Optic phase Modulator. $\lambda_{0}$ : center lasing wavelength. $\tau_{\mathrm{p}}$ : measured pulse duration. $E_{\mathrm{p}}$ : pulse energy. $f_{\text {rep }}$ : pulse repetition rate.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $E_{\text {p }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nd:YAG |  |  |  |  |  |  |  |
|  | active-EOM | $1.064 \mu \mathrm{~m}$ | 760 ps |  | 4 kHz | pumped by $Q$-switched intracavity SHG Nd:YAG laser | [89Zay] |
|  |  |  | 270 ps | $6.8 \mu \mathrm{~J}$ | 5 kHz | pulse width increases with increased $f_{\text {rep }}$ for $5-500 \mathrm{kHz}: 13.3 \mathrm{~ns}$ at 500 kHz | [92Zay] |
|  | $\mathrm{Cr}^{4+}$ :YAG |  | 337 ps | $11 \mu \mathrm{~J}$ | 6 kHz |  | [94Zay] |
|  |  |  | 148 ps |  | 4 kHz | optimization for max. energy [04Bur] | [03Zay] |


| active-EOM | $1.064 \mu \mathrm{~m}$ | 115 ps | $12 \mu \mathrm{~J}$ | 1 kHz |  | [95Zay] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SESAM | $1.064 \mu \mathrm{~m}$ | 56 ps | 62 nJ | 85 kHz | 1.1 kW peak, 5.3 mW average | [97Bra] |
|  |  | 68 ps | 0.37 JJ | 160 kHz | 5.4 kW peak, 58 mW average | [97Bra] |
|  |  | 143 ps | 48 nJ |  | Output Coupling (OC) SESAM | [01Spu1] |
|  |  | 37 ps | 53 nJ | 160 kHz | 1.4 kW peak, 8.5 mW average | $\begin{aligned} & \text { [99Spu1, } \\ & \text { 01Spu3] } \end{aligned}$ |
|  |  | 117 ps | $0.16 \mu \mathrm{~J}$ | 510 kHz | 1.4 kW peak, 82 mW average | $\begin{aligned} & \text { [99Spu1, } \\ & \text { 01Spu3] } \end{aligned}$ |
|  |  | 181 ps | $0.28 \mu \mathrm{~J}$ | 440 kHz | 1.6 kW peak, 120 mW average | $\begin{aligned} & \text { [99Spu1, } \\ & \text { 01Spu3] } \end{aligned}$ |
|  |  | 2.64 ns | 45 nJ | 7.8 MHz | 17 W peak, 350 mW average | $\begin{aligned} & \text { [99Spu1, } \\ & \text { 01Spu3] } \end{aligned}$ |
|  | $1.34 \mu \mathrm{~m}$ | 230 ps |  | 53 kHz | 450 kW peak | [97Flu] |

Table 2.1.3 continued.

| Laser material | ML technique | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $E_{\text {p }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nd:LSB |  |  |  |  |  |  |  |
|  | $\begin{aligned} & \text { SESAM } \\ & \mathrm{Cr}^{4+}: \mathrm{YAG} \end{aligned}$ | $\begin{aligned} & 1.062 \mu \mathrm{~m} \\ & 1.063 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 180 \mathrm{ps} \\ & 650 \mathrm{ps} \end{aligned}$ | $\begin{aligned} & 0.1 \mu \mathrm{~J} \\ & 3-4 \mu \mathrm{~J} \end{aligned}$ | 110 kHz |  | [96Bra1] [05Voi] |
| Yb:YAG |  |  |  |  |  |  |  |
|  | SESAM | $1.03 \mu \mathrm{~m}$ | 530 ps | $1.1 \mu \mathrm{~J}$ | 12 kHz | 1.9 kW peak | [01Spu2] |
| Er:Yb:glass |  |  |  |  |  |  |  |
|  | SESAM | $1.535 \mu \mathrm{~m}$ | $1.2 \mathrm{~ns}$ | $45 \mathrm{~nJ}$ | $47 \mathrm{kHz}$ | 2.1 mW average | [98Flu] |
|  | p-i-n modulator | $\begin{aligned} & \approx 1.5 \mu \mathrm{~m} \\ & 1.553 \mu \mathrm{~m} \end{aligned}$ | $\begin{aligned} & 840 \mathrm{ps} \\ & 56 \mathrm{~ns} \end{aligned}$ | $\begin{aligned} & \mathbf{1 1 . 2} \boldsymbol{\mu \mathrm { J }} \\ & 470 \mathrm{~nJ} \end{aligned}$ | $\begin{aligned} & 1.4 \mathrm{kHz} \\ & 10 \mathrm{kHz} \end{aligned}$ | 16 mW average, 10.6 kW peak previously p-i-n modulator for ML [95Bro3] | [01Hae1] [01Han] |
| Cr:YAG |  |  |  |  |  |  |  |
|  |  | $\approx 1.5 \mu \mathrm{~m}$ | 42 ns |  | 1 MHz | diode-pumped $\mathrm{Nd}: \mathrm{YVO}_{4}$ pumped, $Q$-switched ML | [01Sch] |

### 2.1.3.1.2 Mode-locked rare-earth-doped solid-state lasers

The rare-earth-doped (e.g. $\mathrm{Nd}^{3+}, \mathrm{Tm}^{3+}, \mathrm{Ho}^{3+}, \mathrm{Er}^{3+}, \mathrm{Yb}^{3+}$ ) solid-state lasers have favorable properties for diode-pumped high-power operation, but cannot be used in the high-power regime for femtosecond pulse generation because of their relatively small amplification bandwidth. These lasers have 4 f -electrons responsible for the laser transition, which are shielded from the crystal host. Thus the gain bandwidth is normally not very large and pulse durations are limited to a few 100 fs (Table 2.1.1 and Table 2.1.2). Shorter pulses can only be obtained in inhomogeneously broadened rare-earth-doped lasers in glass hosts for example but at the expense of lower power due to the limited thermal conductivity of glasses (Table 2.1.1 and Table 2.1.2).

Typical examples are $\mathrm{Nd}^{3+}: \mathrm{YAG}$ and $\mathrm{Nd}^{3+}: \mathrm{YVO}_{4}$. With high-power laser diodes, one or several conventional end-pumped or side-pumped laser rods and a SESAM for mode-locking, up to 27 W of average power in 19-ps pulses has been achieved with $\mathrm{Nd}^{3+}: \mathrm{YAG}$ [ 00 Spu ], or 23.5 W in $22-\mathrm{ps}$ pulses with $\mathrm{Nd}^{3+}: \mathrm{YVO}_{4}$ [01Che1]. Significantly shorter pulse durations have been achieved with Nd :YAG at lower output powers, down to 1.7 ps with 25 mW [90Goo] using the technique of Additive Pulse Mode-locking (APM). For all these $\mathrm{Nd}^{3+}$-doped crystals, the relatively large laser cross sections usually make it relatively easy to achieve stable mode-locked operation without $Q$-switching instabilities, if the laser mode area in the gain medium is not made too large.

Phosphate or silicate glasses doped with rare-earth ions such as $\mathrm{Nd}^{3+}$ or $\mathrm{Yb}^{3+}$ have been used for pulse durations down to $\approx 60 \mathrm{fs}$ [97Aus, 98 Hoe$]$ and output powers of a few hundred milliwatts. The relatively poor thermal properties make high-power operation challenging. Up to 1.4 W of average power in 275 -fs pulses [00Pas1], or 1 W in 175 -fs pulses [97Aus], have been obtained from $\mathrm{Nd}^{3+}$ :glass by using a specially adapted elliptical mode pumping geometry [00Pas2] initially developed for diode-pumped Cr:LiSAF lasers [97Kop1, 95Kop3]. Here, a strongly elliptical pump beam and laser mode allow the use of a fairly thin gain medium which can be efficiently cooled from both flat sides. The resulting nearly one-dimensional heat flow reduces the thermal lensing compared to cylindrical rod geometries, if the aspect ratio is large enough. A totally different route toward high peak powers is to use a cavity-dumped laser; with such a device, based on $\mathrm{Yb}^{3+}$ :glass, 400-nJ pulses with more than 1 MW peak power have been generated [04Kil].
$\mathrm{Yb}^{3+}$ :YAG has similar thermal properties as $\mathrm{Nd}^{3+}: \mathrm{YAG}$ and at the same time a much larger amplification bandwidth. Another favorable property is the small quantum defect. However, challenges arise from the quasi-three-level nature of this medium and from the small laser cross sections, which favor $Q$-switching instabilities. High pump intensities help in both respects. An end-pumped laser based on a $\mathrm{Yb}^{3+}: \mathrm{YAG}$ rod has generated $340-\mathrm{fs}$ pulses with 170 mW [95Hoe]. As much as 8.1 W in 2.2-ps pulses was obtained from an elliptical-mode $\mathrm{Yb}^{3+}: \mathrm{YAG}$ laser. In 2000, the first $\mathrm{Yb}^{3+}$ :YAG thin-disk laser has been passively mode-locked, generating 700 -fs pulses with 16.2 W average power [99Aus]. The concept of the passively mode-locked thin-disk laser has been demonstrated to be power scalable, which so far lead up to 80 W in 0.7 -ps pulses [06Inn].

In recent years, a few $\mathrm{Yb}^{3+}$-doped crystalline gain materials have been developed which combine a relatively broad amplification bandwidth (sufficient for pulse durations of a few hundred femtoseconds) with thermal properties which are better than those of other broad-band materials, although not as good as e.g. those of YAG or sapphire. Examples are shown in Table 2.1.1 and Table 2.1.2. With an end-pumped $\mathrm{Yb}^{3+}: \mathrm{KGW}$ rod, 1.1 W of average power have been achieved in 176 -fs pulses [00Bru]. A Kerr-lens mode-locked $\mathrm{Yb}^{3+}: \mathrm{KYW}$ laser produced pulses as short as 71 fs [01Liu], while a SESAM mode-locked $\mathrm{Yb}^{3+}: \mathrm{KYW}$ produced pulses as short as 107 fs [04Pau]. Around 70 -fs pulses have been obtain with SESAM mode-locked $\mathrm{Yb}^{3+}$ :NGW laser with 23 mW average power [06Riv], $\mathrm{Yb}^{3+}:$ BOYS laser with 80 mW [02Dru1], $\mathrm{Yb}^{3+}$ :SYS laser with 156 mW [04Dru]. However, so far the shortest pulses are still obtained with Yb:glass lasers [98Hoe]. Note that some of these media exhibit rather low emission cross sections and therefore make stable passive mode-locking difficult, while they might be very useful e.g. in regenerative amplifiers. Tungstate crystals $\left(\mathrm{Yb}^{3+}: \mathrm{KGW}, \mathrm{Yb}^{3+}: \mathrm{KYW}\right)$ have been rather useful for passive mode-locking since they have relatively high cross sections. $\mathrm{Yb}^{3+}$ :KYW has been applied in a thin-disk laser, generating

22 W in $240-\mathrm{fs}$ pulses [02Bru]. With improved crystal quality, significant performance enhancements appear to be feasible. Another new class of materials with particular importance are the $\mathrm{Yb}^{3+}$-doped sesquioxides such as $\mathrm{Y}_{2} \mathrm{O}_{3}, \mathrm{Sc}_{2} \mathrm{O}_{3}$ and $\mathrm{Lu}_{2} \mathrm{O}_{3}$, which appear to be very suitable for high-power operation with short pulses.

Up to a few years ago, the repetition rate of passively mode-locked solid-state lasers was limited to a few gigahertz. $Q$-switching instabilities have limited the highest pulse repetition rates (Sect. 2.1.6.8). In recent years, the consequent exploitation of the flexibility of SESAMs supported passively mode-locked lasers with multi-GHz pulse repetition rates, very good pulse quality, comparatively high output powers, and wavelength tunability in the areas of interest (for example the ITU-specified C-band from approximately 1525 nm to 1565 nm , ITU stands for International Telecommunication Union). Passive mode-locking means that the pulses are achieved without using any expensive multi-gigahertz electronics. In addition, the pulses originate from fundamental mode-locking. Thus, every output pulse is a copy of the same single pulse, which travels back and forth in the cavity. Therefore, pulse-to-pulse variations are minimized and the phase of the pulses is constant. For the first time, pulse repetition rates above 10 GHz from passively mode-locked iondoped solid-state lasers have been generated with $\mathrm{Nd}: \mathrm{YVO}_{4}$ lasers at a center wavelength around $1 \mu \mathrm{~m}$ [99Kra1]. This laser has a large gain cross section and therefore $Q$-switching instabilities are more strongly suppressed. Shortly afterwards the frontier was pushed up to $77 \mathrm{GHz}[00 \mathrm{Kra} 2]$ and 160 GHz [02Kra2]. The average power has been optimized at a 10 GHz pulse repetition rate to as high as 2.1 W [04Lec]. The peak power was sufficient for efficient nonlinear frequency conversion. For example, a synchronously pumped Optical Parametric Oscillator (OPO) was demonstrated producing picosecond pulses broadly tunable around $1.55 \mu \mathrm{~m}$ with up to 350 mW average output power [04Lec, 02Lec]. Such all-solid-state synch-pumped OPOs can reach the S-, C- and L-band in telecommunication. With an additional Yb-doped fiber amplifier the repetition rate was pushed up to 80 GHz [ 05 Lec 2$]$. Particularly in the telecom wavelength ranges (around $1.3 \mu \mathrm{~m}$ and $1.55 \mu \mathrm{~m}$ ), where only few solid-state gain media are available, multi- GHz pulse repetition rates initially were not directly possible [97Col, 95Lap]. However, with improved SESAM designs [05Spu3] and an improved understanding of the $Q$-switching instabilities [04Sch1, 05Gra2] full C-band tuning [03Spu] and up to 77 GHz pulse repetition rate $[07 \mathrm{Zel}]$ has been demonstrated with a diode-pumped Er:Yb:glass laser. At $1.3 \mu \mathrm{~m}$ both Nd:YLF [06Zel] and Nd: $\mathrm{YVO}_{4}$ [05Spu2] have been passively mode-locked at GHz repetition rates. In addition, the timing jitter of diode-pumped solid-state lasers is very close to the quantum noise limit [05Sch2].

### 2.1.3.1.3 Mode-locked transition-metal-doped solid-state laser

Transition-metal-doped (e.g. $\mathrm{Cr}^{2+}, \mathrm{Cr}^{3+}, \mathrm{Cr}^{4+}, \mathrm{Ti}^{3+}, \mathrm{Ni}^{2+}, \mathrm{Co}^{2+}$ ) solid-state lasers are characterized by a much broader amplification bandwidth, typically allowing for pulse durations well below 0.5 ps , but also usually by significantly poorer thermal properties and lower laser cross sections. $\mathrm{Ti}^{3+}$ :sapphire is a notable exception, combining nearly all desired properties for powerful ultrafast lasers, except that the short pump wavelength excludes the use of high-power diode pump lasers, and that the quantum defect is large. These lasers have 3d-electrons responsible for the laser transition, which are not very well shielded from the host material. Thus these lasers are strongly phonon-broadened and can support much shorter pulses than the rare-earth-doped crystal. Presently, the shortest pulses generated from a laser are based on Ti:sapphire using KLM (Table 2.1.1).

Using a frequency-doubled solid-state laser as a pump source, $\mathrm{Ti}^{3+}$ :sapphire lasers have been demonstrated to generate pulses with durations below 6 fs and a few hundred milliwatts of average power [99Sut, 01Ell]. For these pulse durations, KLM is required, and self-starting may be achieved with a SESAM in addition [99Sut, 00Sut]. With a SESAM alone, 13 -fs pulses with 80 mW have been demonstrated [96Kae]. If significantly longer pulse durations are acceptable, several watts of average power can be generated with a commercially available $\mathrm{Ti}^{3+}$ :sapphire laser, usually pumped
with a frequency-doubled diode-pumped solid-state laser at $\approx 1 \mu \mathrm{~m}$. Another option is to achieve rather high pulse energies and peak powers by using a very long laser cavity and limiting the peak intensities by the use of longer and chirped pulses in the cavity, which may be compressed externally. Such a laser has been demonstrated to produce 130-nJ pulses with $<30$ fs pulse duration and $>5$ MW peak power [04Fer]. And more recently with a $2-\mathrm{MHz}$ cavity pulse energies as high as $0.5 \mu \mathrm{~J}$ have been demonstrated still maintaining $<40$-fs pulses [05Nau].

Diode-pumped femtosecond lasers can be build with crystals like $\mathrm{Cr}^{3+}: \mathrm{LiSAF}, \mathrm{Cr}^{3+}: \mathrm{LiSGaF}$, $\mathrm{Cr}^{3+}$ :LiSCAF etc. (see Table 2.1.2) which can be pumped at longer wavelengths than $\mathrm{Ti}^{3+}$ :sapphire. However, these media have much poorer thermal properties and thus can not compete with $\mathrm{Ti}^{3+}$ :sapphire in terms of output power; the achievable optical bandwidth is also lower. $\mathrm{Cr}^{3+}$ :LiSAF lasers have generated pulses as short as 12 fs [99Uem], but only with 23 mW of output power, using KLM without self-starting ability. This has been more recently further reduced to 9.9 fs [03Uem]. The highest achieved mode-locked power was 0.5 W in 110 -fs pulses [97Kop3] using SESAM modelocking. More recently, compact $\mathrm{Cr}^{3+}:$ LiSAF lasers with very low pump threshold have been developed, delivering e.g. 136 -fs pulses with 20 mW average power for $<100 \mathrm{~mW}$ optical pump power using again SESAM mode-locking in order to optimize the laser cavity design independently of the saturable absorber [02Aga].
$\mathrm{Cr}^{4+}$ :forsterite emits around $1.3 \mu \mathrm{~m}$ and is suitable for pulse durations down to 14 fs with 80 mW using KLM [01Chu], or for 800 mW in 78 -fs pulses using SESAM [98Pet]. Normally, a $\mathrm{Nd}^{3+}$-doped laser (which may be diode-pumped) is used for pumping of $\mathrm{Cr}^{4+}$ :forsterite. The same holds for $\mathrm{Cr}^{4+}: \mathrm{YAG}$, which emits around 1.4-1.5 $\mu \mathrm{m}$ and has allowed to generate pulses with 20 fs , 400 mW [02Rip1].
$\mathrm{Cr}^{2+}$-doped II-VI materials have become interesting for ultrafast solid-state lasers in the midinfrared regime [04Sor, 05Sor]. In recent years, $\mathrm{Cr}^{2+}: \mathrm{ZnSe}$ has been identified as another very interesting gain material which is in various ways similar to $\mathrm{Ti}^{3+}$ :sapphire, but emits at mid-infrared wavelengths around $2.2-2.8 \mu \mathrm{~m}$. This very broad bandwidth should allow for pulse durations below 20 fs , although until recently the shortest achieved pulse duration is much longer, $\approx 4 \mathrm{ps}$ [00Car]. The large Kerr nonlinearity of this medium is causing significant problems for shortpulse generation. However, the main obstruction for femtosecond pulses turned out to be the water absorption lines in the resonator around $2.5 \mu \mathrm{~m}$ [07Sor]. Water absorption lines have been identified as a problem for SESAM mode-locking before [96Flu2]. Removing the water absorption in the $\mathrm{Cr}: \mathrm{ZnSe}$ laser resulted in 80 fs pulses at a center wavelength of $2.5 \mu \mathrm{~m}$. These are only about 10 optical cycles [07Sor].

### 2.1.3.1.4 $Q$-switched ion-doped solid-state microchip lasers

$Q$-switching results are restricted to microchip lasers because the pulse duration scales with the photon cavity lifetime. Thus, the shorter the laser cavity, the shorter the pulses that can be generated. Microchip lasers [89Zay] are single axial frequency lasers using a miniature, monolithic, flat-flat, solid-state cavity whose mode spacing is greater than the medium-gain bandwidth. They rely on gain guiding, temperature effects and/or other nonlinear optical effects to define the transverse dimension of the lasing mode. The microchip lasers are longitudinal-pumped with a diode laser. Table 2.1.3 summarizes the results obtained with actively and passively $Q$-switched microchip lasers. The shortest pulses of only 37 ps were obtained with $\mathrm{Nd}: \mathrm{YVO}_{4}$ passively $Q$-switched with a SESAM attached to the microchip laser (Fig. 2.1.6) [99Spu1, 01Spu3]. Using different laser crystal thicknesses ranging from $185 \mu \mathrm{~m}$ to $440 \mu \mathrm{~m}$ the pulse duration could be changed from 37 ps to 2.6 ns and the pulse repetition rate from 160 kHz to 7.8 MHz . Such a laser therefore can be easily adapted to different application requirements. Active $Q$-switched microchip lasers generated pulses as short as 115 ps [95Zay]. These results also demonstrate that passively $Q$-switched microchip lasers can bridge the gap in terms of pulse durations between mode-locking and $Q$-switching. Generally the pulse energies in actively $Q$-switched microchip lasers tend to be higher (e.g. $12 \mu \mathrm{~J}$ in [95Zay]),


Fig. 2.1.6. Passively $Q$-switched $\mathrm{Nd}: \mathrm{YVO}_{4}$ microchip laser producing pulses as short as 37 ps with 53 nJ pulse energy, 160 kHz pulse repetition rate, and an average power of 8.5 mW . The SESAM design is based on an A-FPSA with 35 InGaAs/GaAs multiple-quantum-well saturable absorbers and a $50 \%$ top reflector resulting in a modulation depth of $13 \%$.
however a passively $Q$-switched Yb:YAG microchip laser using a SESAM resulted in $1.1 \mu \mathrm{~J}$ pulse energy [01Spu2]. More results are summarized in Table 2.1.3.

### 2.1.3.1.5 Ultrafast semiconductor lasers

Diode-pumped Vertical-External-Cavity Surface-Emitting Lasers (VECSELs) [99Kuz] combine the world of diode-pumped solid-state lasers and semiconductor lasers: The semiconductor gain medium allows for flexible choice of emission wavelength via bandgap engineering. The combination of the mature optical pumping technology extensively used for diode-pumped solid-state lasers with efficient heat removal of solid-state thin-disk lasers resulted in performance of VECSELs that surpasses anything possible to date with conventional semiconductor lasers. Continuous-wave output powers of up to 30 W with an $M^{2}$ of 3 have been reported from such optically pumped VECSELs [04Chi], and electrically pumped devices have reached 0.5 W single-mode output power [03McI]. A more detailed review of passively mode-locked VECSELs has been given recently [06Kel].

Concerning high-performance passive mode-locking, a domain where diode-pumped solid-state lasers have been dominant for years using SEmiconductor Saturable Absorber Mirrors (SESAMs) (Table 2.1.2), the VECSEL possesses the advantage of a large gain cross-section which suppresses $Q$-switching instabilities. Thus, VECSELs are ideally suited for high-repetition-rate mode-locking in combination with high average output powers. After the first demonstration of a passively modelocked VECSEL in 2000 [00Hoo], pulse width and output power have improved continuously to 486 -fs pulses at 10 GHz with 30 mW [ 05 Hoo ] and 4.7 -ps pulses at 4 GHz with 2.1 W average output power [05Asc1]. More results are summarized in Table 2.1.4.

Novel SESAMs based on Quantum-Dot SEmiconductor Saturable Absorber Mirrors (QDSESAMs) were developed to move towards an even more ambitious goal: the integration of the absorber into the VECSEL gain structure [04Lor]. In a first step passive mode-locking with the same mode area in the gain and the absorber had to be demonstrated for the full wafer-scale integration. We refer to this as "1:1 mode-locking" which was successfully demonstrated using these new QD-SESAMs and therefore the viability of the integrated-absorber VECSEL concept
Table 2.1.4. Passively mode-locked Vertical External Cavity Surface Emitting semiconductor Lasers (VECSELs) using different mode-locking techniques. letters. The VECSELs are either electrically pumped (EP-VECSELs) or optically pumped using diode lasers (OP-VECSELs). ML: Mode-Locking. QW Quantum Well. $\lambda_{0}$ : center lasing wavelength. $\tau_{\mathrm{p}}$ : measured pulse duration. $P_{\mathrm{av}, \text { out }}$ : average output power. $f_{\mathrm{rep}}$ : pulse repetition rate.

| Laser material | ML | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ML OP-VECSEL |  |  |  |  |  |  |  |
| GaAs-based |  |  |  |  |  |  |  |
| GaAs/AlGaAs QWs | active | 850 nm | 100 ps |  |  | acousto-optic modulator | [99Hol] |
| InGaAs-based |  |  |  |  |  |  |  |
| 12 InGaAs/GaAs QWs | SESAM | 1030 nm | 22 ps | 20 mW | 4.4 GHz | first passively ML VECSEL | [00Hoo] |
| 9 InGaAs/GaAs QWs |  | 950 nm | 3.2 ps | 213 mW | 2 GHz |  | [01Hae2] |
| $7 \mathrm{InGaAs} / \mathrm{GaAs}$ QWs |  | 1040 nm | 15 ps | $<100 \mathrm{~mW}$ | 2.1 GHz | harmonic mode-locking | [07Saa] |
| 6 InGaAs/GaAsP QWs |  | 1030 nm | 13.2 ps | 16 mW | 328 MHz |  | [01Gar] |
|  |  | 1040 nm | 477 fs | 100 mW | 1.21 GHz | strain-balanced InGaAs QW | [02Gar] |
| 6 InGaAs/GaAs QWs |  | 1034 nm | 486 fs | 30 mW | 10 GHz |  | [05Hoo] |
| 5 InGaAs/GaAs QWs |  | 950 nm | $\begin{aligned} & 15 \mathrm{ps} \\ & 3.9 \mathrm{ps} \end{aligned}$ | $\begin{aligned} & 950 \mathrm{~mW} \\ & 530 \mathrm{~mW} \end{aligned}$ | 6 GHz | soliton-like pulse shaping in the positive GVD regime [02Pas] | [02Hae] |
| 7 InGaAs/GaAsP QWs |  | 980 nm | 9.7 ps | 55 mW | 21 GHz | low saturation QD-SESAM | [04Lor] |
|  |  | 960 nm | 4.7 ps | 25 mW | 30 GHz | 1:1 ML for the first time towards wafer scale integration |  |
|  |  | 957 nm | 4.7 ps | 2.1 W | 4 GHz |  | [05Asc1] |
|  |  | 960 nm | 6.1 ps | 1.4 W | 10 GHz |  | [05Asc2] |
|  |  | 960 nm | 3 ps | 100 mW | 50 GHz |  | [06Lor] |
| 13 InGaAs/AlGaAsP |  | 975 nm | 3.8 ps | 83 mW | 1.88 GHz |  | [05Cas] |
| + intracavity LBO |  | 489 nm | 3.9 ps | 6 mW | 1.88 GHz |  |  |

Table 2.1.4 continued.

| Laser material | ML | $\lambda_{0}$ | $\tau_{\mathrm{p}}$ | $P_{\text {av,out }}$ | $f_{\text {rep }}$ | Remarks | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| InGaAsP-based |  |  |  |  |  |  |  |
| 7 InGaAsP QWs |  | $1.5 \mu \mathrm{~m}$ | 6.5 ps | 13.5 mW | 1.34 GHz |  | [03Hoo] |
| $20 \mathrm{InGaAsP} / \mathrm{InGaAsP}$ QWs |  | $1.554 \mu \mathrm{~m}$ | 3.2 ps | 120 mW | 2.97 GHz |  | [05Lin2] |
| ML EP-VECSEL |  |  |  |  |  |  |  |
| InGaAs-based |  |  |  |  |  |  |  |
| GaAs/AlGaAs QWs | active | 830 nm | 81 ps | 4 mW | 960 MHz | quasi-cw, liquid $\mathrm{N}_{2}$ cryostat cooling | [93Jia] |
| 7 InGaAs/GaAs QWs | SESAM | 980 nm | 57 ps | 40 mW | 1.1 GHz | first electrically pumped passively ML VECSEL | [03Jas] |
|  |  |  | 14.8 ps | $\approx 10 \mathrm{~mW}$ | 15 GHz | novel compact linear cavity | [04Jas] |
|  |  |  | 50 ps | 30 mW | 6 GHz | SA dynamics [05Zha2] | [04Zha2] |

has been demonstrated [04Lor]. With the QD-SESAM we can resolve the saturation issue for higher pulse repetition rates (i.e. shorter cavities) with nearly equal laser beam sizes in the gain and the absorber to obtain a stable cavity design. This requires a lower saturation fluence. With QD-SESAMs we can obtain both a low saturation fluence and a sufficiently low modulation depth with the optimization of the dot density and the design of the structure (i.e. moving from a antiresonant to a resonant design) [07Maa]. This is not possible with quantum-well absorbers. With an optimized QD-SESAM consisting of only one single self-assembled InAs quantum-dot layer at low growth temperatures we succeeded to push the repetition rate of passively modelocked VECSELs up to 50 GHz [06Lor]. In addition, these QD-SESAMs allowed for the first demonstration of passively modelocked VECSEL with an integrated saturable absorber layer in the gain structure [07Bel, 07 Maa ]. This will ultimately offer the potential for wafer-scale fabrication and operation at even higher repetition rates. We refer to this device as the Modelocked Integrated eXternal-cavity Surface Emitting Laser (MIXSEL). Such lasers could become an enabling technology basis for ultra-compact high-repetition-rate laser devices suitable for cost-efficient high-volume fabrication.

The ultimate goal is to extend the excellent results with optically pumped VECSELs to electrical pumping. However, this is not just a simple extension even though very promising results have been achieved in the cw regime with 500 mW average output power [03McI]. Initial mode-locking results reported however only very moderate average output power well below 100 mW [04Zha2].

For comparison, it is also instructive to consider briefly the performance of pulsed edge-emitting semiconductor diode lasers, which can exhibit the highest pulse repetition rates of any optical source. The obvious advantages of compactness, efficiency of pumping, and ease of manufacture and integration make these sources primary candidates for applications such as optical time-domain multiplexing, microwave carrier generation and optical clock recovery. The efficiency of direct modulation of the diode current falls off exponentially with increasing frequency above the diode relaxation resonance, which lies typically in the range $1-10 \mathrm{GHz}$ : Thus the highest repetition frequencies are achieved using mode-locking of monolithic diode lasers, with gain, saturable absorption and/or external modulation all built into a single chip. Mode-locked edge-emitting diodes are immensely versatile in repetition frequency, from individual gain-switched pulses, through the microwave region of the spectrum and up to THz. The various schemes developed to realize lasers of this type have been reviewed by Avrutin et al. [00Avr]. Passive mode-locking, with a reverse-biased saturable absorber section included in the monolithic cavity, is particularly well-adapted to the generation of ultrashort pulses at high repetition rate because it does not require electrical modulation, which imposes a bandwidth limitation on repetition rate, and also impresses phase structure on the pulses. The first demonstration of such a monolithic device was reported by Vasil'ev et al. [89Vas], who reported a $100-\mathrm{GHz}$ train of $2.5-\mathrm{ps}$ pulses from an $\mathrm{AlGaAs} / \mathrm{GaAs}$ injection laser, corresponding to fundamental mode-locking of the $380-\mu \mathrm{m}$ long cavity. The highest output power to date is 250 mW at 4.3 GHz [06Pla]. Unfortunately, such high average power cannot be extended to pulse repetition rates well above 10 GHz because gain guiding at higher current densities gives rise to higher-order transverse modes. In addition, edge-emitting semiconductor lasers have strongly asymmetric beam profiles, which often need to be corrected with precisely mounted lenses. Typically, the same epitaxial layer forms both the gain (with a forward-biased section) and the saturable absorber (with a reverse-biased section) - and can therefore not be optimized independently. The long interaction length in the device introduces significant dispersion and nonlinearities. It is also challenging to fabricate an edge-emitting laser cavity length with a very precise pulse repetition rate and have this laser synchronized to an external reference clock. A more extensive recent review of ultrashort pulse generation with edge-emitting semiconductor lasers is given in [95Jia, 95Vai, 03Del, 00Avr].

Higher output power can be achieved from Semiconductor Optical Amplifiers (SOAs) [92Del, $95 \mathrm{Del}]$; it is outside the scope of this review. However, mode-locking of SOAs in external cavities currently attracts considerable interest. It involves extreme pulse chirping, so that the amplifier is re-pumped during the passage of the pulse. Stretching and external recompression of these pulses is accomplished using chirped fiber Bragg gratings, with dispersion $>1600 \mathrm{ps} \mathrm{nm}^{-1}$. A system of
this type has recently been reported by the Delfyett group achieving 590 -fs pulses with 1.4 kW of peak power [05Kim].

### 2.1.3.1.6 Ultrafast fiber lasers

Mode-locked and $Q$-switched ion-doped fiber lasers also showed a lot of progress during the last ten years. More recent reviews on mode-locked fiber lasers are given in book chapters and review articles by I.N. Duling et al. [95Dul], by M.E. Fermann [94Fer, 95Fer, 97Fer, 03Fer] and by H.A. Haus [95Hau1, 95Hau2]. Generally, mode-locked fiber lasers generate significantly lower pulse energies and longer pulse durations than bulk lasers. However, recent progress in mode-locked fiber lasers resulted in Er/Yb-doped fiber lasers that generate $2.7-\mathrm{nJ}$ pulses at 32 MHz with 100 fs pulse duration [96Nel]. Much shorter pulses but also at much lower pulse energies have been obtained in Nd-doped fiber lasers with pulse durations as short as 38 fs [92Hof] and in erbium fiber lasers with pulses as short as 84 fs [ 93 Fer ] and 63 fs [95Tam]. Fiber lasers require somewhat different saturable absorber parameters than bulk lasers. However, as has been demonstrated early on, the SESAM parameters can be adjusted for stable cw mode-locking of fiber lasers [91Zir, 93Obe]. Thus, the interested readers are referred to the review articles given above.

Impressive results have been obtained with fiber amplifiers and we refer interested readers to a more recent review given by A. Galvanauskas [03Gal]. A. Tünnermann's group achieved new world record results with $400-\mathrm{fs}$ pulses at 75 MHz and an average power of 76 W based on Yb -doped double-clad fiber-based Chirped Pulse Amplification (CPA) system [03Lim]. This system is based on a SESAM mode-locked Nd:glass laser, a fiber stretcher, one Yb-doped preamplifier, one Ybdoped power amplifier and a transmission grating pulse compressor. This result has been further improved using an Yb-doped photonic-crystal-fiber-based CPA system producing 220 -fs pulses at 73 MHz and an average power of 131 W [05Ros]. This corresponds to a pulse energy of $1.8 \mu \mathrm{~J}$ and a peak power as high as 8.2 MW . In this case the seed laser is a SESAM mode-locked Yb:KGW laser followed by a bulk grating stretcher.

### 2.1.3.2 Design guidelines of diode-pumped solid-state lasers

An all-solid-state ultrafast laser technology is based on diode-pumped solid-state lasers. These lasers have to be optimized to support stable pulse generation. The discussion in the following sections will show that a small saturation energy of the laser medium results in a lower tendency of self- $Q$-switching instabilities. The saturation fluence of a four-level laser system is

$$
\begin{equation*}
F_{\mathrm{sat}, \mathrm{~L}}=\frac{h \nu}{m \sigma_{\mathrm{L}}} \tag{2.1.1}
\end{equation*}
$$

and for a three-level system

$$
\begin{equation*}
F_{\mathrm{sat}, \mathrm{~L}}=\frac{h \nu}{m\left(\sigma_{\mathrm{L}}+\sigma_{\mathrm{L}}^{\mathrm{abs}}\right)}, \tag{2.1.2}
\end{equation*}
$$

where $h \nu$ is the lasing photon energy, $\sigma_{\mathrm{L}}$ is the gain cross section, $\sigma_{\mathrm{L}}^{\text {abs }}$ is the absorption cross section of the three-level gain medium and $m$ is the number of passes through the gain medium per cavity round trip. In case of a standing-wave laser cavity this factor is $m=2$, in a unidirectional ring laser cavity it is $m=1$. A small saturation energy, low pump threshold and good beam quality is obtained with a small pump and cavity mode volume while maintaining good spatial overlap of the pump laser and laser mode. This can be easily obtained when a diffraction-limited pump laser is used, as for example in a Ti:sapphire laser. The lower limit of the pump volume is then set
by diffraction, and ultimately pump-induced damage to the crystal. However, diode laser arrays or bars do not generate diffraction-limited pump beams, which makes the situation a bit more complicated and is therefore explained next.

The propagation of diffraction-limited Gaussian laser beams is extensively described in many text books, as for example in [91Sal2] and [86Sie]. A beam quality factor $M^{2}$ was introduced to describe the propagation of non-diffraction-limited beams [89Sas]. The objective was to provide propagation equations for non-diffraction-limited beams that retain the simplicity of the fundamental Gaussian mode beam equations. The $M^{2}$-factor is given by

$$
\begin{equation*}
M^{2} \equiv \frac{\theta}{\theta_{\mathrm{G}}} \quad \text { with } \quad \theta_{\mathrm{G}} \equiv \frac{\lambda}{\pi W_{0, \mathrm{G}}} \tag{2.1.3}
\end{equation*}
$$

where $\theta$ is the actual far-field divergence angle of any beam with any mixtures of modes, $\theta_{\mathrm{G}}$ the far-field Gaussian beam divergence angle, $W_{0, \mathrm{G}}$ the beam waist of a Gaussian beam which is set equal to the beam waist of the non-diffraction-limited beam. The quantity $M^{2}$ is then a numerical expression of (inverse) beam quality with 1 being a perfect Gaussian beam and higher values indicating "poorer" quality. This is entirely equivalent to the "number of times diffraction limit" quantity introduced by Siegman [86Sie]. The beam quality does not give any information about the details of higher-order mode content in the beam. The propagation of laser beams with $M^{2}$ larger than 1, can be reduced to standard Gaussian beam propagation after substituting the wavelength $\lambda_{n}$ with a new "effective wavelength" $\lambda_{\text {eff }}$ given by

$$
\begin{equation*}
\lambda_{\mathrm{eff}}=M^{2} \cdot \lambda_{n} \tag{2.1.4}
\end{equation*}
$$

where $\lambda_{n}$ is the wavelength in the dispersive medium (i.e. $\lambda_{n}=\lambda / n$ ) in which the beam is propagating. Physically, this means that non-diffraction-limited beams propagate like an ideal diffractionlimited Gaussian beam but with the new, longer "effective wavelength". Beams with larger $M^{2}$ have larger "effective wavelengths", and therefore a smaller depth of focus for a given beam waist.

The output beam of a laser diode array or broad-stripe diode suffers from poor beam quality. In the so-called "fast" axis, perpendicular to the pn-junction of the diode laser, the light diverges with a large angle ( $25^{\circ}$ to $40^{\circ}$ typically) from a narrow aperture of $\approx 1 \mu \mathrm{~m}$. However, in this direction the light is nearly diffraction-limited with $M_{\text {fast }}^{2} \approx 1$. Thus, even though the light in the fast axis is highly divergent, it can be efficiently collected with a "fast" high-numerical aperture lens and tightly focused due to its diffraction-limited nature. In the "slow" axis, parallel to the pnjunction of the diode laser, the beam typically has a divergence of $\approx 10^{\circ}$. For single-stripe diodes, the emitting aperture is $\approx 3 \mu \mathrm{~m}$, resulting in a beam close to diffraction-limited. For higher-power "arrays" of such apertures, the divergence is also $\approx 10^{\circ}$, but the total aperture has increased to typically $50 \mu \mathrm{~m}$ to more than $200 \mu \mathrm{~m}$, or in case of "arrays of arrays" (i.e. bars) to a width of approximately 1 cm . The diode laser light in the slow axis is therefore many times worse than diffraction-limited. High-brightness diode arrays with $\approx 1 \mathrm{~W}$ output power and $\approx 100 \mu \mathrm{~m}$ stripe width typically have $M_{\text {slow }}^{2} \approx 10$, whereas low brightness bars with $\approx 20 \mathrm{~W}$ and $\approx 1 \mathrm{~cm}$ stripe width have $M_{\text {slow }}^{2}>1000$. The slow axis ultimately limits the spot size of focused pump due to the requirements of mode matching to the laser mode.

With such pump lasers, the lowest pump threshold can be achieved with the following Optimized-Mode-Matching (OMM) design guidelines applied to both fast and slow axis of the diode pump laser [90Fan, 97Kop3]:

1. Determine $M^{2}$ for the pump beam (2.1.3) where $2 W_{0, \mathrm{G}}$ is set equal to the width of the pump source $D_{\mathrm{p}}$. The width of the pump source is approximately given by the stripe width of a diode array or bar or more accurately by the second-order intensity moment.
2. Determine the "effective wavelength" $\lambda_{\text {eff }}$ (2.1.4).
3. Set the depth of focus or confocal parameter $b$ of the pump beam approximately equal to the absorption length $L_{\mathrm{a}}$ of the pump beam in the laser medium, i.e. $b \approx L_{\mathrm{a}}$.
4. Determine the smallest pump beam waist $W_{0, \text { opt }}$ for which a good mode overlap over the absorption length of the pump and the cavity mode can be obtained. This is the minimum pump spot size in the gain medium that still guarantees good laser beam quality and therefore determines the lowest pump threshold: Calculate optimum beam waist radius $W_{0, \text { opt }}$ using Rayleigh range formula for an ideal Gaussian beam (i.e. $b=2 z_{0}$, where $z_{0}$ is the Rayleigh range of a Gaussian beam) with the "effective wavelength" given in (2.1.4) and a confocal parameter $b$ given in 3. of this enumeration:

$$
\begin{equation*}
W_{0, \mathrm{opt}}=\sqrt{\frac{\lambda_{\mathrm{eff}} b}{2 \pi}}=\sqrt{\frac{M^{2} \lambda_{n} L_{\mathrm{a}}}{2 \pi}} . \tag{2.1.5}
\end{equation*}
$$

From (2.1.5) it becomes clear that for a small spot size the absorption length $L_{\mathrm{a}}$ in the gain medium should be as short as possible. The absorption length, however, limits the maximum pump power at which some thermal effects will start to degrade the laser's performance. This will be more severe for "thermally challenged" lasers which exhibit a low thermal heat conductivity and/or upper-state lifetime quenching. Low thermal conductivity results in large thermal lenses and distortions, which limit the maximum pump power. Such a thermally challenged laser material is Cr:LiSAF which is interesting for an all-solid-state femtosecond laser. Upper-state lifetime quenching as observed in Cr :LiSAF results in the following: As the temperature in the laser medium increases, the upperstate lifetime of the laser drops, and the pump threshold increases. Beyond a critical temperature, the laser actually switches off. If the absorption length is too short for these materials, this critical temperature occurs at relatively low pump powers. There is an optimum doping level for best mode matching to the available pump diodes and for minimizing pump-induced upper-state lifetime quenching.

In standard diode pumping, we use high-brightness diode arrays (i.e. brightness as high as possible) and apply OMM, (2.1.1)-(2.1.5), only in the slow axis of the diodes and weaker focusing in the fast axis. This results in an approximately circular pump beam that becomes slightly elliptical when the laser crystal is pumped at a Brewster angle. The standard diode pumping is explained in more detail by the example of a diode-pumped Cr:LiSAF laser [94Kop1]. With this standard pumping approach, the average output power was limited by the mentioned thermal problems to 230 mW cw and 125 mW mode-locked with $60-\mathrm{fs}$ pulses [97Kop2]. Standard diode pumping has also been successfully used with most other solid-state lasers such as Nd:YAG. Such lasers are not "thermally challenged", and much higher average output power has been achieved with this approach.

Significantly more output power can be obtained with a diode-pumped Cr:LiSAF laser for which OMM, (2.1.1)-(2.1.5), is applied in both axes in combination with a long absorption length and efficient cooling [97Kop1, 95Kop3]. Optimized mode matching in both axes results in a highly elliptical laser mode in the crystal, because the pump beam can be focused to a much smaller beam radius in the diffraction-limited fast axis compared to the slow axis. Additionally, we can extract the heat very efficiently with a thin crystal of $\approx 1 \mathrm{~mm}$ height and obtain approximately a onedimensional heat flow. With cylindrical cavity mirror we still obtained nearly ideal $\mathrm{TEM}_{00}$ output beams. Using a $15 \mathrm{~W}, 0.9 \mathrm{~cm}$ wide diode pump array with $M_{\text {slow }}^{2}=1200$ and $M_{\text {fast }}^{2}=1$ [95Ski], the average output power of such a diode-pumped Cr:LiSAF laser was $1.4 \mathrm{~W} \mathrm{cw}, 500 \mathrm{~mW}$ modelocked with $110-\mathrm{fs}$ pulses, and 340 mW mode-locked with $50-\mathrm{fs}$ pulses [97Kop2]. Combined with a relatively long absorption length, we pumped a thin sheet volume with a width of approximately 1 mm , a length of $L_{\mathrm{a}} \approx 4 \mathrm{~mm}$ and a thickness of $\approx 80 \mu \mathrm{~m}$ in the laser crystal. This approach has been also applied to a diode-pumped Nd:glass laser, resulting in an average output power of about 2 W cw and 1 W mode-locked with pulses as short as 175 fs [98Aus] and more recently 1.4 W with pulses as short as 275 fs [00Pas1]. In addition, a diode-pumped Yb:YAG laser with the same approach produced 3.5 W average power with $1-\mathrm{ps}$ pulses and 8.1 W with 2.2 -ps pulses [99Aus].

### 2.1.3.3 Laser cavity designs

### 2.1.3.3.1 Typical picosecond lasers

The setups of picosecond lasers typically do not differ very much from those of lasers for continuouswave operation. Some mode-locker is installed, which might be either an Acousto-Optic Modulator (AOM) for active mode-locking (Sect. 2.1.4.1) or e.g. a SESAM (Sect. 2.1.4.2 and Sect. 2.1.4.3) for passive mode-locking. Also, the cavity design needs to fulfill a few additional demands. As an example, we refer to Fig. 2.1.7a, which shows the setup of a high-power $\mathrm{Nd}^{3+}$ :YAG laser [00Spu], passively mode-locked with a SESAM. The cavity design must provide appropriate beam radii both in the laser head (where the fundamental Gaussian mode should just fill the usable area) and on the SESAM to obtain an appropriate degree of saturation. This depends on a number of factors: the output power, the output coupler transmission, the cavity length, and the saturation fluence of the SESAM. Obviously the cavity length must be chosen to obtain the desired repetition rate. The equations given in Sect. 2.1.6.8 can be used to ensure that the chosen design will not suffer from $Q$-switching instabilities. The laser head is side-pumped in the mentioned example, but end-pumped laser heads can also be used, where the pump light is typically injected through a folding mirror which is highly reflective for the laser light.

The SESAM should typically be used as an end mirror, not as a folding mirror. Otherwise a tendency for the generation of multiple pulses, which would meet on the SESAM, might be induced. Similar setups can be used for actively mode-locked lasers, where the SESAM is replaced by an AOM. The AOM should be placed close to an end mirror, for similar reasons as discussed above for the SESAM.

b


Fig. 2.1.7. (a) Setup of a passively mode-locked high-power $\mathrm{Nd}^{3+}$ :YAG laser, containing a Direct-Coupled Pump (DCP) laser head, two curved mirrors, a SESAM, and an Output Coupler mirror (OC) with $7 \%$ transmission. (b) Quasi-monolithic setup as used for passively mode-locked $\mathrm{Nd}^{3+}: \mathrm{YVO}_{4}$ lasers with repetition rates above 20 GHz . (c) Typical setup of a femtosecond laser. The gain medium is pumped with a laser diode. A prism pair is used for dispersion compensation, and a SESAM as mode-locker.

For high pulse repetition rate an even simpler cavity design has been used. In the $1-\mu \mathrm{m}$ spectral region, $\mathrm{Nd}: \mathrm{YVO}_{4}$ has been found to be a particularly suitable gain medium for very high repetition rates, as already discussed in Sect. 2.1.3.1. For repetition rates of 40 GHz and above, a quasimonolithic design [99Kra2] is useful, where the output-coupler mirror is a dielectric coating directly fabricated on a curved and polished side of the laser crystal, while the SESAM is attached to the other side of the crystal (see Fig. 2.1.7b). The crystal may be anti-reflection-coated on the flat side, or just uncoated. Note that with a reflecting coating on this side, there is a cavity effect: Depending on the exact size of the air gap between crystal and SESAM, the optical field can more or less penetrate the SESAM structure, and accordingly the effective modulation depth and saturation fluence of the SESAM are modified. In this case for optimum performance, one has to manipulate the width of the air gap. A quasi-monolithic cavity design has also been used for $Q$-switched microchip lasers (Fig. 2.1.6) and described in more detail in Sect. 2.1.3.1.

Counterpropagating waves overlap in the crystal, leading to the phenomenon of spatial hole burning, which can have significant influence on the mode-locking behavior [95Bra2, 95Kae3, 01Pas2]. In particular, it allows for shorter pulses, although often with some amount of chirp, because gain narrowing is effectively eliminated: even without a mode-locker, such lasers tend to run with a significant emission bandwidth, and the mode-locker more or less only has to lock the phases of the running cavity modes.

### 2.1.3.3.2 Typical femtosecond lasers

Most femtosecond lasers are based on an end-pumped laser setup, with a broad-band laser medium such as $\mathrm{Ti}^{3+}$ :sapphire, $\mathrm{Cr}^{3+}$ :LiSAF, Nd:glass or $\mathrm{Yb}^{3+}$ :glass (see Sect. 2.1.3.1 for an overview). In the case of $\mathrm{Ti}^{3+}$ :sapphire, the pump source can be either an Ar ion laser or a frequency-doubled solid-state laser. In any case, one typically uses a few watts of pump power in a beam with good transverse beam quality, because the mode radius in the $\mathrm{Ti}^{3+}$ :sapphire rod is usually rather small. Other gain media like $\mathrm{Cr}^{3+}$ :LiSAF, Nd :glass or $\mathrm{Yb}^{3+}$ :glass are typically pumped with highbrightness diode lasers, delivering a few watts with beam-quality factor $M^{2}$ in the order of 10 in one direction and $<5$ in the other direction, which allows for diffraction-limited laser output with typically a few hundred milliwatts.

The typical laser cavities (see Fig. 2.1.7c as an example) contain two curved mirrors in a distance of a few centimeters on both sides of the gain medium. The pump power is usually injected through one or both of these mirrors, which also focus the intracavity laser beam to an appropriate beam waist. One of the two "arms" of the cavity ends with the output coupler mirror, while the other one may be used for a SESAM as a passive mode-locker. One arm typically contains a prism pair (Sect. 2.1.5.2.3), GTI (Sect. 2.1.5.2.1) or chirped mirrors (Sect. 2.1.5.2.4) for dispersion compensation, which is necessary for femtosecond pulse generation. In most cases, femtosecond lasers operate in the regime of negative overall intracavity dispersion so that soliton-like pulses are formed.

Instead of a SESAM, or in addition to it, the Kerr lens in the gain medium can be used for mode-locking (Sect. 2.1.4.4). In most cases, soft-aperture KLM is used. Here, the cavity design is made so that the Kerr lens reduces the mode area for high intensities and thus improves the overlap with the (strongly focused) pump beam. This is achieved by operating the laser cavity near one of the stability limits of the cavity, which are found by varying the distance between the above mentioned curved folding mirrors, or some other distance in the cavity.

For the shortest pulse durations around 5-6 fs, the strong action of KLM as an effective fast saturable absorber is definitely required. Also double-chirped mirrors (Sect. 2.1.5.2.4) are required for precise dispersion compensation over a very broad bandwidth. Typically, several dispersive mirrors are used in the laser cavity, and additional mirrors may be used for further external compression. A broadband SESAM allows for self-starting mode-locking.

Higher pulse energies and peak powers have been generated by using laser setups with reduced repetition rates of only a few MHz . The long cavity length required for such repetition rates is achieved by inserting a multi-pass cell $[64 \mathrm{Her}]$. However, the limiting factor to the pulse energy is ultimately not the practically achievable cavity length but rather the nonlinearity of the gain crystal - at least in the sub-30-femtosecond domain: If self-phase modulation becomes too strong, this destabilizes the mode-locking process.

### 2.1.3.3.3 High-power thin-disk laser

The by far highest average powers in the sub-picosecond domain can be obtained from thin-disk $\mathrm{Yb}^{3+}$ :YAG lasers, passively mode-locked with a SESAM. The first result, with 16.2 W in 700 -fs pulses [00Aus], received a lot of attention for its unusually high output power. More importantly, this new approach introduced the first power-scalable technology for sub-picosecond lasers. For this reason, further big improvements became possible, first to 60 W average power [03Inn] and later even to 80 W [04Bru], in both cases with pulse durations near 700 fs . Recently, pulse energies well above $1 \mu$ s have been generated directly from the passively mode-locked thin-disk laser first with $5.1 \mu \mathrm{~s}[06 \mathrm{Mar}]$ and then even with $11 \mu \mathrm{~s}$ [07Mar] pulse energies. These lasers are operated in the soliton mode-locked regime (Sect. 2.1.6.7). For thermal reasons negative dispersion was obtained with GTI dispersive mirrors (Sect. 2.1.5.2.1), which however also have to be carefully optimized.

The power scalability of the passively mode-locked thin-disk laser is important. First of all, the thin-disk laser head [94Gie] itself is power-scalable because of the nearly one-dimensional heat flow in the beam direction: Thermal effects (like thermal lensing) do not become more severe if the mode area is scaled up proportional to the power level. A possible problem is only the effect of stress, which has to be limited with refined techniques for mounting the crystal on the heat sink. The SESAM also has the geometry of a thin disk and thus does not limit the power: More power on an accordingly larger area does not significantly increase the temperature excursion, nor the optical intensities in the device. Finally, the tendency for $Q$-switching instabilities does not become stronger if e.g. the pump power and the mode areas in the disk and the absorber are all doubled while leaving pump intensity and cavity length unchanged. Thus the whole concept of the passively mode-locked thin-disk laser is power-scalable in the sense that the output power can be increased without making the following key challenges more severe: heating in the disk, heating or nonthermal damage of the SESAM, and $Q$-switching instabilities. Of course, further power increases can introduce other challenges which are no issue at lower powers, such as the difficulty to do dispersion compensation with optical elements that can stand the very high intracavity powers.

For a longer period the maximum pulse energy obtained directly from a passively mode-locked thin-disk laser had been $1.75 \mu \mathrm{~J}$ [03Inn]. A further increase of the pulse energy was limited by strong nonlinearities of initially unknown origin. We then discovered that the Kerr nonlinearity of the air inside the cavity was large enough to add a significant amount of nonlinear phase shift per cavity roundtrip. Numerical estimations using the nonlinear refractive index of air show good agreement with the missing nonlinearity in [03Inn]. To avoid contributions of the air to the nonlinear phase shift, we thus covered the laser cavity with a box that was then flooded with helium, which has a negligible nonlinearity compared to air. This resulted in pulse energies of $5.1 \mu \mathrm{~J}$ and then even $11 \mu \mathrm{~J}$ with transform-limited soliton pulses of about 790 fs duration. These are the highest pulse energies ever obtained directly from a cw modelocked laser without any further amplification.

We believe that in the near future we can scale cw mode-locked thin-disk lasers to average powers of around 500 W and to pulse energies well above $100 \mu \mathrm{~J}$. In comparison low-repetitionrate Ti:sapphire lasers will not scale as well and are currently limited to the sub-1- $\mu \mathrm{J}$ regime, even with cavity dumping (Table 2.1.2) Simple pulse compression of the high-energy ultrafast Yb:YAG thin-disk laser resulted in 33 -fs pulses with a peak power of 12 MW [03Sue]. Further improvements resulted in pulses as short as 24 fs and peak intensity around $1014 \mathrm{~W} / \mathrm{cm}^{2}$. Such a source even makes high-field physics experiments possible but at a much higher pulse repetition rate than the
typical $1-\mathrm{kHz}$ rate. This greatly increases the signal-to-noise ratio in measurements [07Mar] and reduces space-charge effects that tend to hide the underlying interesting physical processes with current sources at 1 kHz .

### 2.1.4 Loss modulation

### 2.1.4.1 Optical modulators: acousto-optic and electro-optic modulators

Many textbooks, for example [86Sie, 84Yar, 98 Sve ], have reviewed optical modulators for pulse generation. Today the most important optical modulators for short pulse generation are the acoustooptic and electro-optic modulators. The acousto-optic modulators have the advantage of low optical insertion loss and can readily be driven at high repetition rates. They are typically used for cw mode-locking. However, for $Q$-switching their loss modulation is limited and the switching time is rather slow. Therefore, acousto-optic modulators are primarily used for repetitive $Q$-switching of cw-pumped lasers (e.g. Nd:YAG) and electro-optic modulators are used for $Q$-switching in general.

For mode-locking the acousto-optic modulator typically consists of an acousto-optic substrate (typically fused quartz) and a transducer that launches an acoustic wave into the substrate. An acoustic resonator is formed when opposite to the transducer the crystal substrate is air backed. Then the acoustic wave is reflected and an acoustic standing wave is formed which produces a light modulator at twice the microwave drive frequency. At higher frequencies (a few hundreds of megahertz to a few gigahertz) the loss modulation is strongly reduced by the acoustic attenuation in the substrate. Thus, at higher modulation frequencies a sapphire [90Kel1, 90 Wei ] or a GaP [90Wal] substrate has been used successfully.

### 2.1.4.2 Saturable absorber: self-amplitude modulation (SAM)

Saturable absorbers have been used to passively $Q$-switch and mode-lock many lasers. Different saturable absorbers, such as organic dyes, color filter glasses, dye-doped solids, ion-doped crystals and semiconductors have been used. Independent of the specific saturable absorber material, we can define a few macroscopic absorber parameters that will determine the pulse generation process.

The relevant macroscopic properties of a saturable absorber are the modulation depth, the nonsaturable loss, the saturation fluence, the saturation intensity and the impulse response or recovery times (Table 2.1.5). These parameters determine the operation of a passively mode-locked or $Q$-switched laser. In our notation we assume that the saturable absorber is integrated within a mirror structure thus we are interested in the nonlinear reflectivity change $R(t)$ as a function of time and $R\left(F_{\mathrm{p}, \mathrm{A}}\right)$ as a function of the incident pulse energy fluence on the saturable absorber. If the saturable absorber is used in transmission, we simply characterize the absorber by nonlinear transmission measurements, i.e. $T(t)$ and $T\left(F_{\mathrm{p}, \mathrm{A}}\right)$. Both the saturation fluence $F_{\mathrm{sat}, \mathrm{A}}$ and the absorber recovery time $\tau_{\mathrm{A}}$ are determined experimentally without any needs to determine the microscopic properties of the nonlinearities. The saturation fluence of the absorber does not only depend on material properties but also on the specific device structure in which the absorber is integrated, which gives significantly more design freedom.

Standard pump-probe techniques determine the impulse response $R(t)$ and therefore $\tau_{\mathrm{A}}$. In the picosecond regime we typically only have to consider one picosecond recovery time, because much faster femtosecond nonlinearities in the saturable absorber give negligible modulation depth. This is shown with a semiconductor saturable absorber in Fig. 2.1.8, where the differential impulse

Table 2.1.5. Saturable absorber quantities, their defining equations and units.

| Quantity | Symbol | Defining equation or measurement | Unit |
| :--- | :--- | :--- | :--- |
| Saturation fluence | $F_{\mathrm{sat}, \mathrm{A}}$ | measurement $R\left(F_{\mathrm{p}, \mathrm{A}}\right)$ or $T\left(F_{\mathrm{p}, \mathrm{A}}\right),($ Fig. 2.1.9 $)$ | $\mathrm{J} / \mathrm{cm}^{2}$ |
| Recovery time | $\tau_{\mathrm{A}}$ | measurement $R(t)$ or $T(t),($ Fig. 2.1.8) | s |
| Incident beam area | $A_{\mathrm{A}}$ | measurement | $\mathrm{cm}^{2}$ |
| Saturation energy | $E_{\mathrm{sat}, \mathrm{A}}$ | $E_{\mathrm{sat}, \mathrm{A}}=A_{\mathrm{A}} F_{\mathrm{sat}, \mathrm{A}}$ | J |
| Saturation intensity | $I_{\mathrm{sat}, \mathrm{A}}$ | $I_{\mathrm{sat}, \mathrm{A}}=F_{\mathrm{sat}, \mathrm{A}} / \tau_{\mathrm{A}}$ | $\mathrm{W} / \mathrm{cm}^{2}$ |
| Modulation depth | $\Delta R$ or $\Delta T$ | measurement $R\left(F_{\mathrm{p}, \mathrm{A}}\right)$ or $T\left(F_{\mathrm{p}, \mathrm{A}}\right),($ Fig. 2.1.9 $)$ |  |
| Nonsaturable loss | $\Delta R_{\mathrm{ns}}$ or $\Delta T_{\mathrm{ns}}$ | measurement $R\left(F_{\mathrm{p}, \mathrm{A}}\right)$ or $T\left(F_{\mathrm{p}, \mathrm{A}}\right),($ Fig. 2.1.9 $)$ |  |
| Incident pulse energy | $E_{\mathrm{p}}$ | measurement | J |
| Incident pulse fluence | $F_{\mathrm{p}, \mathrm{A}}$ | $F_{\mathrm{p}, \mathrm{A}}=E_{\mathrm{p}} / A_{\mathrm{A}}$ | $\mathrm{J} / \mathrm{cm}^{2}$ |
| Incident intensity | $I_{\mathrm{A}}(t)$ | $F_{\mathrm{p}, \mathrm{A}}=\int I_{\mathrm{A}}(t) \mathrm{d} t$ | $\mathrm{~W} / \mathrm{cm}^{2}$ |



Fig. 2.1.8. Typical measured impulse response of a SESAM measured with standard degenerate pumpprobe measurements using two different excitation pulse durations. The saturable was grown at low temperature, which reduced the recovery time to about 20 ps . The short intraband thermalization recovery time results in negligible modulation depth with a 4 ps excitation pulse. Thus, only the slower recovery time due to carrier trapping is important in the picosecond regime.
response $D R(t)$ was measured for two different excitation pulse durations using a semiconductor saturable absorber. For excitation with a picosecond pulse the pump-probe trace clearly shows no significant modulation depth with a fast time constant. In the femtosecond pulse regime we normally have to consider more than one absorber recovery time. In this case the slow component normally helps to start the initial pulse formation process. The modulation depth of the fast component then determines the pulse duration at steady state. Further improvements of the saturable absorber normally require some better understanding of the underlying physics of the nonlinearities which can be very interesting and rather complex. A more detailed review about the microscopic properties of ultrafast semiconductor nonlinearities for saturable absorber applications is given in a recent book chapter [00Sie]. Ultrafast semiconductor dynamics in general are discussed in much more detail by [99Sha]. However, the basic knowledge of the macroscopic properties of the absorber and how to measure [04Hai] and adjust them to a certain value is normally sufficient for stable pulse generation.

The saturation fluence $F_{\text {sat, } \mathrm{A}}$ is determined and defined by the measurement of the nonlinear change in reflectivity $R\left(F_{\mathrm{p}, \mathrm{A}}\right)$ as a function of increased incident pulse fluence (Fig. 2.1.9). The traveling-wave rate equations [89Agr] in the slow absorber approximation give normally a very


Fig. 2.1.9. Measured nonlinear reflectivity as a function of incident pulse fluence on a typical SESAM. Theoretical fit determines the macroscopic saturable absorber parameters: saturation fluence $F_{\text {sat, A }}$, modulation depth $\Delta R$ and nonsaturable loss $\Delta R_{\mathrm{ns}}$.
good fit and determine the saturation fluence $F_{\text {sat, } \mathrm{A}}$, modulation depth $\Delta R$ and nonsaturable losses $\Delta R_{\mathrm{ns}}$ of the absorber [95Bro1, 04Hai].

The modulation depth is typically small (i.e. a few percent to a fraction of a percent!) to prevent $Q$-switching instabilities in passively mode-locked solid-state lasers [99Hoe1]. Thus it is reasonable to make the following approximation:

$$
\begin{equation*}
\Delta R=1-\mathrm{e}^{-2 q_{0}} \approx 2 q_{0}, \quad q_{0} \ll 1 \tag{2.1.6}
\end{equation*}
$$

where $q_{0}$ is the unsaturated amplitude loss coefficient.
The saturation of an absorber can be described with the following differential equation [89 Agr]:

$$
\begin{equation*}
\frac{\mathrm{d} q(t)}{\mathrm{d} t}=-\frac{q(t)-q_{0}}{\tau_{\mathrm{A}}}-\frac{q(t) P(t)}{E_{\mathrm{sat}, \mathrm{~A}}} \tag{2.1.7}
\end{equation*}
$$

where $q(t)$ is the saturable amplitude loss coefficient that does not include any nonsaturable losses and $P(t)$ is the time-dependent power incident on the absorber. Note that (2.1.7) may not be precise for high excitations where inverse saturable absorption can start to become important: For example, high excitation many times above the saturation fluence can result in additional effects such as two-photon absorptions, free carrier absorption, thermal and even various damage effects [99Tho], [05Gra2]. Two-photon absorption only starts to become significant in the femtosecond pulse width regime and results in an earlier roll-off of the nonlinear reflectivity at high incident pulse fluences. This is a well-known effect and has been used in power-limiting devices before [ 86 Wal ]. In this regime, however, the absorber is operated more closely to the damage threshold which needs to be evaluated separately. Our experience is that damage in semiconductor saturable absorbers typically occurs at around 100 times the saturation fluence of the absorber with longterm degradation observed close to below this damage threshold. Therefore, we normally operate the device a least an order of magnitude below this damage threshold, ideally at an incident pulse fluence of 3 to 5 times the saturation fluence of the absorber. We therefore neglect these very high-fluence effects in the following discussion. They, however, will become important again for suppressing $Q$-switching instabilities and will be discussed in more detail in Sect. 2.1.6.8.

At any time $t$ the reflected (or transmitted) intensity $I_{\text {out }}(t)$ from the saturable absorber is given by

$$
\begin{equation*}
I_{\mathrm{out}}(t)=R(t) I_{\mathrm{in}}(t)=\mathrm{e}^{-2 q(t)} I_{\mathrm{in}}(t) \tag{2.1.8}
\end{equation*}
$$

for a given input pulse $I_{\mathrm{in}}(t)$. Then the total net reflectivity is given by

$$
\begin{equation*}
R_{\mathrm{tot}}=\frac{F_{\mathrm{out}}}{F_{\mathrm{in}}}=\frac{\int I_{\mathrm{out}}(t) \mathrm{d} t}{\int I_{\mathrm{in}}(t) \mathrm{d} t}=1-\frac{2}{F_{\mathrm{in}}} \int q(t) I_{\mathrm{in}}(t) \mathrm{d} t \tag{2.1.9}
\end{equation*}
$$

This determines the total absorber loss coefficient $q_{\mathrm{p}}$, which results from the fact that part of the excitation pulse needs to be absorbed to saturate the absorber:

$$
\begin{equation*}
R_{\mathrm{tot}}=\mathrm{e}^{-2 q_{\mathrm{p}}} \approx 1-2 q_{p} \tag{2.1.10}
\end{equation*}
$$

From (2.1.9) and (2.1.10) it then follows

$$
\begin{equation*}
q_{\mathrm{p}}=\frac{1}{F_{\mathrm{in}}} \int q(t) I_{\mathrm{in}}(t) \mathrm{d} t=\int q(t) f(t) \mathrm{d} t \tag{2.1.11}
\end{equation*}
$$

where

$$
\begin{equation*}
f(t) \equiv \frac{I_{\mathrm{in}}(t)}{F_{\mathrm{in}}}=\frac{P_{\mathrm{in}}(t)}{E_{\mathrm{p}, \mathrm{in}}} \quad \text { with } \quad \int f(t) \mathrm{d} t=\frac{1}{F_{\mathrm{in}}} \int I_{\mathrm{in}}(t) \mathrm{d} t=1 \tag{2.1.12}
\end{equation*}
$$

We then distinguish between two typical cases: a slow and a fast saturable absorber.

### 2.1.4.2.1 Slow saturable absorber

In the case of a slow saturable absorber, we assume that the excitation pulse duration is much shorter than the recovery time of the absorber (i.e. $\tau_{\mathrm{p}} \ll \tau_{\mathrm{A}}$ ). Thus, we can neglect the recovery of the absorber during pulse excitation and (2.1.7) reduces to:

$$
\begin{equation*}
\frac{\mathrm{d} q(t)}{\mathrm{d} t} \approx-\frac{q(t) P(t)}{E_{\mathrm{sat}, \mathrm{~A}}} \tag{2.1.13}
\end{equation*}
$$

This differential equation can be solved and we obtain for the Self-Amplitude Modulation (SAM):

$$
\begin{equation*}
q(t)=q_{0} \exp \left[-\frac{E_{\mathrm{p}}}{E_{\mathrm{sat}, \mathrm{~A}}} \int_{0}^{t} f\left(t^{\prime}\right) \mathrm{d} t^{\prime}\right] . \tag{2.1.14}
\end{equation*}
$$

Equation (2.1.11) then determines the total absorber loss coefficient for a given incident pulse fluence $F_{\mathrm{p}, \mathrm{A}}$ :

$$
\begin{equation*}
q_{\mathrm{p}}\left(F_{\mathrm{p}, \mathrm{~A}}\right)=\int q(t) f(t) \mathrm{d} t=q_{0} \frac{F_{\mathrm{sat}, \mathrm{~A}}}{F_{\mathrm{p}, \mathrm{~A}}}\left(1-\mathrm{e}^{-F_{\mathrm{p}, \mathrm{~A}} / F_{\mathrm{sat}, \mathrm{~A}}}\right) \tag{2.1.15}
\end{equation*}
$$

It is not surprising that $q_{\mathrm{p}}$ does not depend on any specific pulse form because $\tau_{\mathrm{p}} \ll \tau_{\mathrm{A}}$. It is useful to introduce a saturation parameter $S \equiv F_{\mathrm{p}, \mathrm{A}} / F_{\mathrm{sat}, \mathrm{A}}$. For strong saturation $(S>3)$, we have $q_{\mathrm{p}}\left(F_{\mathrm{p}, \mathrm{A}}\right) \approx q_{0} / S(2.1 .15)$ and the absorbed pulse fluence is about $F_{\mathrm{sat}, \mathrm{A}} \Delta R$.

### 2.1.4.2.2 Fast saturable absorber

In the case of a fast saturable absorber, the absorber recovery time is much faster than the pulse duration (i.e. $\tau_{\mathrm{p}} \gg \tau_{\mathrm{A}}$ ). Thus, we can assume that the absorption instantaneously follows the absorption of a certain power $P(t)$ and (2.1.7) reduces to

$$
\begin{equation*}
0=-\frac{q(t)-q_{0}}{\tau_{\mathrm{A}}}-\frac{q(t) P(t)}{E_{\mathrm{sat}, \mathrm{~A}}} . \tag{2.1.16}
\end{equation*}
$$

The saturation of the fast absorber then follows directly from (2.1.16):

$$
\begin{equation*}
q(t)=\frac{q_{0}}{1+\frac{I_{\mathrm{A}}(t)}{I_{\mathrm{sat}, \mathrm{~A}}}} \tag{2.1.17}
\end{equation*}
$$

where we used the fact that $P_{\text {sat }, \mathrm{A}}=E_{\text {sat, } \mathrm{A}} / \tau_{\mathrm{A}}$ and $P(t) / P_{\text {sat }, \mathrm{A}}=I_{\mathrm{A}}(t) / I_{\mathrm{sat}, \mathrm{A}}$. In the linear regime we can make the following approximation in (2.1.17):

$$
\begin{equation*}
q(t) \approx q_{0}-\gamma_{\mathrm{A}} P(t) \quad \text { with } \quad \gamma_{\mathrm{A}} \equiv \frac{q_{0}}{I_{\mathrm{sat}, \mathrm{~A}} A_{\mathrm{A}}} \tag{2.1.18}
\end{equation*}
$$

The total absorber loss coefficient $q_{\mathrm{p}}$, (2.1.10)-(2.1.11), now depends on the pulse form and for a sech ${ }^{2}$-pulse shape we obtain for an incident pulse fluence $F_{\mathrm{p}, \mathrm{A}}$ and the linear approximation of $q(t)$ for weak absorber saturation (2.1.18):

$$
\begin{equation*}
q_{\mathrm{p}}\left(F_{\mathrm{p}, \mathrm{~A}}\right)=\frac{1}{F_{\mathrm{p}, \mathrm{~A}}} \int q(t) I_{\mathrm{A}}(t) \mathrm{d} t=q_{0}\left(1-\frac{1}{3} \frac{F_{\mathrm{p}, \mathrm{~A}}}{\tau I_{\mathrm{sat}, \mathrm{~A}}}\right) . \tag{2.1.19}
\end{equation*}
$$

We will later see that we only obtain an analytic solution for fast saturable absorber mode-locking, if we assume an ideal fast absorber that saturates linearly with pulse intensity (2.1.18) - which in principle only applies for weak absorber saturation in a real absorber. For a maximum modulation depth, we then can assume that $q_{0}=\gamma_{\mathrm{A}} P_{0}$ (assuming an ideal fast absorber over the full modulation depth). We then obtain with (2.1.19) a residual saturable absorber loss of $q_{0} / 3$, which the pulse experiences to fully saturate the ideal fast saturable absorber.

### 2.1.4.3 Semiconductor saturable absorbers

### 2.1.4.3.1 Semiconductor dynamics

Semiconductors are well suited absorber materials for ultrashort pulse generation. In contrast to saturable absorber mechanisms based on the Kerr effect, ultrafast semiconductor nonlinearities can be independently optimized from the laser cavity design. In addition, ultrafast semiconductor spectroscopy techniques [99Sha] provide the basis for many improvements of ultrashort pulse generation with semiconductor saturable absorbers.

The semiconductor electronic structure gives rise to strong interaction among optical excitations on ultrafast time scales and very complex dynamics. Despite the complexity of the dynamics, different time regimes can be distinguished in the evolution of optical excitations in semiconductors. These different time regimes are schematically illustrated in Fig. 2.1.10, which shows the energy dispersion diagram of a 2-band bulk semiconductor which is typical for a III-V semiconductor material. Optical excitation with an ultrafast laser pulse prepares the semiconductor in the coherent regime (time regime I in Fig. 2.1.10). In this regime, a well-defined phase relation exists between the optical excitations and the electric field of the laser pulse and among the optical excitations themselves. The coherence among the excitations in the semiconductor gives rise to a macroscopic polarization (dipole moment density). Since the macroscopic polarization enters as a source term in Maxwell's equations, it leads to an electric field which is experimentally accessible. The magnitude and decay of the polarization provide information on the properties of the semiconductor in the coherent regime. The irreversible decay of the polarization is due to scattering processes (i.e. electron-electron and electron-phonon scattering) and is usually described by the so-called dephasing or transversal relaxation time. For a mathematical definition of this time constant the reader is referred to [99Sha, $90 \mathrm{Goe}, 75 \mathrm{All}]$.


Fig. 2.1.10. Schematic dispersion diagram of a 2 -band bulk semiconductor showing the time regimes I-IV after optical excitation, see text for more details. e-e: electron-electron scattering. e-phonon: electron-phonon scattering.

After the loss of coherence, ultrafast spectroscopy of semiconductors is solely concerned with the dynamics of the population, i.e., electron and hole distributions. In this incoherent regime, the time regimes II-IV in Fig. 2.1.10 can be distinguished, as described as follows. The initial electron and hole distributions are non-thermal in most cases, i.e., they cannot be described by Fermi-Dirac statistics with a well-defined temperature [85Oud, 86Kno, 87Sch]. Scattering among charge carriers is mainly responsible for the redistribution of energy within the carrier distributions and for the formation of thermal distributions. This thermalization is shown as time regime II in Fig. 2.1.10, for the example of a thermalizing electron distribution where thermalization occurs through scattering among the electrons. For excitation of the continuum, thermalization usually occurs on a time scale of 100 fs under most experimental conditions. The exact thermalization time strongly depends on the carrier density, the excess photon energy with respect to the band edge and the type of carrier [99Sha].

In general, the carriers have a temperature different from the lattice temperature after thermalization has been completed. In Fig. 2.1.10 it is assumed that the carriers have a higher temperature than the lattice. For this case, Fig. 2.1.10 schematically shows the cooling of carriers by the emission of phonons, i.e., energy transfer to the lattice. Cooling defines the time regime III. Typical time constants are in the picosecond and tens of picosecond range.

Finally, the optically excited semiconductor returns to thermodynamic equilibrium by the recombination of electron-hole pairs. Recombination is shown as time regime IV in Fig. 2.1.10. In a perfect semiconductor crystal, recombination proceeds via the emission of photons or Auger processes at high carrier densities. These recombination processes in a good quality semiconductor (i.e. with a low level of defect states) take place on time scales of hundreds of picoseconds and longer.

Another ultrafast process is encountered if large densities of deep-level traps are incorporated in a semiconductor. Trapping of carriers into deep levels can proceed on sub-picosecond time scales (not shown in Fig. 2.1.10). Since carrier trapping is important in many saturable absorber applications, it is discussed in more details in Sect. 2.1.4.3.2.

We note that the different time regimes temporally overlap. For example, a scattering process may destroy the coherence and contribute to thermalization. Nevertheless, it is very useful to distinguish between the different time regimes because they are a convenient means for the description of the complex semiconductor dynamics. The schematic picture of the different time regimes also demonstrates that two or more time constants are usually required to describe the temporal response of a semiconductor absorber. For example, we recall that thermalization typically takes place on the $100-\mathrm{fs}$ time scale while carrier trapping proceeds on time scales from a few hundreds


Fig. 2.1.11. Typical Self-Amplitude Modulation (SAM) observed in a semiconductor saturable absorber: A semiconductor can absorb light if the photon energy is sufficient to excite carriers from the valence band to the conduction band. Under conditions of strong excitation, the absorption is saturated because possible initial states of the pump transition are depleted while the final states are partially occupied. Within typically 60-300 fs after the excitation, the carriers in each band thermalize, and this already leads to a partial recovery of the absorption. On a longer time scale - typically between a few ps and a few ns depending on defect engineering - they will be removed by recombination and trapping. Both processes can be used for mode-locking of lasers.
of femtoseconds to tens of picoseconds. This results in the measured Self-Amplitude Modulation (SAM) of a semiconductor saturable absorber as shown in Fig. 2.1.11. This corresponds to the loss modulation used for passive mode-locking in Fig. 2.1.3.

### 2.1.4.3.2 Typical self-amplitude modulation (SAM) from semiconductor saturable absorbers

Figure 2.1.11 shows a typical Self-Amplitude Modulation (SAM) observed in semiconductor saturable absorbers and their different relaxation processes as discussed in Sect. 2.1.4.3.1. Semiconductor saturable absorber applications in ultrashort pulse generation often require picosecond or sub-picosecond absorber recovery times [01Pas1]. The simplest way to obtain such short absorber recovery times would be to remove the optically excited carriers from the bands a few hundreds of femtoseconds to a few tens of picosecond after they have been created. However, intrinsic recombination processes are usually too slow to deplete the band states of a semiconductor on picosecond or sub-picosecond time scales. Therefore, one generates defect states in the band gap which give rise to fast carrier trapping to deplete the bands. The trapping time is determined by the density and the type of the traps. Higher trap densities give rise to faster trapping.

Standard methods for the controlled incorporation of defect and trap states are ion implantation [89Zie] and Low-Temperature (LT) molecular beam epitaxy [88Smi]. More uncontrolled incorporation of defects occurs close to surfaces. In ion-implanted semiconductors, the trap density and the type of defect are determined by the implantation dose. The growth temperature controls the defect density in LT semiconductors where larger defect densities are incorporated at lower temperatures [94Liu, 93Wit]. Semiconductor saturable absorbers can be produced either with Molecular

Beam Epitaxy (MBE) or with Metal-Organic chemical Vapor deposition (MOVPE). MBE gives us the additional flexibility to grow semiconductors at lower temperatures, down to $\approx 200^{\circ} \mathrm{C}$, while MOVPE usually requires growth temperatures of $\approx 600^{\circ} \mathrm{C}$ to break up the incident molecules on the wafer surface during the growth. Lower growth temperatures lead to microscopic structural defects which act as traps for excited carriers and thus reduce the recovery time, which is beneficial for the use in ultrafast lasers. Optimized materials combine an ultrafast recovery time with low saturation fluence, high modulation and small nonsaturable losses. This material optimization issue has been addressed for ion-implanted [99Led] and LT-grown [96Sie, 99Hai1, 99Hai2] semiconductor saturable absorbers.

### 2.1.4.3.3 Semiconductor saturable absorber materials

Semiconductor materials offer a wide flexibility in choosing the emission wavelength of the lasers. It ranges from $\approx 400 \mathrm{~nm}$ in the UV using GaN-based materials to $\approx 2.5 \mu \mathrm{~m}$ in the mid-infrared using GaInAsSb-based materials. More standard high-performance semiconductor material systems which can be grown today cover the infrared wavelength range from 800 nm up to $1.5 \mu \mathrm{~m}$. Semiconductor compounds used for these wavelengths are AlGaAs ( 800 nm to 870 nm ), InGaAs ( 870 nm to about 1150 nm ), GaInNAs ( $1.1 \mu \mathrm{~m}$ to $1.5 \mu \mathrm{~m}$ ), or InGaAsP ( $1.5-\mu \mathrm{m}$ range). A larger wavelength range for a given material composition may only be obtained at the expense of increased defect concentrations because of an increased lattice mismatch to a given substrate material. Generally, bulk quantum-well and quantum-dot semiconductor saturable absorbers have been used. Especially, the quantum-dot saturable absorbers turned out to be advantageous for the integration into the VECSEL structure [04Lor, 07Maa].

### 2.1.4.3.3.1 InGaAs/GaAs/AlGaAs semiconductor material system

This material is best-suited for the $800 \mathrm{~nm}-1.1 \mu \mathrm{~m}$ wavelength range because of the near-perfect lattice match between GaAs and AlGaAs. InGaAs saturable absorbers have been grown on AlAs/GaAs Bragg mirrors and have been the material of choice for SESAMs at an operation wavelength of $\approx 1 \mu \mathrm{~m}$. However, thicker InGaAs saturable absorbers above the critical thickness had surface striations that introduced too much scattering losses to be used inside a laser [94Kel]. Low-temperature MBE growth (see more details in Sect. 2.1.4.3.2) resulted in strain-relaxed structures with surfaces that were optically flat, but with strongly increased defect densities. For SESAM applications this is actually advantageous, and has been exploited to optimize the dynamic response of the SESAM. InGaAs saturable absorbers on AlAs/GaAs Bragg mirrors have even been used at an operation wavelength of $1.3 \mu \mathrm{~m}$ [96Flu2, 97Flu] and $1.55 \mu \mathrm{~m}$ [03Spu, 04Zel]. However, these highly strained layers with high indium content exceed the critical thickness, and show significant nonsaturable losses due to strain and defect formation. Optimized low-temperature MBE growth, however, (Sect. 2.1.4.3.2) allowed improved InGaAs SESAMs to support stable mode-locking and $Q$-switching in diode-pumped solid-state lasers.

### 2.1.4.3.3.2 GaInAsP/InP semiconductor material system

This material system can be lattice-matched on the InP substrate but suffers from low refractiveindex contrast and poor temperature characteristics. Due to the low refractive-index contrast, a high number of $\operatorname{InP} / G a I n A s P$ mirror pairs are required to form Distributed Bragg Reflectors (DBRs). This demands very precise control of the growth to achieve DBRs with uniform and accurate layer thickness.

### 2.1.4.3.3.3 GaInNAs semiconductor material

Recently, dilute nitrides (i.e. GaInNAs) have attracted strong attention for laser devices in the telecommunication wavelength range between $1.3 \mu \mathrm{~m}$ and $1.55 \mu \mathrm{~m}$ that can use high-contrast GaAs/AlGaAs DBR mirrors [02Har, 02Rie]. Adding a few percent of nitrogen to InGaAs has two advantages: a redshift of the absorption wavelength and a reduction of the lattice mismatch to GaAs. The drawback is that the nitrogen incorporation decreases the crystalline quality, which is a big challenge for the fabrication of active devices. However, SESAMs are passive devices relying on fast defect-induced nonradiative carrier recombination to allow for short-pulse generation. GaInNAs saturable absorber on GaAs/AlsAs Bragg mirrors operating at $1.3 \mu \mathrm{~m}$ have been demonstrated for solid-state laser mode-locking. The first GaInNAs SESAM was reported to mode-lock a quasi-cw pumped Nd:YLF and Nd:YALO laser at $1.3 \mu \mathrm{~m}$ [02Sun]. Self-starting stable passive cw modelocking of a solid-state laser with a GaInNAs SESAM was demonstrated more recently [04Liv]. A detailed study of the absorber properties and the mode-locking behavior revealed that GaInNAs SESAMs provide low saturation fluences and possess extremely low losses [04Liv, 04Sch2, 05Gra3]. These SESAMs supported mode-locking at repetition rates of 5 GHz and 10 GHz [05Spu2]. In 2003, GaInNAs SESAMs at $1.5 \mu \mathrm{~m}$ were shown to mode-lock Er-doped fiber lasers but had too much loss for solid-state lasers [03Okh]. Just recently for the first time successful mode-locking of a solid-state laser at $1.54 \mu \mathrm{~m}$ using a GaInNAs SESAM has been demonstrated [05Rut].

### 2.1.4.3.3.4 AlGaAsSb semiconductor material

Another interesting long-wavelength semiconductor saturable absorber material is based on antimonide. The quaternary alloy AlGaAsSb has a wide band-gap tunability ( $1.55 \mu \mathrm{~m}$ to $0.54 \mu \mathrm{~m}$ ) and intrinsically low modulation depth [03Saa, 04Ost]. Similar to InGaAsP, AlGaAsSb is latticematched to InP, but its absorption edge is not as steep as the one of InGaAsP [87Ada]. Therefore, operating the absorber in the bandtail results in a sufficiently small modulation depth (i.e. usually below $0.5 \%$ ) suitable for high-repetition-rate lasers. An Sb-based SESAM can be grown by MOVPE with AlGaAsSb/InP DBRs [06Ost]. Compared to InGaAsP, AlGaAsSb forms a high refractive-index contrast with InP (0.4) allowing for a lower number of Bragg periods. The first antimonide SESAM self-started and mode-locked a $61-\mathrm{MHz}$ Er:Yb:glass laser [04Gra]. More recently, this was extended to an Er:Yb:glass laser at $10 \mathrm{GHz}, 1535 \mathrm{~nm}$ and with 4.7 ps pulse duration [06Gra].

### 2.1.4.3.3.5 GaAs wafer for $\approx 1 \mu \mathrm{~m}$

Simple GaAs wafers have been used as saturable absorbers to mode-lock [04Kon] and $Q$-switch [ $00 \mathrm{Li}, 01 \mathrm{Che} 1]$ solid-state lasers at a wavelength of $\approx 1 \mu \mathrm{~m}$. Photo electrons in the conduction band are generated from mid-gap defect states (i.e. EL2) present in GaAs wafers. These EL2-defects have similar properties as the arsenic antiside point defects in LT-grown materials (Sect. 2.1.4.3.2). This transition, however, has a very high saturation fluence in the range of $1 \mathrm{~mJ} / \mathrm{cm}^{2}$ [06Li] which is typically about 100 times higher than the standard valence-to-conduction band transition generally used for SESAMs. This strongly increases the tendency for $Q$-switching instabilities (Sect. 2.1.6.8).

### 2.1.4.3.3.6 Semiconductor-doped dielectric films

Saturable absorbers based on semiconductor-doped dielectric films have been demonstrated [99Bil]. In this case, InAs-doped thin-film rf-sputtering technology was used which offers similar advantages as SESAMs, i.e. the integration of the absorber into a mirror structure. At this point, however,
the saturation fluence of $\approx 10 \mathrm{~mJ} / \mathrm{cm}^{2}$ is still rather high for stable solid-state laser mode-locking. In comparison, epitaxially grown SESAMs typically have a saturation fluence in the range of $10 \mu \mathrm{~J} / \mathrm{cm}^{2}$ depending on the specific device structure.

### 2.1.4.3.4 Historical perspective and SESAM structure

Semiconductor saturable absorbers have been used as early as 1974 in $\mathrm{CO}_{2}$ lasers [74Gib] and 1980 for semiconductor diode lasers [80Ipp]. A color-center laser was the first solid-state laser that was cw mode-locked with an intracavity semiconductor saturable absorber [89Isl]. However, for both the diode and color-center laser, dynamic gain saturation supported pulse formation and the recovery time of the slow saturable absorber was not relevant for pulse generation (Fig. 2.1.5a). In addition, because of the large gain cross section (i.e. approximately $10^{-14} \mathrm{~cm}^{2}$ for diode lasers and $10^{-16} \mathrm{~cm}^{2}$ for color-center lasers) $Q$-switching instabilities were not a problem. This is not the case for most other solid-state lasers, such as ion-doped solid-state lasers, which have typically 1000 or even more times smaller gain cross sections. Thus, the semiconductor saturable absorber parameters (Fig. 2.1.8 and Fig. 2.1.9) have to be chosen much more carefully for stable cw mode-locking.

We typically integrate the semiconductor saturable absorber into a mirror structure, which results in a device whose reflectivity increases as the incident optical intensity increases. This general class of devices is called SEmiconductor Saturable Absorber Mirrors (SESAMs) [92Kel2, $96 \mathrm{Kel}, 03 \mathrm{Kel}]$. A detailed description and guideline how to design a SESAM for either passive modelocking or $Q$-switching for different laser parameters is given in recent book chapters [99Kel, 03Pas]. SESAMs are well-established as a useful device for passive mode-locking and $Q$-switching of many kinds of solid-state lasers. The main reason for this device's utility is that both the linear and nonlinear optical properties can be engineered over a wide range, allowing for more freedom in the specific laser cavity design. In addition, semiconductor saturable absorbers are ideally suited for passive mode-locking solid-state lasers because the large absorber cross section (in the range of $10^{-14} \mathrm{~cm}^{2}$ ) and therefore small saturation fluence is ideally suited for suppressing $Q$-switching instabilities [99Hoe1].

Initially, SESAMs for solid-state lasers were used in coupled cavities [90Kel2, 92Kel1], because these early SESAM designs introduced too much loss for the laser cavity (Fig. 2.1.12b). In 1992, this work resulted in a new type of intracavity saturable absorber mirror, the Antiresonant Fabry-Perot Saturable Absorber (A-FPSA) [92Kel2, 94Kel] where the absorber was integrated inside a Fabry-Perot structure of which the bottom reflector was a high reflector (i.e. approximately $100 \%$ ) (Fig. 2.1.12c). This was the first intracavity saturable absorber design that allowed for passive mode-locking of diode-pumped solid-state lasers without $Q$-switching instabilities. The Fabry-Perot was operated at antiresonance to obtain broad bandwidth and low loss. The A-FPSA mirror was mainly based on absorber layers sandwiched between the lower semiconductor and the higher $\mathrm{SiO}_{2} / \mathrm{TiO}_{2}$ dielectric Bragg mirrors. The top reflector of the A-FPSA provides an adjustable parameter that determines the intensity entering the semiconductor saturable absorber and therefore the saturation fluence of the saturable absorber device. Therefore, this design allowed for a large variation of absorber parameters by simply changing absorber thickness and top reflectors [95Bro1, 95Jun1]. This resulted in an even simpler SESAM design with a single quantum well absorber layer integrated into a Bragg mirror [95Bro2] (Fig. 2.1.12d) - this was later referred to as Saturable Bragg Reflectors (SBRs) [95Tsu].

In the 10 -fs regime with Tisapphire lasers we have typically replaced the lower semiconductor Bragg mirror with a metal mirror to support the required large reflection bandwidth [96Flu1, 97Jun1]. No post-growth processing is required with an ultrabroadband monolithically grown fluoride semiconductor saturable absorber mirror that covers nearly the entire gain spectrum of the Ti:sapphire laser. Using this SESAM inside a Ti:sapphire laser resulted in 9.5 -fs pulses [02Sch2]. The reflection bandwidth was achieved with a $\mathrm{AlGaAs} / \mathrm{CaF}_{2}$ semiconductor Bragg mirror [00Sch]. More recently a broadband SESAM was fabricated by increasing the reflection bandwidth


Fig. 2.1.12. Historical evolution of different SESAM designs: (a) Ordinary cw laser. (b) Initially the semiconductor saturable absorber was used inside a nonlinear coupled cavity, termed Resonant Passive Mode-locking (RPM) [90Kel2]. (c) First intracavity saturable absorber to passively mode-lock diodepumped solid-state lasers without $Q$-switching instabilities: Antiresonant Fabry-Perot Saturable Absorber (A-FPSA) [92Kel2]. (d) Scaling of the A-FPSA resulted in a single quantum well saturable absorber integrated into a Bragg mirror [95Bro2] - later also referred to as Saturable Bragg Reflector (SBR) [95Tsu]. (e) General concept of SEmiconductor Saturable Absorber Mirror (SESAM) without any restrictions on the mirror design [95Kel, 96 Kel$]$.
of an AlGaAs/AlAs or InGaAlP/AlAs Bragg mirror using wet oxidation of AlAs which creates low-index $\mathrm{Al}_{x} \mathrm{O}_{y}$ layers [04Tan].

In 1995 [ 95 Kel$]$ it was further realized that the intracavity saturable absorber can be integrated in a more general mirror structure that allows for both saturable absorption and negative dispersion control, which is now generally referred to as a SEmiconductor Saturable Absorber Mirror (SESAM) (Fig. 2.1.12e). In a general sense we then can reduce the design problem of a SESAM to the analysis of multilayered interference filters for a given desired nonlinear reflectivity response for both the amplitude and phase. The A-FPSA [92Kel2], the Saturable Bragg Reflector (SBR) [95Bro2, $95 \mathrm{Tsu}, 95 \mathrm{Kno}$ ] and the Dispersive Saturable Absorber Mirror (D-SAM) [96Kop2] are then special examples of SESAM designs. In this more general class of design we do not restrict ourselves to Bragg mirror structures, which are defined by a stack of quarter-wave layers with alternating high and low refractive indices (e.g. [95Kno]). For example, we have demonstrated with many examples that non-quarter-wave layers in mirrors give more design freedom for integrating the absorber layers into the mirror structure. Furthermore, double-chirped semiconductor mirror structures can provide very broadband negative dispersion [99Pas1].

One important parameter of a SESAM device is its saturation fluence, which has typical values in the range of $10-100 \mu \mathrm{~J} / \mathrm{cm}^{2}$. Lower saturation fluence is particularly relevant for fundamentally mode-locked solid-state lasers with GHz pulse repetition rates and high average power [05Spu3]. Novel design structures allowed to substantially lower the saturation fluence of SESAMs into the $1 \mu \mathrm{~J} / \mathrm{cm}^{2}$ regime [05Spu3]. New terms "LOw-Field-Enhancement Resonant-like SESAM device" (LOFERS) [03Wei1] and "Enhanced SESAM device" (E-SESAM) [03Wei2] were introduced. A LOFERS can be used to further reduce saturation fluence without the detrimental effects of strongly resonant structures such as bistability and narrow bandwidth. Such a design has a low-finesse resonant structure such that the field strength is substantially higher in the spacer layer containing the absorber and therefore reducing the saturation fluence further.

So far the SESAM is mostly used as an end mirror of a standing-wave cavity. Very compact cavity designs have been achieved for example in passively $Q$-switched microchip lasers (Fig. 2.1.6)
and passively mode-locked miniature lasers (Fig. 2.1.7b) where a short laser crystal defines a simple monolithic cavity. The SESAM attached directly to the laser crystal then formed one end-mirror of this laser cavity. As the laser cannot be pumped through the SESAM, the laser output needs to be separated from the collinear pump by a dichroic mirror. These examples suggest that there is need for a device that combines the nonlinear properties of the SESAM with an output coupler. This has been demonstrated before for a passively mode-locked fiber laser [96Sha] and later also for solid-state lasers [01Spu1].

### 2.1.4.4 Effective saturable absorbers using the Kerr effect

### 2.1.4.4.1 Transverse and longitudinal Kerr effect

The extremely rapid response and the broad bandwidth of the Kerr nonlinearity are very attractive for a mode-locking process. For high intensities, the polarization inside a dielectric medium does not proportionally follow the electric field anymore. This gives rise to an index change proportional to intensity. Off-resonance, this nonlinear optical effect is extremely fast, with estimated response times in the few-femtosecond range. The transverse and longitudinal effects resulting from the intensity dependence are shown schematically in Fig. 2.1.13. The transverse Kerr effect retards the central and most intense part of a plane wave front and thus acts as a focusing lens, referred to as the Kerr lens. Along the axis of propagation, the longitudinal Kerr effect retards the center of an optical pulse, producing a red shift of the leading part of the pulse, and a blue shift in the trailing part. Consequently, the longitudinal Kerr effect has been named Self-Phase Modulation (SPM).

Longitudinal Kerr effect: self - phase modulation (SPM)


Fig. 2.1.13. The Kerr effect gives rise to an increase of the refractive index with intensity, causing a retardation of the most intense parts of a pulse (i.e. for $n_{2}>0$ ). In its longitudinal form, the Kerr effect causes Self-Phase Modulation (SPM) and in its transverse form, a nonlinear lens is formed in the central part of the beam profiles (i.e. Kerr lens).

### 2.1.4.4.2 Nonlinear coupled cavity

The longitudinal Kerr effect can also be used to produce the same effect as a fast saturable absorber. To do this, the phase nonlinearity provided by the longitudinal Kerr effect has to be converted into an effective amplitude nonlinearity. The earliest mode-locking schemes based only on SPM used a coupled cavity to convert SPM into SAM. In the soliton laser [84Mol], pulses compressed by SPM and anomalous dispersion in the coupled cavity are directly coupled back into the main laser cavity. This provides more gain for the center of the pulse. Pulses as short as 19 fs have been
demonstrated with color-center lasers [87Mit]. Later, the SPM-to-SAM conversion with a coupled cavity was demonstrated even when the pulses inside the coupled cavity were broadened due to positive group velocity dispersion [89Kea]. In this case, no compressed pulse was fed back into the main cavity. An effective SAM was obtained because SPM inside the coupled cavity generates a phase modulation on the pulse that adds constructively at the peak of the pulse in the main cavity and destructively in the wings, thus shortening the pulse duration inside the main cavity. This was also later referred to as Additive Pulse Mode-locking (APM) [89Ipp]. Although very powerful in principle, these coupled-cavity schemes have the severe disadvantage that the auxiliary cavity has to be stabilized interferometrically. An alternative method for converting the reactive Kerr nonlinearity into an effective saturable absorber was discovered in 1991: Kerr-Lens Mode-locking (KLM) [91Spe].

### 2.1.4.4.3 Kerr lens

The discovery of Kerr-lens mode-locking has been a breakthrough in ultrashort pulse generation [91Spe]. Initially the mode-locking mechanism was not understood and was somewhat of a mystery. But within a short time after the initial discovery it became clear that the transverse Kerr effect provides a fast saturable absorber. In KLM, the transverse Kerr effect produces a Kerr lens (Fig. 2.1.13) that focuses the high-intensity part of the beam more strongly than the low-intensity part. Thus, combined with an intracavity aperture the Kerr lens produces less loss for high intensity and forms an effective fast saturable absorber [91Kel, 91Sal1, 91Neg] (Fig. 2.1.14). A similar modelocking effect can be obtained without a hard aperture when the Kerr lens produces an increased


Fig. 2.1.14. Kerr-Lens Mode-locking (KLM) is obtained due to the Kerr lens at an intracavity focus in the gain medium or in another material, where the refractive index is increased with increased intensity $\Delta n=n_{2} I(r, t)$, where $n_{2}$ is the nonlinear refractive index and $I(r, t)$ the radial- and time-dependent intensity of a short-pulsed laser beam. In combination with a hard aperture inside the cavity, the cavity design is made such that the Kerr lens reduces the laser mode area for high intensities at the aperture and therefore forms an effective fast saturable absorber. In most cases, however, soft-aperture KLM is used where the reduced mode area in the gain medium improves for a short time the overlap with the (strongly focused) pump beam and therefore the effective gain. A significant change in mode size is only achieved by operating the laser cavity near one of the stability limits of the cavity.
overlap of the laser mode with the pump profile in the gain medium [93Pic]. The Kerr lens provides the strongest advantage for the pulsed operation when the cavity is operated close to the stability limit. Optimization guidelines for SAM produced by the Kerr lens in different cavities can be found in [95Mag]. Unfortunately, the transverse Kerr effect couples the mode-locking process with the laser cavity mode. In contrast, the use of only the longitudinal Kerr effect in mode-locking totally decouples the mode-locking process from the laser mode. This allows optimum cavity design for scaling the laser to higher powers and to higher pulse repetition rates without being constrained by the Kerr lens.

### 2.1.4.4.4 Nonlinear polarization rotation

In fiber lasers a different Kerr-effect-based effective saturable absorber has been used to generate pulses as short as 38 fs [ 92 Hof ] - the shortest pulses generated directly from a fiber laser so far. An effective fast saturable absorber is obtained with a Kerr-induced nonlinear polarization rotation in a weakly birefringent fiber combined with a polarization-dependent loss. Previously, a similar idea has been used to "clean up" high-intensity pulses by reducing the low-intensity pulse pedestals [92Tap, 92Bea].

### 2.1.4.5 Nonlinear mirror based on second-harmonic generation

The second-order nonlinear susceptibility $\chi^{(2)}$ nonlinearities can also be used to construct effective saturable absorbers [88Sta]. A nonlinear mirror based on this principle consists of a frequencydoubling crystal and a dichroic mirror. For short pulses, a part of the incident laser light is converted to the second harmonic, for which the mirror is highly reflective, and converted back to the fundamental wave, if an appropriate relative phase shift for fundamental and second-harmonic light is applied. On the other hand, unconverted fundamental light experiences a significant loss at the mirror. Thus the device has a higher reflectivity at higher intensities. This has been used for mode-locking e.g. with up to 1.35 W of average output power in 7.9 -ps pulses from a $\mathrm{Nd}^{3+}: \mathrm{YVO}_{4}$ laser [ 97 Agn ]. The achievable pulse duration is often limited by group-velocity mismatch between fundamental and second-harmonic light.

### 2.1.5 Pulse propagation in dispersive media

### 2.1.5.1 Dispersive pulse broadening

Dispersion compensation is important in ultrashort pulse generation. When a pulse travels through a medium, it acquires a frequency-dependent phase shift $\phi(\omega)=k n(\omega) L$, where $k$ is the wave number, $n(\omega)$ the refractive index and $L$ the medium length. A phase shift which varies linearly with the frequency corresponds to a time delay, without any change of the temporal shape of the pulse. Higher-order phase shifts, however, tend to modify the pulse shape and are thus of relevance for the formation of short pulses.

The phase shift can be expanded in a Taylor series around the center angular frequency $\omega_{0}$ of the pulse:

$$
\phi(\omega)=\phi_{0}+\frac{\partial \phi}{\partial \omega}\left(\omega-\omega_{0}\right)+\frac{1}{2} \frac{\partial^{2} \phi}{\partial \omega^{2}}\left(\omega-\omega_{0}\right)^{2}+\frac{1}{6} \frac{\partial^{3} \phi}{\partial \omega^{3}}\left(\omega-\omega_{0}\right)^{3}+\ldots
$$

Table 2.1.6. Sellmeier equations for different materials. The wavelength $\lambda$ is given in units of $\mu \mathrm{m}$.

| Material | Defining Sellmeier equation | Constants |
| :---: | :---: | :---: |
| Fused quartz | $n^{2}=1+\frac{A \lambda^{2}}{\lambda^{2}-\lambda_{1}^{2}}+\frac{B \lambda^{2}}{\lambda^{2}-\lambda_{2}^{2}}+\frac{C \lambda^{2}}{\lambda^{2}-\lambda_{3}^{2}}$ | $\begin{aligned} & A=0.6961663 \\ & \lambda_{1}=0.0684043 \\ & B=0.4079426 \\ & \lambda_{2}=0.1162414 \\ & C=0.8974794 \\ & \lambda_{3}=9.896161 \end{aligned}$ |
| SF10 glass | $n^{2}=a_{0}+a_{1} \lambda^{2}+\frac{a_{2}}{\lambda^{2}}+\frac{a_{3}}{\lambda^{4}}+\frac{a_{4}}{\lambda^{6}}+\frac{a_{5}}{\lambda^{8}}$ | $\begin{aligned} & a_{0}=2.8784725 \\ & a_{1}=-0.010565453 \\ & a_{2}=3.327942 \times 10^{-2} \\ & a_{3}=2.0551378 \times 10^{-3} \\ & a_{4}=-1.1396226 \times 10^{-4} \\ & a_{5}=1.6340021 \times 10^{-5} \end{aligned}$ |
| Sapphire | $n^{2}=1+\frac{a_{1} \lambda^{2}}{\lambda^{2}-b_{1}}+\frac{a_{2} \lambda^{2}}{\lambda^{2}-b_{2}}+\frac{a_{3} \lambda^{2}}{\lambda^{2}-b_{3}}$ | $\begin{aligned} & a_{1}=1.023798 \\ & a_{2}=1.058264 \\ & a_{3}=5.280792 \\ & b_{1}=0.00377588 \\ & b_{2}=0.0122544 \\ & b_{3}=321.3616 \end{aligned}$ |

Here, the derivatives are evaluated at $\omega_{0} . \partial \phi / \partial \omega$ is the group delay $T_{\mathrm{g}}, \partial^{2} \phi / \partial \omega^{2}$ the Group Delay Dispersion (GDD), $\partial^{3} \phi / \partial \omega^{3}$ the Third-Order Dispersion (TOD). The GDD describes a linear frequency dependence of the group delay and thus tends to separate the frequency components of a pulse: For positive GDD, e.g., the components with higher frequencies are delayed with respect to those with lower frequencies, which results in a positive "chirp" ("up-chirp") of the pulse. Higher orders of dispersion generate more complicated distortions. Material dispersion is normally described with Sellmeier equations for the refractive index as a function of the wavelength, i.e. $n(\lambda)$. With the Sellmeier equations (Table 2.1.6) all the necessary dispersive quantities can be calculated (Table 2.1.7). An example is given in Table 2.1.8.

The broader the bandwidth of the pulse (i.e., the shorter the pulse duration), the more terms of this expansion are significant. GDD which acts on an initially unchirped Gaussian pulse with Full-Width-at-Half-Maximum (FWHM) pulse duration $\tau_{0}$, increases the pulse duration according to [86Sie]

$$
\begin{equation*}
\frac{\tau_{\mathrm{p}}(z)}{\tau_{0}}=\sqrt{1+\left(\frac{4 \ln 2 \mathrm{~d}^{2} \phi / \mathrm{d} \omega^{2}}{\tau_{0}^{2}}\right)^{2}} \tag{2.1.20}
\end{equation*}
$$

where it is assumed that the incident pulse is transform-limited, i.e. the time-bandwidth product of the Gaussian pulse is $\tau_{0} \Delta \nu_{\mathrm{p}}=0.4413$, where $\Delta \nu_{\mathrm{p}}$ is the Full-Width-at-Half-Maximum (FWHM) spectral width of the pulse intensity (Fig. 2.1.15). Only second-order dispersion (i.e. $\partial^{2} \phi / \partial \omega^{2}$ ) and higher orders are broadening the pulse. The first-order dispersion gives the group delay, i.e. the delay of the peak of the pulse envelope. It is apparent that the effect of GDD becomes strong if GDD $>\tau_{0}^{2}$. Similarly, TOD becomes important if TOD $>\tau_{0}^{3}$. It is important to note that for dispersive pulse broadening (which is in the linear pulse propagation regime) the spectrum of the pulse remains unchanged, only the spectral content of the pulse is redistributed in time. With positive dispersion the long-wavelength part of the spectrum is in the leading edge of the pulse and the short-wavelength part in the trailing edge of the pulse, i.e. "red is faster than blue" (Fig. 2.1.15). In the regime of strong pulse broadening, i.e. $\mathrm{d}^{2} \phi / \mathrm{d} \omega^{2} \gg \tau_{0}^{2}$, we can reduce (2.1.20)

Table 2.1.7. Dispersion quantities, their defining equations and units. $k_{n}$ : wave vector in the dispersive media, i.e. $k_{n}=k n=n 2 \pi / \lambda$, where $\lambda$ is the vacuum wavelength. $z$ : a certain propagation distance. $c$ : vacuum light velocity. $\omega$ : frequency in radians/second.

| Quantity | Symbol | Defining equation | Defining equation using $n(\lambda)$ |
| :--- | :--- | :--- | :--- |
| Phase velocity | $v_{\mathrm{p}}$ | $\frac{\omega}{k_{n}}$ | $\frac{c}{n}$ |
| Group velocity | $v_{\mathrm{g}}$ | $\frac{\mathrm{d} \omega}{\mathrm{d} k_{n}}$ | $\frac{c}{n} \frac{1}{1-\frac{\mathrm{d} n}{\mathrm{~d} \lambda} \frac{\lambda}{n}}$ |
| Group delay | $T_{\mathrm{g}}$ | $T_{\mathrm{g}}=\frac{z}{v_{\mathrm{g}}}=\frac{\mathrm{d} \phi}{\mathrm{d} \omega}, \quad \phi \equiv k_{n} z$ | $\frac{n z}{c}\left(1-\frac{\mathrm{d} n}{\mathrm{~d} \lambda} \frac{\lambda}{n}\right)$ |
| Dispersion: 1st order | $\frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}}$ | $\frac{n z}{c}\left(1-\frac{\mathrm{d} n}{\mathrm{~d} \lambda} \frac{\lambda}{n}\right)$ |  |
| Dispersion: 2nd order | $\frac{\mathrm{d}^{3} \phi}{\mathrm{~d} \omega^{3}}$ | $\frac{\lambda^{3} z}{2 \pi c^{2}} \frac{\mathrm{~d}^{2} n}{\mathrm{~d} \lambda^{2}}$ |  |
| Dispersion: 3 rd order |  | $\frac{-\lambda^{4} z}{4 \pi^{2} c^{3}}\left(3 \frac{\mathrm{~d}^{2} n}{\mathrm{~d} \lambda^{2}}+\lambda \frac{\mathrm{d}^{3} n}{\mathrm{~d} \lambda^{3}}\right)$ |  |



Fig. 2.1.15. Dispersive pulse broadening through a material with positive dispersion.
to

$$
\begin{equation*}
\tau_{\mathrm{p}}(z) \approx \frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}} \Delta \omega_{\mathrm{p}} \tag{2.1.21}
\end{equation*}
$$

where $\Delta \omega_{\mathrm{p}}=2 \pi \Delta \nu_{\mathrm{p}}$ is the FWHM spectral width (in radians/second) of the pulse intensity.

### 2.1.5.2 Dispersion compensation

Without any dispersion compensation the net GDD for one cavity round trip is usually positive, mainly because of the dispersion in the gain medium. Other components like mirrors may also contribute to this. However, in lasers with $>10$ ps pulse duration the dispersion effects can often be ignored, as the total GDD in the laser cavity is typically at most a few thousand $\mathrm{fs}^{2}$, much less than the pulse duration squared (2.1.20). For shorter pulse durations, the GDD has to be considered, and pulse durations well below 30 fs usually require the compensation of Third-Order Dispersion (TOD) or even higher orders of dispersion depending on the thickness of the gain material. In most cases, the desired total GDD is not zero but negative, so that soliton formation

Table 2.1.8. Examples of material dispersions calculated from the Sellmeier equations given in Table 2.1.6 and the equations given in Table 2.1.7.

| Material | Refractive index $n$ <br> at a center wavelength of 800 nm | Propagation constant $k_{n}$ <br> at a center wavelength of 800 nm |
| :--- | :--- | :--- |

Fused quartz $\quad n(0.8 \mu \mathrm{~m})=1.45332$

$$
\begin{aligned}
\left.\frac{\partial n}{\partial \lambda}\right|_{800 \mathrm{~nm}} & =-0.017 \frac{1}{\mu \mathrm{~m}} \\
\left.\frac{\partial^{2} n}{\partial \lambda^{2}}\right|_{800 \mathrm{~nm}} & =0.04 \frac{1}{\mu \mathrm{~m}^{2}} \\
\left.\frac{\partial^{3} n}{\partial \lambda^{3}}\right|_{800 \mathrm{~nm}} & =-0.24 \frac{1}{\mu \mathrm{~m}^{3}}
\end{aligned}
$$

$$
\begin{aligned}
\left.\frac{\partial k_{n}}{\partial \omega}\right|_{800 \mathrm{~nm}} & =4.84 \times 10^{-9} \frac{\mathrm{~s}}{\mathrm{~m}}=4.84 \frac{\mathrm{~ns}}{\mathrm{~m}} \\
\left.\frac{\partial^{2} k_{n}}{\partial \omega^{2}}\right|_{800 \mathrm{~nm}} & =3.61 \times 10^{-26} \frac{\mathrm{~s}^{2}}{\mathrm{~m}}=36.1 \frac{\mathrm{fs}^{2}}{\mathrm{~mm}} \\
\left.\frac{\partial^{3} k_{n}}{\partial \omega^{3}}\right|_{800 \mathrm{~nm}} & =2.74 \times 10^{-41} \frac{\mathrm{~s}^{3}}{\mathrm{~m}}=27.4 \frac{\mathrm{fs}^{3}}{\mathrm{~mm}}
\end{aligned}
$$

SF10 glass $\quad n(0.8 \mu \mathrm{~m})=1.71125$

$$
\begin{aligned}
\left.\frac{\partial n}{\partial \lambda}\right|_{800 \mathrm{~nm}} & =-0.0496 \frac{1}{\mu \mathrm{~m}} \\
\left.\frac{\partial^{2} n}{\partial \lambda^{2}}\right|_{800 \mathrm{~nm}} & =0.176 \frac{1}{\mu \mathrm{~m}^{2}} \\
\left.\frac{\partial^{3} n}{\partial \lambda^{3}}\right|_{800 \mathrm{~nm}} & =-0.997 \frac{1}{\mu \mathrm{~m}^{3}}
\end{aligned}
$$

$$
\begin{aligned}
\left.\frac{\partial k_{n}}{\partial \omega}\right|_{800 \mathrm{~nm}} & =5.70 \times 10^{-9} \frac{\mathrm{~s}}{\mathrm{~m}}=5.70 \frac{\mathrm{~ns}}{\mathrm{~m}} \\
\left.\frac{\partial^{2} k_{n}}{\partial \omega^{2}}\right|_{800 \mathrm{~nm}} & =1.59 \times 10^{-25} \frac{\mathrm{~s}^{2}}{\mathrm{~m}}=159 \frac{\mathrm{fs}^{2}}{\mathrm{~mm}} \\
\left.\frac{\partial^{3} k_{n}}{\partial \omega^{3}}\right|_{800 \mathrm{~nm}} & =1.04 \times 10^{-40} \frac{\mathrm{~s}^{3}}{\mathrm{~m}}=104 \frac{\mathrm{fs}^{3}}{\mathrm{~mm}}
\end{aligned}
$$

Sapphire

$$
\begin{aligned}
n(0.8 \mu \mathrm{~m}) & =1.76019 \\
\left.\frac{\partial n}{\partial \lambda}\right|_{800 \mathrm{~nm}} & =-0.0268 \frac{1}{\mu \mathrm{~m}} \\
\left.\frac{\partial^{2} n}{\partial \lambda^{2}}\right|_{800 \mathrm{~nm}} & =0.064 \frac{1}{\mu \mathrm{~m}^{2}} \\
\left.\frac{\partial^{3} n}{\partial \lambda^{3}}\right|_{800 \mathrm{~nm}} & =-0.377 \frac{1}{\mu \mathrm{~m}^{3}}
\end{aligned}
$$

$$
\begin{aligned}
\left.\frac{\partial k_{n}}{\partial \omega}\right|_{800 \mathrm{~nm}} & =5.87 \times 10^{-9} \frac{\mathrm{~s}}{\mathrm{~m}}=5.87 \frac{\mathrm{~ns}}{\mathrm{~m}} \\
\left.\frac{\partial^{2} k_{n}}{\partial \omega^{2}}\right|_{800 \mathrm{~nm}} & =5.80 \times 10^{-26} \frac{\mathrm{~s}^{2}}{\mathrm{~m}}=58 \frac{\mathrm{fs}^{2}}{\mathrm{~mm}} \\
\left.\frac{\partial^{3} k_{n}}{\partial \omega^{3}}\right|_{800 \mathrm{~nm}} & =4.21 \times 10^{-41} \frac{\mathrm{~s}^{3}}{\mathrm{~m}}=42.1 \frac{\mathrm{fs}^{3}}{\mathrm{~mm}}
\end{aligned}
$$

can be exploited. Usually, one requires sources of negative GDD, and in addition appropriate higherorder dispersion for shorter pulses. The most important techniques for dispersion compensation are discussed in the following subsections. Different optical elements that introduce wavelengthdependent refraction (i.e. prism pairs, Sect. 2.1.5.2.3) or wavelength-dependent diffraction (i.e. grating pairs, Sect. 2.1.5.2.2) can be used to introduce an additional wavelength dependence to the round-trip phase and thus contribute to the overall dispersion. A wavelength-dependent round-trip phase can also be introduced with GTIs (Sect. 2.1.5.2.1) and chirped mirrors (Sect. 2.1.5.2.4).

The challenge in ultrashort pulse generation is dispersion compensation over a large bandwidth to compensate for the dispersive pulse broadening that is occurring in the gain material and other elements inside the laser cavity. Dispersion compensation is important because for example, a 10 -fs (1-fs) Gaussian pulse at the center wavelength of 800 nm is broadened to $100 \mathrm{fs}(1 \mathrm{ps})$ after only 1 cm of fused quartz due to second-order dispersion. This follows from (2.1.21) for the regime of strong pulse broadening and Tables 2.1.6-2.1.8. In addition, in femtosecond lasers the pulses are ideally soliton pulses for which a constant negative dispersion over the full spectral width of the pulse balances the chirp of the self-phase modulation. The necessary negative dispersion required for a certain pulse duration follows from (2.1.74). It is required that all higher-order dispersion terms are negligibly small.

For optimum soliton formation of a sub-10-fs pulse inside the laser, only a very small amount of a constant negative total intracavity dispersion is necessary to form a stable soliton pulse (2.1.74). For example, we estimated the necessary dispersion to be only $-10 \mathrm{fs}^{2}$ for a Ti:sapphire laser producing 6.5 -fs pulses [97Jun3, 98Sut]. Here we assumed an estimated self-phase modulation coefficient of about $0.07 / \mathrm{MW}$, an average output power of 200 mW using a $3 \%$ output coupler and a pulse repetition rate of 86 MHz . This results in an intracavity pulse energy of 77.5 nJ . With (2.1.74) then follows an estimated negative group delay dispersion of $-10 \mathrm{fs}^{2}$ in a cavity round trip.

There are different methods for dispersion compensation, such as the Gires-Tournois Interferometer (GTI), grating pairs, prism pairs and chirped mirrors. The dispersion compensation is summarized in Table 2.1.9 with the symbols defined in Fig. 2.1.16.

### 2.1.5.2.1 Gires-Tournois interferometer (GTI)

A Gires-Tournois Interferometer (GTI) [64Gir, 92Kaf] is a very compact dispersion-compensation element, which basically replaces one flat laser cavity mirror. The negative dispersion is obtained due to the Fabry-Perot interferometer, operated in reflection (Fig. 2.1.16a). Normally, in a GTI the rear mirror is highly reflective over the whole wavelength range (i.e. ideally $100 \%$ ) whereas the front mirror has a relatively low reflectivity, typically a few percent. The spacer layer in the Fabry-Perot should contain a non-absorbing material and is very often air, such that the thickness can be easily changed. The phase shift varies nonlinearly by $2 \pi$ for each free spectral range, calculated as $\Delta \nu=c / 2 n d$, where $n$ and $d$ are the refractive index and the thickness of the spacer material, respectively. Within each free spectral range, the GDD oscillates between two extremes the magnitude of which is proportional to $d^{2}$ and also depends on the front-mirror reflectivity. Ideally, the GTI is operated near a minimum of the GDD, and the usable bandwidth is some fraction (e.g. one tenth) of the free spectral range, which is proportional to $d^{-1}$ :

$$
\begin{equation*}
\frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}} \propto d^{2}, \quad\left\{\text { Bandwidth of } \frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}}\right\} \propto \frac{1}{d} \tag{2.1.22}
\end{equation*}
$$

In Table 2.1.9 the material dispersion in the GTI spacer layer was neglected. The bandwidth compared to the other techniques is limited, thus a GTI is typically used for pulse durations above 100 fs. There is a trade-off: A broader bandwidth is obtained with a smaller Fabry-Perot thickness but then the amount of negative dispersion is strongly reduced. For example, an air-spaced GTI with $80 \mu \mathrm{~m}$ thickness and a top reflectivity of $4 \%$ produces a negative dispersion of about $-0.13 \mathrm{ps}^{2}$ at a wavelength of 799 nm . In comparison a $2.25 \mu \mathrm{~m}$ thick air space results in about $-100 \mathrm{fs}^{2}$ at a wavelength of 870 nm .

Tunable GDD can be achieved if the spacer material is a variable air gap, which however must be carefully stabilized to avoid unwanted drifts. More stable but not tunable GDD can be generated with monolithic designs, based e.g. on thin films of dielectric media like $\mathrm{TiO}_{2}$ and $\mathrm{SiO}_{2}$, particularly for the use in femtosecond lasers. The main drawbacks of GTI are the fundamentally limited bandwidth (for a given amount of GDD) and the limited amount of control of higher-order dispersion.

### 2.1.5.2.2 Grating pairs

Grating pairs [69Tre] produce negative dispersion due to the wavelength-dependent diffraction (Fig. 2.1.16b). To obtain a spatially coherent beam two paths through the grating pair are required. Compared to prism pairs (Sect. 2.1.5.2.3), pairs of diffraction gratings can generate higher dispersion in a compact setup. However, because of the limited diffraction efficiency of gratings, the losses of a grating pair are typically higher than acceptable for use in a laser cavity, except in

Table 2.1.9. Dispersion compensation, its defining equations and figures. $c$ : light velocity in vacuum, $\lambda$ : wavelength in vacuum, $\lambda_{0}$ : center wavelength of pulse spectrum, $\omega$ : frequency in radians/second.

| Quantity | Defining equation |
| :--- | :--- |
| Gires-Tournois | $d$ : thickness of Fabry-Perot |
| Interferometer (GTI) | $n$ : refractive index of material inside Fabry-Perot (airspaced $n=1$ ) |
| (Fig. 2.1.16a) | $t_{0}=\frac{2 n d}{c}:$ round-trip time of the Fabry-Perot |
|  | $R_{\mathrm{t}}$ : intensity reflectivity of top reflector of Fabry-Perot dispersion is neglected.) <br> $($ Bottom reflector is assumed to have a 100\%-reflectivity.) |
|  | $\frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}}=\frac{-2 t_{0}^{2}\left(1-R_{\mathrm{t}}\right) \sqrt{R_{\mathrm{t}}} \sin \omega t_{0}}{\left(1+R_{\mathrm{t}}-2 \sqrt{R_{\mathrm{t}}} \cos \omega t_{0}\right)^{2}}$ |

## Four-grating compressor $\quad L_{\mathrm{g}}$ : grating pair spacing

(Fig. 2.1.16b)

Dispersion: 2nd order
A: grating period
$\theta_{\mathrm{i}}$ : angle of incidence at grating
$\frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}}=-\frac{\lambda^{3} L_{\mathrm{g}}}{\pi c^{2} \Lambda^{2}}\left[1-\left(\frac{\lambda}{\Lambda}-\sin \theta_{\mathrm{i}}\right)^{2}\right]^{-3 / 2}$

Dispersion: 3rd order

$$
\frac{\mathrm{d}^{3} \phi}{\mathrm{~d} \omega^{3}}=-\frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}} \frac{6 \pi \lambda}{c} \frac{1+\frac{\lambda}{\Lambda} \sin \theta_{\mathrm{i}}-\sin ^{2} \theta_{\mathrm{i}}}{1-\left(\frac{\lambda}{\Lambda}-\sin \theta_{\mathrm{i}}\right)^{2}}
$$

## Four-prism compressor

(Fig. 2.1.16c)

Dispersion: 2nd order

Dispersion: 3rd order
$n$ : refractive index of prisms
$\theta_{\mathrm{B}}$ : angle of incidence of prism is at Brewster angle
$\theta_{\mathrm{B}}=\arctan \left[n\left(\lambda_{0}\right)\right]$
$\alpha=\pi-2 \theta_{\mathrm{B}}$ : apex angle of prism
$\theta_{2}(\lambda)=\arcsin \left[n(\lambda) \sin \left(\pi-2 \theta_{\mathrm{B}}-\arcsin \frac{\sin \theta_{\mathrm{B}}}{n(\lambda)}\right)\right]$
$L$ : apex-to-apex prism distance
$h$ : beam insertion into second prism
$\sin \beta=\frac{h}{L} \frac{\cos \theta_{2}}{\cos (\alpha / 2)}$

$$
\frac{\mathrm{d}^{2} \phi}{\mathrm{~d} \omega^{2}}=\frac{\lambda^{3}}{2 \pi c^{2}} \frac{\mathrm{~d}^{2} P}{\mathrm{~d} \lambda^{2}}
$$

$$
\begin{aligned}
\frac{\mathrm{d}^{2} P}{\mathrm{~d} \lambda^{2}} & =2\left[\frac{\partial^{2} n}{\partial \lambda^{2}}\left(\frac{\partial \theta_{2}}{\partial n}\right)+\left(\frac{\partial^{2} \theta_{2}}{\partial n^{2}}\right)\left(\frac{\partial n}{\partial \lambda}\right)^{2}\right] L \sin \beta-2\left(\frac{\partial \theta_{2}}{\partial n} \frac{\partial n}{\partial \lambda}\right)^{2} L \cos \beta \\
& \approx 4\left[\frac{\partial^{2} n}{\partial \lambda^{2}}+\left(2 n-\frac{1}{n^{3}}\right)\left(\frac{\partial n}{\partial \lambda}\right)^{2}\right] L \sin \beta-8\left(\frac{\partial n}{\partial \lambda}\right)^{2} L \cos \beta
\end{aligned}
$$

$\frac{\mathrm{d}^{3} \phi}{\mathrm{~d} \omega^{3}}=\frac{-\lambda^{4}}{4 \pi^{2} c^{3}}\left(3 \frac{\mathrm{~d}^{2} P}{\mathrm{~d} \lambda^{2}}+\lambda \frac{\mathrm{d}^{3} P}{\mathrm{~d} \lambda^{3}}\right)$
$\frac{\mathrm{d}^{3} P}{\mathrm{~d} \lambda^{3}} \approx 4 \frac{\mathrm{~d}^{3} n}{\mathrm{~d} \lambda^{3}} L \sin \beta-24 \frac{\mathrm{~d} n}{\mathrm{~d} \lambda} \frac{\mathrm{~d}^{2} n}{\mathrm{~d} \lambda^{2}} L \cos \beta$


Fig. 2.1.16. Dispersion compensation techniques: (a) Gires-Tournois Interferometer (GTI), (b) grating pair, (c) prism pair, (d) chirped mirror (i.e. shown here: a double-chirped mirror).
cases with a high gain (e.g., in fiber lasers). For this reason, grating pairs are normally only used for external pulse compression [84Tom]. The grating pairs alone can only be used to compensate for second-order dispersion. Higher-order dispersion limits pulse compression in the ultrashort pulse width regime. Therefore, a combination of a grating and prism compressor was used to generate the long-standing world record of 6 -fs pulses with dye lasers [87For].

There are mainly two types of gratings: ruled or holographic. Removing material from a master substrate with a precise instrument called a ruling engine produces ruled gratings. Replicas of the ruled grating are then pressed and the pressings are coated. Holographic gratings are produced by interfering two laser beams on a substrate coated with a photoresist, which is subsequently processed to reproduce the sinusoidal interference pattern. Generally, replicas cannot be produced from holographic masters, i.e. they are more expensive. Higher damage threshold can be obtained with gold-coated ruled gratings (i.e. $>500 \mathrm{~mJ} / \mathrm{cm}^{2}$ at 1 ps ). The diffraction efficiency in this case is around $88 \%$ to $92 \%$ depending on the grating. Because four paths through the gratings are required for dispersion compensation and a spatially coherent beam, this amounts to at least about $30 \%$ loss.

### 2.1.5.2.3 Prism pairs

Prism pairs [84For] are well established for intracavity dispersion compensation. Negative dispersion is obtained with the wavelength-dependent refraction (Fig. 2.1.16c): The different wavelength components travel in different directions after the first prism and along parallel but separated paths after the second prism. The wavelength components can be recombined simply on the way back after reflection at a plane end mirror (of a standing-wave cavity) or by a second prism pair (in a ring cavity). Spatial separation of different wavelengths occurs only in a part of the cavity. The obtained negative GDD from the geometric effect is proportional to the prism separation, and an additional (usually positive) GDD contribution results from the propagation in the prism material. Thus, to obtain a spatially coherent beam two paths through the prism pair are required. The insertion loss is very small because the angle of incidence is at Brewster angle. The prism apex angle is chosen such that the incident beam at Brewster angle is also at the minimum deviation. Prism pairs offer two advantages. First, the pulse width can be varied by simply moving one of the prisms which adjusts the prism insertion and therefore the amount of positive GDD from the propagation in the prism material (see Fig. 2.1.16c). Second, the laser can be tuned in wavelength by simply moving a knife edge at a position where the beam is spectrally broadened. Both properties are often desired for spectroscopic applications, for example. However, the prism pair suffers from higher-order dispersion, which is the main limitation in ultrashort pulse generation in the sub-10-fs regime. Different prism materials introduce different amounts of higher-order dispersion. For compact lasers with pulse durations of few tens to hundreds of femtoseconds the more dispersive SF10-prisms are better because they require a smaller prism separation than fused quartz prism for example. But the smaller prism separation comes at the expense of a larger higher-order dispersion. Fused quartz is one of the best materials for ultrashort pulse generation with minimal higher-order dispersion. The higher-order dispersion of the prism pairs is dominated by the prism spacing, which is not changed significantly when we adjust the dispersion by inserting the prisms into the laser beam.

More compact geometries for dispersion compensation make use of a single prism only [94Ram, $96 \mathrm{Kop} 1]$. In this case, the wavelength components are spatially separated in the whole resonator, not only in a part of it. Even without any additional prisms, refraction at a Brewster interface of the gain medium can generate negative dispersion. In certain configurations, where the cavity is operated near a stability limit, the refraction effect can be strongly increased [99Pas2], so that significant negative GDD can be generated in a compact cavity. The amount of GDD may then also strongly depend on the thermal lens in the gain medium and on certain cavity dimensions.

For example, at a fused quartz prism spacing of 40 cm , the total dispersion that is produced by a double pass through the prism pairs amounts to $-862 \mathrm{fs}^{2}$ and a third-order dispersion of $-970 \mathrm{fs}^{3}$ at a center wavelength of 800 nm , assuming zero prism insertion into the beam (Table 2.1.9). We can reduce the negative dispersion by moving the prisms into the laser beam: Each additional millimeter of prism insertion produces a positive dispersion of $101 \mathrm{fs}^{2}$ but only a third-order dispersion of $78 \mathrm{fs}^{3}$ per cavity round trip. Thus, the prism pairs can generally only be used to compensate for either second- or third-order dispersion. With fused quartz prisms alone pulses as short as 10 fs can be produced with a Ti:sapphire laser [93Asa, 96Flu1]. Slightly shorter pulses can be achieved if the Ti:sapphire laser is operated at a center wavelength of approximately 850 nm , where nearzero second- and third-order dispersion can be obtained for a Ti:sapphire crystal of about 2 mm thickness. In this case 8.5 fs have been generated [94Zho]. Another dispersion compensation is then required for shorter pulse generation. Therefore, the chirped mirrors were designed to show the inverse higher-order group delay dispersion of the dispersion of the prism pair plus laser crystal to eliminate the higher-order dispersion and obtain a slightly negative but constant group delay dispersion required for an ideal soliton pulse.

### 2.1.5.2.4 Chirped mirrors

Dielectric Bragg mirrors with regular quarter-wave layer stacks have a fairly small dispersion when operated well within their reflection bandwidth, but increasing dispersion at the edges of this range. Modified designs can be used to obtain well-controlled dispersion over a large wavelength range. One possibility already discussed is the use of a GTI structure (see Sect. 2.1.5.2.1). Another broad range of designs is based on the concept of the chirped mirrors [94Szi] (Fig. 2.1.16d): If the Bragg wavelength is appropriately varied within a Bragg mirror design, longer wavelengths can be reflected deeper in the mirror structure, thus acquire a larger phase change, which leads to negative dispersion. However, the straight-forward implementation of this idea leads to strong oscillations of the GDD (as a function of frequency) which render such simple designs useless. These oscillations can be greatly reduced by numerical optimizations which introduce complicated (and not analytically explainable) deviations from the simple chirp law. A great difficulty is that the figure of merit to optimize is a complicated function of many layer thickness variables, which typically has a large number of local maxima and minima and thus is quite difficult to optimize. Nevertheless, refined computing algorithms have lead to designs with respectable performance, which were realized with precision growth of dielectric mirrors. Such mirrors can compensate the dispersion in $\mathrm{Ti}^{3+}$ :sapphire lasers for operation with pulse durations well below 10 fs. Figure 2.1.16d shows a typical chirped mirror structure which schematically shows the path of a long-wavelength (i.e. 1000 nm ) and short-wavelength (i.e. 650 nm ) beam. This results in negative dispersion, because the long wavelengths are made to penetrate deeper into the mirror structure than short wavelengths. Figure 2.1.16d also shows the standing-wave electric field patterns in a chirped mirror structure versus wavelength. The negative dispersion of the mirrors is clearly illustrated by the dependence of penetration depth on wavelength for the range of 650 to 1050 nm . The highly transmissive region around 500 nm is used for pumping the Ti:sapphire laser through these chirped mirrors. According to [94Szi], chirping means that the Bragg wavelength $\lambda_{\mathrm{B}}$ is gradually increased along the mirror, producing a negative Group Delay Dispersion (GDD). However, no analytical explanation of the unwanted oscillations typically observed in the group delay and GDD of such a simple-chirped mirror was given. These oscillations were minimized purely by computer optimization.

The original chirped mirror design was further refined by the Double-Chirped Mirror (DCM) [97Kae, 99 Mat ] concept which takes into account the impedance matching problem which occurs at the air-mirror interface and the grating structure in the mirror. An exact coupled-mode analysis [97Mat] was used to develop a double-chirp technique. The impedance matching concept allowed a much better insight to the design limitations and allowed for the first time for an analytical design with custom-tailored dispersion characteristics which required only minor numerical optimization
[99Mat]. The strong periodic variation in the group delay of the original chirped mirrors occurs due to impedance mismatch between the incident medium (i.e. typically air) and the mirror stack and also within the mirror stack. Using the accurate analytical expressions for phase, group delay, and GDD [99Mat], DCMs could be designed and fabricated with a smooth and custom-tailored GDD suitable for generating pulses in the two-cycle regime directly from a Ti:sapphire laser [99Sut, 99Mor1, 99Mor2].

A Double-Chirped Mirror (DCM) [97Kae, 99Mat] is a multilayer interference coating that can be considered as a composition of at least two sections, each with a different task. The layer materials are typically $\mathrm{SiO}_{2}$ and $\mathrm{TiO}_{2}$. The first section is the AR coating, typically composed of 10 to 14 layers. It is necessary because the theory is derived assuming an ideal matching to air. The other section represents the actual DCM structure, as derived from theory. The double-chirp section is responsible for the elimination of the oscillations in the GDD from within the mirror stack. Double-chirping means that in addition to the local Bragg wavelength $\lambda_{\mathrm{B}}$ the local coupling of the incident wave to the reflected wave is independently chirped as well. The local coupling is adjusted by slowly increasing the high-index layer thickness in every pair so that the total optical thickness remains $\lambda_{\mathrm{B}} / 2$. This corresponds to an adiabatic matching of the impedance. The AR-coating, together with the rest of the mirror, is used as a starting design for a numerical optimization program. Since theoretical design is close to the desired design goal, a local optimization using a standard gradient algorithm is sufficient. At this point, only the broadband AR-coating sets a limitation on the reduction of the GDD oscillations. An AR-coating with a residual reflectivity of less than $10^{-4}$ is required for a DCM at a center wavelength of around 800 nm , which results in a bandwidth of only 250 nm [00Mat]. This bandwidth limitation cannot be removed with more layers in the mirror structure [96Dob].

The invention of the BAck-SIde-Coated (BASIC) mirrors [00Mat] or later the tilted front-side mirrors [01Tem] resolved this issue. In the BASIC mirror the ideal DCM structure is matched to the low-index material of the mirror which ideally matches the mirror substrate material. This DCM structure is deposited on the back of the substrate and the AR-coating is deposited on the front of the slightly wedged or curved substrate, so that the residual reflection is directed out of the beam and does not deteriorate the dispersion properties of the DCM structure on the other side of the substrate. Thus, the purpose of the AR-coating is only to reduce the insertion losses of the mirror at the air-substrate interface. For most applications it is sufficient to get this losses as low as $0.5 \%$. Therefore, the bandwidth of such an AR-coating can be much broader. Both the DCM and AR-coating multilayer structures can be independently designed and optimized. Based on this analysis, we designed a BAck-SIde-Coated Double-Chirped Mirror (BASIC DCM) that supports a bandwidth of 220 THz with group delay dispersion oscillations of about $2 \mathrm{fs}^{2}$ (rms), an order-ofmagnitude improvement compared to previous designs of similar bandwidth [00Mat]. Ultrabroad BASIC DCMs with a bandwidth of 270 THz have also been used to compress supercontinuum of cascaded hollow fibers down to 4.6 fs [04San]. The trade-off is that the substrate has to be as thin as possible to minimize the overall material dispersion. In addition, the wedged mirror leads to an undesired angular dispersion of the beam.

Another possibility to overcome the AR-coating problem is given with the idea to use an ideal DCM under Brewster-angle incidence [03Ste]. In this case, the low-index layer is matched to air. However, under p-polarized incidence the index contrast and therefore the Fresnel reflectivity of a layer pair is reduced and more layer pairs are necessary to achieve high reflectivity. This increases the penetration depth into the mirror which has the advantage that these mirrors can produce more dispersion per reflection but this means that scattering and other losses and also fabrication tolerances become even more severe. In addition, this concept is difficult to apply to curved mirrors. Furthermore, the spatial chirp of the reflected beam has to be removed by back reflection or an additional reflection from another Brewster-angle mirror.

Other methods to overcome the AR-coating problem are based on using different chirped mirrors with slightly shifted GTI oscillations that partially cancel each other. Normally, these chirped mirrors are very difficult to fabricate [00Mat]. Many different growth runs normally result in strong
shifts of those GTI oscillations so that a special selection of mirrors makes it ultimately possible to obtain the right dispersion compensation. Some tuning of the oscillation peaks can be obtained by the angle of incidence [00Sut]. A specially designed pair of DCMs has been used to cancel the spurious GTI oscillation [01Kae] where an additional quarter-wave layer between the AR-coating and the DCM structure was added in one of the DCMs. Also this design has its drawbacks and limitations because it requires an extremely high precision in fabrication and restricts the range of angles of incidence.

After this overview it becomes clear that there is no perfect solution to the challenge of ultrabroadband dispersion compensation. At this point ultrabroadband chirped mirrors are the only way to compress pulses in the one- to two-optical-cycle regime and normally a larger selection of chirped mirrors are required to "match and reduce" the residual unwanted GDD oscillations from all mirrors inside the laser cavity.

### 2.1.6 Mode-locking techniques

### 2.1.6.1 Overview

Passive mode-locking mechanisms are well-explained by three fundamental models: slow saturable absorber mode-locking with dynamic gain saturation [72New, 74 New ] (Fig. 2.1.5a), fast saturable absorber mode-locking [75Hau1, 92Hau] (Fig. 2.1.5b) and slow saturable absorber modelocking without dynamic gain saturation which in the femtosecond regime is described by soliton mode-locking [95Kae1, 95Jun2, 96Kae] and in the picosecond regime by Paschotta et al. [01Pas1] (Fig. 2.1.5c). The physics of most of these techniques can be well explained with Haus's master equation formalism as long as at steady state the changes in the pulse envelope during the propagation inside the cavity are small. At steady state the pulse envelope has to be unchanged after one round trip through the cavity.

Passive mode-locking, however, can only be analytically modeled in the weak saturation regime, which is typically not the case in SESAM mode-locked solid-state lasers. However, this formalism still provides a useful approach to describe mode-locking techniques in an unified fashion. Recent numerical simulations show that analytical results with fast saturable absorbers only slightly underestimate numerical solutions and correctly describe the dependence on saturated gain, gain bandwidth and absorber modulation taking into account more strongly saturated absorbers and somewhat longer saturation recovery times in SESAM mode-locked solid-state lasers [01Pas1].

A short introduction to Haus's formalism is given in Sect. 2.1.6.2 and Table 2.1.10. Afterwards we will describe all mode-locking techniques using this formalism and summarize the theoretical prediction for pulse shape and pulse duration (Table 2.1.11). For solid-state lasers self- $Q$-switching instabilities in passive mode-locking are a serious challenge. Simple guidelines to prevent those instabilities and obtain stable cw mode-locking are presented in Sect. 2.1.6.8.

### 2.1.6.2 Haus's master equations

Haus's master equation formalism [95Hau2] is based on linearized differential operators that describe the temporal evolution of a pulse envelope inside the laser cavity. At steady state we then obtain the differential equation:
Table 2.1.10. Linearized operators that model the change in the pulse envelope $A(t)$ for each element in the laser cavity and their defining equations, The pulse envelope is normalized such that $|A(z, t)|^{2}$ is the pulse power $P(z, t)(2.1 .24) . k_{n}$ : wave vector in the dispersive media, i.e. $k_{n}=k n=n 2 \pi / \lambda$, where $\lambda$ is the vacuum wavelength. $z$ : the relevant propagation distance for negative dispersion or SPM, respectively. $c$ : vacuum light velocity. $\omega$ : frequency in radians/second.

| Laser cavity element | Eq. | Linearized operator | New constants | Constants |
| :---: | :---: | :---: | :---: | :---: |
| Gain | (2.1.32) | $\Delta A \approx\left[g+D_{\mathrm{g}} \frac{\partial^{2}}{\partial t^{2}}\right] A$ | $D_{\mathrm{g}} \equiv \frac{g}{\Omega_{\mathrm{g}}^{2}}$ | $D_{\mathrm{g}}$ : gain dispersion (2.1.32) <br> $g$ : saturated amplitude gain coefficient <br> $\Omega_{\mathrm{g}}$ : HWHM of gain bandwidth in radians/second <br> $\Delta \nu_{\mathrm{g}}:$ FWHM of gain bandwidth, i.e. $\Delta \nu_{\mathrm{g}}=\Omega_{\mathrm{g}} / \pi$ |
| Loss modulator | (2.1.34) | $\Delta A \approx-M_{\mathrm{s}} \mathrm{t}^{2} A$ | $M_{\mathrm{s}} \equiv \frac{M \omega_{\mathrm{m}}^{2}}{2}$ | $\omega_{\mathrm{m}}$ : loss modulation frequency in radians/second <br> $2 M$ : peak-to-peak modulation depth for amplitude loss coefficient |
| Constant loss |  | $\Delta A \approx-l A$ |  | $l$ : amplitude loss coefficient |
| Constant phase shift |  | $\Delta A \approx \mathrm{i} \psi A$ |  | $\psi$ : phase shift |
| Fast saturable absorber | (2.1.36) | $\Delta A \approx \gamma_{\mathrm{A}}\|A\|^{2} A$ | $\gamma_{\mathrm{A}} \equiv \frac{q_{0}}{I_{\mathrm{sat}, \mathrm{~A}} A_{\mathrm{A}}}$ | $\gamma_{\mathrm{A}}$ : absorber coefficient (2.1.18) and (2.1.35) <br> $q_{0}$ : maximum saturable amplitude loss coefficient <br> $I_{\text {sat, } \mathrm{A}}$ : saturation intensity <br> $A_{\mathrm{A}}$ : laser mode area in saturable absorber |
| Dispersion: 2nd order | (2.1.41) | $\Delta A \approx \mathrm{i} D \frac{\partial^{2}}{\partial t^{2}} A$ | $D \equiv \frac{1}{2} k_{n}^{\prime \prime} z$ | $D$ : dispersion parameter (half of the total group delay dispersion per cavity round trip - Table 2.1.7) (2.1.40) $k_{n}^{\prime \prime}=\frac{\mathrm{d}^{2} k_{n}}{\mathrm{~d} \omega^{2}}$ |
| SPM | (2.1.47) | $\Delta A \approx-\mathrm{i} \delta_{\mathrm{L}}\|A\|^{2} A$ | $\delta_{\mathrm{L}} \equiv \frac{k n_{2} z}{A_{\mathrm{L}}}$ | $\delta_{\mathrm{L}}$ : SPM coefficient (2.1.44) <br> $n_{2}$ : nonlinear refractive index <br> $A_{\mathrm{L}}$ : laser mode area inside laser material <br> (Note: Here we assume that the dominant SPM occurs in the laser material. Then $z$ is equal to 2 times the length of the laser crystal in a standing-wave cavity.) |

Table 2.1.11. Predicted pulse duration for the different ModeLocking (ML) techniques. The parameters used here are summarized and defined in Table 2.1.10. The pulse is transform-limited for proper dispersion compensation and is either an unchirped Gaussian or soliton pulse.

| ML technique | Eq. | Pulse shape | Pulse duration (FWHM) |
| :---: | :---: | :---: | :---: |
| Active ML: <br> Amplitude loss modulation | (2.1.49) | Gauss | $\tau_{\mathrm{p}}=1.66 \times \sqrt[4]{\frac{D_{\mathrm{g}}}{M_{\mathrm{s}}}}=1.66 \times \sqrt[4]{\frac{2 g}{M}} \sqrt{\frac{1}{\omega_{\mathrm{m}} \Omega_{\mathrm{g}}}}$ |
| Passive ML: <br> Slow saturable absorber and dynamic gain saturation | (2.1.62) | soliton | $\tau_{\mathrm{p}} \approx 1.76 \times \frac{4}{\pi} \frac{1}{\Delta \nu_{\mathrm{g}}}$ |
| Slow saturable absorber for solid-state lasers and strongly saturated absorbers $(S>3)$ | (2.1.70) | numerical simulations | $\tau_{p, \min } \approx \frac{1.5}{\Delta \nu_{\mathrm{g}}} \sqrt{\frac{g}{\Delta R}}$ for $\tau_{\mathrm{A}} \lesssim 30 \tau_{\mathrm{p}}$ |
| Fast Saturable Absorber (FSA) | (2.1.65) | soliton | $\tau_{\mathrm{p}}=1.76 \frac{4 D_{\mathrm{g}}}{\gamma_{\mathrm{A}} E_{\mathrm{p}}}$ <br> only transform-limited soliton pulses for a well-defined intracavity group delay dispersion (assuming negligible higher-order dispersion): $\|D\| / \delta_{\mathrm{L}}=D_{\mathrm{g}} / \gamma_{\mathrm{A}}$ |
| Fully saturated ideal fast saturable absorber | (2.1.67) |  | $\tau_{p, \text { min }}=\frac{1.76}{\Omega_{\mathrm{g}}} \sqrt{\frac{2 g}{q_{0}}} \approx \frac{1.12}{\Delta \nu_{\mathrm{g}}} \sqrt{\frac{g}{\Delta R}} \text { for } \frac{\|D\|}{\delta_{\mathrm{L}}}=\frac{D_{\mathrm{g}}}{\gamma_{\mathrm{A}}}$ |
| Soliton mode-locking | (2.1.74) | soliton | $\tau_{\mathrm{p}}=1.76 \frac{2\|D\|}{\delta_{\mathrm{L}} E_{\mathrm{p}}}$ <br> transform-limited soliton pulses for the total intracavity group delay dispersion (assuming negligible higher-order dispersion) |
|  | (2.1.76) |  | $\tau_{p, \text { min }}=1.7627\left(\frac{1}{\sqrt{6} \Omega_{\mathrm{g}}}\right)^{3 / 4} \phi_{\mathrm{s}}^{-1 / 8}\left(\frac{\tau_{\mathrm{A}} g^{3 / 2}}{q_{0}}\right)^{1 / 4} \approx 0.45\left(\frac{1}{\Delta \nu_{\mathrm{g}}}\right)^{3 / 4}\left(\frac{\tau_{\mathrm{A}}}{\Delta R}\right)^{1 / 4} \frac{g^{3 / 8}}{\phi_{\mathrm{s}}^{1 / 8}}$ |

$$
\begin{equation*}
T_{\mathrm{R}} \frac{\partial A(T, t)}{\partial T}=\sum_{i} \Delta A_{i}=0 \tag{2.1.23}
\end{equation*}
$$

where $A$ is the pulse envelope, $T_{\mathrm{R}}$ is the cavity round-trip time, $T$ is the time that develops on a time scale of the order of $T_{\mathrm{R}}, t$ is the fast time of the order of the pulse duration, and $\Delta A_{i}$ are the changes of the pulse envelope due to different elements in the cavity (such as gain, loss modulator or saturable absorber, dispersion etc.) (Table 2.1.10). Equation (2.1.23) basically means that at steady state after one laser round trip the pulse envelope cannot change and all the small changes due to the different elements in the cavity have to sum up to zero. Each element is modeled as a linearized operator, which will be discussed in more detail below.

The pulse envelope is normalized such that $|A(z, t)|^{2}$ is the pulse power $P(z, t)$ :

$$
\begin{equation*}
E(z, t) \propto A(z, t) \mathrm{e}^{\mathrm{i}\left[\omega_{0} t-k_{n}\left(\omega_{0}\right) z\right]} \quad \text { with } \quad|A(z, t)|^{2} \equiv P(z, t) \tag{2.1.24}
\end{equation*}
$$

where $E(z, t)$ is the electric field, $\omega_{0}$ the center frequency in radians/second of the pulse spectrum and $k_{n}=n k$ with $k=2 \pi / \lambda$ the wave number with $\lambda$ the vacuum wavelength and $n$ the refractive index. Before we discuss the different mode-locking models we briefly discuss the linearized operators for the differential equations.

### 2.1.6.2.1 Gain

A homogeneously broadened gain medium is described by a Lorentzian lineshape for which the frequency-dependent gain coefficient $g(\omega)$ is given by

$$
\begin{equation*}
g(\omega)=\frac{g}{1+\left(\frac{\omega-\omega_{0}}{\Omega_{\mathrm{g}}}\right)^{2}} \approx g\left(1-\frac{\Delta \omega^{2}}{\Omega_{\mathrm{g}}^{2}}\right) \quad \text { for } \quad\left(\left(\omega-\omega_{0}\right) / \Omega_{\mathrm{g}}\right)^{2} \ll 1 \tag{2.1.25}
\end{equation*}
$$

where $\Delta \omega=\omega-\omega_{0}, g$ is the saturated gain coefficient for a cavity round trip, and $\Omega_{\mathrm{g}}$ is the Half Width at Half Maximum (HWHM) of the gain bandwidth in radians/seconds. In the frequency domain the pulse envelope after the gain medium is given by

$$
\begin{equation*}
\tilde{A}_{\text {out }}(\omega)=\mathrm{e}^{g(\omega)} \tilde{A}_{\text {in }}(\omega) \approx[1+g(\omega)] \tilde{A}_{\text {in }}(\omega) \quad \text { for } \quad g \ll 1, \tag{2.1.26}
\end{equation*}
$$

where $\tilde{A}(\omega)$ is the Fourier transformation of $A(t)$. Equations (2.1.25) and (2.1.26) then give

$$
\begin{equation*}
\tilde{A}_{\text {out }}(\omega)=\left[1+g-\frac{g}{\Omega_{\mathrm{g}}^{2}} \Delta \omega^{2}\right] \tilde{A}_{\text {in }}(\omega) \Rightarrow A_{\text {out }}(t)=\left[1+g+\frac{g}{\Omega_{\mathrm{g}}^{2}} \frac{\partial^{2}}{\partial t^{2}}\right] A_{\text {in }}(t) \tag{2.1.27}
\end{equation*}
$$

where we used the fact that a factor of $\Delta \omega$ in the frequency domain produces a time derivative in the time domain. For example for the electric field we obtain:

$$
\begin{equation*}
\frac{\partial}{\partial t} E(t)=\frac{\partial}{\partial t}\left\{\frac{1}{2 \pi} \int \tilde{E}(\omega) \mathrm{e}^{\mathrm{i} \omega t} \mathrm{~d} \omega\right\}=\frac{1}{2 \pi} \int \tilde{E}(\omega) \mathrm{i} \omega \mathrm{e}^{\mathrm{i} \omega t} \mathrm{~d} \omega \tag{2.1.28}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{\partial^{2}}{\partial t^{2}} E(t)=\frac{\partial^{2}}{\partial t^{2}}\left\{\frac{1}{2 \pi} \int \tilde{E}(\omega) \mathrm{e}^{\mathrm{i} \omega t} \mathrm{~d} \omega\right\}=\frac{1}{2 \pi} \int \tilde{E}(\omega)\left[-\omega^{2}\right] \mathrm{e}^{\mathrm{i} \omega t} \mathrm{~d} \omega \tag{2.1.29}
\end{equation*}
$$

and similarly for the pulse envelope:

$$
\begin{equation*}
\frac{\partial}{\partial t} A(t)=\frac{\partial}{\partial t}\left\{\frac{1}{2 \pi} \int \tilde{A}(\omega) \mathrm{e}^{\mathrm{i} \Delta \omega t} \mathrm{~d} \omega\right\}=\frac{1}{2 \pi} \int \tilde{A}(\omega) \mathrm{i} \Delta \omega \mathrm{e}^{\mathrm{i} \Delta \omega t} \mathrm{~d} \omega \tag{2.1.30}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{\partial^{2}}{\partial t^{2}} A(t)=\frac{\partial^{2}}{\partial t^{2}}\left\{\frac{1}{2 \pi} \int \tilde{A}(\omega) \mathrm{e}^{\mathrm{i} \Delta \omega t} \mathrm{~d} \omega\right\}=\frac{1}{2 \pi} \int \tilde{A}(\omega)\left[-\Delta \omega^{2}\right] \mathrm{e}^{\mathrm{i} \Delta \omega t} \mathrm{~d} \omega \tag{2.1.31}
\end{equation*}
$$

For the change in the pulse envelope $\Delta A=A_{\text {out }}-A_{\text {in }}$ after the gain medium we then obtain:

$$
\begin{equation*}
\Delta A \approx\left[g+D_{\mathrm{g}} \frac{\partial^{2}}{\partial t^{2}}\right] A, \quad D_{\mathrm{g}} \equiv \frac{g}{\Omega_{\mathrm{g}}^{2}} \tag{2.1.32}
\end{equation*}
$$

where $D_{\mathrm{g}}$ is the gain dispersion.

### 2.1.6.2.2 Loss modulator

A loss modulator inside a laser cavity is typically an acousto-optic modulator and produces a sinusoidal loss modulation given by a time-dependent loss coefficient:

$$
\begin{equation*}
l(t)=M\left(1-\cos \omega_{\mathrm{m}} t\right) \approx M_{\mathrm{s}} t^{2}, \quad M_{\mathrm{s}} \equiv \frac{M \omega_{\mathrm{m}}^{2}}{2} \tag{2.1.33}
\end{equation*}
$$

where $M_{\mathrm{s}}$ is the curvature of the loss modulation, $2 M$ is the peak-to-peak modulation depth and $\omega_{\mathrm{m}}$ the modulation frequency which corresponds to the axial mode spacing in fundamental modelocking. In fundamental mode-locking we only have one pulse per cavity round trip. The change in the pulse envelope is then given by

$$
\begin{equation*}
A_{\mathrm{out}}(t)=\mathrm{e}^{-l(t)} A_{\mathrm{in}}(t) \approx[1-l(t)] A_{\text {in }}(t) \Rightarrow \Delta A \approx-M_{\mathrm{s}} t^{2} A \tag{2.1.34}
\end{equation*}
$$

### 2.1.6.2.3 Fast saturable absorber

In case of an ideal fast saturable absorber we assume that the loss recovers instantaneously and therefore shows the same time dependence as the pulse envelope, (2.1.17) and (2.1.18):

$$
\begin{equation*}
q(t)=\frac{q_{0}}{1+I_{\mathrm{A}}(t) / I_{\mathrm{sat}, \mathrm{~A}}} \approx q_{0}-\gamma_{\mathrm{A}} P(t), \quad \gamma_{\mathrm{A}} \equiv \frac{q_{0}}{I_{\mathrm{sat}, \mathrm{~A}} A_{\mathrm{A}}} . \tag{2.1.35}
\end{equation*}
$$

The change in the pulse envelope is then given by

$$
\begin{equation*}
A_{\text {out }}(t)=\mathrm{e}^{-q(t)} A_{\text {in }}(t) \approx[1-q(t)] A_{\text {in }}(t) \Rightarrow \Delta A \approx \gamma_{\mathrm{A}}|A|^{2} A \tag{2.1.36}
\end{equation*}
$$

### 2.1.6.2.4 Group velocity dispersion (GVD)

The wave number $k_{n}(\omega)$ in a dispersive material depends on the frequency and can be approximately written as:

$$
\begin{equation*}
k_{n}(\omega) \approx k_{n}\left(\omega_{0}\right)+k_{n}^{\prime} \Delta \omega+\frac{1}{2} k_{n}^{\prime \prime} \Delta \omega^{2}+\ldots, \tag{2.1.37}
\end{equation*}
$$

where $\Delta \omega=\omega-\omega_{0}, k_{n}^{\prime}=\left.\frac{\partial k_{n}}{\partial \omega}\right|_{\omega=\omega_{0}}$ and $k_{n}^{\prime \prime}=\left.\frac{\partial^{2} k_{n}}{\partial \omega^{2}}\right|_{\omega=\omega_{0}}$. In the frequency domain the pulse envelope in a dispersive medium after a propagation distance of $z$ is given by

$$
\begin{equation*}
\tilde{A}(z, \omega)=\mathrm{e}^{-\mathrm{i}\left[k_{n}(\omega)-k_{n}\left(\omega_{0}\right)\right] z} \tilde{A}(0, \omega) \approx\left\{1-\mathrm{i}\left[k_{n}(\omega)-k_{n}\left(\omega_{0}\right)\right] z\right\} \tilde{A}(0, \omega) \tag{2.1.38}
\end{equation*}
$$

where we used the slowly-varying-envelope approximation (which is applicable for pulse durations of more than 10 fs in the near infrared wavelength regime). Taking into account only the first-order and second-order dispersion terms we then obtain:

$$
\begin{equation*}
\tilde{A}(z, \omega) \approx\left[1-\mathrm{i} k_{n}^{\prime} \Delta \omega z-\mathrm{i} \frac{1}{2} k_{n}^{\prime \prime} \Delta \omega^{2} z\right] \tilde{A}(0, \omega) . \tag{2.1.39}
\end{equation*}
$$

The linear term in $\Delta \omega$ determines the propagation velocity of the pulse envelope (i.e. the group velocity $v_{\mathrm{g}}$ ) and the quadratic term in $\Delta \omega$ determines how the pulse envelope gets deformed due to second-order dispersion. The influence of higher-order dispersion can be considered with more terms in the expansion of $k_{n}(\omega)$ (2.1.37). However, higher-order dispersion only becomes important for ultrashort pulse generation with pulse durations below approximately 30 fs depending how much material is inside the cavity. Normally we are only interested in the changes of the pulse envelope and therefore it is useful to restrict our observation to a reference system that is moving with the pulse envelope. In this reference system we only need to consider second- and higher-order dispersion. In the time domain we then obtain for second-order dispersion:

$$
\begin{equation*}
A(z, t) \approx\left[1+\mathrm{i} D \frac{\partial^{2}}{\partial t^{2}}\right] A(0, t), \quad D \equiv \frac{1}{2} k_{n}^{\prime \prime} z=\frac{1}{2} \frac{\mathrm{~d}^{2} \phi}{\mathrm{~d} \omega^{2}} \tag{2.1.40}
\end{equation*}
$$

where $D$ is the dispersion parameter which is half of the total group delay dispersion per cavity round trip. Therefore we obtain for the change in the pulse envelope:

$$
\begin{equation*}
\Delta A \approx \mathrm{i} D \frac{\partial^{2}}{\partial t^{2}} A \tag{2.1.41}
\end{equation*}
$$

### 2.1.6.2.5 Self-phase modulation (SPM)

The Kerr effect introduces a space- and time-dependent refractive index:

$$
\begin{equation*}
n(r, t)=n+n_{2} I(r, t) \tag{2.1.42}
\end{equation*}
$$

where $n$ is the linear refractive index, $n_{2}$ the nonlinear refractive index and $I(r, t)$ the intensity of the laser beam, typically a Gaussian beam profile. For laser host materials, $n_{2}$ is typically of the order of $10^{-16} \mathrm{~cm}^{2} / \mathrm{W}$ and does not change very much for different materials. For example, for sapphire $n_{2}=3 \times 10^{-16} \mathrm{~cm}^{2} / \mathrm{W}$, fused quartz $n_{2}=2.46 \times 10^{-16} \mathrm{~cm}^{2} / \mathrm{W}$, Schott glass LG-760 $n_{2}=2.9 \times 10^{-16} \mathrm{~cm}^{2} / \mathrm{W}$, YAG $n_{2}=6.2 \times 10^{-16} \mathrm{~cm}^{2} / \mathrm{W}$, and YLF $n_{2}=1.72 \times 10^{-16} \mathrm{~cm}^{2} / \mathrm{W}$. The nonlinear refractive index produces a nonlinear phase shift during pulse propagation:

$$
\begin{equation*}
\phi(z, r, t)=-k n(r, t) z=-k\left[n+n_{2} I(r, t)\right] z=-k n z-\delta_{\mathrm{L}}|A(r, t)|^{2} \tag{2.1.43}
\end{equation*}
$$

where $\delta_{\mathrm{L}}$ is the Self-Phase Modulation coefficient (SPM coefficient):

$$
\begin{equation*}
\delta_{\mathrm{L}} \equiv k n_{2} z / A_{\mathrm{L}} \tag{2.1.44}
\end{equation*}
$$

where $A_{\mathrm{L}}$ is the laser mode area inside the laser medium. Here we assume that the dominant SPM inside the laser occurs in the gain medium. In this case, $z$ is equal to twice the laser material length. Of course the mode area can be also very small in other materials. In this case, we will have to add up all the SPM contributions inside the laser resonator. The laser mode area $A_{\mathrm{L}}$ is an "averaged value" in case the mode is changing within the gain medium.

The electric field during propagation is changing due to SPM:

$$
\begin{equation*}
E(z, t)=\mathrm{e}^{\mathrm{i} \phi} E(0, t) \propto \mathrm{e}^{-\mathrm{i} \delta_{\mathrm{L}}|A(t)|^{2}} A(0, t) \mathrm{e}^{\mathrm{i} \omega_{0} t-\mathrm{i} k_{n}\left(\omega_{0}\right) z} \tag{2.1.45}
\end{equation*}
$$

For $\delta_{\mathrm{L}}|A|^{2} \ll 1$ we obtain:

$$
\begin{equation*}
A(z, t)=\mathrm{e}^{-\mathrm{i} \delta_{\mathrm{L}}|A(t)|^{2}} A(0, t) \mathrm{e}^{-\mathrm{i} k_{n}\left(\omega_{0}\right) z} \approx\left(1-\mathrm{i} \delta_{\mathrm{L}}|A(t)|^{2}\right) A(0, t) \mathrm{e}^{-\mathrm{i} k_{n}\left(\omega_{0}\right) z} . \tag{2.1.46}
\end{equation*}
$$

After one cavity round trip we then obtain

$$
\begin{equation*}
\Delta A \approx-\mathrm{i} \delta_{\mathrm{L}}|A|^{2} A \tag{2.1.47}
\end{equation*}
$$

### 2.1.6.3 Active mode-locking

Short pulses from a laser can be generated with a loss or phase modulator inside the resonator. For example, the laser beam is amplitude-modulated when it passes through an acousto-optic modulator. Such a modulator can modulate the loss of the resonator at a period equal to the round-trip time $T_{\mathrm{R}}$ of the resonator (i.e. fundamental mode-locking). The pulse evolution in an actively mode-locked laser without Self-Phase Modulation (SPM) and Group-Velocity Dispersion (GVD) can be described by the master equation of Haus [75Hau2]. Taking into account gain dispersion and loss modulation we obtain with (2.1.32) and (2.1.34) (Table 2.1.10) the following differential equation:

$$
\begin{equation*}
\sum_{i} \Delta A_{i}=\left[g\left(1+\frac{1}{\Omega_{\mathrm{g}}^{2}} \frac{\partial^{2}}{\partial t^{2}}\right)-l-M \frac{\omega_{\mathrm{m}} t^{2}}{2}\right] A(T, t)=0 \tag{2.1.48}
\end{equation*}
$$

Typically we obtain pulses which are much shorter than the round-trip time in the cavity and which are placed in time at the position where the modulator introduces the least amount of loss. Therefore, we were able to approximate the cosine modulation by a parabola (2.1.33). The only stable solution to this differential equation is a Gaussian pulse shape with a pulse duration:

$$
\begin{equation*}
\tau_{\mathrm{p}}=1.66 \times \sqrt[4]{D_{\mathrm{g}} / M_{\mathrm{s}}} \tag{2.1.49}
\end{equation*}
$$

where $D_{\mathrm{g}}$ is the gain dispersion $\left((2.1 .32)\right.$ and Table 2.1.10) and $M_{\mathrm{s}}$ is the curvature of the loss modulation ((2.1.33) and Table 2.1.10). Therefore, in active mode-locking the pulse duration becomes shorter until the pulse shortening of the loss modulator balances the pulse broadening of the gain filter. Basically, the curvature of the gain is given by the gain dispersion $D_{\mathrm{g}}$ and the curvature of the loss modulation is given by $M_{\mathrm{s}}$. The pulse duration is only scaling with the fourth root of the saturated gain (i.e. $\tau_{\mathrm{p}} \propto \sqrt[4]{g}$ ) and the modulation depth (i.e. $\tau_{\mathrm{p}} \propto \sqrt[4]{1 / M}$ ) and with the square root of the modulation frequency (i.e. $\tau_{\mathrm{p}} \propto \sqrt{1 / \omega_{\mathrm{m}}}$ ) and the gain bandwidth (i.e. $\tau_{\mathrm{p}} \propto \sqrt{1 / \Delta \omega_{\mathrm{g}}}$ ). A higher modulation frequency or a higher modulation depth increases the curvature of the loss modulation and a larger gain bandwidth decreases gain dispersion. Therefore, we obtain shorter pulse durations in all cases. At steady state the saturated gain is equal to the total cavity losses, therefore, a larger output coupler will result in longer pulses. Thus, higher average output power is generally obtained at the expense of longer pulses (Table 2.1.2).

The results that have been obtained in actively mode-locked flashlamp-pumped Nd:YAG and Nd:YLF lasers can be very well explained by this result. For example, with Nd:YAG at a lasing wavelength of $1.064 \mu \mathrm{~m}$ we have a gain bandwidth of $\Delta \lambda_{\mathrm{g}}=0.45 \mathrm{~nm}$. With a modulation frequency of 100 MHz (i.e. $\omega_{\mathrm{m}}=2 \pi \cdot 100 \mathrm{MHz}$ ), a $10 \%$ output coupler (i.e. $2 g \approx T_{\text {out }}=0.1$ ) and a modulation depth $M=0.2$, we obtain a FWHM pulse duration of $93 \mathrm{ps}(2.1 .49)$. For example, with Nd:YLF at a lasing wavelength of $1.047 \mu \mathrm{~m}$ and a gain bandwidth of $\Delta \lambda_{\mathrm{g}}=1.3 \mathrm{~nm}$ we obtain with the same mode-locking parameters a pulse duration of 53 ps (2.1.49).

The same result for the pulse duration (2.1.49) has been previously derived by Kuizenga and Siegman [70Kui1, 70Kui2] where they assumed a Gaussian pulse shape and then followed the pulse once around the laser cavity, through the gain and the modulator. They then obtained a self-consistent solution when no net change occurs in the complete round trip. The advantage of

Haus's theory is that no prior assumption has to be made for the pulse shape. His theory then predicts a Gaussian pulse shape for actively mode-locked lasers, which then in principle justifies Kuizenga and Siegman's assumption.

Equation (2.1.49) shows that increasing the modulation frequency is an effective method to shorten the pulses. Harmonic mode-locking is a technique in which the cavity is modulated at a frequency that is some integer multiple of the fundamental pulse repetition rate with a period given by the cavity round-trip time. This technique was first introduced and analyzed by Becker et al. [72Bec] in a phase mode-locked Nd:YAG laser. Second-harmonic mode-locking of a flashlamppumped Nd:YAG laser at $1.06 \mu \mathrm{~m}$ resulted in less than 50 ps [83Joh, 85Joh] and at $1.32 \mu \mathrm{~m}$ in 53 ps [88Kel].

It has been well known for quite some time that the addition of a nonlinear index medium to a passively [ $84 \mathrm{Mar}, 85 \mathrm{Mar}$ ] or actively [ 86 Hau ] mode-locked laser system can lead to shorter pulses. The bandwidth limitation that results from gain dispersion can be partially overcome by the spectral broadening caused by the nonlinearity. We can extend the differential equation (2.1.48) with the additional terms for SPM ((2.1.47) and Table 2.1.10):

$$
\begin{equation*}
\sum_{i} \Delta A_{i}=\left[g\left(1+\frac{1}{\Omega_{\mathrm{g}}^{2}} \frac{\partial^{2}}{\partial t^{2}}\right)-l-M \frac{\omega_{\mathrm{m}} t^{2}}{2}-\mathrm{i} \delta_{\mathrm{L}}|A|^{2}+\mathrm{i} \psi\right] A(T, t)=0 \tag{2.1.50}
\end{equation*}
$$

In this case, however, we have to include an additional phase shift $\psi$ to obtain a self-consistent solution. So far, we always assumed $\psi=0$. This phase shift is an additional degree of freedom because the boundary condition for intracavity pulses only requires that the pulse envelope is unchanged after one cavity round trip. The electric field, however, can have an arbitrary phase shift $\psi$ after one round trip. This is normally the case because the phase and the group velocity are not the same. It is important to note, that for ultrashort pulses in the one- to two-cycle regime this becomes important and stabilization of the electric field with respect to the peak of the pulse envelope is required [99Tel].

We can obtain an analytic solution of (2.1.50) if we assume a parabolic approximation for $|A|^{2}$ :

$$
\begin{equation*}
|A|^{2}=\left|A_{0}\right|^{2} \mathrm{e}^{-t^{2} / \tau^{2}} \approx P_{0}\left(1-\frac{t^{2}}{\tau^{2}}\right) \tag{2.1.51}
\end{equation*}
$$

The solution of (2.1.50) is then a chirped Gaussian pulse

$$
\begin{equation*}
A(t)=A_{0} \exp \left[-\frac{1}{2} \frac{t^{2}}{\tau^{2}}(1-\mathrm{i} x)\right] \tag{2.1.52}
\end{equation*}
$$

with the chirp parameter

$$
\begin{equation*}
x=\frac{\tau^{2} \phi_{\mathrm{nl}}}{2 D_{\mathrm{g}}} \tag{2.1.53}
\end{equation*}
$$

and the FWHM pulse duration

$$
\begin{equation*}
\tau_{\mathrm{p}}=1.66 \cdot \tau=1.66 \cdot \sqrt[4]{\frac{D_{\mathrm{g}}}{M_{\mathrm{s}}+\phi_{\mathrm{nl}}^{2} / 4 D_{\mathrm{g}}}} \tag{2.1.54}
\end{equation*}
$$

where $\phi_{\mathrm{nl}}$ is the nonlinear phase shift per cavity round trip at peak intensity. Typically, the beam diameter is very small in the laser gain material, thus the dominant SPM contribution comes from propagation through the gain material:

$$
\begin{equation*}
\phi_{\mathrm{nl}}=2 k L_{\mathrm{g}} n_{2} I_{0, \mathrm{~L}} \tag{2.1.55}
\end{equation*}
$$

where $L_{\mathrm{g}}$ is the length of the laser gain material (assuming a standing-wave cavity) and $I_{0, \mathrm{~L}}$ the peak intensity inside the SPM medium, i.e. the laser gain medium.

This analytical result can explain the much shorter $7-12 \mathrm{ps}$ pulses in actively mode-locked diode-pumped Nd:YAG [89Mak1] and Nd:YLF [89Mak2, 90Kel1, 90Wei, 90Juh] lasers because the laser mode area in those diode-pumped lasers is very small which results in significant SPM pulse shortening (2.1.54). For example, our experiments with an actively mode-locked diode-pumped Nd :YLF laser [95Bra2] are very well explained with (2.1.54). In this case the lasing wavelength is $1.047 \mu \mathrm{~m}$, the gain bandwidth is $\Delta \lambda_{\mathrm{g}}=1.3 \mathrm{~nm}$, the pulse repetition rate is 250 MHz , the output coupler is $2.5 \%$, the average output power is 620 mW , the mode radius inside the 5 mm long Nd:YLF crystal is $127 \mu \mathrm{~m} \times 87 \mu \mathrm{~m}$ and the loss modulation of the acousto-optic mode-locker is about $20 \%$. We then obtain a FWHM pulse duration of $17.8 \mathrm{ps}(2.1 .54)$ which agrees well with the experimentally observed pulse duration of 17 ps . Without SPM we would predict a pulse duration of 33 ps (2.1.49).

Equation (2.1.54) would predict that more SPM continues to reduce the pulse duration. However, too much SPM will ultimately drive the laser unstable. This has been shown by the numerical simulations of Haus and Silberberg [86Hau] which predict that pulse shortening in an actively modelocked system is limited by roughly a factor of 2 in the case of SPM only. They also showed that the addition of negative GVD can undo the chirp introduced by SPM, and therefore both effects together may lead to stable pulse shortening by a factor of 2.5 .

However, experimental results with fiber lasers and solid-state lasers indicate that soliton shaping in the negative GVD regime can lead to pulse stabilization and considerable more pulse shortening. We have extended the analysis of Haus and Silberberg by investigating the possible reduction in pulse width of an actively mode-locked laser as a result of soliton-like pulse formation, i.e., the presence of SPM and an excessive amount of negative GVD [95Kae2]. We show, by means of soliton perturbation theory, that beyond a critical amount of negative GVD a soliton-like pulse is formed and kept stable by an active mode-locker. If the bandwidth of the gain is large enough, the width of this solitary pulse can be much less than the width of a Gaussian pulse generated by the active mode-locker and gain dispersion alone. We established analytically that the pulse shortening possible by addition of SPM and GVD does not have a firm limit of 2.5 . Numerical simulations and experiments with a regeneratively actively mode-locked Nd:glass laser [94Kop2] confirm these analytical results. The pulse-width reduction achievable depends on the amount of negative GVD available. For an actively mode-locked Nd:glass laser a pulse shortening up to a factor of 6 may result, until instabilities arise.

### 2.1.6.4 Passive mode-locking with a slow saturable absorber and dynamic gain saturation

Dynamic gain saturation can strongly support pulse formation in passive mode-locking and has allowed pulses with duration much shorter than the absorber recovery time. Dynamic gain saturation means that the gain undergoes a fast pulse-induced saturation that recovers between consecutive pulses. This technique has been used to produce sub- $100-\mathrm{fs}$ pulses with dye lasers and dye saturable absorbers even though the absorber recovery time was in the nanosecond regime. Dynamic gain saturation can only help if the following conditions are fulfilled (Fig. 2.1.5a):

1. The loss needs to be larger than the gain before the pulse:

$$
\begin{equation*}
q_{0}>g_{0}, \tag{2.1.56}
\end{equation*}
$$

where $q_{0}$ is the unsaturated loss coefficient (2.1.6) and $g_{0}$ is the small signal gain coefficient in the laser.
2. The absorber needs to saturate faster than the gain. From (2.1.14) (i.e. slow saturable absorber and gain) then follows that

Table 2.1.12. Femtosecond Rhodamin 6G dye laser with its saturable absorber DODCI at a wavelength of $620 \mathrm{~nm} . \sigma_{\mathrm{L}}$ gain and $\sigma_{\mathrm{A}}$ absorber cross-section, $\tau_{\mathrm{L}}$ upper-state lifetime, $\tau_{\mathrm{A}}$ absorber recovery time.

| Dye material | Cross-section | Time |
| :--- | :--- | :--- |
| Rhodamin 6G | $\sigma_{\mathrm{L}}=1.36 \times 10^{-16} \mathrm{~cm}^{2}$ | $\tau_{\mathrm{L}}=4 \mathrm{~ns}$ |
| DODCI | $\sigma_{\mathrm{A}}=0.52 \times 10^{-16} \mathrm{~cm}^{2}$ | $\tau_{\mathrm{A}}=2.2 \mathrm{~ns}$ |
| Photoisomer | $\tilde{\sigma}_{\mathrm{A}}=1.08 \times 10^{-16} \mathrm{~cm}^{2}$ | $\tilde{\tau}_{\mathrm{L}}=1 \mathrm{~ns}$ |

$$
\begin{equation*}
E_{\mathrm{sat}, \mathrm{~A}}<E_{\mathrm{sat}, \mathrm{~L}} \Leftrightarrow \frac{A_{\mathrm{A}}}{\sigma_{\mathrm{A}}}<\frac{A_{\mathrm{L}}}{\sigma_{\mathrm{L}}} \tag{2.1.57}
\end{equation*}
$$

where $E_{\mathrm{sat}, \mathrm{A}}$ and $E_{\mathrm{sat}, \mathrm{L}}$ are the saturation energy of the absorber and the gain, $\sigma_{\mathrm{A}}$ and $\sigma_{\mathrm{L}}$ the absorber and gain cross section, and $A_{\mathrm{A}}$ and $A_{\mathrm{L}}$ the laser mode area in the absorber and gain.
3. The absorber has to recover faster than the gain:

$$
\begin{equation*}
\tau_{\mathrm{A}}<\tau_{\mathrm{L}} \tag{2.1.58}
\end{equation*}
$$

where $\tau_{\mathrm{A}}$ is the absorber recovery time and $\tau_{\mathrm{L}}$ the upper-state lifetime of the gain medium (Table 2.1.1).
Passively mode-locked dye lasers are based on this mode-locking technique and a more extensive review of ultrashort pulse generation with dye lasers is given in [88Sha, 90Die]. The most important dye laser for sub-100-fs pulse generation is the Colliding Pulse Mode-locked (CPM) laser [81For]. The design considerations of such a laser are very well described in [86Val]. This laser is based on Rhodamin 6G as the gain medium and on DODCI as the absorber [72Ipp]. From Table 2.1.12 follows that the conditions (2.1.56)-(2.1.58) are only fulfilled if the mode area in the absorber jet is smaller than in the gain jet. In addition, a six-mirror ring cavity design where the absorber and the gain jet are separated by $1 / 4$ of the resonator round trip gives the two counter-propagating pulses the same gain and the absorber is more strongly saturated because of the two pulses colliding inside the saturable absorber jet (i.e. Colliding Pulse Mode-locking - CPM). This effectively shortens the pulses and increases the stability. The best performance of this laser was only obtained after both the gain and the absorber dyes have been freshly prepared, because both photodegrade within a relatively short time (i.e. 1-3 weeks). The best result was 27 fs pulses at a center wavelength of 620 nm with an average output power of 20 mW each in two output beams at a pulse repetition rate of 100 MHz [85Val, 86 Val . More typically, this laser produced slightly below 100 fs pulses. This laser was the "work horse" for all the pioneering work on sub-100-fs spectroscopy for nearly 10 years in the 1980's. However, the rather large maintenance of this laser explains the success of the Ti:sapphire laser at the beginning of the 1990's. Today, solid-state lasers with much shorter pulses, higher output powers and better stability have replaced practically all ultrafast dye laser systems.

Another important application of this mode-locking technique are semiconductor lasers, which also have an upper-state lifetime in the nanosecond regime and a large gain cross section in the range of $10^{-14} \mathrm{~cm}^{2}$. A more extensive recent review of ultrashort pulse generation with semiconductor lasers is given in [95Jia, 95Vai]. The CPM technique, as developed for dye lasers, has been also used for passively mode-locked semiconductor lasers [81Zie, 86Vas]. Wu and Chen et al. [90Wu, 92Che] monolithically incorporated the CPM technique in quantum-well lasers. Pulses of 0.64 ps at a repetition rate of 710 MHz were generated [91Che].

The master equation for this mode-locking mechanism (Fig. 2.1.5a) is given by [75Hau3, 94Ipp]:

$$
\begin{equation*}
\sum_{i} \Delta A_{i}=\left[g(t)-q(t)+\frac{g_{0}}{\Omega_{\mathrm{g}}^{2}} \frac{\mathrm{~d}^{2}}{\mathrm{~d} t^{2}}+t_{\mathrm{D}} \frac{\mathrm{~d}}{\mathrm{~d} t}\right] A(T, t)=0 \tag{2.1.59}
\end{equation*}
$$

For a self-consistent solution we will have to include a time shift $t_{\mathrm{D}}$ of the pulse envelope due to the saturation of the absorber. $g(t)$ and $q(t)$ are given by the slow-saturation approximation (2.1.14).

For an analytical solution we have to expand the exponential function up to the second order, i.e. $\mathrm{e}^{x} \approx 1+x+\frac{x^{2}}{2}:$

$$
\begin{align*}
q(t) & =q_{0} \exp \left[-\frac{\sigma_{\mathrm{A}}}{A_{\mathrm{A}} h \nu} \int_{-\infty}^{t}\left|A\left(t^{\prime}\right)\right|^{2} \mathrm{~d} t^{\prime}\right] \\
& \approx q_{0}\left[1-\frac{\sigma_{\mathrm{A}}}{A_{\mathrm{A}} h \nu} \int_{-\infty}^{t}\left|A\left(t^{\prime}\right)\right|^{2} \mathrm{~d} t^{\prime}+\frac{\sigma_{\mathrm{A}}^{2}}{2\left(A_{\mathrm{A}} h \nu\right)^{2}}\left(\int_{-\infty}^{t}\left|A\left(t^{\prime}\right)\right|^{2} \mathrm{~d} t^{\prime}\right)^{2}\right] \tag{2.1.60}
\end{align*}
$$

and analogous for $g(t)$. In this case we can obtain an analytical solution with a sech ${ }^{2}$-pulse shape:

$$
\begin{equation*}
A(t)=A_{0} \operatorname{sech}\left(\frac{t}{\tau}\right) \tag{2.1.61}
\end{equation*}
$$

and a FWHM pulse duration

$$
\begin{equation*}
\tau_{\mathrm{p}} \approx 1.76 \times \frac{4}{\pi} \frac{1}{\Delta \nu_{\mathrm{g}}} \tag{2.1.62}
\end{equation*}
$$

where $\Delta \nu_{\mathrm{g}}$ is the FWHM gain bandwidth of the laser. In (2.1.62) the conditions (2.1.56)-(2.1.58) are assumed and in addition $E_{\mathrm{sat}, \mathrm{L}} \gg E_{\mathrm{sat}, \mathrm{A}}$ and $E_{\mathrm{p}} \gg E_{\mathrm{sat}, \mathrm{A}}$ (i.e. a fully saturated absorber).

For the example of Rhodamin 6G and DODCI (Table 2.1.12) we then obtain for a gain bandwidth of $\Delta \nu_{\mathrm{g}} \approx 4 \times 10^{13} \mathrm{~Hz}$ a pulse duration of about 56 fs (2.1.62). Pulses as short as 27 fs have been demonstrated [85Val]. However, it was recognized early on that SPM together with negative dispersion results in soliton formation and further reduces pulse duration by about a factor of 2 in dye lasers [ 84 Mar , 85 Mar ]. This would explain the difference in the theoretical prediction of (2.1.62) from the experimentally demonstrated 27 fs. However, at that time an analytic solution for the pulse-shortening effect was not presented.

For semiconductor lasers we typically observe strongly chirped pulses [95Jia]. Therefore, we would have to include dispersion and self-phase modulation in the rate equation. This is not so easy because we would have to also include the refractive-index change that occurs during gain saturation.

### 2.1.6.5 Passive mode-locking with a fast saturable absorber

In passive mode-locking the loss modulation is obtained by Self-Amplitude Modulation (SAM), where the pulse saturates an absorber, for example. In the ideal case, the SAM follows the intensity profile of the pulse. This is the case of an ideal fast saturable absorber. In this case, SAM produces a much larger curvature of loss modulation than in the sinusoidal loss modulation of active modelocking, because the mode-locked pulse duration is much shorter than the cavity round-trip time. Therefore, we would expect from the previous discussion of active mode-locking, that we obtain much shorter pulses with passive mode-locking. This is indeed observed.

In the fast saturable absorber model no dynamic gain saturation is required and the short netgain window is formed by a fast recovering saturable absorber alone (Fig. 2.1.5b). This was initially believed to be the only stable approach to passively mode-lock solid-state lasers with long upperstate lifetimes. Additive Pulse Mode-locking (APM) was the first fast saturable absorber for such solid-state lasers (Sect. 2.1.4.4.2). However, APM required interferometric cavity-length stabilization. Kerr-Lens Mode-locking (KLM) [91Spe] (Sect. 2.1.4.4.3) was the first useful demonstration of an intracavity fast saturable absorber for a solid-state laser and because of its simplicity replaced
coupled cavity mode-locking techniques. KLM is very close to an ideal fast saturable absorber, where the modulation depth is produced either by the decreased losses because of self-focusing through a hard aperture [91Kel, $91 \mathrm{Sall}, 91 \mathrm{Neg}$ ] or by increased gain in the laser as a result of an increased overlap of the laser mode with the pump mode in the laser crystal [93Pic]. Only in the ultrashort pulse regime of a few optical cycles more complicated space-time coupling occurs and wavelength-dependent effects start to limit further pulse reduction.

Besides the tremendous success of KLM, there are some significant limitations for practical or "real-world" ultrafast lasers. First, the cavity is typically operated near one end of its stability range, where the Kerr-lens-induced change of the beam diameter is large enough to sustain modelocking. This results in a requirement for critical cavity alignment where mirrors and the laser crystal have to be positioned to an accuracy of several hundred microns typically. Once the cavity is correctly aligned, KLM can be very stable and under certain conditions even self-starting. However, self-starting KLM lasers in the sub-50-fs regime have not yet been demonstrated without any additional starting mechanisms. This is not surprising, since in a $10-\mathrm{fs}$ Ti:sapphire laser with a 100 MHz repetition rate, the peak power changes by 6 orders of magnitude when the laser switches from cw to pulsed operation. Therefore, nonlinear effects that are still effective in the sub-10-fs regime are typically too small to initiate mode-locking in the cw-operation regime. In contrast, if self-starting is optimized, KLM tends to saturate in the ultrashort pulse regime or the large Self-Phase Modulation (SPM) will drive the laser unstable.

For an ideal fast saturable absorber, Haus et al. [92Hau] developed an analytic solution for the pulse width starting with the following master equation:

$$
\begin{equation*}
\sum_{i} \Delta A_{i}=\left[g\left(1+\frac{1}{\Omega_{\mathrm{g}}^{2}} \frac{\partial^{2}}{\partial t^{2}}\right)-l+\gamma_{\mathrm{A}}|A|^{2}\right] A(T, t)=0 \tag{2.1.63}
\end{equation*}
$$

not taking into account GVD and SPM. The solution is an unchirped sech ${ }^{2}$-pulse shape

$$
\begin{equation*}
P(t)=P_{0} \operatorname{sech}^{2}\left(\frac{t}{\tau}\right) \tag{2.1.64}
\end{equation*}
$$

with a FWHM pulse width:

$$
\begin{equation*}
\tau_{\mathrm{p}}=1.7627 \cdot \tau=1.7627 \frac{4 D_{\mathrm{g}}}{\gamma_{\mathrm{A}} E_{\mathrm{p}}} \tag{2.1.65}
\end{equation*}
$$

where $P_{0}$ is the peak power of the pulse, $E_{\mathrm{p}}$ is the intracavity pulse energy and $D_{\mathrm{g}}$ is the gain dispersion of the laser medium (2.1.32).

The shortest possible pulses can be obtained when we use the full modulation depth of the fast saturable absorber. We only obtain an analytic solution if we assume an ideal fast absorber that saturates linearly with the pulse intensity (2.1.18) over the full modulation depth. This is clearly a strong approximation because (2.1.18) only holds for weak absorber saturation. For a maximum modulation depth and this linear approximation we then can assume that $\gamma_{\mathrm{A}} P_{0}=q_{0}$. For a sech $^{2}$-shaped pulse (2.1.64), the pulse energy is given by

$$
\begin{equation*}
E_{\mathrm{p}}=\int I(t) \mathrm{d} t=2 \tau P_{0} \tag{2.1.66}
\end{equation*}
$$

The minimal pulse width for a fully saturated ideal fast absorber then follows from (2.1.65):

$$
\begin{equation*}
\tau_{p, \text { min }}=\frac{1.7627}{\Omega_{\mathrm{g}}} \sqrt{\frac{2 g}{q_{0}}} \tag{2.1.67}
\end{equation*}
$$

This occurs right at the stability limit when the filter loss due to gain dispersion is equal to the residual loss a soliton undergoes in an ideal fast saturable absorber (2.1.19):

Filter loss $=\frac{D_{\mathrm{g}}}{3 \tau^{2}}=\frac{q_{0}}{3}=q_{\mathrm{s}}=$ residual saturable absorber loss .
The residual saturable absorber loss $q_{\mathrm{s}}$ results from the fact that the soliton pulse initially experiences loss to fully saturate the absorber (see Sect. 2.1.4.2.2). This residual loss is exactly $q_{0} / 3$ for a sech ${ }^{2}$-pulse shape and a fully saturated ideal fast saturable absorber. This condition results in a minimal FWHM pulse duration given by (2.1.67).

Including GVD and SPM, i.e. soliton formation, in the fast saturable absorber model, an additional pulse shortening of a factor of 2 was predicted. However, unchirped soliton pulses (i.e. ideal sech ${ }^{2}$-shaped pulses) are only obtained for a certain negative dispersion value given by

$$
\begin{equation*}
\frac{|D|}{\delta_{\mathrm{L}}}=\frac{D_{\mathrm{g}}}{\gamma_{\mathrm{A}}} . \tag{2.1.69}
\end{equation*}
$$

This is also where we obtain the shortest pulses with a fast saturable absorber. Here we assume that higher-order dispersion is fully compensated or negligibly small. In addition, computer simulations show that too much self-phase modulation drives the laser unstable.

KLM is well described by the fast absorber mode-locking model discussed above even though it is not so easy to determine the exact saturable absorber parameters such as the effective saturation fluence. However, the linearized model does not describe the pulse generation with Ti:sapphire lasers in the sub-10-fs regime very well. Pulse-shaping processes in these lasers are more complex [91Bra, 92Kra2]. Under the influence of the different linear and nonlinear pulse shaping mechanisms, the pulse is significantly broadened and recompressed, giving rise to a "breathing" of the pulse width. The order of the pulse shaping elements in the laser cavity becomes relevant and the spectrum of the mode-locked pulses becomes more complex. In this case, an analytical solution can no longer be obtained. As a rough approximation, the pulses still behave like solitons and consequently these lasers are also called solitary lasers [91Bra].

### 2.1.6.6 Passive mode-locking with a slow saturable absorber without gain saturation and soliton formation

Over many years we consistently observed in experiments that even without soliton effects the pulse duration can be much shorter than the absorber recovery time in SESAM mode-locked solidstate lasers. It has always been postulated that without soliton pulse shaping, we need to have a fast saturable absorber for stable mode-locking, which is in disagreement with our experimental observations. More recently, we therefore performed some more detailed numerical investigations [01Pas1]. For a strongly saturated slow absorber with a saturation parameter $S>3$ and an absorber recovery time smaller than 10 to 30 times the pulse duration, we found a useful guideline for the predicted pulse duration

$$
\begin{equation*}
\tau_{p, \min } \approx \frac{1.5}{\Delta \nu_{\mathrm{g}}} \sqrt{\frac{g}{\Delta R}} \tag{2.1.70}
\end{equation*}
$$

We neglected similar to the ideal fast saturable absorber mode-locking model, the effects of Kerr nonlinearity and dispersion in the cavity, phase changes on the absorber and spatial hole burning in the gain medium. Compared to the analytical solution of a fully saturated absorber (2.1.67) we would predict a slightly longer pulse duration given by a factor of about 1.3. Otherwise, the dependence with regards to gain saturation, gain bandwidth and absorber modulation depth has been explained very well with the analytical solution.

Numerical simulations show that the pulse duration in (2.1.70) can be significantly shorter than the absorber recovery time and has little influence on the pulse duration as long as $\tau_{\mathrm{A}}<10 \tau_{\mathrm{p}}$
to $30 \tau_{\mathrm{p}}$. Numerical simulations show that this is a reasonable estimate and that with too long recovery time, the pulse does not simply become longer but unstable.

At first this long recovery time might be surprising, because on the trailing edge of the pulse there is no shaping action of the absorber. There is even net gain, because the loss caused by the absorber is very small for the trailing edge (always assuming a fully saturated absorber), while the total loss for the pulse is larger and is balanced by the saturated gain in steady state. Thus, one might expect that this net gain after the pulse would destabilize the pulse - but this is not the case. The reason is that the pulses experience a temporal shift by the absorber, which limits the time in which noise behind the pulse can be amplified. The absorber attenuates mostly the leading wing of the pulse, thus shifting the pulse center backwards in each cavity round trip. This means that the pulse is constantly moving backward and swallows any noise growing behind itself. An upper limit on the recovery time than follows from the condition that this noise cannot grow too much. Note that weak reflections in the laser cavity could generate weak satellite pulses behind the main pulse. These satellite pulses could be stronger than the noise level and thus significantly reduce maximum tolerable recovery time of the absorber.

So far we have not included any additional pulse-shaping effects such as SPM or solitons. Further simulations show that SPM alone in the positive dispersion regime should always be kept small because it always makes pulses longer and even destabilizes them, particularly for absorbers with small modulation depth [01Pas1]. This result might be surprising at first - but again the temporal delay caused by the absorber gives a simple explanation. SPM (with positive $n_{2}$, as is the usual case) decreases the instantaneous frequency in the leading wing and increases the frequency in the trailing wing. The absorber always attenuates the leading wing, thus removing the lower frequency components, which results in an increased center frequency and broader pulses due to the decrease in pulse bandwidth. For strong SPM the pulses become unstable. A rule of thumb is that the nonlinear phase shift for the peak should be at most a few mrad per $1 \%$ of modulation depth. It is clear that SPM could hardly be made weak enough in the sub-picosecond regime. For this reason, soliton mode-locking is usually required in the sub-picosecond domain, because there the nonlinear phase changes can be much larger.

### 2.1.6.7 Soliton mode-locking

In soliton mode-locking, the pulse shaping is done solely by soliton formation, i.e. the balance of Group-Velocity Dispersion (GVD) and Self-Phase Modulation (SPM) at steady state, with no additional requirements on the cavity stability regime as for example for KLM. In contrast to KLM we use only the time-dependent part of the Kerr effect at the peak intensity (i.e. $\left.n(t)=n+n_{2} I_{0}(t),(2.1 .42)\right)$ and not the radially dependent part as well (i.e. $n(r, t)=n+n_{2} I(r, t)$, (2.1.42)). The radially dependent part of the Kerr effect is responsible for KLM because it forms the nonlinear lens that reduces the beam diameter at an intracavity aperture inside the gain medium. Thus, this nonlinear lens forms an effective fast saturable absorber because the intensity-dependent beam-diameter reduction at an aperture introduces less loss at high intensity and more loss at low intensity. Such a radially dependent effective saturable however couples the mode-locking mechanism with the cavity mode. In contrast, soliton mode-locking does not depend on the transverse Kerr effect and has therefore the advantage that the mode-locking mechanism is decoupled from the cavity design and no critical cavity stability regime is required - it basically works over the full cavity stability range.

In soliton mode-locking, an additional loss mechanism, such as a saturable absorber [95Kae1], or an acousto-optic modulator [95Kae2], is necessary to start the mode-locking process and to stabilize the soliton pulse-forming process. In soliton mode-locking, we have shown that the netgain window (Fig. 2.1.5c) can remain open for significantly more than 10 times longer than the ultrashort pulse, depending on the specific laser parameters [95Jun2, 96Kae]. This strongly relaxes
the requirements on the saturable absorber and we can obtain ultrashort pulses even in the 10 -fs regime with semiconductor saturable absorbers that have much longer recovery times. With the same modulation depth, one can obtain almost the same minimal pulse duration as with a fast saturable absorber, as long as the absorber recovery time is roughly less than ten times longer than the final pulse width. In addition, high dynamic range autocorrelation measurements showed excellent pulse pedestal suppression over more than seven orders of magnitude in 130 -fs pulses of a Nd:glass laser [95Kop1] and very similar to or even better than KLM pulses in the 10 -fs pulse width regime [97Jun2]. Even better performance can be expected if the saturable absorber also shows a negative refractive-index change coupled with the absorption change as is the case for semiconductor materials [96Kae].

With a slow saturable absorber as a starting and stabilizing mechanism for soliton mode-locking, there remains a time window with net round-trip gain behind the pulse, where the loss of the still saturated absorber is smaller than the total loss for the pulse that is balancing the saturated gain. At a first glance it may seem that the discussion in the last section, Sect. 2.1.6.6, with slow saturable absorbers would apply here as well. However, there is another limiting effect which usually becomes more effective in soliton mode-locked lasers: The dispersion causes the background to temporally broaden and thus permanently loosing the energy in those parts which drift into the time regions with net loss.

We can describe soliton mode-locking by the Haus's master equation formalism, where we take into account GVD, SPM and a slow saturable absorber $q(T, t)$ that recovers slower than the pulse duration (see Fig. 2.1.5c) [95Kae1, 96Kae]:

$$
\begin{align*}
\sum_{i} \Delta A_{i} & =\left[-\mathrm{i} D \frac{\partial^{2}}{\partial t^{2}}+\mathrm{i} \delta_{\mathrm{L}}|A(T, t)|^{2}\right] A(T, t)+\left[g-l+D_{\mathrm{g}} \frac{\partial^{2}}{\partial t^{2}}-q(T, t)\right] A(T, t) \\
& =0 \tag{2.1.71}
\end{align*}
$$

This differential equation can be solved analytically using soliton perturbation theory. The first bracket term of this differential equation determines the nonlinear Schrödinger equation for which the soliton pulse is a stable solution for negative GVD (i.e. $D<0$ ) and positive SPM (i.e. $n_{2}>0$ ):

$$
\begin{equation*}
A(z, t)=A_{0} \operatorname{sech}\left(\frac{t}{\tau}\right) \mathrm{e}^{-\mathrm{i} \phi_{\mathbf{s}}(z)} \tag{2.1.72}
\end{equation*}
$$

This soliton pulse propagates without distortion through a medium with negative GVD and positive SPM because the effect of SPM exactly cancels that due to dispersion. The FWHM soliton pulse duration is given by $\tau_{\mathrm{p}}=1.7627 \cdot \tau$ and the time-bandwidth product by $\Delta \nu_{\mathrm{p}} \tau_{\mathrm{p}}=0.3148 . \phi_{\mathrm{s}}(z)$ is the phase shift of the soliton during propagation along the $z$-axis

$$
\begin{equation*}
\phi_{\mathrm{s}}(z)=\frac{1}{2} k n_{2} I_{0} z \equiv \frac{1}{2} \phi_{\mathrm{nl}}(z), \tag{2.1.73}
\end{equation*}
$$

where $I_{0}$ is the peak intensity inside the SPM medium (i.e. typically the gain medium). Thus, the soliton pulse experiences during propagation a constant phase shift over the full beam profile. For a given negative dispersion and an intracavity pulse energy $E_{\mathrm{p}}$ we obtain a pulse duration

$$
\begin{equation*}
\tau_{\mathrm{p}}=1.7627 \frac{2|D|}{\delta_{\mathrm{L}} E_{\mathrm{p}}} \tag{2.1.74}
\end{equation*}
$$

for which the effects of SPM and GVD are balanced with a stable soliton pulse.
This soliton pulse looses energy due to gain dispersion and losses in the cavity. Gain dispersion and losses can be treated as perturbation to the nonlinear Schrödinger equation for which a soliton is a stable solution (i.e. second bracket term in (2.1.71)). This lost energy, called continuum in soliton perturbation theory, is initially contained in a low-intensity background pulse, which experiences negligible SPM, but spreads in time due to GDD (Fig. 2.1.17a). In soliton mode-locking a stable


Fig. 2.1.17. Soliton mode-locking in (a) time and (b) frequency domain. The continuum pulse spreads in time due to group velocity dispersion and thus undergoes more loss in the relatively slow absorber, which is saturated by the shorter soliton pulse. However, the longer continuum pulse has a narrower spectrum and thus undergoes more gain than the spectrally broader soliton pulse.
soliton pulse is formed for all group delay dispersion values as long as the continuum loss is larger than the soliton loss [96Kae] or the pulses break up in two or more pulses [97Aus]. Thus, for smaller negative dispersion the pulse duration becomes shorter (2.1.74) until minimal pulse duration is reached. With no pulse-break-up, the minimal pulse duration is given when the loss for the continuum pulse becomes equal to the loss of the soliton pulse. When the soliton pulse is stable, then the saturated gain is equal to the loss:

$$
\begin{equation*}
g=l+l_{\mathrm{s}} \quad \text { with } \quad l_{\mathrm{s}}=\frac{D_{\mathrm{g}}}{3 \tau^{2}}+q_{0} \frac{E_{\mathrm{sat}, \mathrm{~A}}}{E_{\mathrm{p}}}\left[1-\exp \left(-\frac{E_{\mathrm{p}}}{E_{\mathrm{sat}, \mathrm{~A}}}\right)\right] \tag{2.1.75}
\end{equation*}
$$

where $l$ is the total saturated amplitude loss coefficient per cavity round trip (i.e. output coupler, residual cavity losses and nonsaturable absorber loss of the saturable absorber) and $l_{\mathrm{s}}$ the additional loss experienced by the soliton as a result of gain filtering (2.1.68) and the amplitude loss coefficient for saturation of the slow absorber (2.1.15). Soliton perturbation theory then determines the roundtrip loss of the continuum pulse [96Kae]. The continuum is spread in time because of dispersion and therefore experiences enhanced loss in the recovering absorber that has been saturated by the much shorter soliton pulse.

We then predict a minimum pulse duration for a soliton pulse [95Kae1, 96Kae]:

$$
\begin{equation*}
\tau_{\mathrm{p}, \min }=1.7627\left(\frac{1}{\sqrt{6} \Omega_{\mathrm{g}}}\right)^{3 / 4} \phi_{\mathrm{s}}^{-1 / 8}\left(\frac{\tau_{\mathrm{A}} g^{3 / 2}}{q_{0}}\right)^{1 / 4} \approx 0.45\left(\frac{1}{\Delta \nu_{\mathrm{g}}}\right)^{3 / 4}\left(\frac{\tau_{\mathrm{A}}}{\Delta R}\right)^{1 / 4} \frac{g^{3 / 8}}{\phi_{\mathrm{s}}^{1 / 8}} \tag{2.1.76}
\end{equation*}
$$

where $\phi_{\mathrm{s}}$ is the phase shift of the soliton per cavity round trip (assuming that the dominant SPM occurs in the laser gain medium), $\Delta \nu_{\mathrm{g}}$ the FWHM gain bandwidth and $\Delta R \approx 2 q_{0}$ (2.1.6). With (2.1.73) then follows $\phi_{\mathrm{s}}=\phi_{\mathrm{s}}\left(z=2 L_{\mathrm{g}}\right)=k n_{2} L_{\mathrm{g}} I_{0, \mathrm{~L}}=\frac{1}{2} \delta_{\mathrm{L}} P_{0}$, where $\delta_{\mathrm{L}}$ is the SPM coefficient (2.1.47) and $P_{0}$ the peak power inside the laser cavity. In (2.1.76) we assume a fully saturated slow saturable absorber and a linear approximation for the exponential decay of the slow saturable absorber. The analytical solution for soliton mode-locking (2.1.76) has been experimentally confirmed with a Ti:sapphire laser where a Fabry-Perot filter has been inserted to give a well-defined gain bandwidth [95Jun2]. However, this equation still does not tell us what soliton phase shift would be ideal. Equation (2.1.76) would suggest that very high values are preferred, which actually leads to instabilities. Also this equation is not taking into account that the soliton pulse may break up into two solitons which occurs more easily if the absorber is too strongly saturated. Numerical simulations can give better estimates for these open questions [01Pas1].

In soliton mode-locking, the dominant pulse-formation process is assumed to be soliton formation. Therefore, the pulse has to be a soliton for which the negative GVD is balanced with the SPM inside the laser cavity. The pulse duration is then given by the simple soliton solution (2.1.74). This means that the pulse duration scales linearly with the negative group delay dispersion inside the laser cavity (i.e. $\tau_{\mathrm{p}} \propto|D|$ ). In the case of an ideal fast saturable absorber, an unchirped soliton pulse is only obtained at a very specific dispersion setting (2.1.69), whereas for soliton mode-locking an unchirped transform-limited soliton is obtained for all dispersion levels as long as the stability requirement against the continuum is fulfilled. This fact has been also used to experimentally confirm that soliton mode-locking is the dominant pulse-formation process and not a fast saturable absorber such as KLM [97Aus]. Higher-order dispersion only increases the pulse duration, therefore it is undesirable and is assumed to be compensated.

Solitons alone in the cavity are not stable. The continuum pulse is much longer and therefore experiences only the gain at line center, while the soliton exhibits an effectively lower average gain due to its larger bandwidth. Thus, the continuum exhibits a higher gain than the soliton. After a sufficient build-up time, the continuum would actually grow until it reaches lasing threshold, destabilizing the soliton. However, we can stabilize the soliton by introducing a relatively slow saturable absorber into the cavity. This absorber is fast enough to add sufficient additional loss for the growing continuum that spreads in time during its build-up phase so that it no longer reaches lasing threshold.

The break-up into two or even three pulses can be explained as follows: Beyond a certain pulse energy, two soliton pulses with lower power, longer duration, and narrower spectrum will be preferred, since their loss introduced by the limited gain bandwidth decreases so much that the slightly increased residual loss of the less saturated saturable absorber cannot compensate for it. This results in a lower total round-trip loss and thus a reduced saturated or average gain for two pulses compared to one pulse. The threshold for multiple pulsing is lower for shorter pulses, i.e. with spectra which are broad compared to the gain bandwidth of the laser. A more detailed description of multiple pulsing is given elsewhere [98Kae]. Numerical simulations show, however, that the tendency for pulse break-up in cases with strong absorber saturation is found to be significantly weaker than expected from simple gain/loss arguments [01Pas1].

To conclude, soliton shaping effects can allow for the generation of significantly shorter pulses, compared to cases without SPM and dispersion. The improvement is particularly large for absorbers with a relatively low modulation depth and when the absorber recovery is not too slow. In this regime, the pulse shaping is mainly done by the soliton effects, and the absorber is only needed to stabilize the solitons against growth of the continuum. The absorber parameters are generally not very critical. It is important not only to adjust the ratio of dispersion and SPM to obtain the desired soliton pulse duration (2.1.74), but also to keep their absolute values in a reasonable range where the nonlinear phase change is in the order of a few hundred mrad per round trip (i.e. significantly larger than acceptable in cases without negative dispersion). Soliton formation is generally very important in femtosecond lasers, which has been already recognized in colliding pulse mode-locked dye lasers. However, no analytic solution was presented for the soliton pulse shortening. It was always assumed that for a stable solution the mode-locking mechanism without soliton effects has to generate a net gain window as short as the pulse (Fig. 2.1.5a and b). In contrast to these cases, in soliton mode-locking we present an analytic solution based on soliton perturbation theory, where soliton pulse shaping is clearly assumed to be the dominant pulse formation process, and the saturable absorber required for a stable solution is treated as a perturbation. Then, the net gain window can be much longer than the pulse (Fig. 2.1.5c). Stability of the soliton against the continuum then determines the shortest possible pulse duration. This is a fundamentally different mode-locking model than previously described. We therefore refer to it as soliton mode-locking, emphasizing the fact that soliton pulse shaping is the dominant factor.

### 2.1.6.8 Design guidelines to prevent $Q$-switching instabilities

For picosecond solid-state lasers the self-amplitude modulation of a saturable absorber with a picosecond or tens of picoseconds recovery time is sufficient for stable pulse generation. A picosecond recovery time can be achieved with low-temperature grown semiconductor saturable absorbers where mid-gap defect states form very efficient traps for the photoexcited electrons in the conduction band (Sect. 2.1.4.3) . In the picosecond regime, we developed a very simple stability criterion for stable passive mode-locking without $Q$-switching instabilities [99Hoe1]:

$$
\begin{equation*}
E_{\mathrm{p}}^{2}>E_{\mathrm{p}, \mathrm{c}}^{2}=E_{\mathrm{sat}, \mathrm{~L}} E_{\mathrm{sat}, \mathrm{~A}} \Delta R . \tag{2.1.77}
\end{equation*}
$$

The critical intracavity pulse energy $E_{\mathrm{p}, \mathrm{c}}$ is the minimum intracavity pulse energy, which is required to obtain stable cw mode-locking, that is, for $E_{\mathrm{p}}>E_{\mathrm{p}, \mathrm{c}}$ we obtain stable cw mode-locking and for $E_{\mathrm{p}}<E_{\mathrm{p}, \mathrm{c}}$ we obtain $Q$-switched mode-locking. For good stability of a mode-locked laser against unwanted fluctuations of pulse energy, operation close to the stability limit is not recommended. Thus, a large modulation depth supports shorter pulses (Table 2.1.11), but an upper limit is given by the onset of self- $Q$-switching instabilities (2.1.77).

In the femtosecond regime, we observe a significant reduction of the tendency of $Q$-switching instabilities compared to pure saturable absorber mode-locked picosecond lasers (2.1.77). This can be explained as follows: If the energy of an ultrashort pulse rises slightly due to relaxation oscillations, SPM and/or SAM broadens the pulse spectrum. A broader pulse spectrum, however, increases the loss due to the finite gain bandwidth, (2.1.68) and (2.1.74), which provides some negative feedback, thus decreasing the critical pulse energy which is necessary for stable cw modelocking. The simple stability requirement of (2.1.77) then has to be modified as follows [99Hoe1]:

$$
\begin{equation*}
E_{\mathrm{sat}, \mathrm{~L}} g K^{2} E_{\mathrm{p}}^{2}+E_{\mathrm{p}}^{2}>E_{\mathrm{sat}, \mathrm{~L}} E_{\mathrm{sat}, \mathrm{~A}} \Delta R \tag{2.1.78}
\end{equation*}
$$

where $K$ is given by

$$
\begin{equation*}
K \equiv \frac{0.315}{1.76} \frac{2 \pi n_{2} L_{\mathrm{g}}}{D A_{\mathrm{L}} \lambda_{0} \Delta \nu_{\mathrm{g}}} \tag{2.1.79}
\end{equation*}
$$

Here we assume a standing-wave cavity and that the dominant SPM is produced in the laser medium. In other cases we have to add all other contributions as well.

Theoretical results for the QML threshold, (2.1.77)-(2.1.79), have generally been found to be in good agreement with experimental values. However, inverse saturable absorption can show some significant improvement of the QML threshold. Two-Photon Absorption (TPA) has been widely used for optical power limiter [86Wal] and a roll-over which lowers the $Q$-switching threshold [99Tho]. In addition, for some recent high-repetition-rate lasers [04Pas] the QML threshold was found to be significantly lower than expected even taking into account TPA. It was shown that for some Er: Yb:glass lasers this could be explained with modified saturation characteristics of the used SESAMs, namely with a roll-over of the nonlinear reflectivity for higher pulse fluences [04Sch1]. However, for picosecond pulse durations TPA cannot explain the observed significant roll-over (Fig. 2.1.18). The reflectivity of a SESAM is generally expected to increase with increasing pulse energy. However, for higher pulse energies the reflectivity can decrease again; we call this a "rollover" of the nonlinear reflectivity curve caused by inverse saturable absorption (Fig. 2.1.18). We showed for several SESAMs that the measured roll-over is consistent with TPA only for short (femtosecond) pulses, while a stronger kind of nonlinear absorption is dominant for longer (picosecond) pulses [05Gra2]. The QML threshold criteria of (2.1.77) then have to be modified to [05Gra2]

$$
\begin{equation*}
E_{\mathrm{p}}^{2}>\frac{E_{\mathrm{sat}, \mathrm{~A}} \Delta R}{\frac{1}{E_{\mathrm{sat}, \mathrm{~L}}}+\frac{1}{A_{\mathrm{A}} F_{2}}} \tag{2.1.80}
\end{equation*}
$$



Fig. 2.1.18. Nonlinear reflectivity as function of saturation parameter $S$ which is equal to $F_{\mathrm{p}} / F_{\text {sat, } \mathrm{A}}$. $F_{\mathrm{p}}$ is the pulse fluence incident on the absorber mirror (i.e. pulse energy density) and $F_{\text {sat, } \mathrm{A}}$ is the saturation fluence of the absorber mirror. Inverse saturable absorption decreases the reflectivity at higher pulse energies such that a "roll-over" is observed. This decreases the effective modulation depth and increases the effective nonsaturable absorption. However, it improves the $Q$-switching mode-locking threshold.

For $F_{2} \rightarrow \infty$ (i.e. without induced nonlinear losses) we retrieve the simpler equation (2.1.77). $F_{2}$ is the inverse slope of the induced absorption effect and can be determined from nonlinear SESAM reflectivity measurements (Fig. 2.1.18) [05Gra2, 04Hai]:

$$
\begin{equation*}
R_{\mathrm{ISA}}\left(F_{\mathrm{p}}\right)=R\left(F_{\mathrm{p}}\right)-\frac{F_{\mathrm{p}}}{F_{2}}, \tag{2.1.81}
\end{equation*}
$$

where $F_{\mathrm{p}}$ is the pulse fluence incident on the SESAM (i.e. pulse energy density), $R\left(F_{\mathrm{p}}\right)$ the measured nonlinear reflectivity without Inverse Saturable Absorption (ISA) and $R_{\text {ISA }}\left(F_{\mathrm{p}}\right)$ the measured reflectivity with inverse saturable absorption. The smaller the inverse slope of the roll-over $F_{2}$, the stronger is the roll-over. The stronger the roll-over, the smaller the maximum modulation depth of the SESAM.

### 2.1.6.9 External pulse compression

SPM generates extra frequency components. The superposition with the other frequency components in the pulse can spectrally broaden the pulse (i.e. for positively chirped pulses assuming $\left.n_{2}>0\right)$. SPM alone does not modify the pulse width, but with proper dispersion compensation a much shorter pulse can be generated with the extra bandwidth [ 80 Mol ]. The positively chirped spectrally broadened pulse then can be compressed with appropriate negative dispersion compensation, where the "blue" spectral components have to be advanced relative to the "red" ones. A careful balance between a nonlinear spectral broadening process and negative dispersion is needed for efficient compression of a pulse. Typically, self-phase modulation in a single-mode fiber with optimized length was used to linearly chirp the pulse, which is then compressed with a grating pair compressor [84Tom].

Ultimately, uncompensated higher-order dispersion and higher-order nonlinearities limit compression schemes. For pulses shorter than 100 fs , compression is typically limited to factors of less than 10. Compression of amplified CPM dye laser pulses with 50 fs duration produced the long-standing world record of 6 fs [87For]. Similar concepts have been used for external pulse compression of 13 -fs pulses from a cavity-dumped Ti:sapphire laser [97Bal] and of $20-\mathrm{fs}$ pulses from a Ti:sapphire laser amplifier [97Nis] resulting, in both cases, in approximately 4.5 -fs pulses. In the latter case, the use of a noble-gas-filled hollow fiber instead of a normal fiber allows for much higher pulse energies. For example, pulse energies of about 0.5 mJ with 5.2 -fs pulses and a peak power of 0.1 TW [97Sar]. More recently, adaptive pulse compression of a super-continuum produced in two cascaded hollow fibers generated 3.8 -fs pulses with energies of up to $15 \mu \mathrm{~J}$ [03Sch]. Further improvements resulted in 3.4 -fs pulses but with only 500 nJ pulse energies [03Yam]. The pulse duration was fully characterized by Spectral-Phase Interferometry for Direct Electric-field Reconstruction (SPIDER) (Sect. 2.1.7.3). This is currently the world record in the visible and near-infrared spectral regime.

The extra bandwidth obtained with SPM can be extremely large producing a white-light continuum [83For], which can be used as a seed for broadband parametric amplification. Parametric processes can provide amplification with an even broader bandwidth than can typically be achieved in laser amplifiers. Noncollinear phase-matching at a crossing angle of $3.8^{\circ}$ in beta barium borate (BBO) provides more than 150 THz amplification bandwidth [95Gal]. With this type of set-up, parametric amplification has been successfully demonstrated with pulse durations of less than 5 fs [99Shi, 02Zav].

### 2.1.7 Pulse characterization

### 2.1.7.1 Electronic techniques

Electronic techniques for pulse-width measurements are typically limited to the picosecond regime. Photodetectors and sampling heads with bandwidths up to 60 GHz are commercially available. This means that the measured pulse duration is limited to about 7 ps . This follows from simple linear system analysis for which the impulse response of a photodetector or a sampling head can be approximated by a Gauss-function. The impulse response for a given system bandwidth $B$ has a FWHM $\tau_{\text {FWHM }}$ in units of ps:

$$
\begin{equation*}
\tau_{\mathrm{FWHM}}[\mathrm{ps}] \approx \frac{312 \mathrm{GHz}}{B[\mathrm{GHz}]} . \tag{2.1.82}
\end{equation*}
$$

The impulse response of a measurement system can be determined from the impulse response of each element in the detection chain:

$$
\begin{equation*}
\tau_{\mathrm{FWHM}}^{2}=\sqrt{\tau_{1}^{2}+\tau_{2}^{2}+\tau_{3}^{2}+\ldots} \tag{2.1.83}
\end{equation*}
$$

where for example $\tau_{1}$ is the FWHM of the impulse response of the photodetector, $\tau_{2}$ of the sampling head and so on. Thus, with a 40 GHz sampling head and a 60 GHz photodetector we only measure a impulse response with FWHM of 9.4 ps .

### 2.1.7.2 Optical autocorrelation

Optical autocorrelation techniques with second-harmonic generation of two identical pulses that are delayed with respect to each other are typically used to measure shorter pulses [80Sal, 83 Wei ]. We distinguish between collinear and non-collinear intensity autocorrelation measurements for which the two pulse beams in the nonlinear crystal are either collinear or non-collinear. In the non-collinear case the second-harmonic signal only depends on the pulse overlap and is given by

$$
\begin{equation*}
I_{2 \omega}(\Delta t) \propto \int I(t) I(t-\Delta t) \mathrm{d} t \tag{2.1.84}
\end{equation*}
$$

The FWHM of the autocorrelation signal $I_{2 \omega}(\Delta t)$ is given by $\tau_{\text {Au }}$ and determines the FWHM pulse duration $\tau_{\mathrm{p}}$ of the incoming pulse $I(t)$. However, $\tau_{\mathrm{Au}}$ depends on the specific pulse shape (Table 2.1.13) and any phase information is lost in this measurement. So normally, transformlimited pulses are assumed. This assumption is only justified as long as the measured spectrum also agrees with the assumption of pulse shape and constant phase (i.e. the time-bandwidth product corresponds to a transform-limited pulse, Table 2.1.13). For passively mode-locked lasers, for

Table 2.1.13. Optical pulses: defining equations for Gaussian and soliton pulse shapes, FWHM (full-width-half-maximum) intensity pulse duration $\tau_{\mathrm{p}}$, time-bandwidth products $\Delta \nu_{\mathrm{p}} \tau_{\mathrm{p}}$ for which $\Delta \nu_{\mathrm{p}}$ is the FWHM of the spectral intensity, FWHM intensity autocorrelation pulse duration $\tau_{\text {Au }}$.

| Pulse shape | $\tau_{\mathrm{p}} / \tau$ | $\Delta \nu_{\mathrm{p}} \tau_{\mathrm{p}}$ | $\tau_{\mathrm{p}} / \tau_{\mathrm{Au}}$ |
| :--- | :--- | :--- | :--- |
| Gauss: $I(t) \propto \exp \left(\frac{t^{2}}{\tau^{2}}\right)$ | $2 \sqrt{\ln 2}$ | 0.4413 | 0.7071 |
| Soliton: $I(t) \propto \operatorname{sech}^{2}\left(\frac{t}{\tau}\right)$ | 1.7627 | 0.3148 | 0.6482 |

example, that allow for parabolic approximation of pulse-formation mechanisms one expects a sech $^{2}$ temporal and spectral pulse shape (Sects. 2.1.6.4-2.1.6.7). Passively mode-locked solid-state lasers with pulse durations well above 10 fs normally generate pulses close to this ideal sech ${ }^{2}$ shape. Therefore, this non-collinear autocorrelation technique is a good standard diagnostic for such laser sources. For ultrashort pulse generation in the sub-10-fs regime this is generally not the case anymore. Experimentally, this is clearly indicated by more complex pulse spectra.

Interferometric AutoCorrelation (IAC) techniques [83Min] have been used to get more information. In IAC a collinear intensity autocorrelation is fringe-resolved and gives some indication how well the pulse is transform-limited. However, we still do not obtain full phase information about the pulse. The temporal parameters have usually been obtained by fitting an analytical pulse shape with constant phase to the autocorrelation measurement. Theoretical models of the pulse-formation process motivate the particular fitting function. For lasers obeying such a model the a-priori assumption of a theoretically predicted pulse shape is well-motivated and leads to good estimates of the pulse duration as long as the measured spectrum also agrees with the theoretical prediction. However, we have seen that fits to an IAC trace with a more complex pulse spectrum tend to underestimate the true duration of the pulses. Problems with IAC measurement for ultrashort pulses are also discussed in the two-optical-cycle regime [04Yam].

For few-cycle pulses, a limitation in a noncollinear beam geometry arises because of the finite crossing angle of two beams. In this case the temporal delay between two beams is different in the center and in the wings of the spatial beam profile. This geometrical artifact results in a measured pulse duration that is longer than the actual pulse duration $\tau_{\mathrm{p}}$ :

$$
\begin{equation*}
\tau_{\mathrm{p}, \text { meas }}^{2}=\tau_{\mathrm{p}}^{2}+\delta \tau^{2} \tag{2.1.85}
\end{equation*}
$$

For a beam diameter $d$ and a crossing angle $\theta$ between the two beams this results in an $\delta \tau$ of

$$
\begin{equation*}
\delta \tau=\sqrt{2} \frac{d}{c} \tan \frac{\theta}{2} \approx \frac{\theta d}{\sqrt{2} c} \tag{2.1.86}
\end{equation*}
$$

with the speed of light $c$ and the additional approximation for a small crossing angle $\theta$. For example a crossing angle of $1.7^{\circ}$ and a beam diameter of $30 \mu \mathrm{~m}$ results in $\delta \tau=2.1 \mathrm{fs}$. For an actual pulse duration of 10 fs (resp. 5 fs ) this gives a measured pulse duration of 10.2 fs (resp. 5.4 fs ) which corresponds to an error of $2 \%$ (resp. $8 \%$ ). This means this becomes more severe for pulse durations in the few-cycle regime. However, if the crossing angle is significantly increased this can become also more important for longer pulses. For this reason, in the few-cycle-pulse-width regime collinear geometries have always been preferred to avoid geometrical blurring artifacts and to prevent temporal resolution from being reduced.

### 2.1.7.3 New techniques: FROG, FROG-CRAB, SPIDER, ...

For a more precise measurement, a variety of methods have been proposed to fully reconstruct both pulse amplitude and phase from measured data only [91Chi, 93Kan, 95Chu2, 96Rhe, 98Iac]. Initially, especially Frequency-Resolved Optical Gating (FROG, [93Kan, 97Tre]) and Spectral Phase Interferometry for Direct Electric-field Reconstruction (SPIDER, [98Iac, 99Iac]) have found widespread use.

### 2.1.7.3.1 FROG, SHG-FROG, FROG-CRAB

Frequency-Resolved Optical Gating (FROG) [93Kan, 97Tre] is a characterization method based on the measurement of a spectrally resolved autocorrelation signal followed by an iterative phaseretrieval algorithm to extract the intensity and phase of the laser pulse. In a general sense the FROG technique uses a gate $G(t)$ that is being used to measure the spectrum $S(\omega, \tau)$ of a series of temporal slices:

$$
\begin{equation*}
S(\omega, \tau)=\left|\int G(t-\tau) E(t) \mathrm{e}^{\mathrm{i} \omega t} \mathrm{~d} t\right|^{2} \tag{2.1.87}
\end{equation*}
$$

where $E(t)$ is the electric field of the pulse that needs to be characterized and $\tau$ the time delay between the gate and the pulse. The gate can either be an amplitude or phase gate [93Bec, 03Kan]. The most commonly used FROG is based on an amplitude gate using Second-Harmonic Generation (SHG) and the pulse that needs to be characterized (i.e. "blind FROG" because the gate is unknown):

$$
\begin{equation*}
G(t)=\chi^{(2)} E(t) \tag{2.1.88}
\end{equation*}
$$

This is generally referred to as SHG-FROG. Collinear SHG-FROG has been demonstrated using type II phase matching in the $20-\mathrm{fs}$ [99Fit] and sub-10-fs [00Gal1] pulse-width regime. An example for a phase gate would be cross phase modulation using again the same pulse for the gate:

$$
\begin{equation*}
G(t)=\exp \left(-\mathrm{i} k n_{2}|E(t)|^{2}\right) \tag{2.1.89}
\end{equation*}
$$

The iterative retrieval algorithm is not very intuitive and rather complex and is based on a Principal Component Generalized Projections Algorithm (PCGPA) which starts in an initial guess for $G(t)$ and $E(t)$ that is than being compared to the measured $S(\omega, \tau)$ [99Kan]. For femtosecond pulses in the visible to infrared regime nonlinear optics can be used to obtain very good FROG traces.

In the XUV and attosecond-pulse-width regime this becomes more complicated. We basically need a non-stationary filter in the XUV with a response time on the order of the attosecond-pulse duration. A phase gate can be obtained using photoionization of an atom in the presence of a weak InfraRed (IR) pulse that has been used to generate the attosecond pulses and therefore is precisely synchronized. As long as the XUV pulse is shorter than the IR period the temporal information of the XUV pulse is mapped into the electron energy distribution in the linear part of the optical IR field. This technique is referred to as Frequency-Resolved Optical Gating for Complete Reconstruction of Attosecond Burst (FROG-CRAB) where the linear phase modulation is obtained through the photoionization of atoms by the short XUV pulse in the presence of a weak linear part of the IR field and the spectrometer is being replaced by the electron energy detection [05Mai]. The XUV pulse is then converted in a modulated electron wave packet.

### 2.1.7.3.2 SPIDER

Spectral Phase Interferometry for Direct Electric-field Reconstruction (SPIDER) measures the spectral interference of a pulse with a frequency-shifted replica [98Iac, 99Iac]:

$$
\begin{equation*}
S(\omega, \tau)=\left|\tilde{E}\left(\omega-\omega_{0}\right)+\tilde{E}\left(\omega-\omega_{0}-\delta \omega\right) \mathrm{e}^{\mathrm{i} \omega \tau}\right|^{2} \tag{2.1.90}
\end{equation*}
$$

where $\tilde{E}(\omega)$ is the Fourier-transformation of the electric field $E(t)$. To access the spectral phase it is necessary to produce two time-delayed replicas by a predetermined delay $\tau$ of the pulse and with a spectral shear $\delta \omega$ between their carrier frequencies. The spectral shear between the central frequencies of the two replicas is generated by upconversion of the two replicas with a strongly chirped pulse using sum-frequency generation in a nonlinear optical crystal. The strongly chirped pulse is generated by propagating another copy of the original pulse through a thick glass block. The spectral shear arises because the time delay between the replicas assures that each replica is upconverted with a different portion of the chirped pulse containing a different instantaneous frequency [99Gal]. The time delay $\tau$ between the replica is kept constant during the measurements and therefore only a 1D trace needs to be measured for the resulting SPIDER interferogram

$$
\begin{align*}
I_{\mathrm{SPIDER}}(\omega)= & |\tilde{E}(\omega)|^{2}+|\tilde{E}(\omega+\delta \omega)|^{2} \\
& +2|\tilde{E}(\omega) \tilde{E}(\omega+\delta \omega)| \cos [\varphi(\omega+\delta \omega)-\varphi(\omega)+\omega \tau] \tag{2.1.91}
\end{align*}
$$

The phase information can be extracted from the cosine term by the following, purely algebraic, method: The Fourier transform to the time domain of the SPIDER interferogram consists of a peak at zero time and two side peaks located near $\tau$ and $-\tau$. The two side peaks contain equivalent phase information and are equal. One of the peaks is isolated by applying a suitable filter function and an inverse Fourier transform back to the frequency domain yields a complex function $z(\omega)$, whose complex phase gives access to the pulse spectral phase: $\arg (z(\omega))=\varphi(\omega+\delta \omega)-\varphi(\omega)+\omega \tau$. A separate measurement of the linear phase term $\omega \tau$ by spectral interferometry of the short unsheared pulse replicas is subtracted from the previous expression to yield the spectral phase difference $\Delta \varphi(\omega)=\varphi(\omega+\delta \omega)-\varphi(\omega)$. From an arbitrarily chosen starting frequency $\omega_{0}$ one obtains the spectral phase $\varphi(\omega)$ at evenly spaced frequencies $\omega_{i}=\omega_{0}+i \cdot \delta \omega$ by the following concatenation procedure:

$$
\begin{align*}
& \varphi\left(\omega_{0}\right)=\varphi_{0} \\
& \varphi\left(\omega_{1}\right)=\Delta \varphi\left(\omega_{0}\right)+\varphi\left(\omega_{0}\right)=\varphi\left(\omega_{0}+\delta \omega\right)-\varphi\left(\omega_{0}\right)+\varphi\left(\omega_{0}\right)=\varphi\left(\omega_{0}+1 \cdot \delta \omega\right) \\
& \vdots  \tag{2.1.92}\\
& \varphi\left(\omega_{i+1}\right)=\Delta \varphi\left(\omega_{i}\right)+\varphi\left(\omega_{i}\right)
\end{align*}
$$

The constant $\varphi_{0}$ remains undetermined but is only an offset to the spectral phase, which does not affect the temporal pulse shape and we may thus set it equal to zero. The spectral phase is written as:

$$
\begin{equation*}
\varphi\left(\omega_{i+1}\right)=\sum_{k=0}^{i} \Delta \varphi\left(\omega_{k}\right) \tag{2.1.93}
\end{equation*}
$$

If $\delta \omega$ is small relative to features in the spectral phase, $\Delta \varphi(\omega)$ corresponds in first order to the first derivative of the spectral phase and we can approximate the spectral phase by:

$$
\begin{equation*}
\varphi(\omega) \simeq \frac{1}{\delta \omega} \int_{\omega_{0}}^{\omega} \Delta \varphi\left(\omega^{\prime}\right) \mathrm{d} \omega^{\prime} \tag{2.1.94}
\end{equation*}
$$

The integral expression for the spectral phase has the advantage that all the measured sampling points of the interferogram can be used instead of only using a subset with sampling according
to the spectral shear as with the concatenation method. The phase information of the resulting interferogram allows the direct reconstruction of the spectral phase of the input pulse. Combined with the measured spectrum of the pulse the actual pulse can be calculated without any prior assumptions.

Three design parameters determine the range of pulse durations that can be measured by a certain SPIDER apparatus: the delay $\tau$, the spectral shear $\delta \omega$ and the group-delay dispersion $\mathrm{GDD}_{\text {up }}$ used to generate the strongly linearly chirped upconverter pulse. These three parameters are related as:

$$
\begin{equation*}
\delta \omega=\frac{\tau}{\mathrm{GDD}_{\mathrm{up}}} . \tag{2.1.95}
\end{equation*}
$$

The delay $\tau$, which determines the positions of the two side peaks of the Fourier transform of the interferogram, is chosen in such a way as to assure that the side peaks are well-separated from the center peak. On the other hand, the fringe spacing of the interferogram is proportional to $2 \pi / \tau$ and thus $\tau$ must be sufficiently small such that the spectrometer is able to fully resolve the fringes. The stretching factor $\mathrm{GDD}_{\text {up }}$ is then chosen such that the spectral shear $\delta \omega$, which determines the sampling interval of the reconstructed spectral phase, is small enough to assure correct reconstruction of the electric field in the time domain according to the Whittaker-Shannon sampling theorem [00Dor]. The constrained relationship for $\tau$ and $\delta \omega$ expressed by (2.1.95) means that with a particular SPIDER setup, only pulses with a limited range of pulse durations can be measured. A set-up for the sub-10-femtosecond regime in described in [99Gal].

### 2.1.7.3.3 Comparison between FROG and SPIDER techniques

The highest acquisition rates for single-shot pulse characterization reported so far were 1 kHz using SPIDER [03Kor] and 30 Hz using FROG [03Gar]. FROG is not well suited for high acquisition rates for two reasons: FROG requires the measurement of a 2 D trace which makes the acquisition itself inherently slow and moreover the FROG algorithm uses an iterative process which requires a minimum number of steps for convergence depending on the complexity of the measured pulse. SPIDER however only requires the acquisition of two 1D spectra: the so-called SPIDER interferogram and the optical spectrum of the pulse. Furthermore, the SPIDER algorithm is deterministic since it is based on two Fourier transforms with intermittent spectral filtering to reconstruct the spectral phase of the pulse. An additional Fourier transform is then required to calculate the electric field in the time domain and therefore the pulse reconstruction is fast. SPIDER is thus well suited for high acquisition rates and real-time operation. SPIDER has been shown to achieve high accuracy, i.e. the reconstructed electric field matches well with the physical field of the pulse [02Dor1], and high precision [02Dor2], implying a small spread between several reconstructions of the field obtained from the same data. In particular the SPIDER technique is reliable in the presence of limited experimental noise [00And, 04Jen]. SPIDER offers more bandwidth than any other technique and we even can measure pulses in the single-cycle regime [03Sch]. In addition, SPIDER still gives valid results even if the beam profile is not spatially coherent anymore because we can spatially resolve these measurements [01Gal]. A direct comparison between FROG and SPIDER techniques in the sub-10-femtosecond regime is given in [00Gal2].

Only fully characterized pulses in phase and amplitude will provide reliable information about pulse shape and pulse duration - this becomes even more important for pulses with very broad and complex spectra. In such a situation any other technique, such as fitting attempts to IAC traces, is very erroneous and generally underestimates the pulse duration.

### 2.1.8 Carrier envelope offset (CEO)

Progress in ultrashort pulse generation [99Ste] has reached a level where the slowly-varyingenvelope approximation starts to fail. Pulse durations of Ti:sapphire laser oscillators have reached around 5 fs which is so short that only about two optical cycles of the underlying electric field fit into the full-width half maximum of the pulse envelope. For such short pulses the maximum electric-field strength depends strongly on the exact position of the electric field with regards to the pulse envelope, i.e. the Carrier Envelope Offset (CEO) [99Tel]. In passively mode-locked lasers this carrier envelope offset is a freely varying parameter because the steady-state boundary condition only requires that the pulse envelope is the same after one round trip (Fig. 2.1.19). Therefore the CEO phase may exhibit large fluctuations, even when all other laser parameters are stabilized. We have discussed the physical origin of these fluctuations before [ $02 \mathrm{Hel} 2,02 \mathrm{Hel} 1]$. Because nonlinear laser-matter interaction depends strongly on the strength of the electric field, this CEO fluctuations cause strong signal fluctuations in nonlinear experiments such as high-harmonic generation [00Bra], attosecond pulse generation [01Dre], photoelectron emission [01Pau1] etc.


Fig. 2.1.19. Electric field $E(t)$ of three subsequent pulses from a mode-locked laser with a pulse repetition rate of $T_{\mathrm{R}}=1 / f_{\mathrm{rep}}$. The envelope $\pm A(t)$ is shown as dashed lines. The electric-field patterns of the pulses experience large pulse-to-pulse fluctuations.

Different techniques have been proposed to stabilize these CEO fluctuations in the time domain [96Xul] and in the frequency domain [99Tel]. The frequency-domain technique is based on the frequency comb generated from mode-locked lasers (Sect. 2.1.2.2) and is much more sensitive and is the technique that is being used today. Optical frequency comb techniques recently received a lot of attention and were also an important part of the 2005 Nobel Prize in Physics for Theodor W. Hänsch and John L. Hall in the area of laser-based precision spectroscopy [05Nob].

In the following we follow the notation and derivation of Helbing et al. [03Hel]. A very stable frequency comb is generated with a mode-locked laser which follows directly from the time domain:

$$
\begin{equation*}
E_{\text {train }}(t)=A(t) \exp \left(\mathrm{i} \omega_{\mathrm{c}} t+\mathrm{i} \varphi_{0}(t)\right) \otimes \sum_{m=-\infty}^{+\infty} \delta\left(t-m T_{\mathrm{R}}\right) \tag{2.1.96}
\end{equation*}
$$

where $E_{\text {train }}(t)$ is the electric field of a pulse train (Fig. 2.1.19), $\omega_{\mathrm{c}}$ is the (angular) carrier frequency which is the center of gravity of the mode-locked spectrum, $A(t)$ the pulse envelope, and $\varphi_{0}(t)$ the absolute phase of the pulse. The change of the carrier-envelope offset phase $\varphi_{0}$ in (2.1.96) per round trip is given by:

$$
\begin{equation*}
\Delta \varphi_{0}=\Delta \varphi_{\mathrm{GPO}} \bmod 2 \pi \tag{2.1.97}
\end{equation*}
$$

The Group-Phase Offset (GPO) only arises from the first-order dispersion of the material along the beam path:

$$
\begin{equation*}
\Delta \varphi_{\mathrm{GPO}}=-\omega \int_{0}^{\mathrm{L}}\left(\frac{1}{v_{\mathrm{g}}}-\frac{1}{v_{\mathrm{p}}}\right) \mathrm{d} x=\int_{0}^{\mathrm{L}} \frac{\omega^{2}}{c} \frac{\mathrm{~d} n(\omega, x)}{\mathrm{d} \omega} \mathrm{~d} x \tag{2.1.98}
\end{equation*}
$$

where $v_{\mathrm{g}}$ is the group velocity and $v_{\mathrm{p}}$ is the phase velocity (Table 2.1.7).


Fig. 2.1.20. Equidistant frequency comb of a mode-locked laser. The comb lines are spaced by the repetition rate $f_{\text {rep }}$ and exhibit a nonvanishing offset frequency $f_{\text {CEO }}$ at zero frequency unless the electric field pattern exactly reproduces from pulse to pulse.

We define the (angular) carrier-envelope offset frequency as

$$
\begin{equation*}
2 \pi f_{\mathrm{CEO}}=\omega_{\mathrm{CEO}}=\Delta \varphi_{0} f_{\mathrm{rep}}=\frac{\Delta \varphi_{0}}{T_{\mathrm{R}}} \equiv \frac{\Delta \varphi_{\mathrm{GPO}}}{T_{\mathrm{R}}} \bmod 2 \pi \equiv\left(\frac{\partial}{\partial t} \varphi_{\mathrm{GPO}}\right) \bmod 2 \pi \tag{2.1.99}
\end{equation*}
$$

Taking into account the varying carrier-envelope offset phase the electric field of the pulse train becomes:

$$
\begin{equation*}
E_{\text {train }}(t)=A(t) \exp \left(\mathrm{i} \omega_{\mathrm{c}} t+\mathrm{i} \omega_{\mathrm{CEO}} t\right) \otimes \sum_{m=-\infty}^{+\infty} \delta\left(t-m T_{\mathrm{R}}\right) \tag{2.1.100}
\end{equation*}
$$

The Fourier-transformation of (2.1.100) then results in the frequency comb as shown in Fig. 2.1.20:

$$
\begin{equation*}
\tilde{E}_{\text {train }}(f)=\tilde{A}\left(f-f_{\mathrm{c}}\right) \cdot \sum_{m=-\infty}^{+\infty} \delta\left(f-m f_{\mathrm{rep}}-f_{\mathrm{CEO}}\right) \tag{2.1.101}
\end{equation*}
$$

The whole equidistant frequency comb is shifted by $f_{\text {CEO }}$ due to the per round trip carrier-envelope offset phase shift of $\Delta \varphi_{0}$. Therefore, a mode-locked laser generates an equidistant frequency comb with a frequency step given by the pulse repetition frequency $f_{\text {rep }}$ which can be measured and stabilized with very high precision [86Lin, $86 \mathrm{Rod}, 89 \mathrm{Rod}, 89 \mathrm{Kel}]$. The uniformity of the modelocked frequency comb has been demonstrated to a relative uncertainty below $10^{-15}$ [99Ude]. The timing jitter in the arrival time of the pulses (i.e. variations in $f_{\text {rep }}$ ) produces a "breathing" of the fully equidistant frequency comb. The additional freedom of the frequency offset to DC of this frequency comb is given by the CEO frequency $f_{\mathrm{CEO}}$ (Fig. 2.1.20) and every "tick of the frequency ruler" then can be described by [99Tel]

$$
\begin{equation*}
f_{m}=m f_{\mathrm{rep}}+f_{\mathrm{CEO}} \tag{2.1.102}
\end{equation*}
$$

with $m$ being an integer number. The timing jitter of the CEO results in a translation of the full frequency comb. Note that the equidistant frequency-comb spacing is given by the round-trip propagation time of the pulse envelope (i.e. by the group velocity and not the phase velocity). This means that the axial modes of a mode-locked laser are not the same as the ones from a cw laser for which the phase velocity determines the axial mode spacing.

Even though a measurement of the repetition rate is straightforward, it is virtually impossible to access the CEO-frequency directly, as the laser spectrum contains no energy close to zero frequency. One therefore has to use an indirect way to measure the second comb parameter. Depending on the available optical bandwidth different techniques have been proposed by Telle et al. [99Tel] such as $f$-to- $2 f, 2 f$-to- $3 f$ heterodyne techniques and others. Selecting some low-frequency portion of the comb and frequency doubling it gives rise to the comb


$$
2 f_{m}=2 f_{\mathrm{CEO}}+2 m f_{\mathrm{rep}}
$$

Fig. 2.1.21. $f$-to- $2 f$ interference technique to measure the CEO frequency according to [99Tel]: (a) Mode beating of fundamental and second harmonic frequency comb results in the carrier envelope offset frequency $f_{\text {CEO }}=2 f_{1}-f_{2}$, where $f_{\text {rep }}$ is the pulse repetition rate frequency, $f_{\mathrm{CEO}}$ is the carrier envelope offset frequency and $m$ is an integer number. (b) Mode beating signal measurement with a microwave spectrum analyzer which shows a strong peak at the pulse repetition rate and the two CEO beats at $f_{\mathrm{CEO}}$ and $f_{\text {rep }}-f_{\mathrm{CEO}}$ with a signal-to-noise ratio of more than 40 dB . This is ideal for a stabilizing feedback loop using a weak modulation of the pump laser power to compensate for the CEO fluctuations.

If the fundamental comb spectrum covers more than an optical octave it will also contain modes at

$$
\begin{equation*}
f_{2 m}=f_{\mathrm{CEO}}+2 m f_{\mathrm{rep}} \tag{2.1.104}
\end{equation*}
$$

Beating the combs of (2.1.103) and (2.1.104), therefore extracts the CEO-frequency from the comb spectrum [99Tel]:

$$
\begin{equation*}
f_{\mathrm{CEO}}=2 f_{m}-f_{2 m}=\left(2 f_{\mathrm{CEO}}+2 m f_{\mathrm{rep}}\right)-\left(f_{\mathrm{CEO}}+2 m f_{\mathrm{rep}}\right), \tag{2.1.105}
\end{equation*}
$$

see Fig. 2.1.21. Today the most common technique is based on this $f$-to- $2 f$ heterodyne technique because of its simplicity and because an octave-spanning spectrum can be generated with external spectral broadening in a microstructure fiber for example [00Jon, 00Apo]. With this technique we achieved a long-term CEO stabilization with residual 10 attosecond timing jitter which corresponds to 0.025 rad rms CEO phase noise in a $(0.01 \mathrm{~Hz}-100 \mathrm{kHz})$ bandwidth [02Hel1]. The $f$-to- $2 f$ interference technique requires an octave-spanning spectrum. So far, all attempts to generate this spectrum directly from a laser source have only reached unsatisfactory control of the CEO frequency, which was mainly caused by poor signal strength. Therefore most experiments required additional spectral broadening, e.g. in an external microstructure fiber. The continuum generation process with its strong nonlinearity, however, introduces additional CEO noise. It is important to note that the CEO stabilization is achieved for the pulses after the microstructure fiber, which means that the pulses directly from the Ti:sapphire laser will exhibit excess CEO phase noise even with a perfectly working CEO stabilization.

The relative phase between the carrier and the envelope of an optical pulse is the key parameter linking the fields of precision frequency metrology and ultrafast laser physics. As we have discussed, the spectrum of a mode-locked laser consists of a comb of precisely equally spaced frequencies. The uniformity of this frequency comb has been demonstrated to a relative uncertainty below $10^{-15}$
[99Ude]. Knowledge of only two parameters, the comb spacing and a common offset frequency of all modes, provides one with a set of reference frequencies, similar to the tick marks on a ruler. The beat (difference-frequency) signal of this unknown frequency with the closest frequency in the ruler always gives a beat signal smaller than the comb period. Thus, an optical frequency in the 100 THz regime can be translated down to a microwave frequency in the range of 100 MHz , which can then be measured very accurately. This can be used for an all-optical atomic clock that is expected to outperform today's state-of-the-art cesium clocks [02Ude]. The mode-locked laser provides a phaselocked clockwork mediating between radio frequencies and the Terahertz frequencies of the lines in the optical comb, effectively rendering optical frequencies countable. Details on precision frequency measurements with mode-locked laser combs can be found in [99Rei, 01Hol, 01Cun, 02Bau].

### 2.1.9 Conclusion and outlook

We have shown that the technology of ultrafast lasers has become very refined and is now suitable for application in many areas. Points of particular importance in this respect are:

- The transition from dye lasers to solid-state lasers, which can be compact, powerful, efficient and long-lived. It has been shown that solid-state lasers can generate pulses which are even shorter pulses than those generated in dye lasers with much more average output power.
- The development of high-power and high-brightness diode lasers for direct pumping of solidstate lasers. This has lead not only to very efficient and compact lasers, but also to lasers with more than 1000 W of average output power.
- The development of novel saturable absorbers such as KLM which has pushed the frontier in ultrashort pulse duration into the two-optical-cycle regime using novel chirped mirrors for dispersion compensation. New parameters such as the Carrier Envelope Offset (CEO) of the electric field underneath the pulse envelope have become important for many different applications.
- The development of SEmiconductor Saturable Absorber Mirrors (SESAMs) which passively mode-lock many different diode-pumped solid-state lasers without $Q$-switching instabilities and can be optimized for operation in very different parameter regimes such as laser wavelength, pulse duration, pulse repetition rate and power levels. SESAMs can be optimized independently of the cavity design. This allowed for pushing the frontier in ultrafast solid-state lasers by several orders of magnitude: femtosecond mode-locked lasers with close to 100 W of average output power and more than $1 \mu \mathrm{~J}$ of pulse energies and different lasers with high pulse repetition rates up to 160 GHz have been demonstrated so far.

For the next few years we expect many new exciting developments in the field of diode-pumped solid-state lasers:

- Very high power levels ( $>100 \mathrm{~W}$ of average power) should become possible with passively modelocked thin-disk lasers. Pulse durations just below 1 ps are feasible and with new materials the regime of 200 fs or even below should become accessible with similarly high powers.
- Nonlinear frequency conversion stages (based on second-harmonic generation, sum frequency mixing, or parametric oscillation) will be pumped with high-power mode-locked lasers to generate short and powerful pulses at other wavelengths. The high power makes the nonlinear conversion efficiencies very high with very simple arrangements [01Sue, 05 Mar ]. This will be of interest for application in large-screen RGB display systems, for example [04Bru, 06Inn].
- Simple external pulse compression combined with novel high-average-power solid-state lasers now allows for peak intensities as high as 12 MW with 33 -fs pulses at the full pulse repetition rate of the laser oscillator [03Sue]. This could be focused to a peak intensity of $10^{14} \mathrm{~W} / \mathrm{cm}^{2}$, a
regime where high-field laser physics such as high-harmonic generation [88Fer, 94Lew, 98Sal] and laser-plasma-generated X-rays [91Mur] are possible at more than 10 MHz pulse repetition rate. This improves signal-to-noise ratios in measurements by 4 orders of magnitude compared to the standard sources at kHz repetition rates. This would be important for low-power applications such as X-ray imaging and microscopy [02Sch1], femtosecond EUV and soft-X-ray photoelectron spectroscopy [01Bau] and ultrafast X-ray diffraction [99Sid, 01Rou].
- Very high pulse repetition rates with $\gtrsim 100 \mathrm{GHz}$ should be possible from passively mode-locked diode-pumped solid-state lasers at different wavelengths, even in the wavelength range around $1.5 \mu \mathrm{~m}$ and $1.3 \mu \mathrm{~m}$ for telecom applications.
- As an alternative to ion-doped gain media at high pulse-repetition rates (i.e. $>1 \mathrm{GHz}$ ) optically pumped VECSELs and even hopefully electrically pumped VECSELs will become very interesting alternatives [06Kel]. The integration of the SESAM into the VECSEL structure will provide even more compact ultrafast lasers [07Maa].
- So far octave-spanning frequency combs have been mostly generated with KLM Ti:sapphire lasers and supercontinuum generation in a microstructured fiber. However, many applications need more compact sources. The progress in femtosecond diode-pumped solid-state lasers and VECSELs reported here will make this possible in the near future.

Thus, all these examples show that the development of ultrafast diode-pumped sources has not come to its end but will continue to deliver superior performances for many established and new applications.

In addition, research to produce pulses of even shorter duration is underway. Currently, the most promising path to attosecond pulse generation and attosecond spectroscopy is high-harmonic generation (recent reviews are given with [98Sal, 95DiM, 04Ago]). High-order-Harmonic Generation (HHG), being an up-conversion process, provides a laser-like source of temporally and spatially coherent radiation consisting of odd multiples of the laser driving frequency down to the XUV region of the spectrum. Since its discovery in 1987 in Chicago and Saclay [ $88 \mathrm{Fer}, 87 \mathrm{McP}$ ], it has been speculated early on that pulses from existing sources of high-harmonic generation exhibit attosecond time signature [95Cor, 96Ant]. Meanwhile much progress has been made and by controlling its properties, Attosecond Pulse Trains (APT) [01Pau2] and isolated attosecond pulses [02Dre] have been successfully produced and applied in first proof-of-principle experiments. The higher orders are produced simultaneously and fully phase-coherent with the driving IR field, which makes this source ideally suited for two-color or even multi-color pump probe experiments. Furthermore, it is important to note, that much of this progress is directly related to advancements in laser science.

Isolated attosecond pulse generation depends on the maximum amplitude of the driving pulse's electric field, i.e. the exact position of the electric field with regard to the pulse envelope (Carrier Envelope Offset: CEO) [99Tel]. Generally in mode-locked lasers, the CEO phase exhibits large fluctuations, which have to be measured and be corrected for. Until recently the only successful demonstration of CEO-phase-locked intense pulses was based on a CEO-stabilized Ti:sapphire laser, chirped-pulse amplification and pulse compression in a hollow fiber (Sect. 2.1.6.9). Meanwhile, there are some new promising ways to achieve this goal. One is based on Chirped-Pulse Optical Parametric Amplification (CPOPA) [92Dub] and the other on pulse compression through filamentation [04Hau1]. We have demonstrated CEO-phase-stabilized CPOPA for the first time with near-transform-limited 17.3 -fs pulses [04Hau2]. But even more amazing was that even though filamentation is a highly nonlinear process involving plasma generation, the CEO stabilization was maintained and intense CEO-stabilized pulses as short as 5.1 fs with $180 \mu \mathrm{~J}$ pulse energy have been generated [ 05 Hau ]. It is expected that both pulse duration and energies will be further improved in the near future. For example just recently CPOPA resulted in 9.8 fs pulses with 10.5 mJ at 30 Hz pulse repetition rate [05Wit].

We would expect that with attosecond time resolution we open up a new world of physics with as much impact as has been demonstrated in the 70's and 80's with the transition from picosecond to femtosecond time resolution. First time-resolved measurements have been done [02Dre]. At this
point, however, we still have some significant challenges to tackle before we demonstrate standard attosecond pulse generation and attosecond spectroscopy. Solving all of these challenges will make the research in ultrashort pulse generation very exciting and rewarding for many years to come.

### 2.1.10 Glossary

| A | pulse envelope (2.1.23) |
| :---: | :---: |
| $A_{\text {A }}$ | laser mode area on saturable absorber (Table 2.1.5) |
| $A_{\text {L }}$ | laser mode area in laser gain media |
| $A_{\text {p }}$ | pump mode area |
| $B$ | system bandwidth (2.1.82) |
| $b$ | depth of focus or confocal parameter of a Gaussian beam |
| D | dispersion parameter (2.1.40), i.e. half of the total group delay dispersion per cavity round trip |
| $D_{\text {g }}$ | gain dispersion ((2.1.32) and Table 2.1.10) |
| $D_{\text {p }}$ | width of the pump source (i.e. approximately the stripe width of a diode array or bar or more accurately given in Sect. 2.1.3.2) |
| $D R(t)$ | differential impulse response of a saturable absorber mirror measured with standard pump probe (Sect. 2.1.4.2) |
| $d$ | thickness of Fabry-Perot (Table 2.1.9) |
| E | electric field of the electromagnetic wave |
| $E_{\mathrm{p}}$ | intracavity pulse energy |
| $E_{\mathrm{p}, \mathrm{c}}$ | critical $E_{\mathrm{p}}$ (2.1.77) |
| $E_{\mathrm{p}, \text { out }}$ | output pulse energy |
| $E_{\text {sat, }, \mathrm{A}}$ | absorber saturation energy (Table 2.1.5) |
| $E_{\text {sat,L }}$ | laser saturation energy |
| $E_{\text {train }}$ | electric field of a pulse train (2.1.96) |
| $F_{2}$ | inverse slope of roll-over (2.1.81) |
| $F_{\text {in }}$ | incident saturation fluence on SESAM (2.1.9) |
| $F_{\text {out }}$ | reflected saturation fluence on SESAM (2.1.9) |
| $F_{\mathrm{p}, \mathrm{A}}$ | incident pulse fluence on saturable absorber (Table 2.1.5) |
| $F_{\text {sat, }}$ | absorber saturation fluence (Table 2.1.5) |
| $F_{\text {sat,L }}$ | laser saturation fluence (2.1.1) and (2.1.2) |
| $f_{\text {CEO }}$ | carrier envelope offset (CEO) frequency (2.1.99) |
| $f_{\text {rep }}$ | pulse repetition frequency |
| $G(t)$ | gate (see Sect. 2.1.7.3.1) |
| $g$ | saturated amplitude laser gain coefficient |
| $g_{0}$ | small signal amplitude laser gain |
| $h$ | beam insertion into second prism (Table 2.1.9) |
| I | intensity |
| $I_{\text {A }}$ | incident intensity on saturable absorber (Table 2.1.5) |
| $I_{\text {in }}(t)$ | incident intensity onto the saturable absorber (2.1.8) |
| $I_{\text {out }}(t)$ | reflected intensity from the saturable absorber (2.1.8) |
| $I_{\text {sat, } \mathrm{A}}$ | absorber saturation intensity (Table 2.1.5) |
| $k$ | vacuum wave number, i.e. $k=2 \pi / \lambda$ |
| $k_{n}$ | wave number in a dispersive medium, i.e. $k_{n}=n k$ (2.1.24) |
| $L$ | apex-to-apex prism distance (Table 2.1.9) |
| $L_{\text {a }}$ | absorption length |



| $\Delta R$ | modulation depth of a saturable absorber mirror (Fig. 2.1.9 and Table 2.1.5) |
| :---: | :---: |
| $\Delta R_{\mathrm{ns}}$ | nonsaturable reflection loss of a saturable absorber mirror (Fig. 2.1.9 and Table 2.1.5) |
| $\Delta T$ | modulation depth of saturable absorber in transmission |
| $\Delta T_{\text {ns }}$ | nonsaturable transmission loss of saturable absorber |
| $\Delta \lambda_{\mathrm{g}}$ | FWHM gain bandwidth |
| $\Delta \nu_{\mathrm{g}}$ | FWHM gain bandwidth, i.e. $\frac{\Delta \nu_{\mathrm{g}}}{\nu_{0}}=\frac{\Delta \lambda_{\mathrm{g}}}{\lambda_{0}}$ |
| $\Delta \nu_{\mathrm{p}}$ | FWHM of pulse intensity spectrum |
| $\Delta \varphi_{\mathrm{GPO}}$ | group phase offset ((2.1.97) and (2.1.98)) |
| $\delta_{\text {L }}$ | SPM coefficient (2.1.44) |
| $\delta \tau$ | temporal delay between two beams (2.1.86) |
| $\theta$ | divergence angle of a pump source (i.e. the beam radius increases approximately linearly with propagation distance, defining a cone with half-angle $\theta$ ) |
| $\theta_{\text {B }}$ | Brewster angle (Table 2.1.9) |
| $\theta_{\mathrm{G}}$ | divergence angle of a Gaussian beam, i.e. $\theta_{\mathrm{G}}=\lambda /\left(\pi W_{0, \mathrm{G}}\right)(2.1 .3)$ |
| $\theta_{\mathrm{i}}$ | angle of incidence (Table 2.1.9) |
| $\Lambda$ | grating period (Table 2.1.9) |
| $\lambda$ | vacuum wavelength of light |
| $\lambda_{0}$ | center vacuum wavelength |
| $\lambda_{\text {eff }}$ | effective wavelength (2.1.4) |
| $\lambda_{n}$ | wavelength in a dispersive medium with refractive index $n$, i.e. $\lambda_{n}=\lambda / n$ |
| $\nu$ | frequency |
| $\nu_{\text {pump }}$ | pump photon frequency |
| $\sigma_{\text {A }}$ | absorber cross section |
| $\sigma_{\text {L }}$ | gain cross section |
| $\sigma_{\text {L }}^{\text {abs }}$ | absorption cross section of the three-level gain medium |
| $\tau_{0}$ | initial transform-limited pulse duration (2.1.20) |
| $\tau_{\text {A }}$ | recovery time of saturable absorber (Table 2.1.5) |
| $\tau_{\text {Au }}$ | FWHM of intensity autocorrelation pulse |
| $\tau_{\text {c }}$ | photon cavity lifetime |
| $\tau_{\mathrm{L}}$ | upper-state lifetime of laser gain material |
| $\tau_{\mathrm{p}}$ | FWHM intensity pulse duration |
| $\tau_{\mathrm{p}, \text { min }}$ | minimal $\tau_{\mathrm{p}}$ |
| $\Phi(\omega)$ | frequency-dependent phase shift (Sect. 2.1.5.1) |
| $\Phi_{0}$ | phase shift at center angular frequency $\omega_{0}$ |
| $\varphi_{0}(t)$ | absolute phase of pulse (2.1.96) |
| $\phi_{\mathrm{nl}}$ | nonlinear phase shift per cavity round trip (2.1.73) |
| $\phi_{\mathrm{nl}}(z)$ | nonlinear phase shift of a pulse with peak intensity $I_{0}$ during propagation through a Kerr medium along the $z$-axis, i.e. $\phi_{\mathrm{nl}}(z)=k n_{2} I_{0} z(2.1 .73)$ |
| $\phi_{\text {s }}$ | phase shift of the soliton per cavity round trip |
| $\phi_{\mathrm{s}}(z)$ | phase shift of the soliton during propagation along the $z$-axis (2.1.73) |
| $\psi$ | phase shift (Table 2.1.10) |
| $\Omega_{\mathrm{g}}$ | Half-Width-Half-Maximum (HWHM) gain bandwidth of laser in radians/second i.e. $\Omega_{\mathrm{g}}=\pi \Delta \nu_{\mathrm{g}}$ |
| $\omega$ | radian frequency |
| $\omega_{0}$ | center radian frequency |
| $\omega_{\text {c }}$ | carrier radian frequency (2.1.96) |
| $\omega_{\text {CEO }}$ | carrier envelope offset (CEO) frequency in radians/second (2.1.99) |
| $\omega_{\mathrm{m}}$ | modulation frequency in radians/second |

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[^1]:    $\mathrm{Yb}: \mathrm{Lu}_{2} \mathrm{O}_{3} \quad$ soliton-SESAM $\quad 1.034 \mu \mathrm{~m}$

